

This lecture is being recorded

18-452/18-750
Wireless Networks and Applications
Lecture 22: Localization

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<http://www.cs.cmu.edu/~prs/wirelessS21/>

Outline

- **Properties of localization procedures**
- **Approaches**
 - » Proximity
 - » Trilateration and triangulation (GPS)
 - » Finger printing (RADAR)
 - » Hybrid systems

Properties of localization procedures

- **Physical position vs data types**
 - **Reference systems**
 - **Processing: localized vs centralized**
 - **Data quality**
 - » Accuracy and precision
 - » Scale
 - **Deployment aspects**
 - » Limitations
 - » Cost
- ➔ **Very diverse systems – lots of research**

Data types

- **Point locations in terms of coordinates:**
 - » *physical* or *geometric locations*
 - » **GPS: latitude and longitude, height**
 - » **Cartesian coordinate system based on three orthogonal planes**
- **Extended region locations given by names:**
 - » *symbolic locations*
 - » **CMU, Wean Hall, room 8202**

Location-awareness

- **Location model:**
data structure that organizes locations
- **Location-based routing**
 - » symbolic location model
 - » geometric location model
 - » hybrid location model

Examples

- » **symbolic location model:**
address hierarchy
DH.Floor2.2105
- » **geometric location model:**
GPS coordinate
(12.3456°N, 123.456°E)
- » **hybrid location model:**
combination of address and coordinate
DH.Floor2.2105.Seat(0,4)

Quality of Position Information

Positioning accuracy:

**largest distance
between an
estimated position
and the true
position**

**Only pairs of precision
and accuracy make sense**

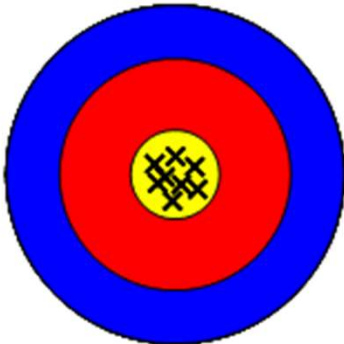
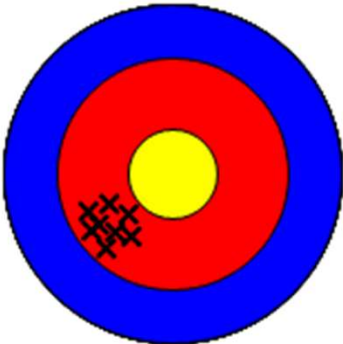

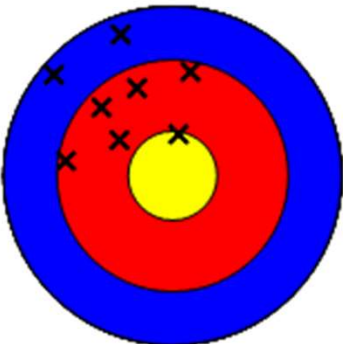
Precision:

**the ratio with which
a given accuracy is
reached, averaged
over many
repeated attempts**

Example:

**average error of less
than 20cm
in 95% of cases**

Precision vs. Accuracy

	Accurate	Inaccurate (systematic error)
Precise		
Imprecise (reproducibility error)		

Approaches

- **Proximity: estimate distance between two nodes**
- **Trilateration and triangulation**
 - » using elementary trigonometric properties: a triangle is completely determined,
 - if two angles and a side length are known
 - if the lengths of all three sides are known
 - » infer a 3d position from information about two triangles
- **Fingerprinting (scene analysis)**
 - » using radio characteristics as fingerprint to identify it
- **Hybrid methods: multiple sources of information**

Proximity and Distance

- **Binary nearness: using finite range of wireless communication and/or threshold**
 - » within range of a beacon signal from a source with known position
 - » yields region locations, e.g.: cell in cellular network
- **Distance measurement (ranging)**
 - » Received signal strength
 - » Time of flight (time of arrival)
 - » Time difference of arrival

