

**This lecture is being recorded**

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**18-452/18-750**

**Wireless Networks and Applications**

**Lecture 11: MIMO and  
WiFi Deployments**

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**Spring Semester 2021**

**<http://www.cs.cmu.edu/~prs/wirelessF21/>**

# Outline

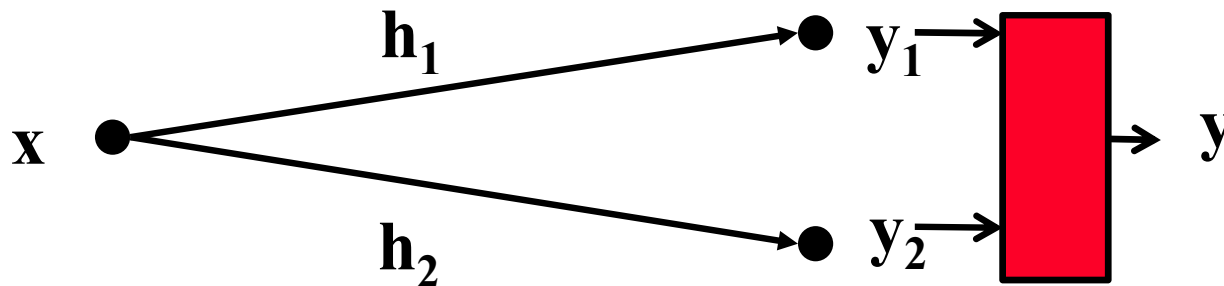
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- **MIMO and recent WiFi versions**
  - » Refresher: spatial diversity
  - » MIMO basics
  - » Single user MIMO: 802.11n
  - » Multi-user MIMO: 802.11ac
  - » Millimeter wave: 802.11ad
- **WiFi deployments**
  - » Planning
  - » Channel selection
  - » Rate adaptation

# Spatial Diversity

- Use multiple antennas that pick up the signal in slightly different locations
  - » Channels uncorrelated with sufficient antenna separation

- Receiver diversity:  $\vec{h}^H \vec{y} = \vec{h}^H (\vec{h} \vec{x} + \vec{n}) = \vec{h}^H \vec{h} \vec{x} + \vec{h}^H \vec{n}$



$$\vec{y} = \vec{h} * \vec{x} + \vec{n}$$

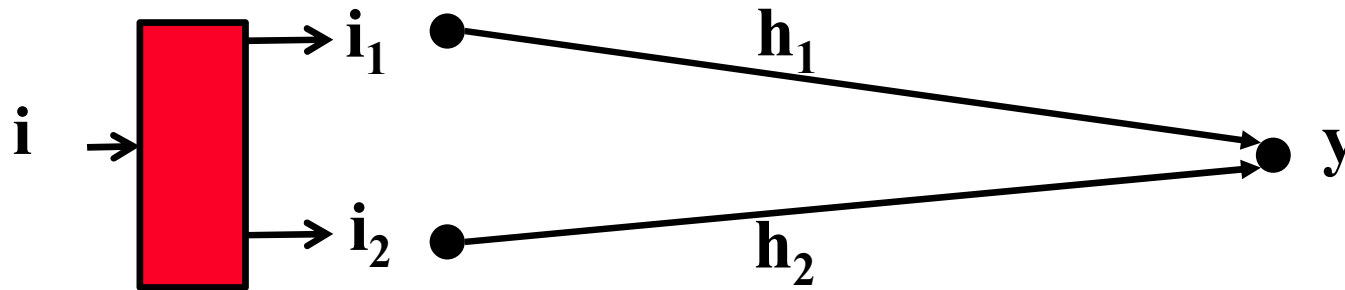
$$y = \vec{h}^* * (\vec{h} * \vec{x} + \vec{n})$$

- Receiver can pick strongest signal:  $y_1$  or  $y_2$
- Or combines the signals: multiply  $y$  with the complex conjugate  $\vec{h}^*$  of the channel vector  $\vec{h}$ 
  - » Can learn  $h$  based on training data (Lecture 5)

