15-779 Lecture 13:

Parallelization Part 2
Model and Pipeline Parallelism

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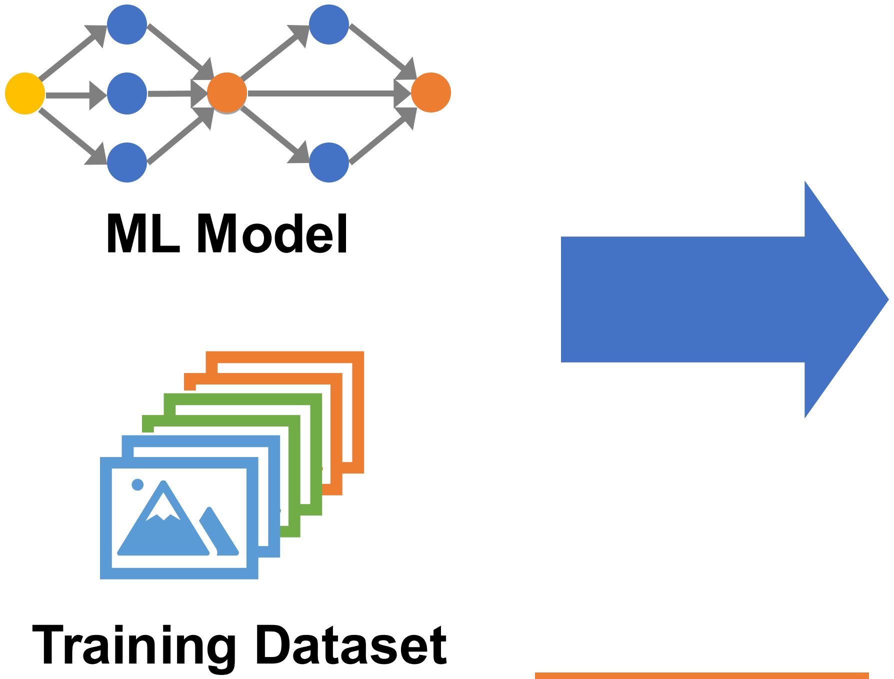
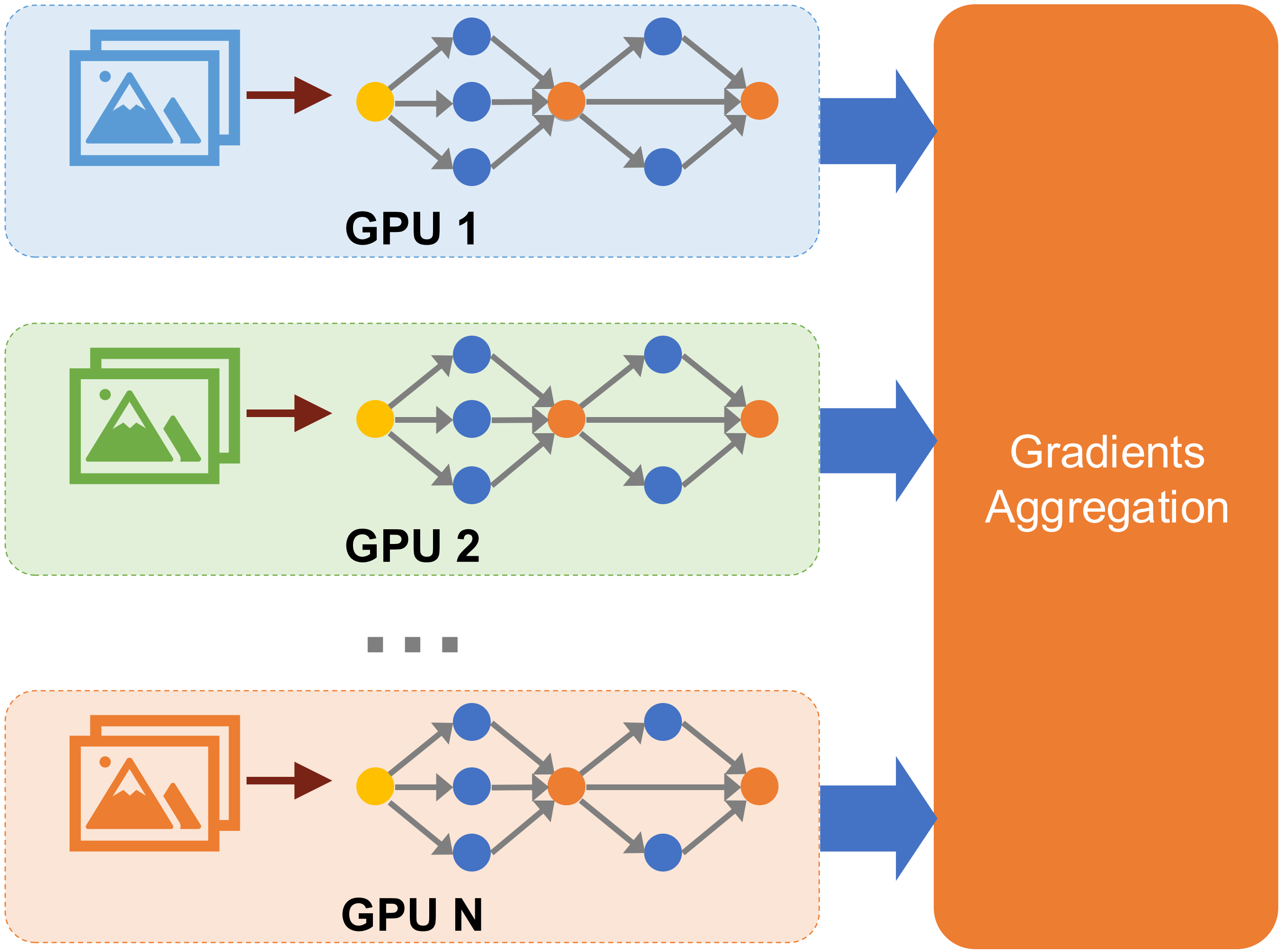
Recap: Data Parallelism





$$w_i := w_i - \gamma \nabla L(w_i) = w_i - \frac{\gamma}{n} \boxed{\sum_{j=1}^{n} \nabla L_j(w_i)}$$

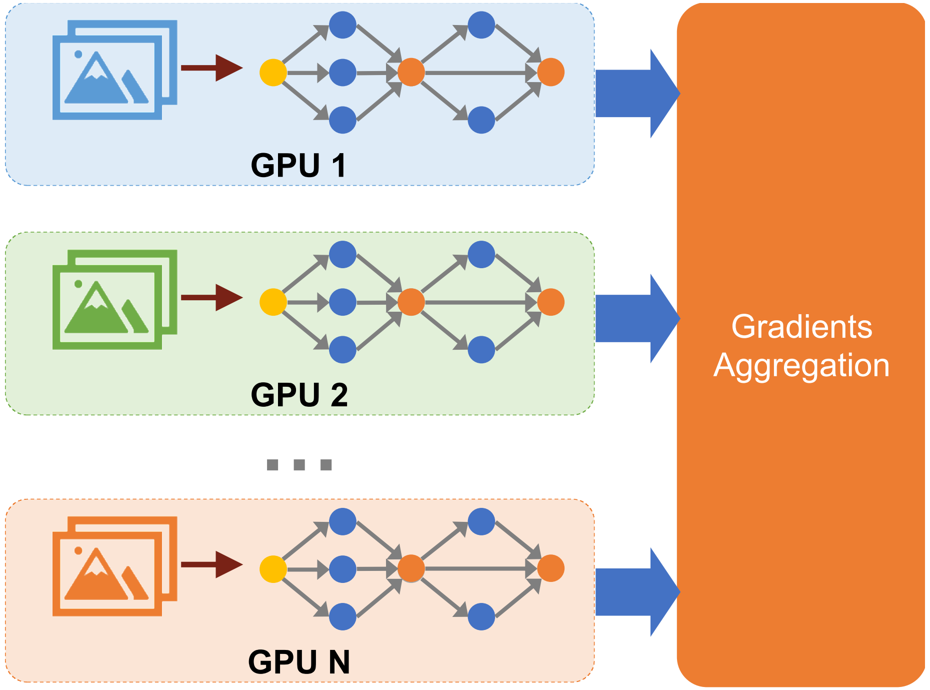
1. Partition training data into batches

2. Compute the gradients of each batch on a GPU

3. Aggregate gradients across GPUs

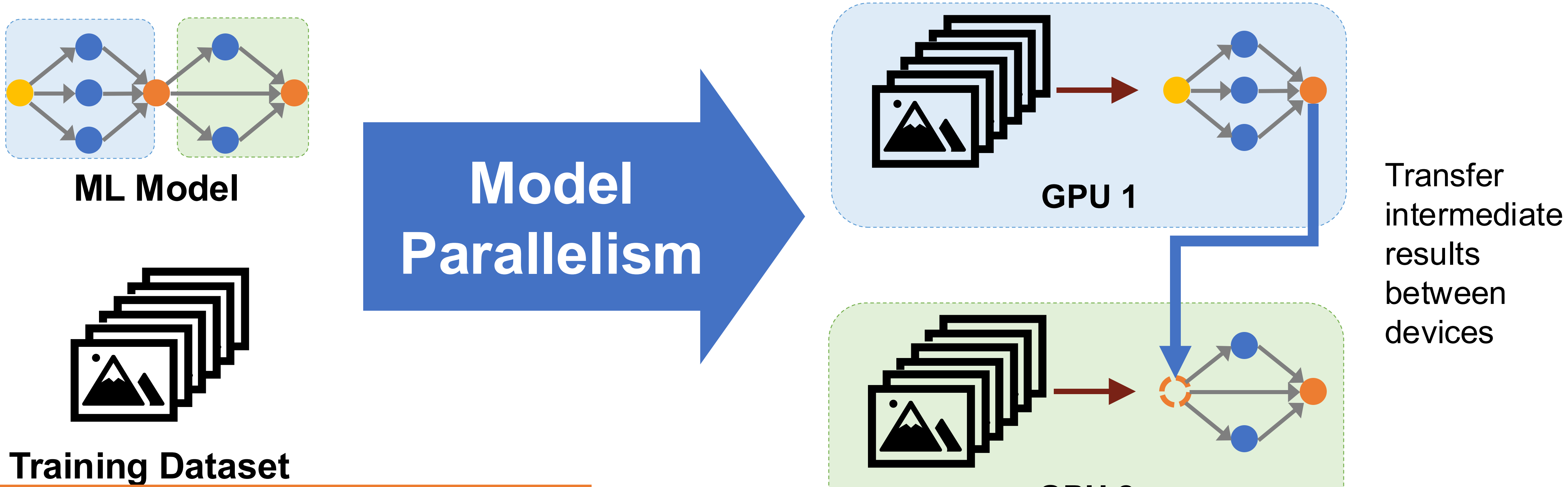
Recap: An Issue with Data Parallelism

- Each GPU saves a replica of the entire model
- Cannot train large models that exceed GPU device memory



Model Parallelism

- Split a model into multiple subgraphs and assign them to different devices

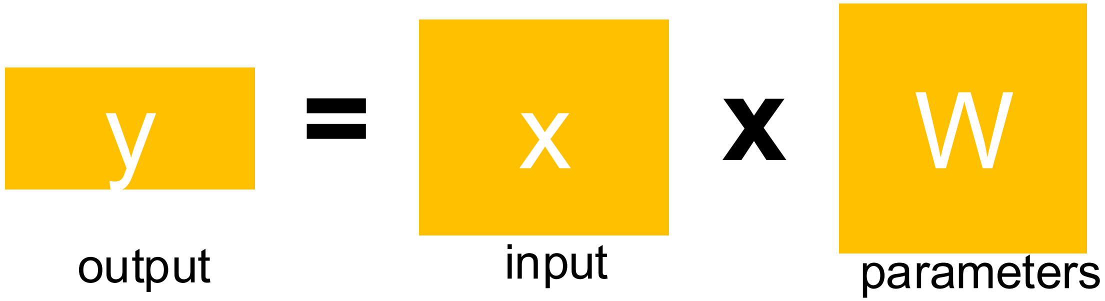


$$w_i \coloneqq w_i - \gamma \nabla L(w_i) = w_i - \frac{\gamma}{n} \sum_{j=1}^{n} \nabla L_j(w_i)$$

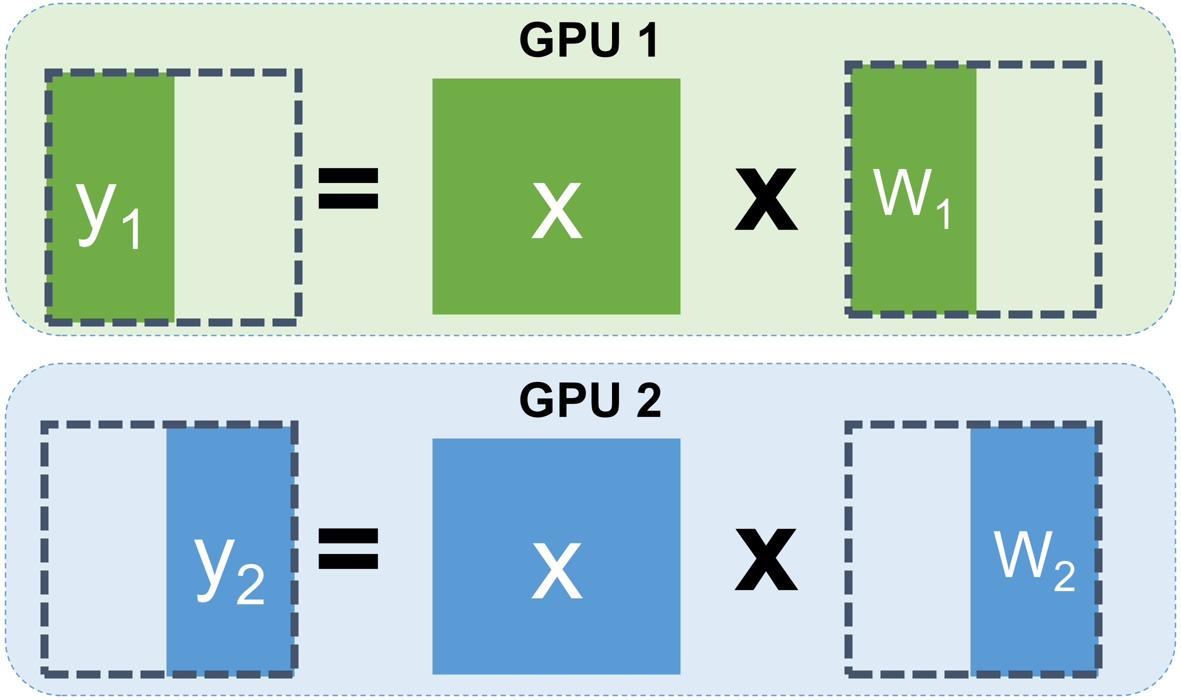
How to parallelize DNN Training?