Measuring Location: Trigonometry Basics

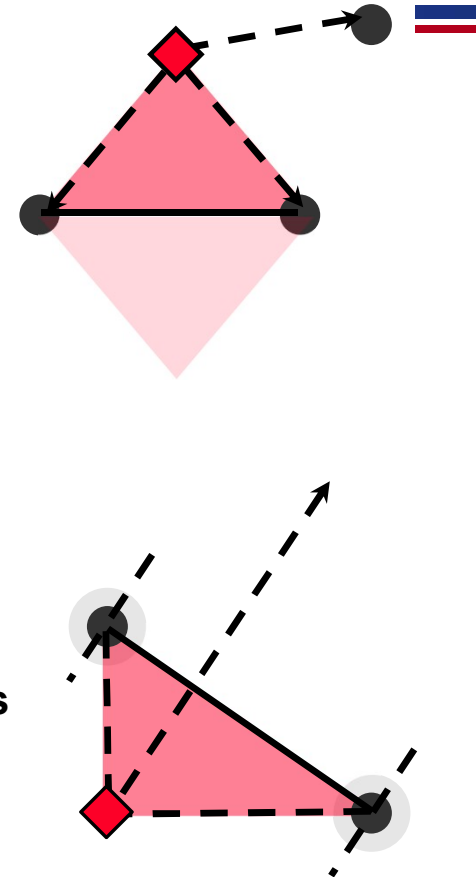
- **Triangles in a plane**

- » **Lateralation:** distance measurement to known reference points

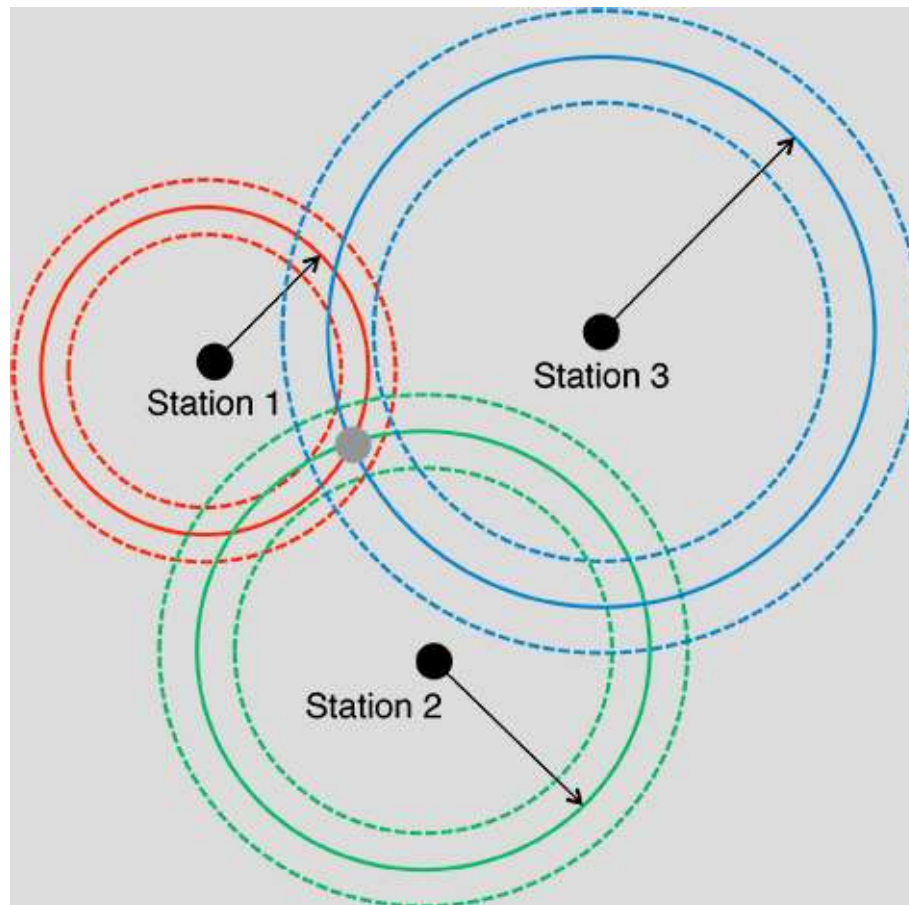
- a triangle is fully determined by the length of its sides
- Time of Flight (e.g. GPS, Active Bat)
- Attenuation (e.g. RSSI)

- » **Angulation:** measuring the angle with respect to two known reference points and a reference direction or a third point

- a triangle is fully determined by two angles and one side as shown
- Phased antenna arrays
- aircraft navigation (VOR)