# Other Diversity Options

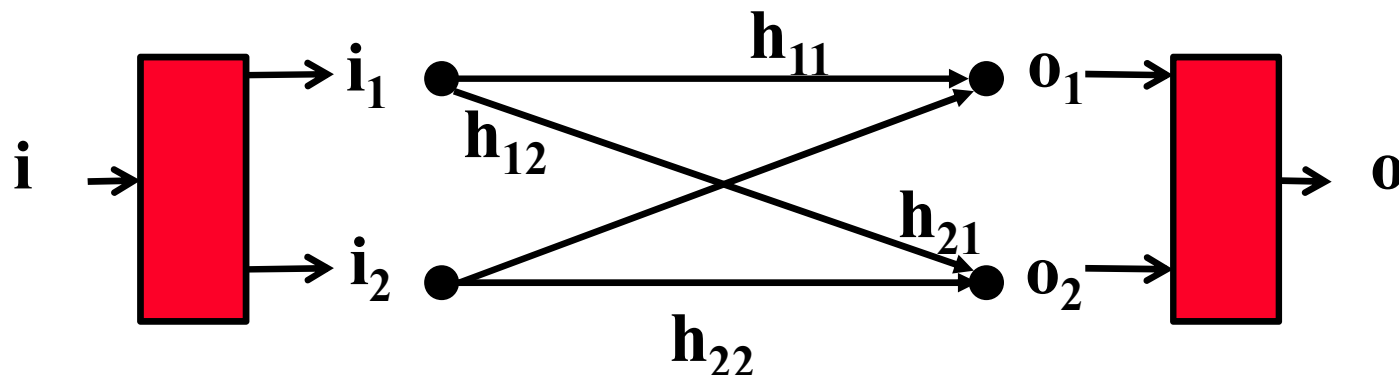
- Transmit diversity:

$$\mathbf{i} \times \vec{\mathbf{P}}_T \times \vec{\mathbf{H}} = \mathbf{0}$$



- Combined:

$$\mathbf{i} \times \vec{\mathbf{P}}_T \times \mathbf{H} \times \vec{\mathbf{P}}_R = \mathbf{0}$$