- Data parallelism
- Model parallelism
  - Tensor model parallelism
  - Pipeline model parallelism

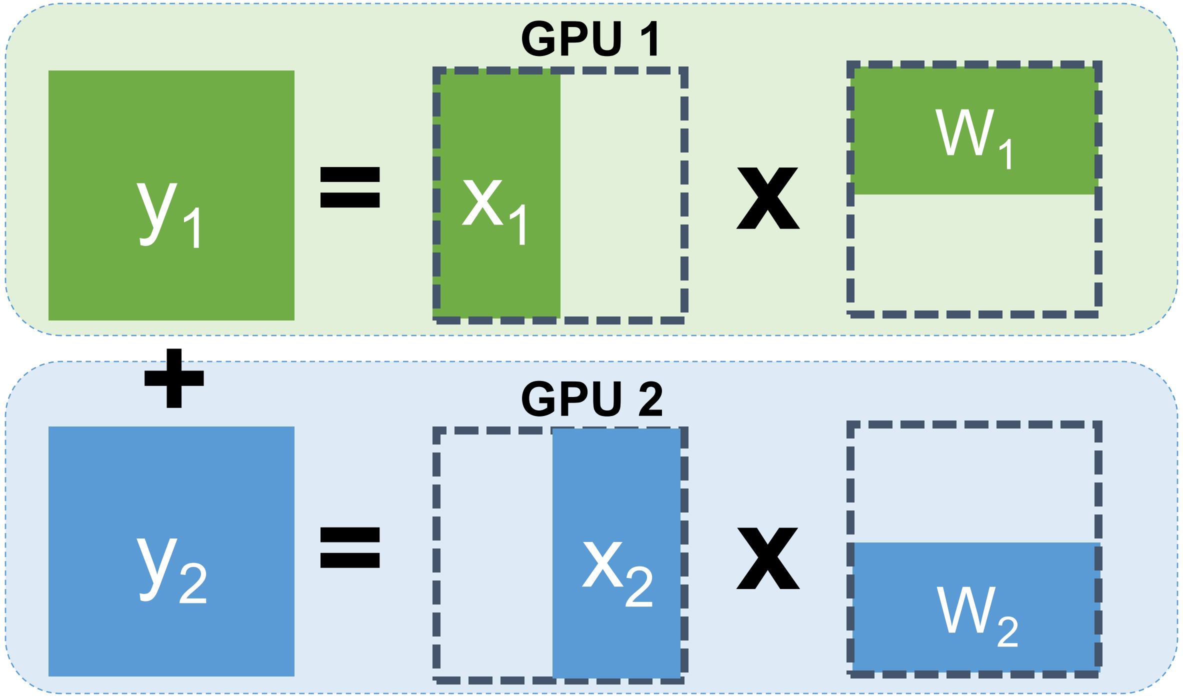
Tensor Model Parallelism



- Partition parameters/gradients ***within*** a layer



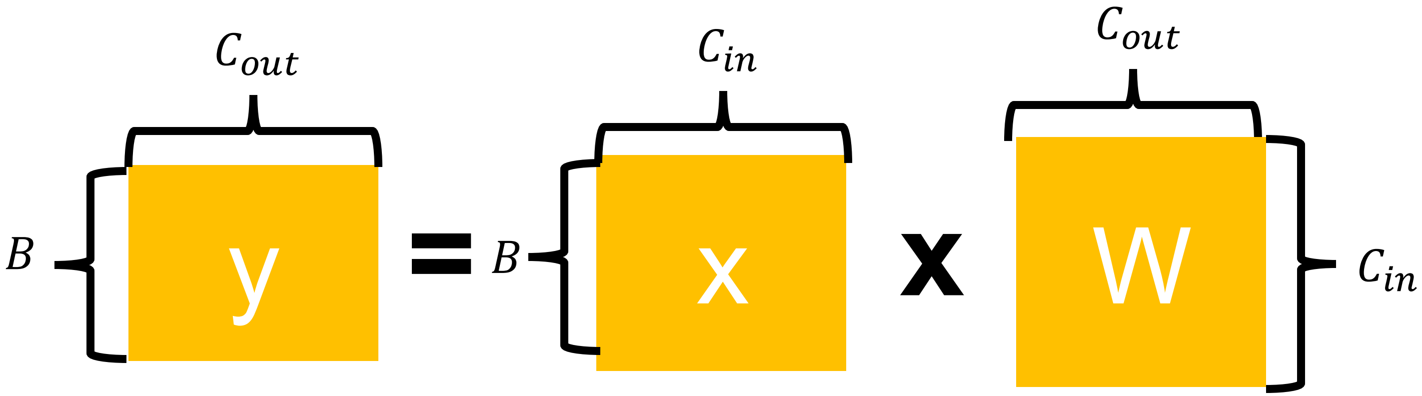
Tensor Model Parallelism (partition output)

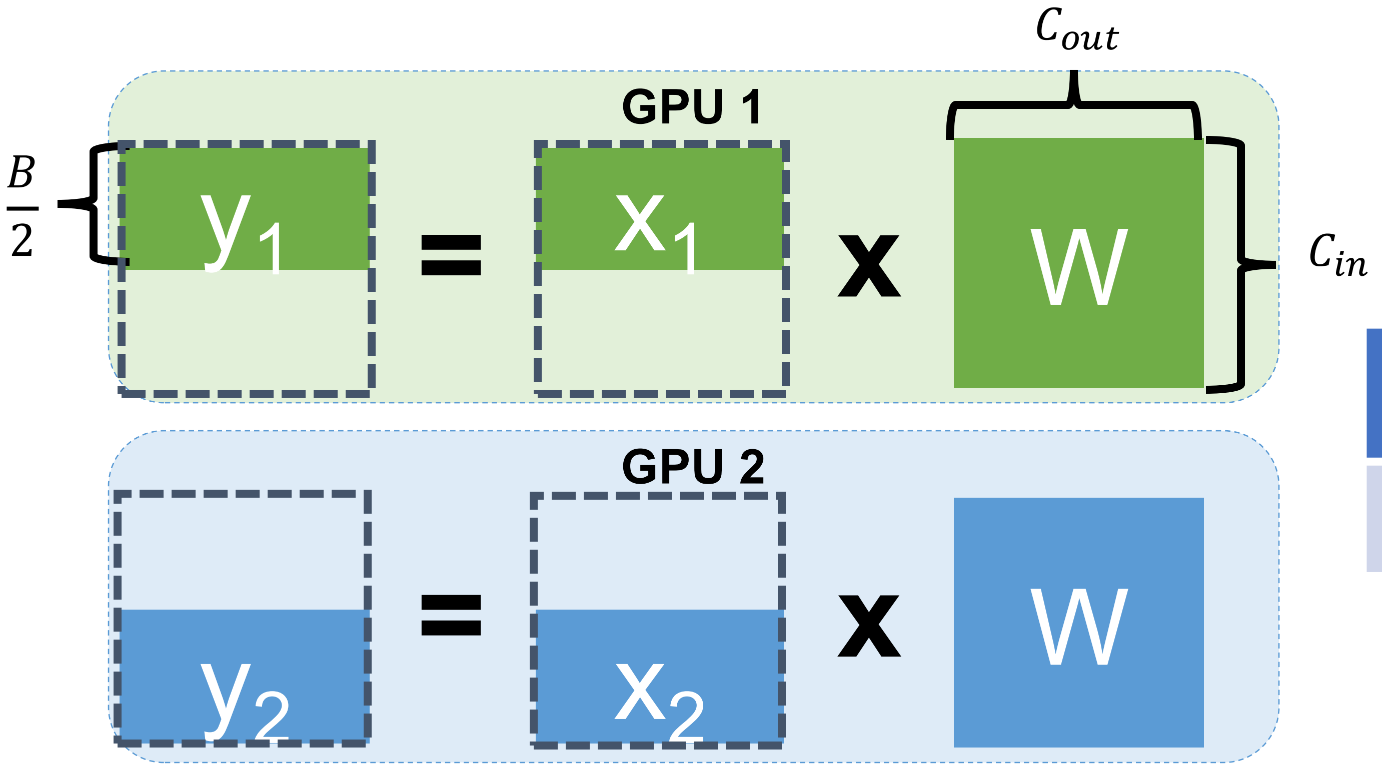


Tensor Model Parallelism (reduce output)