Trilateration



Peter A. Steenkiste, CMU

<http://gpsworld.com/innovation-where-are-we/>

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Mathematical Background

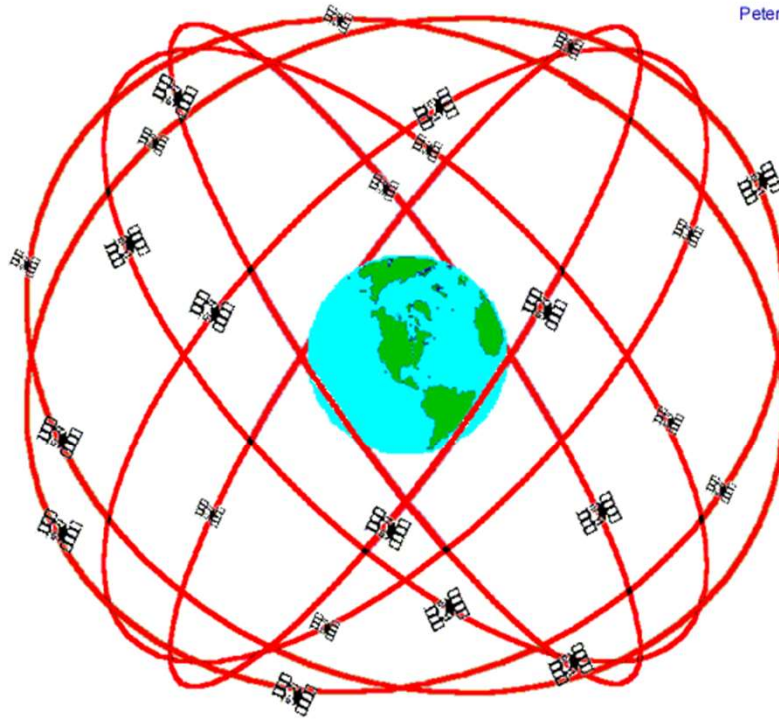
- **Computing positions between three known positions (x_i, y_i) and an unknown position (x_u, y_u) given distances r_i btw (x_i, y_i) and (x_u, y_u)**
- **Yields three equations $(x_i - x_u)^2 + (y_i - y_u)^2 = r_i^2$**
- **Linear equations by subtracting 3rd from 1st and 2nd: quadratic terms x_u^2 and y_u^2 disappear**
 - » $2(x_3 - x_1)x_u + 2(y_3 - y_1)y_u = (r_1^2 - r_3^2) - (x_1^2 - x_3^2) - (y_1^2 - y_3^2)$
 - » $2(x_3 - x_2)x_u + 2(y_3 - y_2)y_u = (r_2^2 - r_3^2) - (x_2^2 - x_3^2) - (y_2^2 - y_3^2)$
- **In 3D: yields two points**
- **Positioning with imprecise information:**
 - » Add redundancy: over determined solution
 - » Least squares estimates

GPS

- **Radio-based navigation system developed by DoD**
 - » Initial operation in 1993
 - » Fully operational in 1995
- **System is called NAVSTAR**
 - » NAVigation with Satellite Timing And Ranging
 - » Referred to as GPS
 - » Has been improved over time
- **Series of 24 (now 32) satellites, in 6 orbital planes**
- **Works anywhere in the world, 24 hours a day, in all weather conditions and provides:**
 - » Location or positional fix
 - » Velocity, direction of travel
 - » Accurate time

GPS Constellation

Peter H. Dana 9/22/98



GPS Nominal Constellation
24 Satellites in 6 Orbital Planes
4 Satellites in each Plane
20,200 km Altitudes, 55 Degree Inclination

- **24 satellites are needed to guarantee that 4 are always visible everywhere**
- **Extra satellites provide redundancy**
 - » Deal with maintenance, replacement, ...

GPS involves 5 Basic Steps

- **Satellite Ranging**
 - » Determining distance from satellite
- **Trilateration**
 - » Intersection of spheres
- **Timing**
 - » Why consistent, accurate clocks are required
- **Positioning**
 - » Knowing where satellite is in space
- **Correction of errors**
 - » Correcting for ionospheric and tropospheric delays

How GPS works?

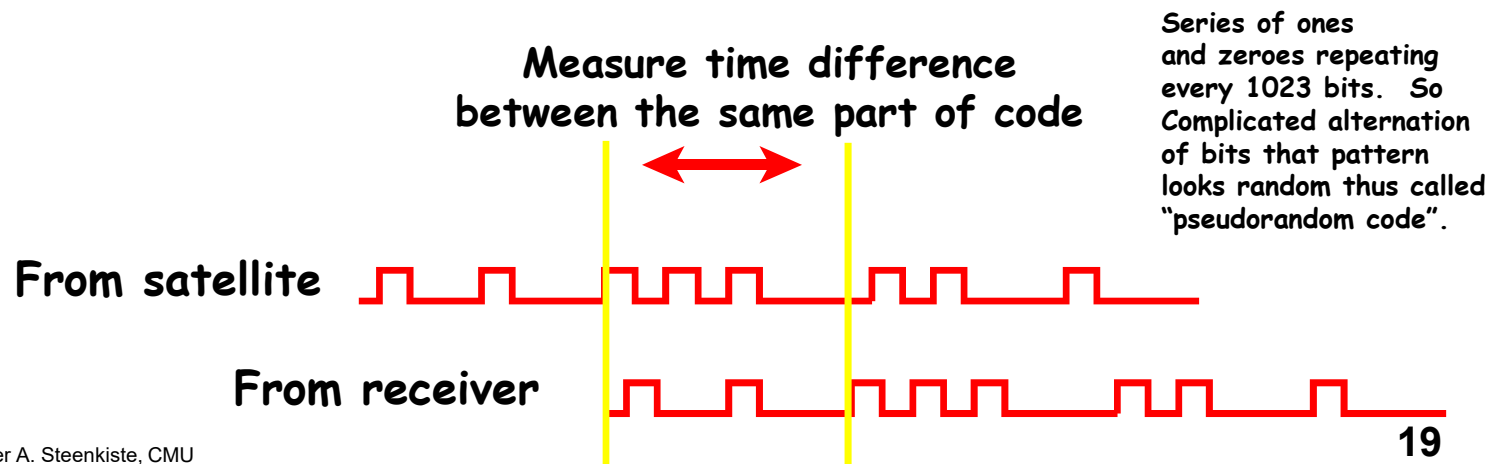
- **Range from each satellite calculated**
range = time delay X speed of light
- **Technique called trilateration is used to determine your position or “fix”**
 - » Intersection of spheres as described earlier
- **At least 3 satellites required for 2D fix**
- **However, 4 satellites are used**
 - » The 4th satellite used to calculate drift of clock in GPS receivers relative to that of the satellites
 - » Yields much better accuracy and provides 3D fix