$y = y1 + y2$

Comparing Data and Tensor Model Parallelism



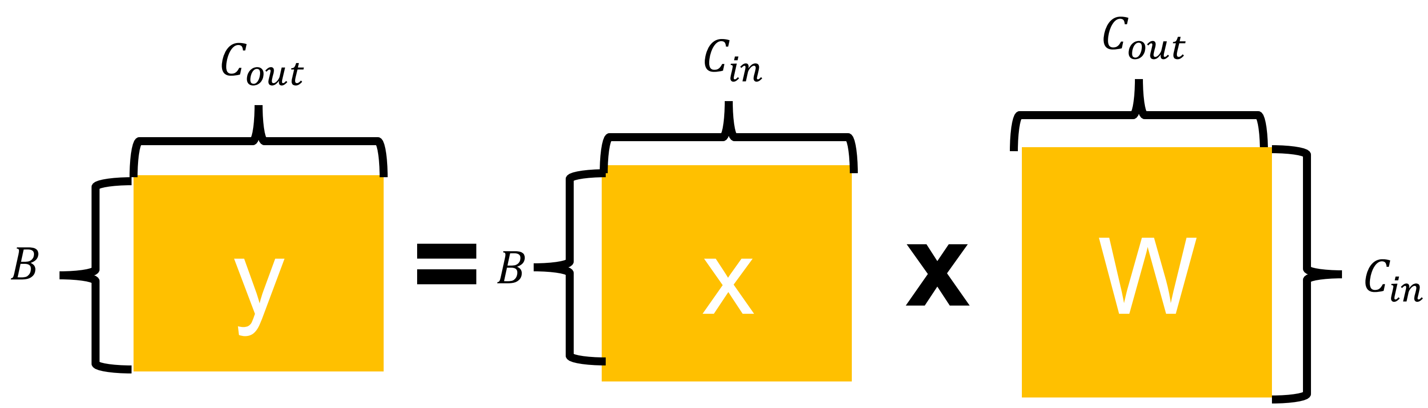


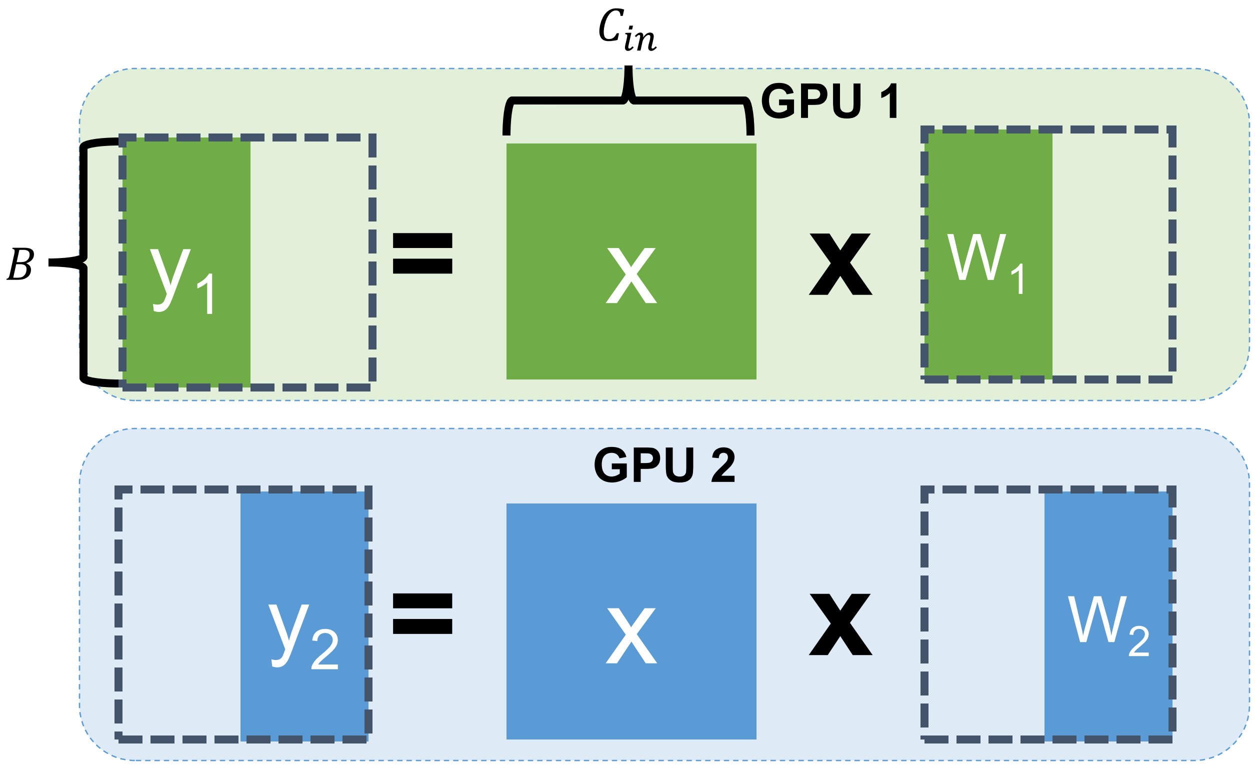
Data parallelism $y = Wx$

Forward Processing	Backward Propagation	Gradients Sync
0	0	$O(C_{out} * C_{in})$

Communication Cost of Data Parallelism

Comparing Data and Tensor Model Parallelism



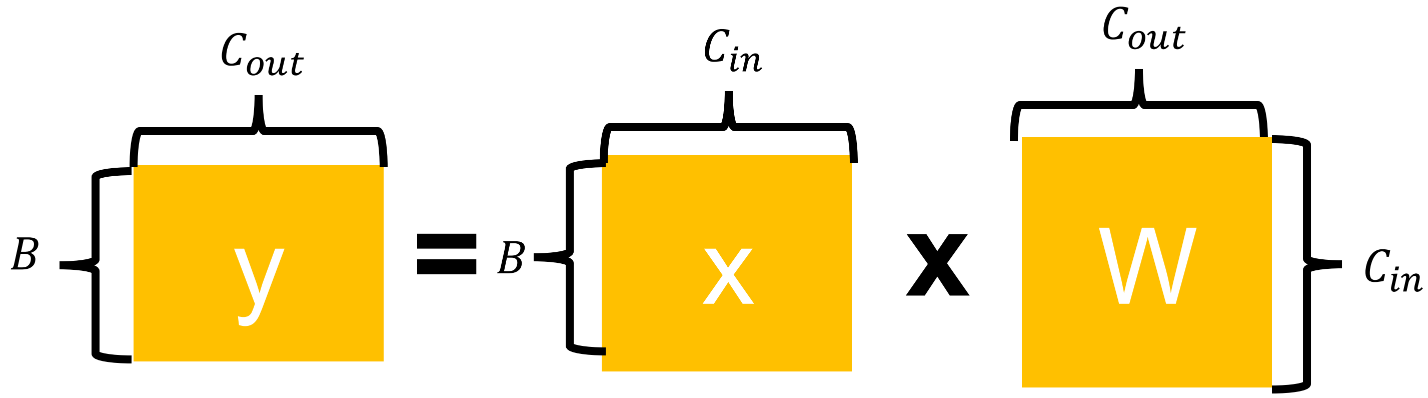


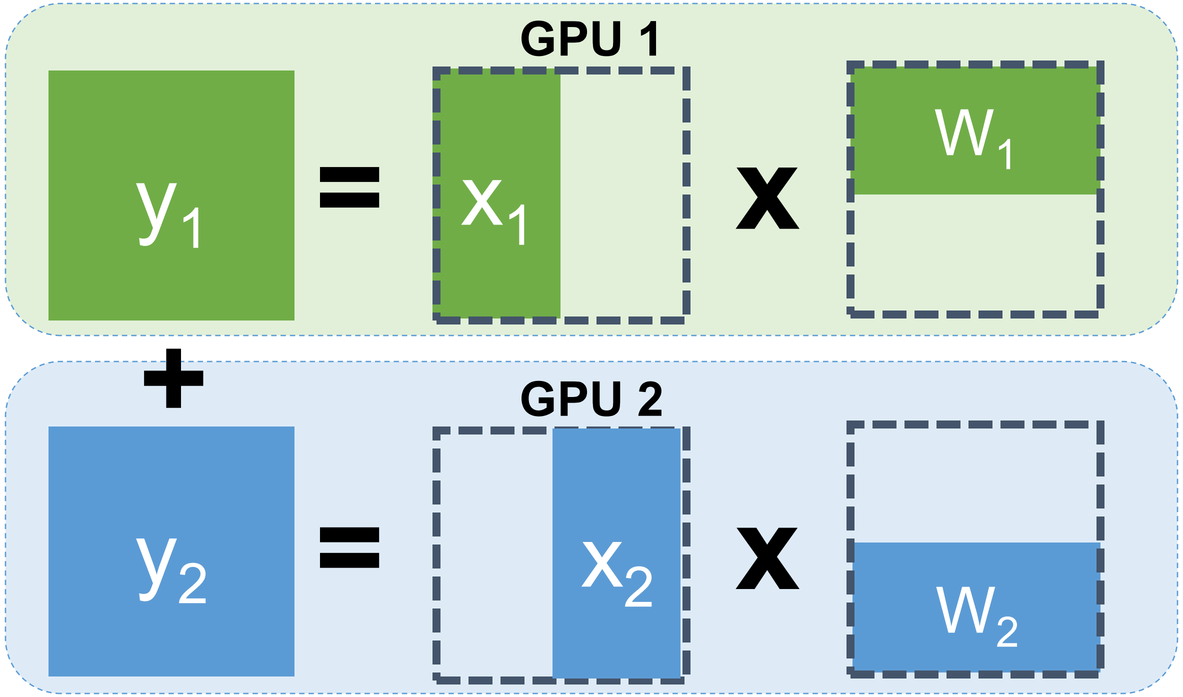
Tensor Model Parallelism (partition output)

Forward Processing	Backward Propagation	Gradients Sync
$O(B * C_{in})$	$O(B * C_{in})$	0

Communication Cost of Tensor Model Parallelism

Comparing Data and Tensor Model Parallelism





Tensor Model Parallelism (Reduce output)

$$y = y1 + y2$$

Forward Processing	Backward Propagation	Gradients Sync
$O(B * C_{out})$	$O(B * C_{out})$	0

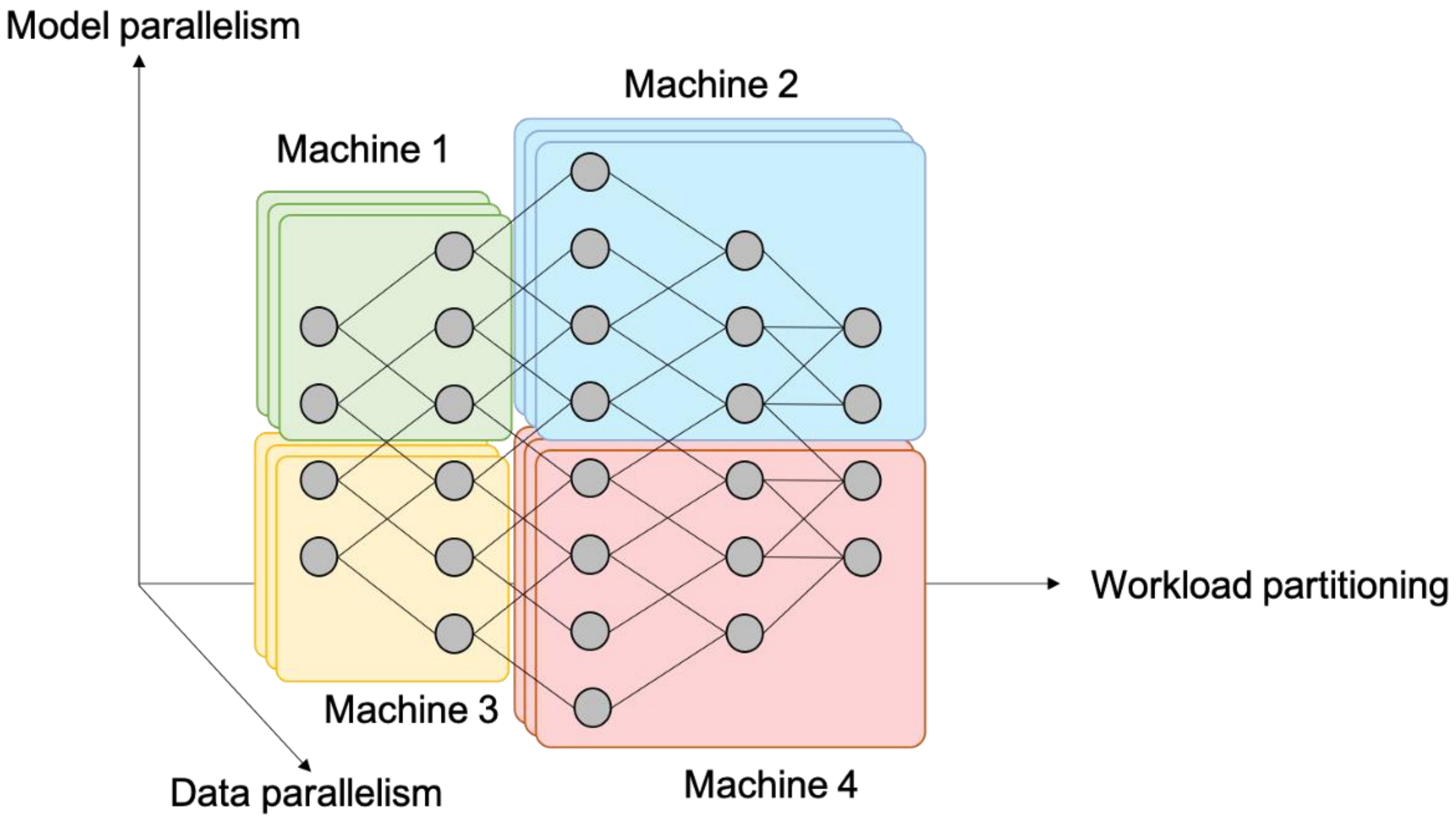
Communication Cost of Tensor Model Parallelism

Comparing Data and Tensor Model Parallelism

- Data parallelism: $O(C_{out} * C_{in})$
- Tensor model parallelism (partition output): $O(B * C_{in})$
- Tensor model parallelism (reduce output): $O(B * C_{out})$

- **The best strategy depends on the model and underlying machine**

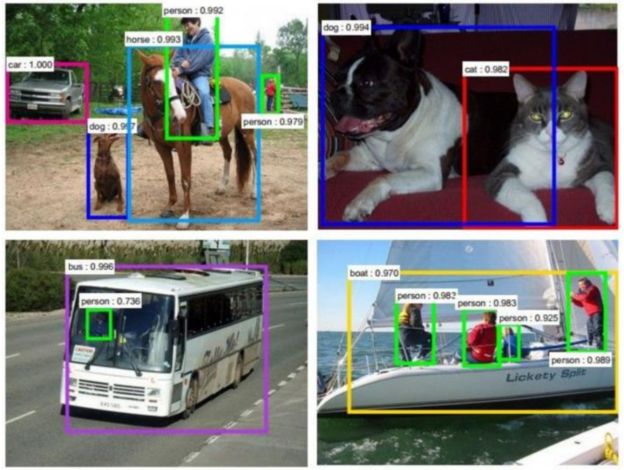
Combine Data and Model Parallelism



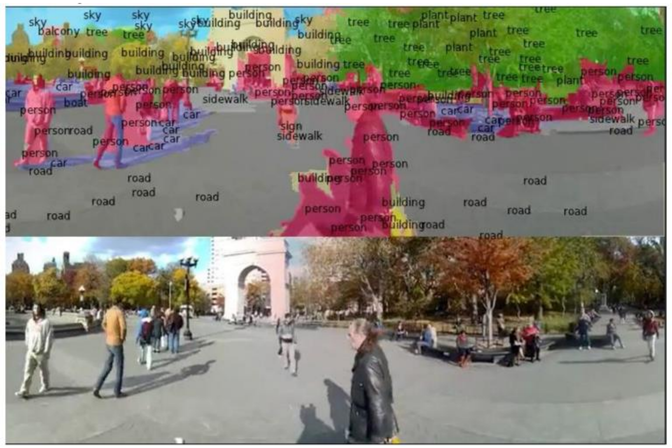
Example: Convolutional Neural Networks

Classification

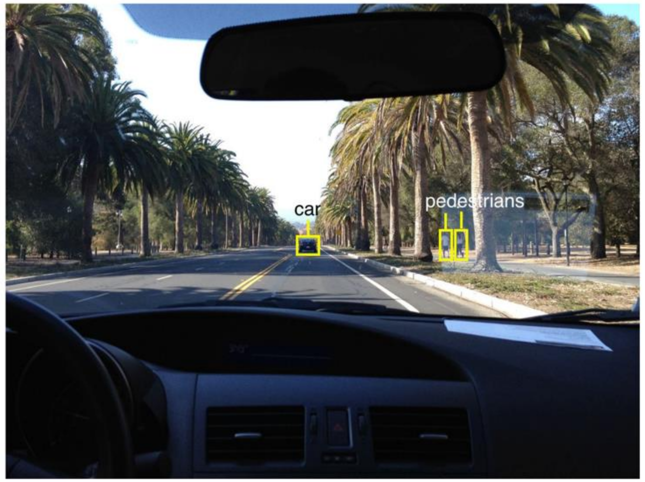
Retrieval



Detection



Segmentation

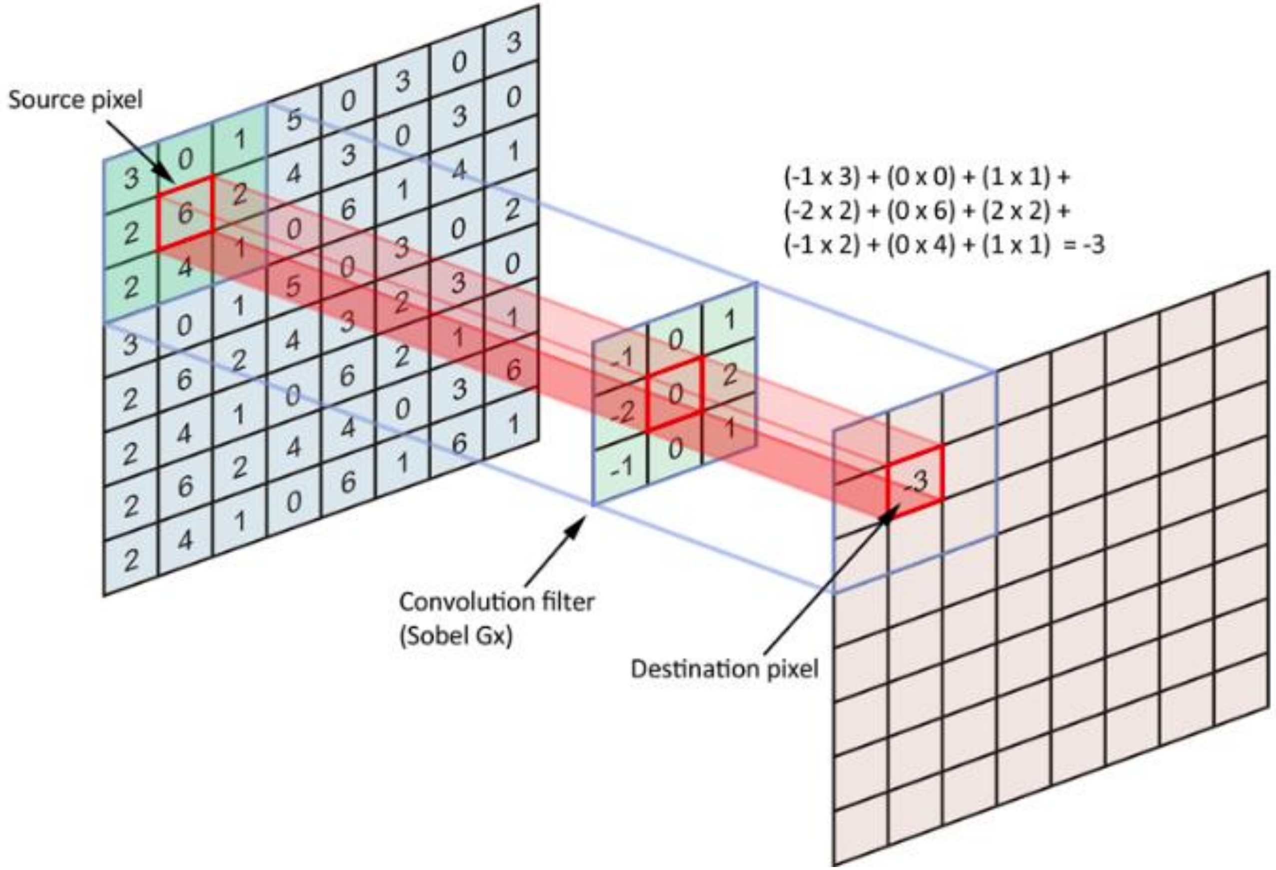


Self-Driving

Synthesis

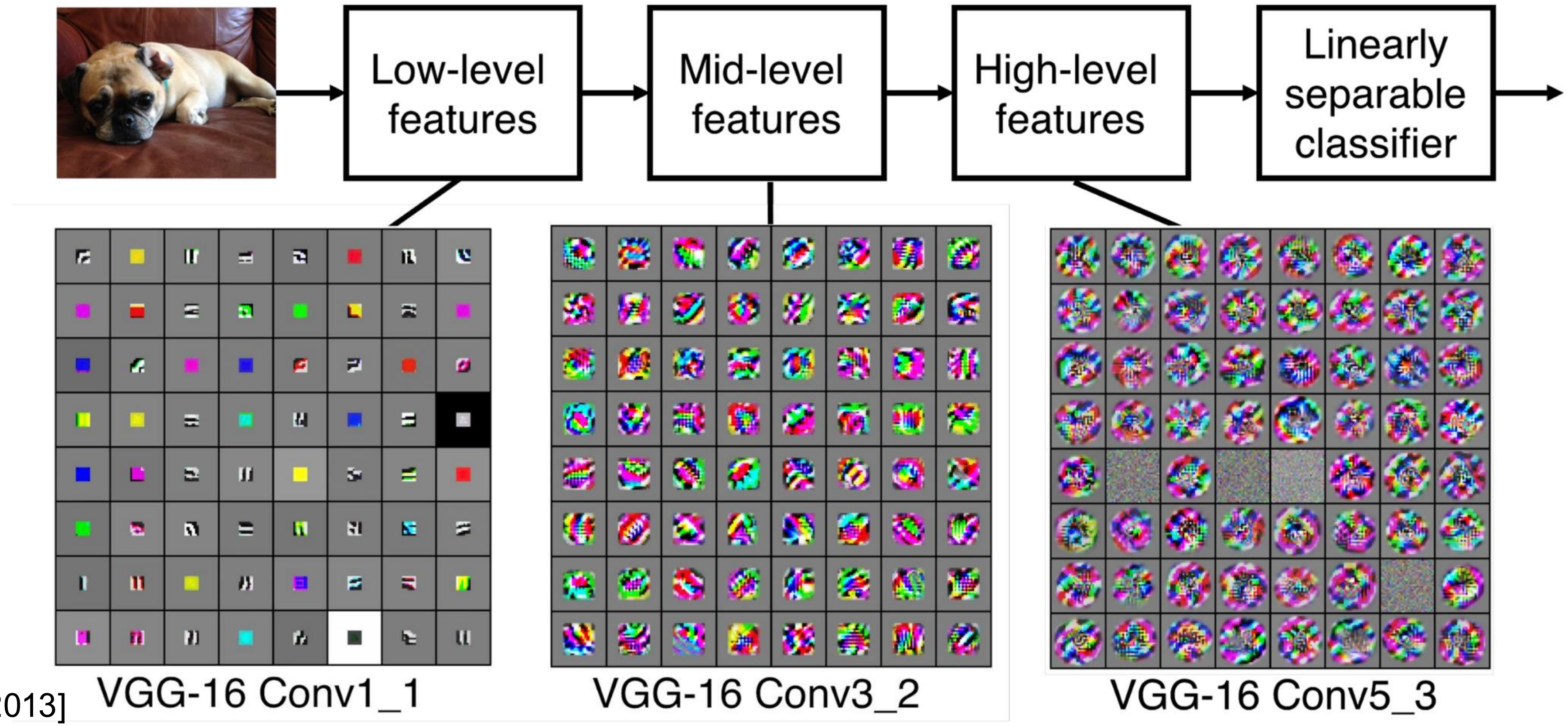
Convolution

- Convolve the filter with the image: slide over the image spatially and compute dot products



CNNs

- A sequence of convolutional layers, interspersed by pooling, normalization, and activation functions



[Zeiler and Fergus 2013]

Parallelizing Convolutional Neural Networks

- Convolutional layers
  - 90-95% of the computation
  - 5% of the parameters
  - Very large intermediate activations

Data parallelism

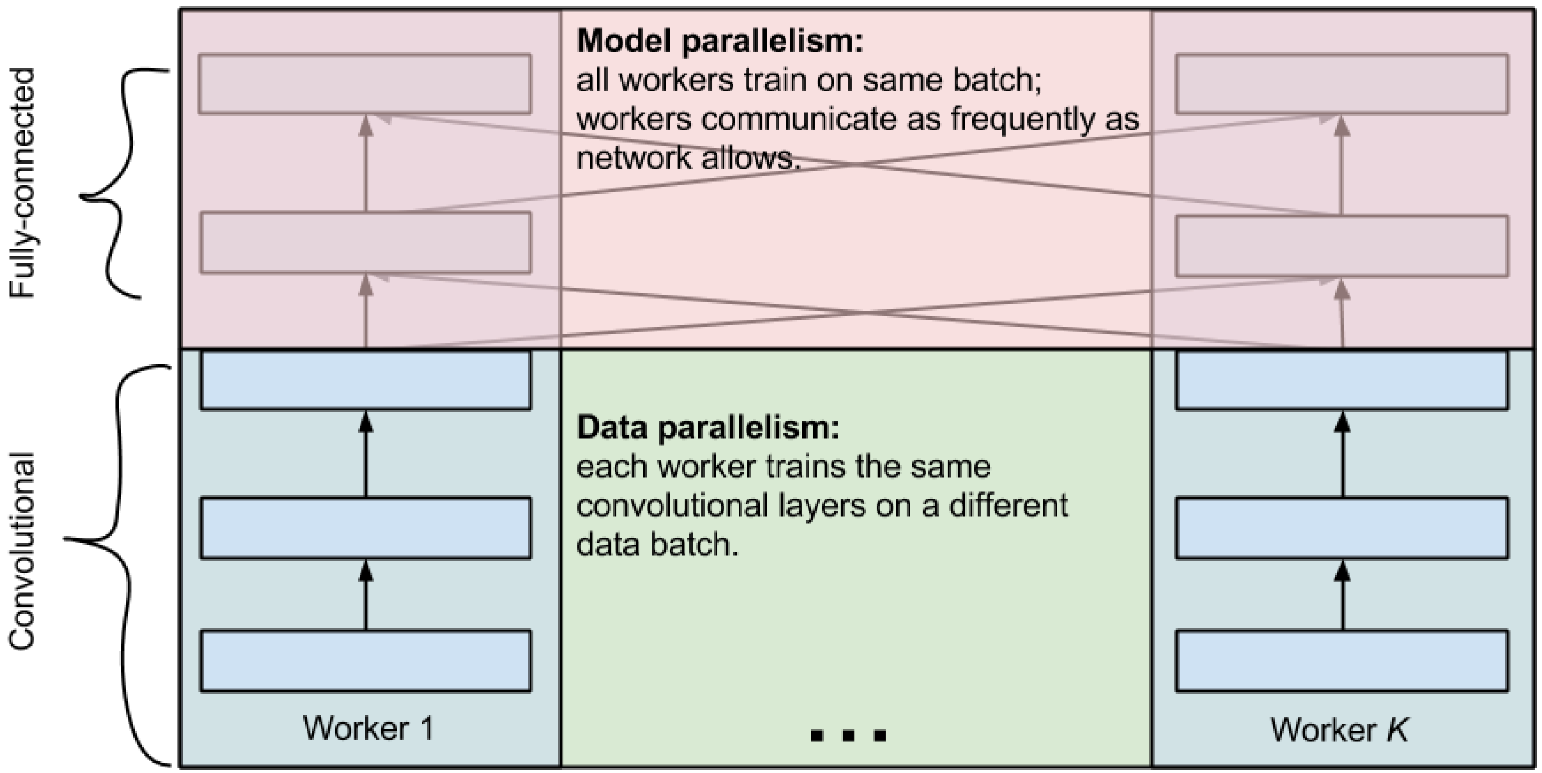
- Fully-connected layers
  - 5-10% of the computation
  - 95% of the parameters
  - Small intermediate activations