Satellite Positions

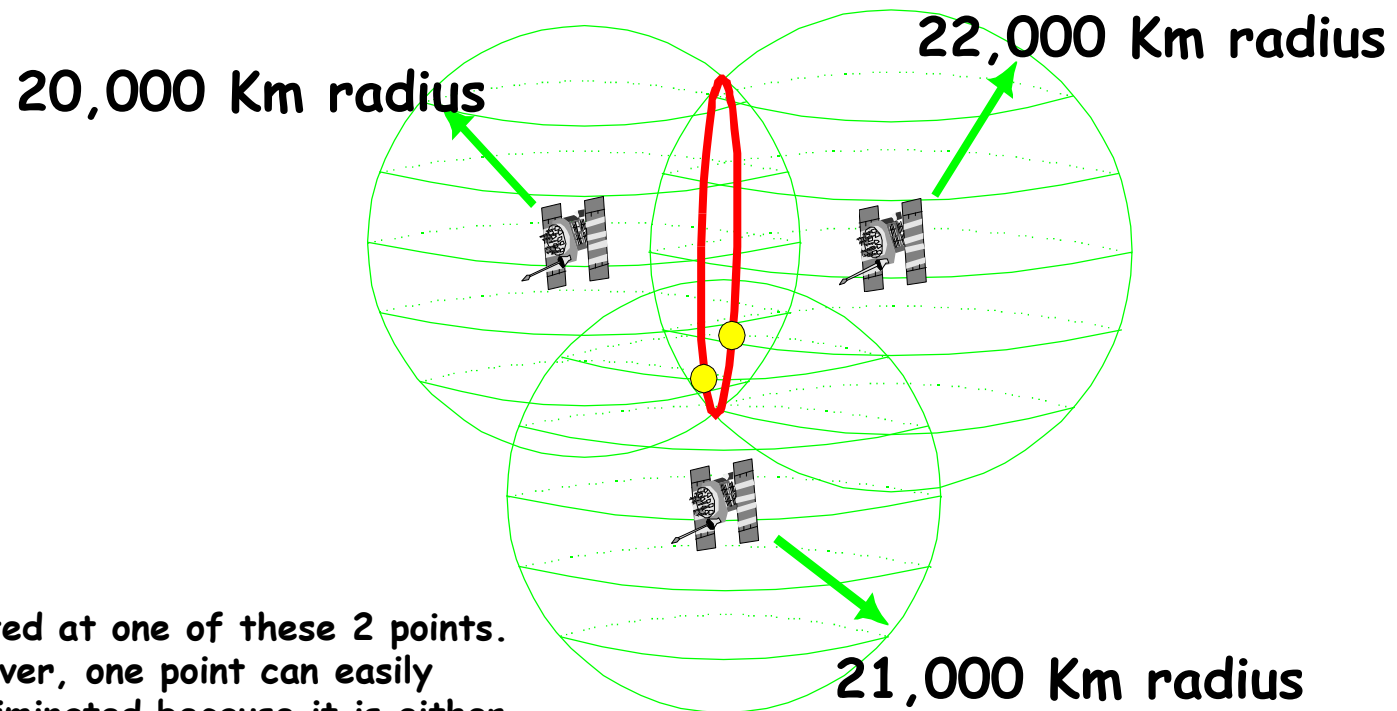
- **Each satellite has an atomic clock that keeps time very accurately**
 - » Satellites synchronize their clocks
 - » Also periodically synchronize with the true time maintained on earth
- **Satellites also know their location very accurately**

Determining Range

- Each satellite periodically generates a pseudo random code
 - » Receivers also locally generate the codes in synchronized fashion
- Receivers measure Time of Arrival (TOA) of codes
- Transmission includes Time of Transmission (TOT) of code and the location of the satellite at that time
 - » Allows receiver to calculate Time of Flight and distance



Three Satellite Ranges Known



Located at one of these 2 points.
However, one point can easily
be eliminated because it is either
not on earth or moving at impossible
rate of speed.