Tensor model parallelism

- **Discussion: how to parallelize CNNs?**

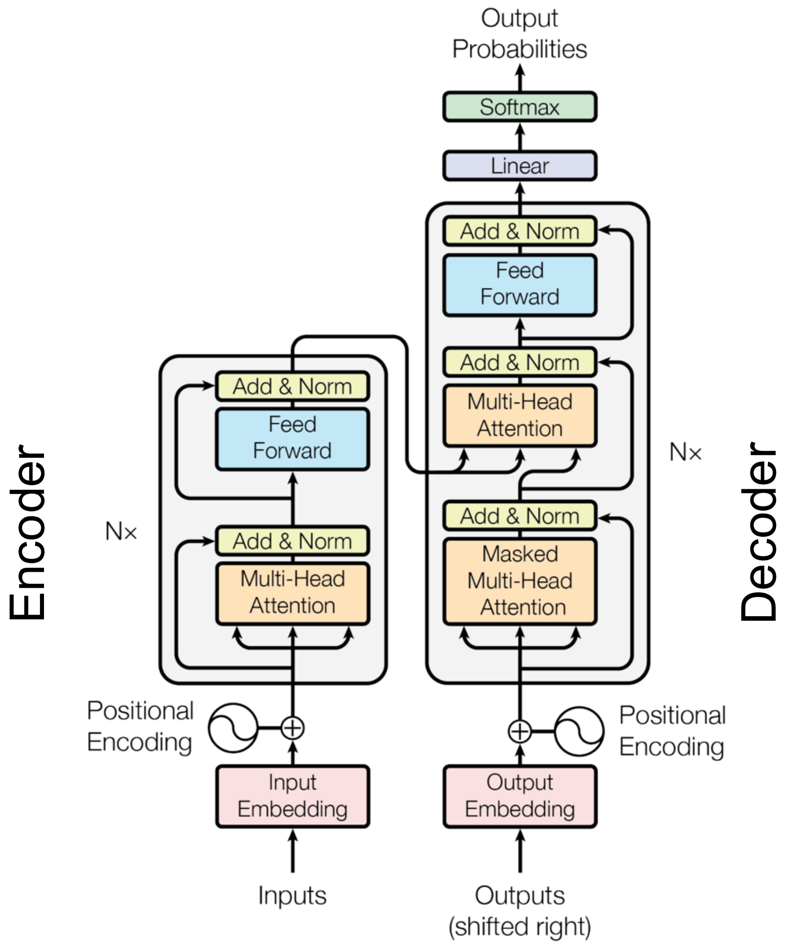
Parallelizing Convolutional Neural Networks

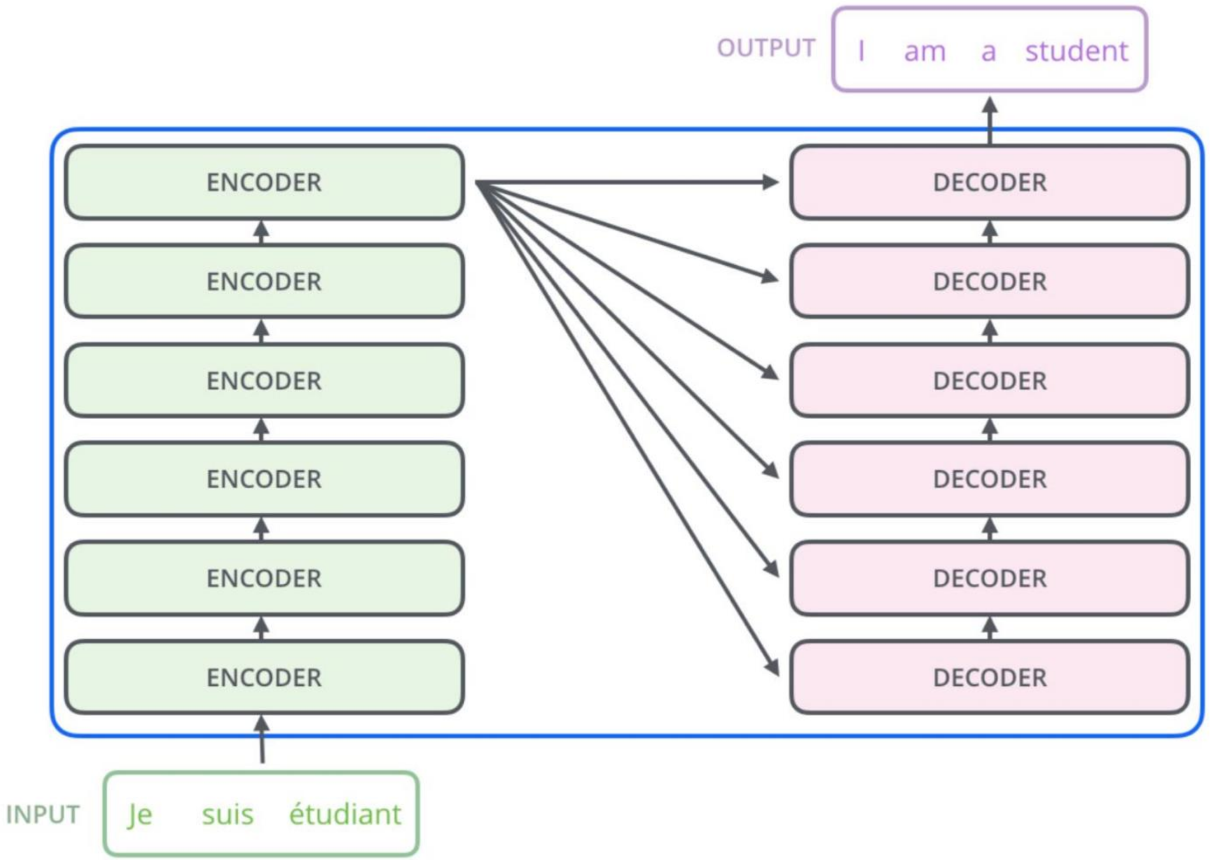
- Data parallelism for convolutional layers
- Tensor model parallelism for fully-connected layers



Example: Parallelizing Transformers

- Transformer: attention mechanism for language understanding



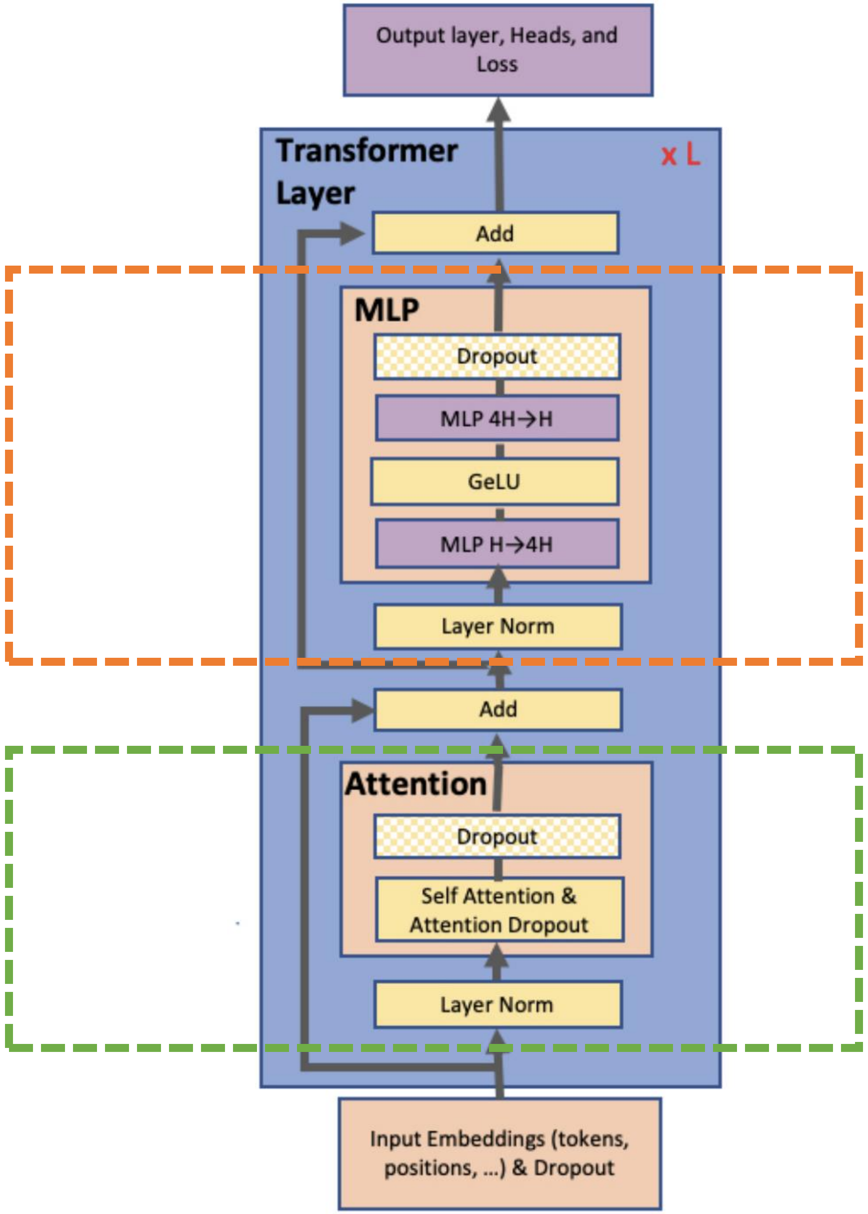


Ashish Vaswani et. al. Attention is all you need.