Accurate Timing is the Key

- **Satellites have very accurate atomic clocks**
- **Receivers have less accurate clocks**
- **Measurements made in nanoseconds**
 - » Speed of light (c) ~ 1 ft/nanosecond
- **$1/100^{\text{th}}$ of a second error could introduce error of 1,860 miles**
- **Discrepancy between the satellite clock and the receiver clocks must be resolved**
- **Fourth satellite is used to solve the 4 unknowns (X, Y, Z and receiver clock error)**

Satellite Positioning

- **Required in the equation to solve the 4 unknowns is the actual location of the satellite.**
 - » 3 coordinates for location, plus clock drift of receiver relative to the satellite clocks
- **Satellites are in relatively stable orbits and constantly monitored on the ground**
- **Satellite's position is broadcast in the "ephemeris" data streamed down to receiver**
 - » Downloading complete set of almanac data requires 12.5 minutes (transmitted at 50 bps)

Sources of Errors

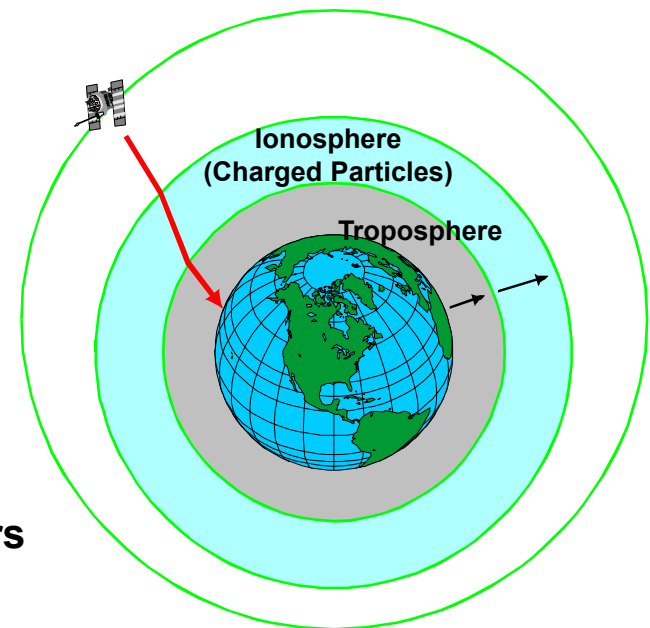
- **Largest source is due to the atmosphere**

- » Atmospheric refraction

- Charged particles
- Water vapor

- **Other sources:**

- » Geometry of satellite positions
- » Multi-path errors
- » Satellite clock errors
- » Satellite position or “ephemeris” errors
- » Quality of GPS receiver



How about Indoors?

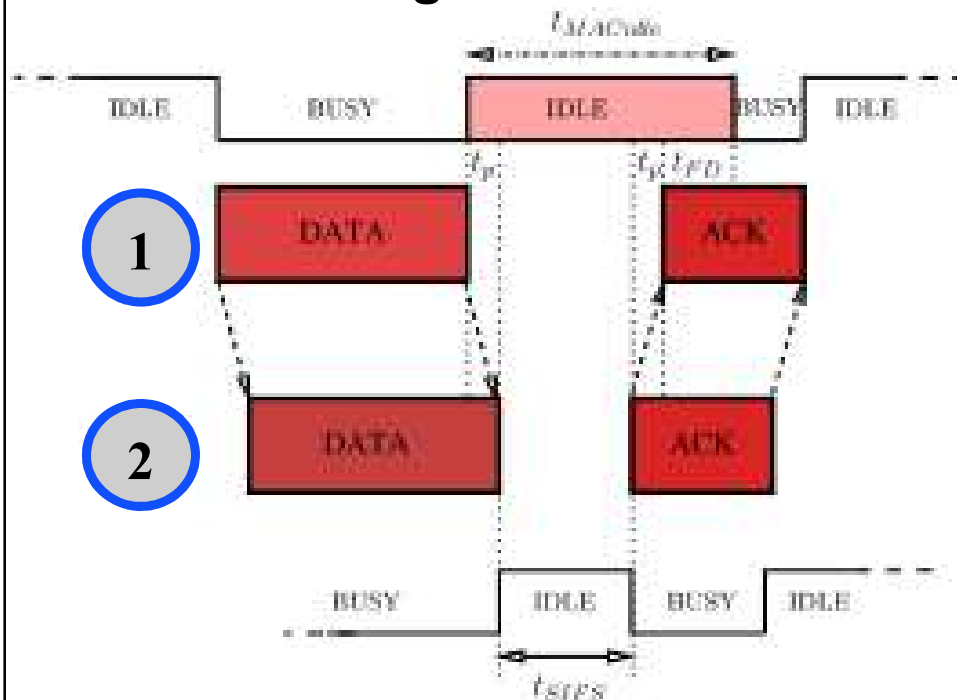
- **We can use received WiFi signal strength (RSS) to measure distance to APs with known location!**
- **Does not work in practice: too many factors affects RSS: objects, people, ...**
 - » Triangulation based on RSS tends to results tend to give large, unpredictable errors
- **How about using time of arrival?**
 - » E.g., based on sound, radar-like techniques, ...
 - » Works better, but it is still hard
 - » Can work well but often requires special infrastructure
 - » Reflections can also create inaccuracies: longer path!