A Single Transformer Layer

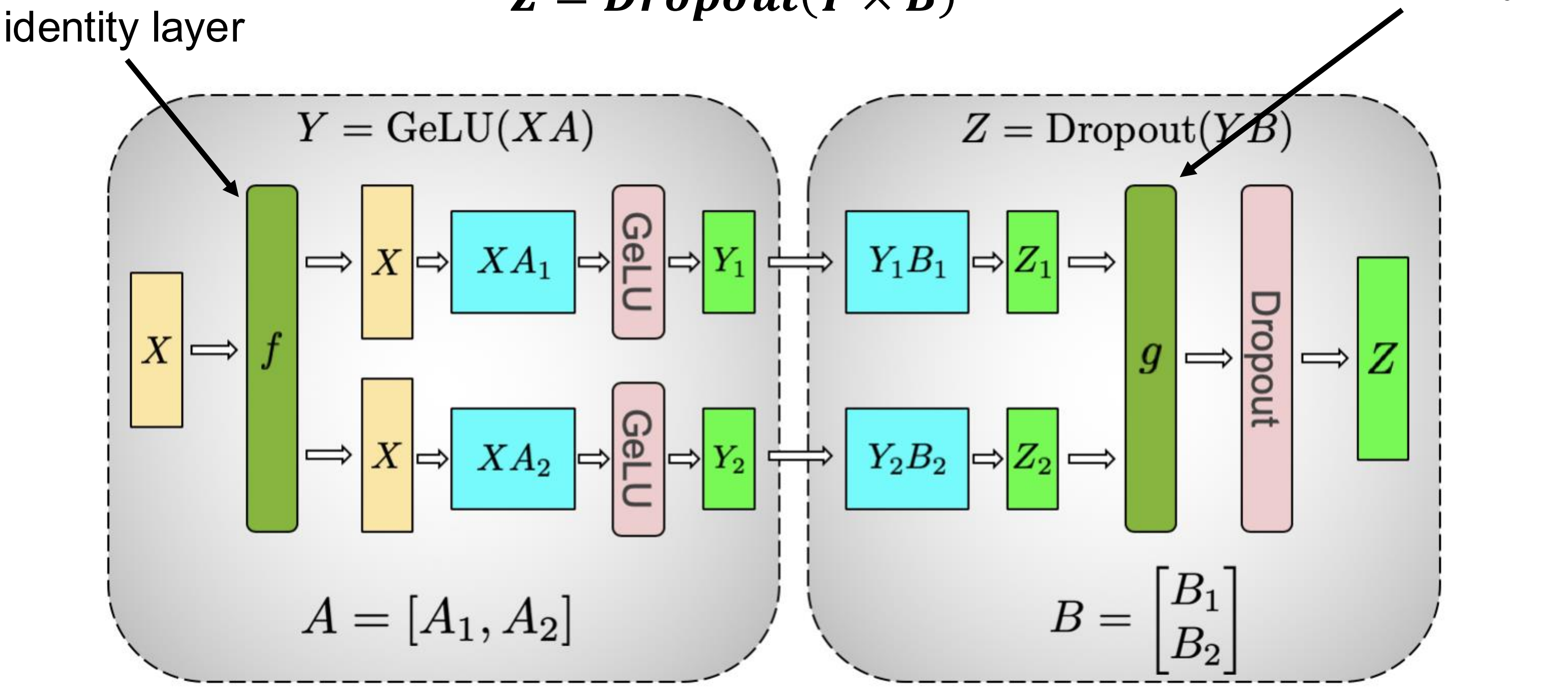
Fully-Connected Layers

Self-Attention Layers



Parallelizing Fully-Connected Layers in Transformers

$$Y = GeLU(X \times A)$$
$$Z = Dropout(Y \times B)$$

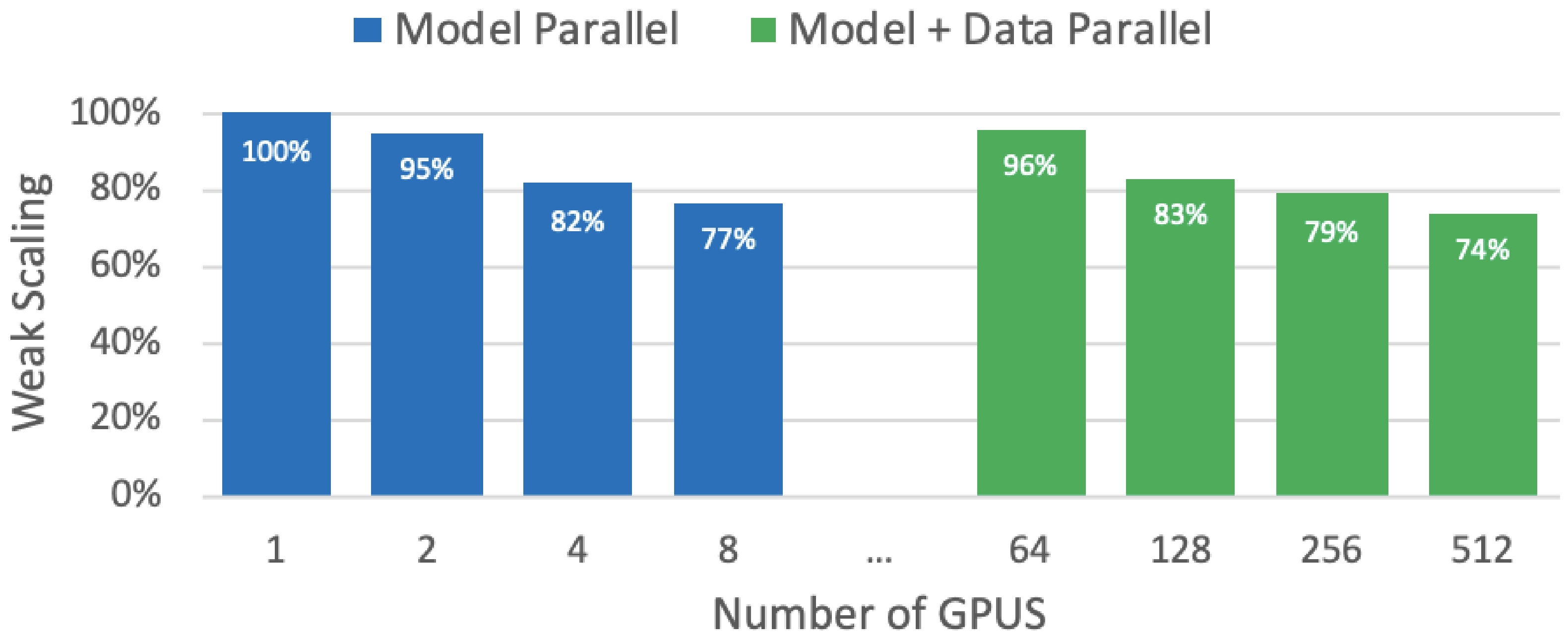


Tensor model parallelism
(partition output)

Tensor model parallelism
(reduce output)

Megatron-LM: Training Multi-Billion Parameter Language Models Using Model Parallelism.

Parallelizing Transformers



Scale to 512 GPUs by combining data and model parallelism

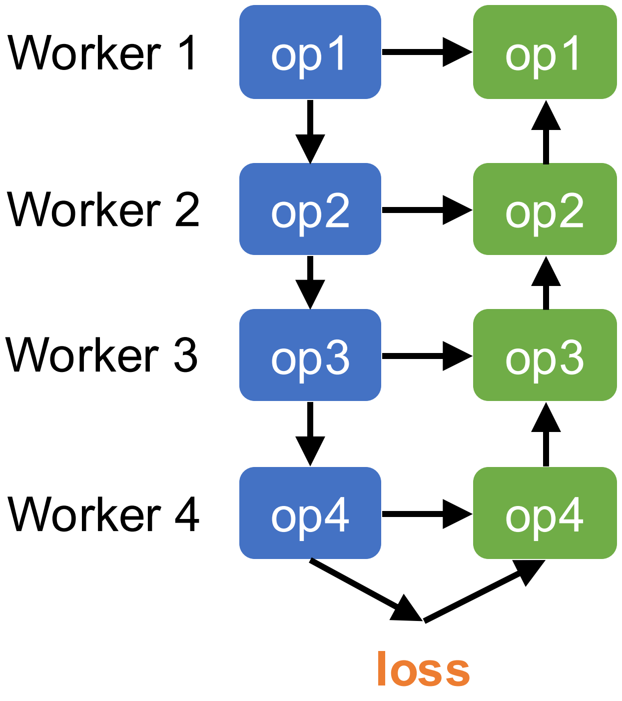
Megatron-LM: Training Multi-Billion Parameter Language Models Using Model Parallelism.

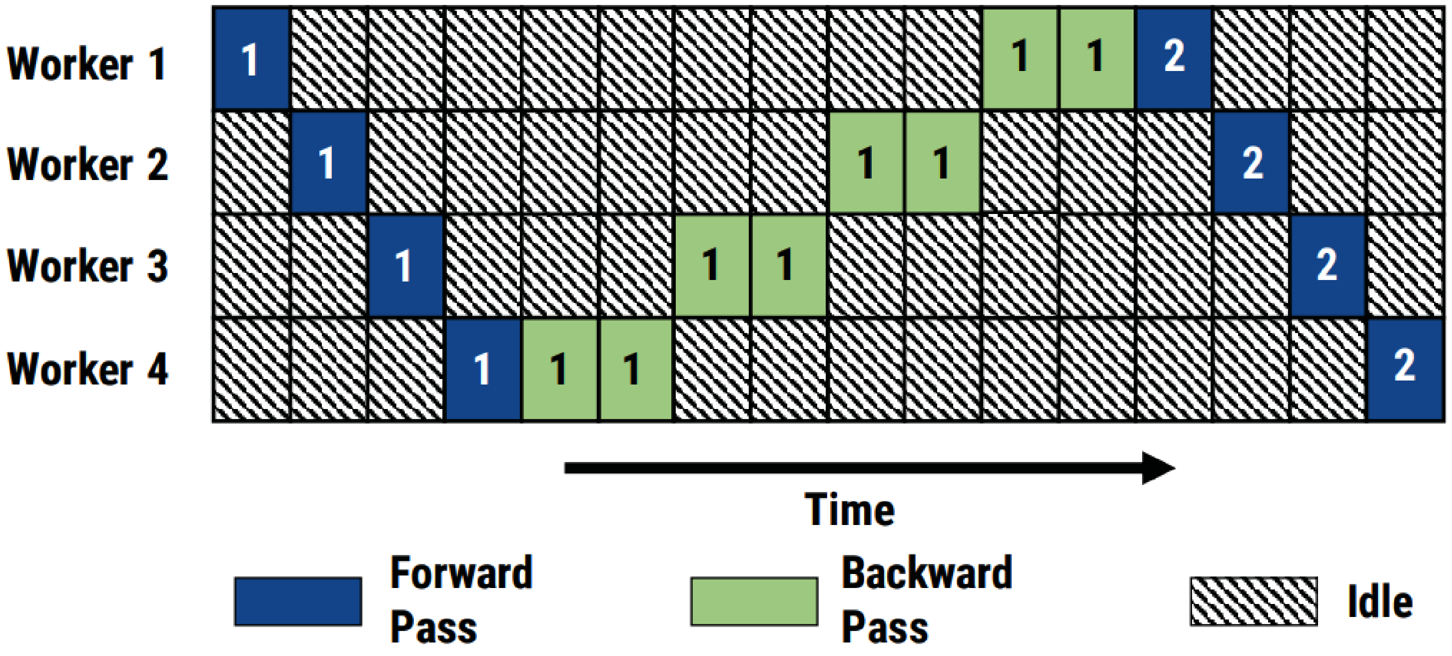
How to parallelize DNN Training?

- Data parallelism
- Model parallelism
  - Tensor model parallelism
  - **Pipeline model parallelism**

An Issue with Model Parallelism

- Under-utilization of compute resources
- Low overall throughput due to resource utilization

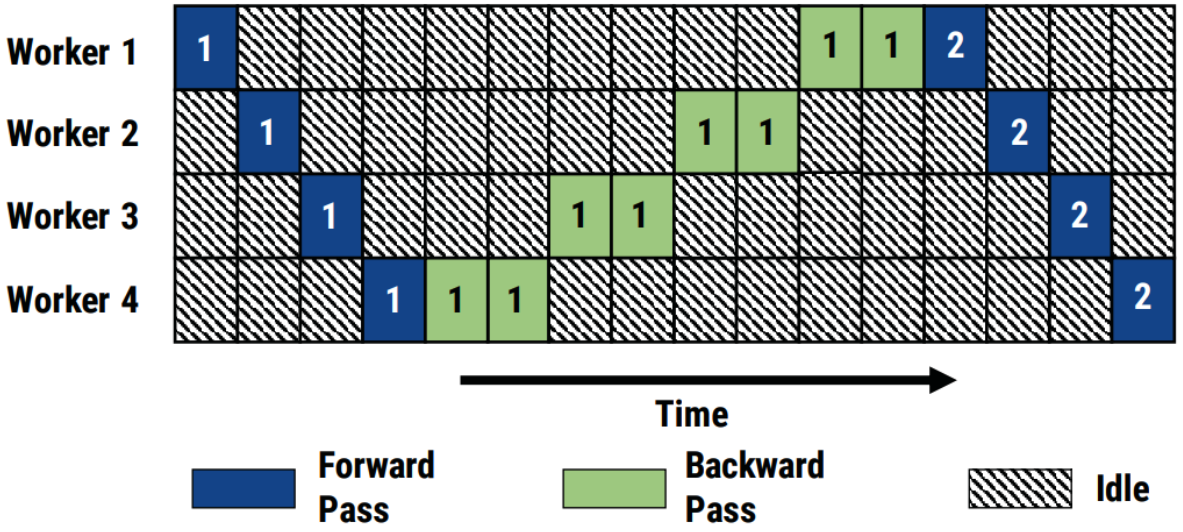




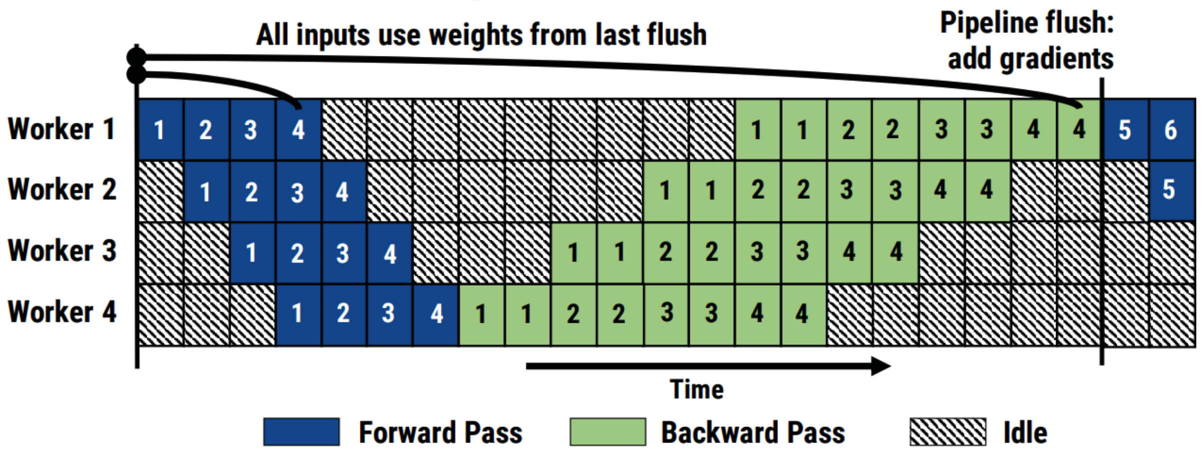
Pipeline Model Parallelism

- **Mini-batch**: the number of samples processed in each iteration
- Divide a mini-batch into multiple **micro-batches**
- Pipeline the forward and backward computations across micro-batches