CAESAR: Carrier Sense-based Ranging

- **Question: can we use time of flight ranging using commodity WiFi hardware?**
- **Yes, but it gets a bit messy**
 - » Need to include SNR measurement
- **Local station determines location of (mobile) remote stations**
- **Design criteria**
 - » Exploit standard 802.11 protocol implementations
 - » Real time results
 - » Low cost (low network usage, no additional hardware, minimal calibration)

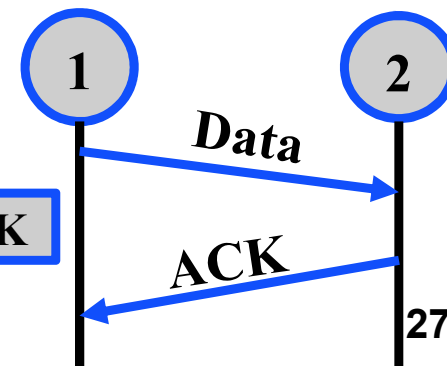
CAESAR: Key Idea

- Time of flight from ACKs



- Speed of light:
 $c = \sim 300\text{m/s}$
- WLAN clock 44MHz
- Resolution:
 $300/(2 \cdot 44) = 3.4\text{m}$
- Distance
 $d = c \cdot (t_{\text{MacIdle}} - t_{\text{SIFS}} - t_{\text{FD}}) / 2$

Distance = $\frac{1}{2}$ time from end of data to beginning of ACK



CAESAR: Adjustment to Noise

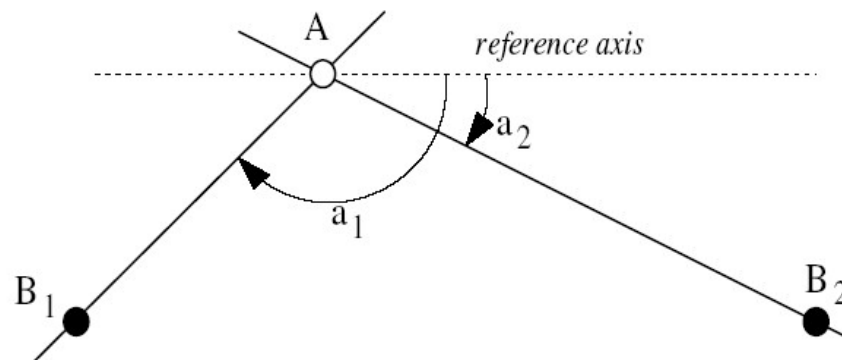
- **Method depends on correct estimation of response time, which depends on the SNR**
- **Automatic gain control is used if**
 - » Preferred region (PR): no AGC
 - » Strong signal detected (SSD): e.g. subtract 30dB from signal
 - » Weak signal detected (WSD): may need adjust signal to bring it into PR (or signal is not detected)
- **Proposed solution:**
 - » Detect states SSD, WSD, and preferred range
 - » Use different values for Time for Frame Detection (t_{FD})

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 - » Hybrid systems

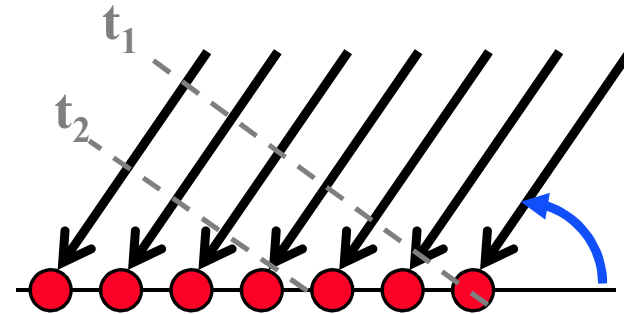
Angle of Arrival (AoA)

- **A measures the direction of the incoming signal using a radio array.**
- **By using 2 anchors, A can determine its position**
- **Alternatively: the anchor measure the angle of A's signal and coordinate**



Angle of Arrival Techniques

- Antenna arrays are increasingly popular
- They are usually used to steer the signal, but can be used to identify the angle at which it arrives
- Difference in arrival time can be used to measure angle



Outline

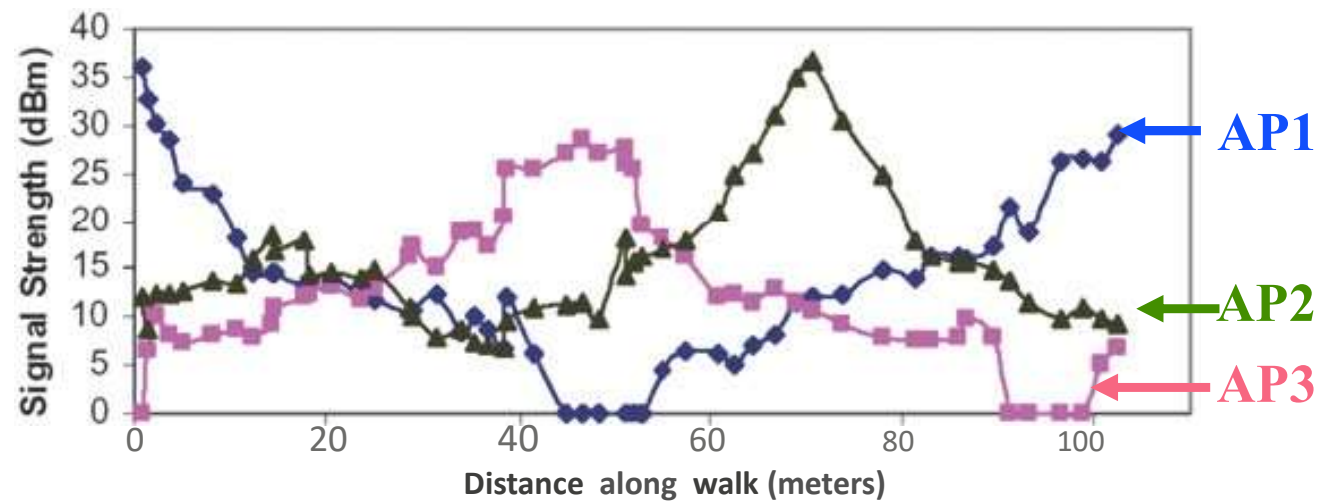
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Location Fingerprinting

- **Fingerprint Methods for Recognizing Locations**
 - » **Examples**
 - Visual identification of places from photos
 - Recognition of horizon shapes
 - Measurement of signal strengths of nearby networks (e.g. RADAR)
 - » **Method: computing the difference between a feature set extracted measurements with a feature database**
 - » **Advantages: passive observation only (protect privacy, prevent communication overhead)**
 - » **Disadvantage: access to feature database needed**

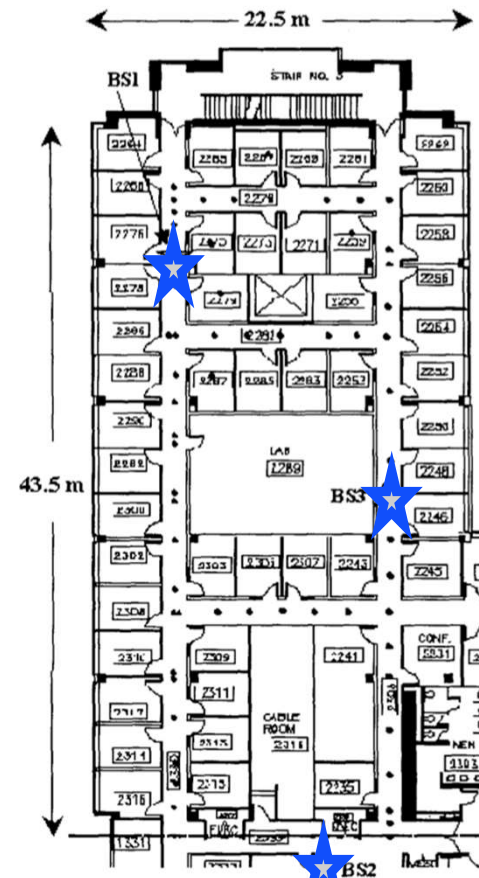
RADAR: Key Idea

- RSS from multiple APs tends to be unique to a location



RADAR Approach

- **Scenario: floor layout with three base stations (in the hallways)**
- **Empirical method**
 - » offline phase: database is constructed
 - collect signal strength measurements from all three base stations at 70 distinct locations
 - store each of the 70 measurement triples together with the spatial location and orientation in a database
 - » online phase: position can be determined
 - measure the current signal strength from all three base stations
 - find the most similar triple(s) in the database
 - » Resolution 2.94m (50th percentile)