Model Parallelism

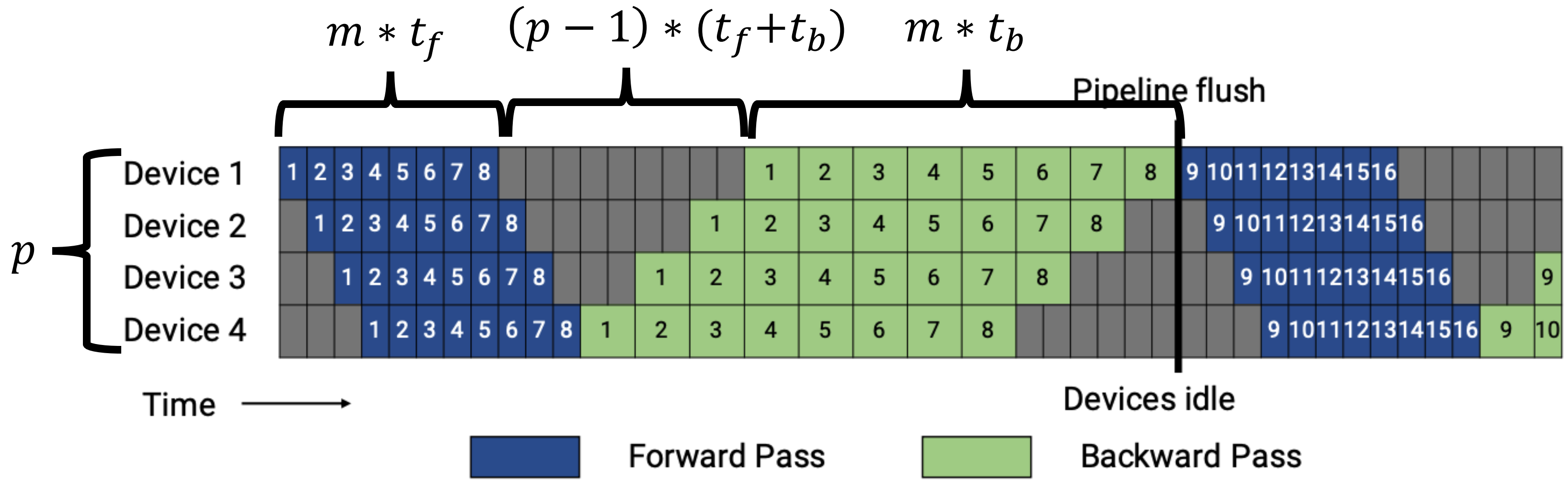


Pipeline Model Parallelism



Pipeline Model Parallelism: Device Utilization

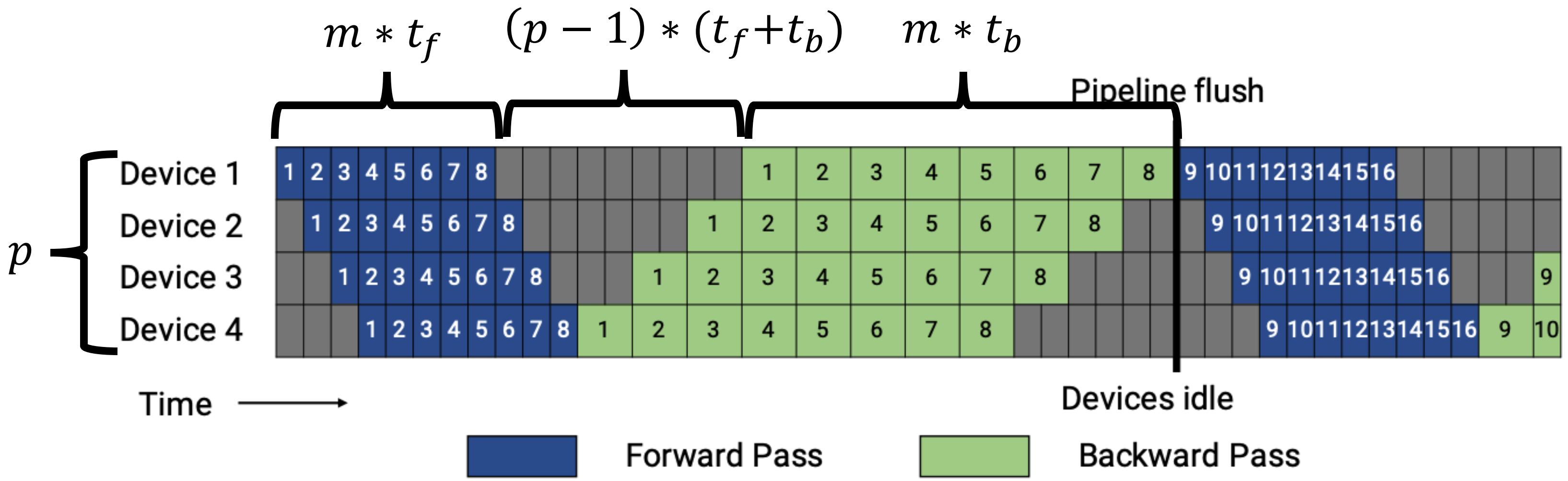
- m : micro-batches in a mini-batch
- p: number of pipeline stages
- All stages take t_f/ t_b to process a forward (backward) micro-batch



$$\boldsymbol{BubbleFraction = \frac{(p-1) * (t_f+t_b)}{m * t_f + m * t_b} = \frac{p-1}{m}}$$

Improving Pipeline Parallelism Efficiency

- m : number of micro-batches in a mini-batch
  - Increase mini-batch size or reduce micro-batch size
  - Caveat: large mini-batch sizes can lead to accuracy loss; small micro-batch sizes reduce GPU utilization
- p: number of pipeline stages
  - Decrease pipeline depth
  - Caveat: increase stage size

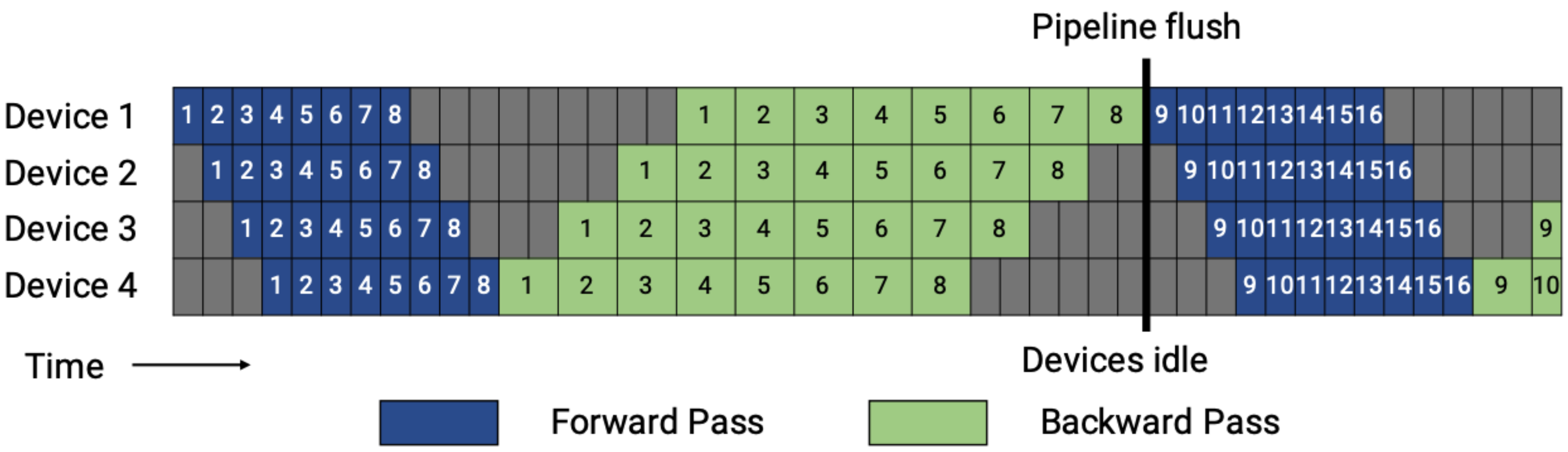


$$BubbleFraction = \frac{(p-1) * (t_f + t_b)}{m * t_f + m * t_b} = \frac{p-1}{m}$$

GPipe: Efficient Training of Giant Neural Networks using Pipeline Parallelism

Pipeline Model Parallelism: Memory Requirement

- An issue: we need to keep the intermediate activations of **all micro-batches** before back propagation



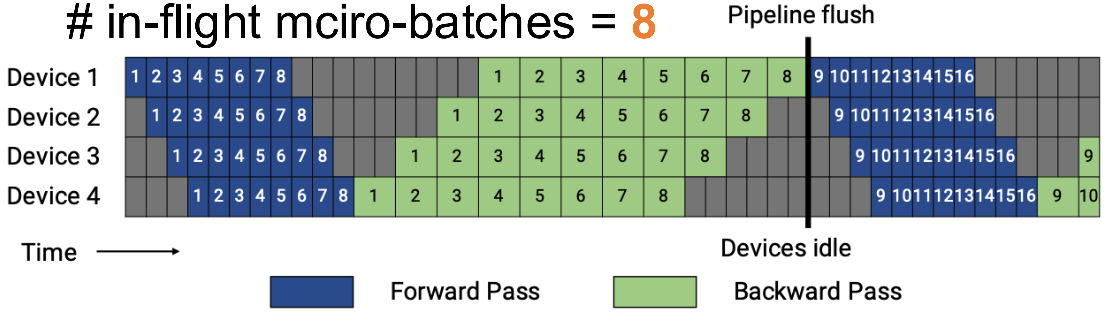
Can we improve the pipeline schedule to reduce memory requirement?

Pipeline Parallelism with 1F1B Schedule

- One-Forward-One-Backward in the steady state
- Limit the number of in-flight micro-batches to the pipeline depth
- **Reduce memory footprint of pipeline parallelism**
- **Doesn't reduce pipeline bubble**

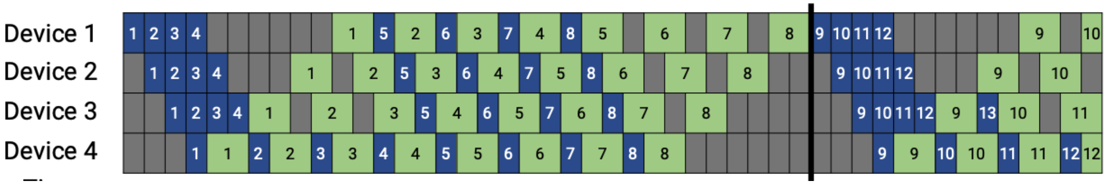
Can we reduce pipeline bubble?

in-flight mciro-batches = 8



Pipeline parallelism with GPipe's schedule

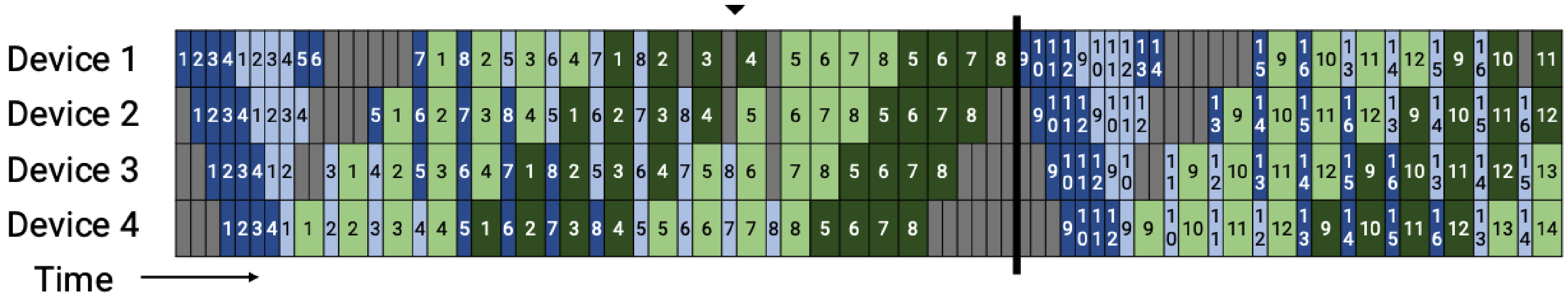
in-flight mciro-batches = 4



Pipeline parallelism with 1F1B schedule

Pipeline Parallelism with Interleaved 1F1B Schedule

- Further divide each stage into v sub-stages
- The forward (backward) time of each sub-stage is $\frac{t_f}{v}$ $(\frac{t_b}{v})$



Each device is assigned two chunks. Dark colors show the first chunk and light colors show the second chunk.

$$\boldsymbol{BubbleFraction} = \frac{(p-1) * \frac{(t_f + t_b)}{v}}{m * t_f \; + m * t_b} = \frac{1}{v} * \frac{p-1}{m}$$