★ - Base Station

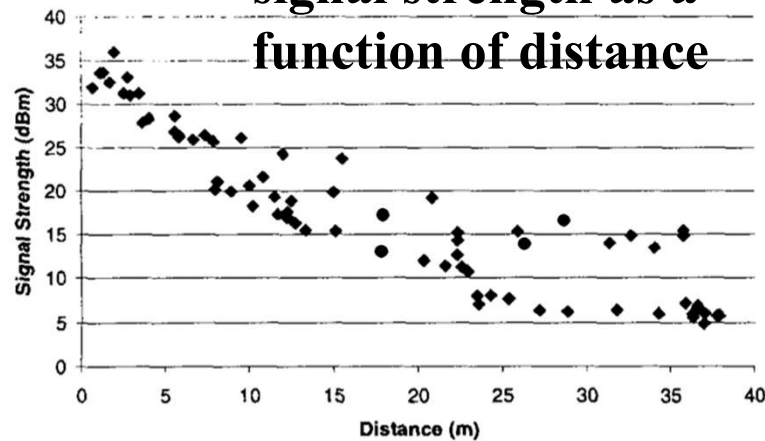
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Model-Based Radio Map

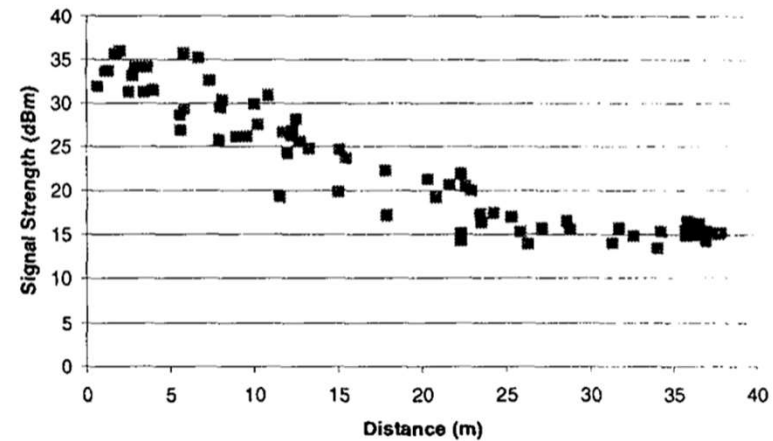
- **Model set-up phase has high cost**
- **Alternative use radio propagation model and floor plan (instead of measurements)**
 - » **Considered models**
 - **Rayleigh fading model: small-scale rapid amplitude fluctuation to model multi-path fading**
 - **Rician distribution model: like Rayleigh but with additional LoS component**
 - **Floor Attenuation Factor propagation model: large scale path loss with building models**
 - **Wall Attenuation Factor model: considers effects from walls between transmitter and receiver**
 - » **Resolution 4.3m (50th percentile)**

Effects of applying correction

**signal strength as a
function of distance**



with correction for walls



Limits of Localization Using Signal Strength

- **Measuring distance based on signal strength is an attractive idea for wireless sensor networks:**
 - » RSS does not require additional hardware
 - » RSS declines with distance
 - » Many different promising methods proposed
- **But accuracy is quite limited**
 - » 802.11 technology with a range of methods and environments tested
 - » Median localization error of 10ft and 97th percentile of 30ft
- **Many technologies with higher accuracy have been developed**
 - » E.g., UWB, use of AoA, ...

Hybrid Technologies

- **Cell phones: have many other sensors**
 - » Accelerometer, compass, ...
- **Can be used to estimate the user's walking speed, direction, ...**
- **This information can be combined with finger printing based techniques**
- **Especially useful if finger printing provides accurate location in specific points**
 - » When entering a store, escalator, elevators
 - » Can use the other sensors starting with these well-known locations

Literature

- **H. Karl and A. Willig (2005). Protocols and Architectures for Wireless Sensor Networks, Ch. 9 Localization and positioning. John Wiley & Sons.**
- **P. Bahl and V. N. Padmanabhan (2000). RADAR: An In-Building RF-based User Location and Tracking System. IEEE INFOCOM 2000, pp. 775-784.**
- **E. Elnahrawy et al. (2004). The limits of localization using signal strength: a comparative study. IEEE SECON 2004, pp. 406-414 .**
- **D. Giustiniano, and S. Mangold (2011). CAESAR: Carrier Sense-Based Ranging in Off-The-Shelf 802.11 Wireless LAN. ACM CoNEXT 2011.**