Reduce bubble time at the cost increased communication

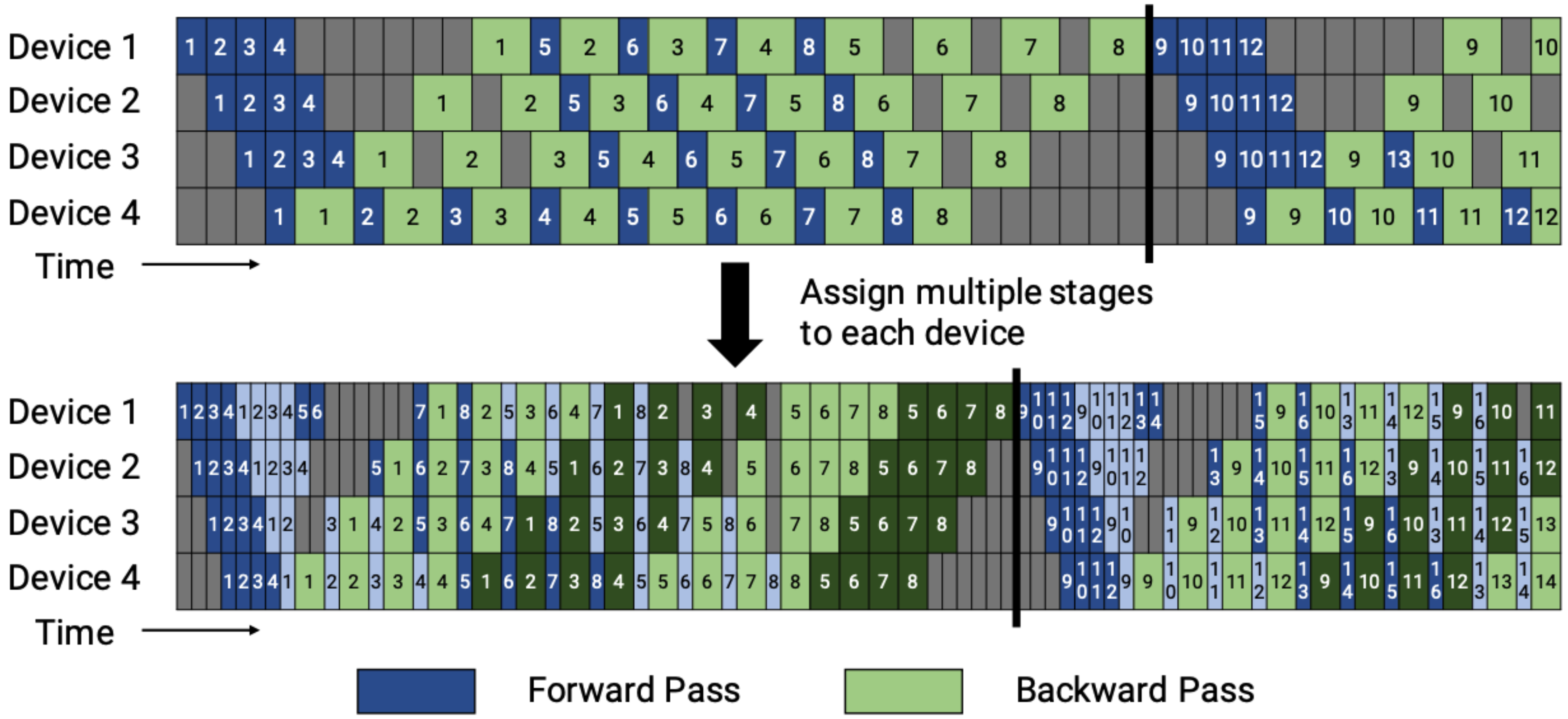
Pipeline Parallelism with Interleaved 1F1B Schedule

Pipeline parallelism with 1F1B Schedule

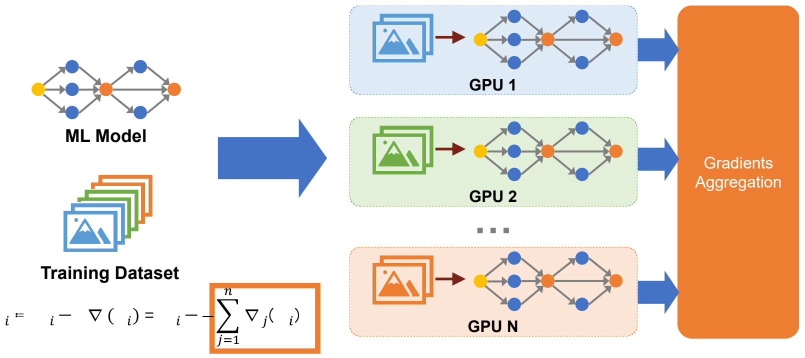
$$BubbleFraction = \frac{p-1}{m}$$

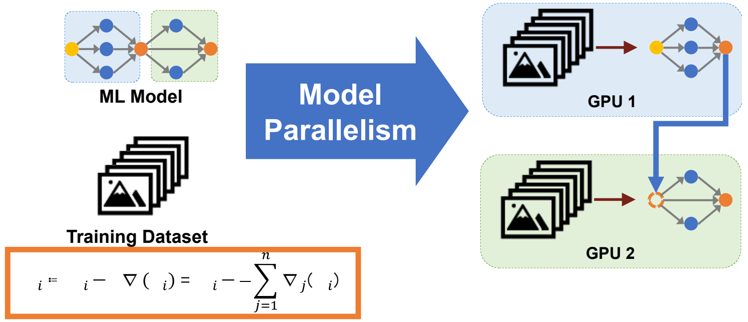
Pipeline parallelism with interleaved 1F1B Schedule

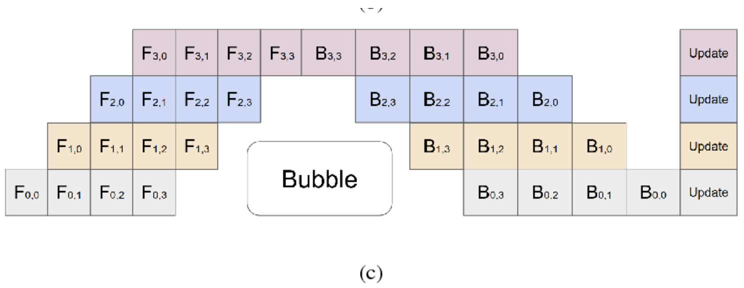
$$BubbleFraction = \frac{1}{v} * \frac{p-1}{m}$$



Summary: Comparing Data/Tensor Model/Pipeline Model Parallelism

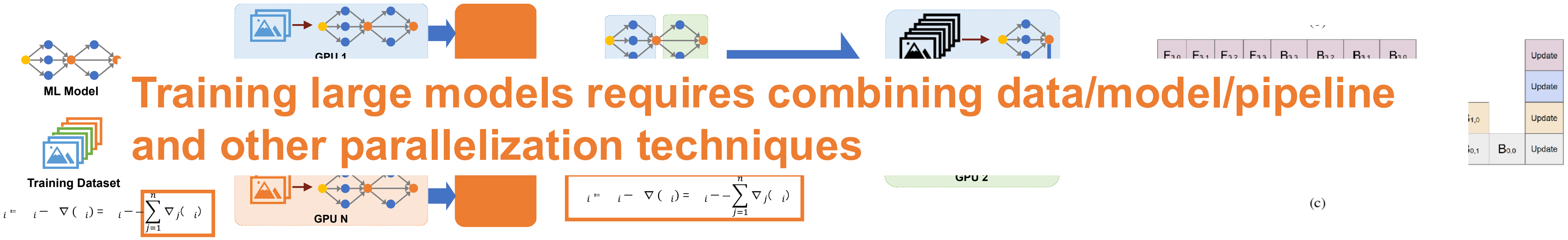






	Data Parallelism	Tensor Model Parallelism	Pipeline Model Parallelism
Pros	✓ Massively parallelizable ✓ Require no communication during forward/backward	✓ Support training large models ✓ Efficient for models with large numbers of parameters	✓ Support large-batch training ✓ Efficient for deep models
Cons	❖ Do not work for models that cannot fit on a GPU ❖ Do not scale for models with large numbers of parameters	❖ Limited parallelizability; cannot scale to large numbers of GPUs ❖ Need to transfer intermediate results in forward/backward	❖ Limited utilization: bubbles in forward/backward

Summary: Comparing Data/Tensor Model/Pipeline Model Parallelism



Training large models requires combining data/model/pipeline and other parallelization techniques

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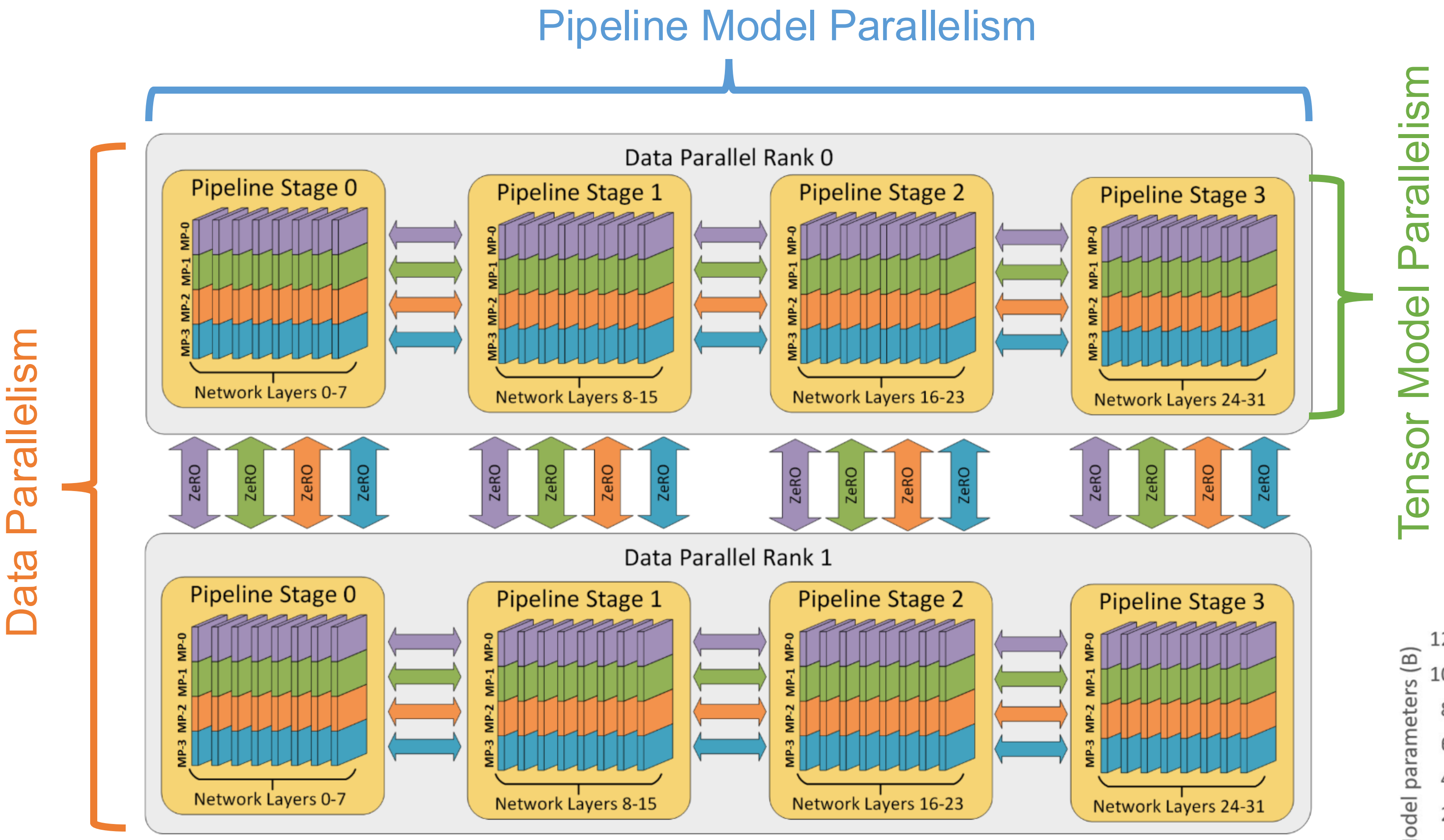
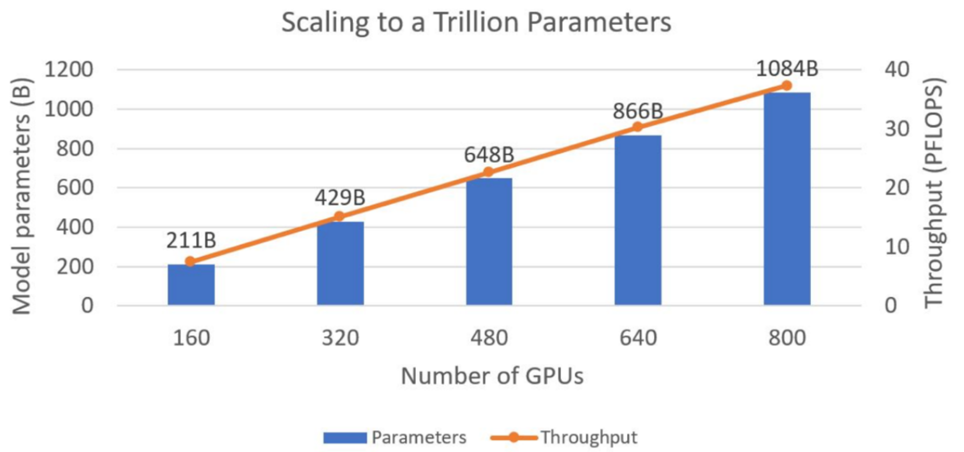
Example: 3D parallelism in DeepSpeed





https://www.microsoft.com/en-us/research/blog/deepspeed-extreme-scale-model-training-for-everyone/