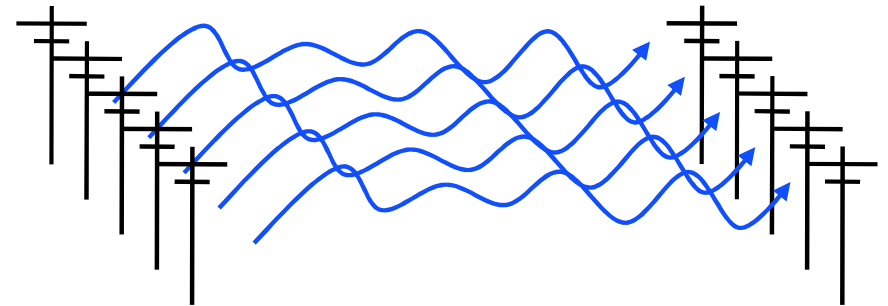


# How Do We Increase Throughput in Wireless?

- **Wired world:**  
**Pull more wires!**



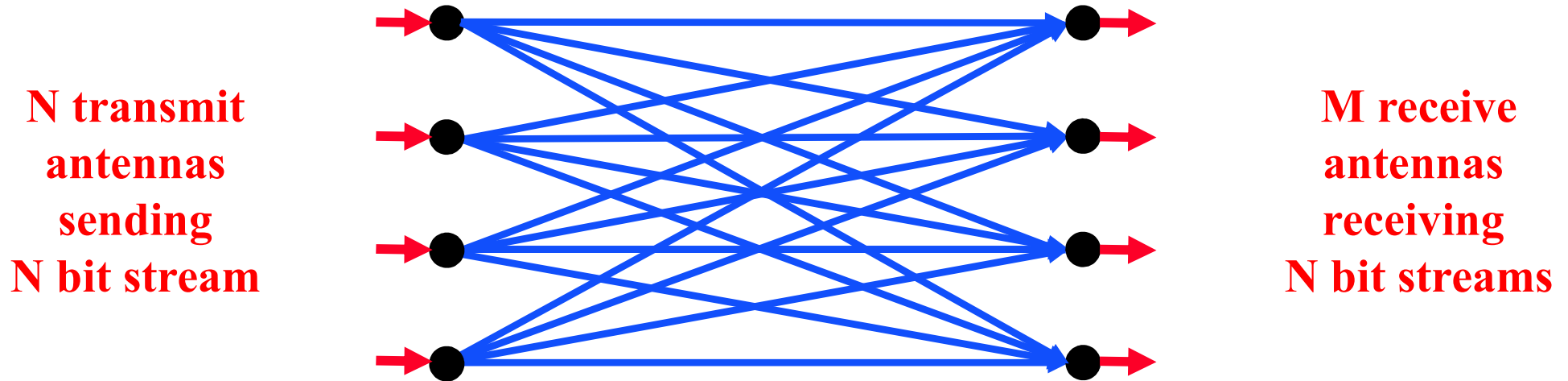
- **Wireless world:**



**How about if we could do the same thing as with wires: send parallel data streams!**

# MIMO

## Multiple In Multiple Out



- **$N \times M$  subchannels that can be used to send multiple data streams simultaneously**
- **Fading on channels is largely independent**
  - » Assuming antennas are separate  $\frac{1}{2}$  wavelength or more
- **Build on ideas from space diversity, e.g.  $1 \times N$  and  $N \times 1$**
- **Very effective if there is no direct line of sight**
  - » Subchannels become more independent

# Why So Exciting?

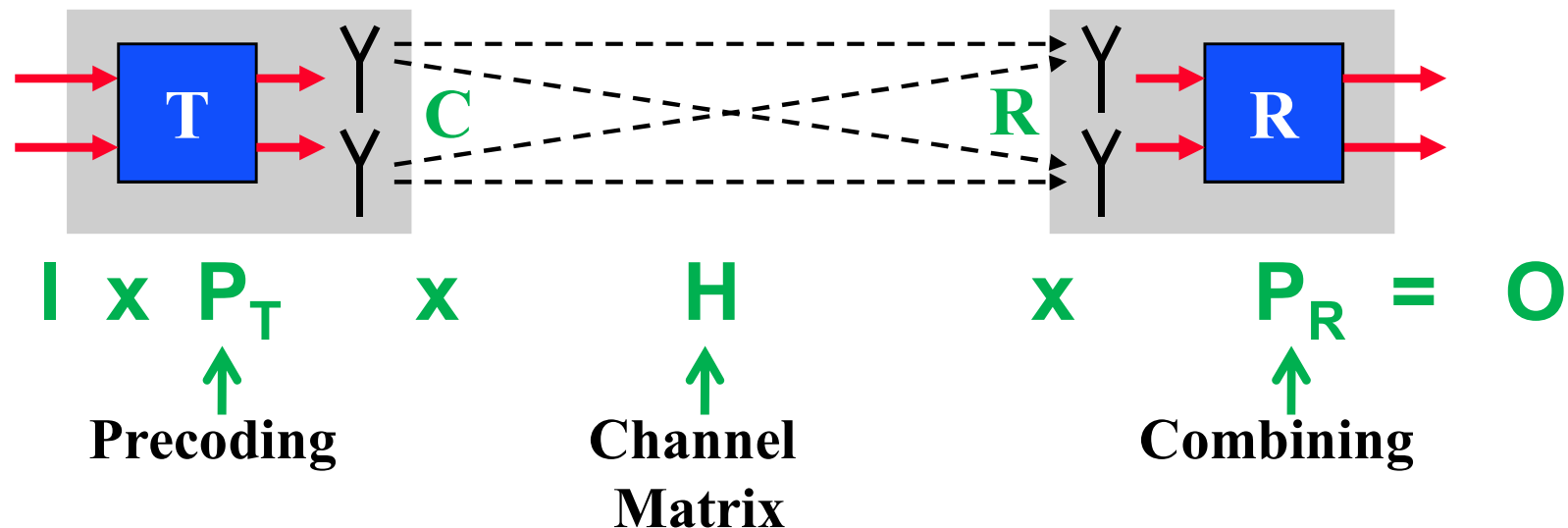
Method	Capacity
<b>SISO</b>	<b><math>B \log_2(1 + \rho)</math></b>
<b>Diversity (1xN or Nx1)</b>	<b><math>B \log_2(1 + \rho N)</math></b>
<b>Diversity (NxN)</b>	<b><math>B \log_2(1 + \rho N^2)</math></b>
<b>Multiplexing</b>	<b><math>NB \log_2(1 + \rho)</math></b>

802.11 with multiple antennas for dummies, Daniel Halperin, Wenjun Hu, Anmol Sheth, David Wetherall, ACM CCR, Jan 2010

# MIMO

## How Does it Work?

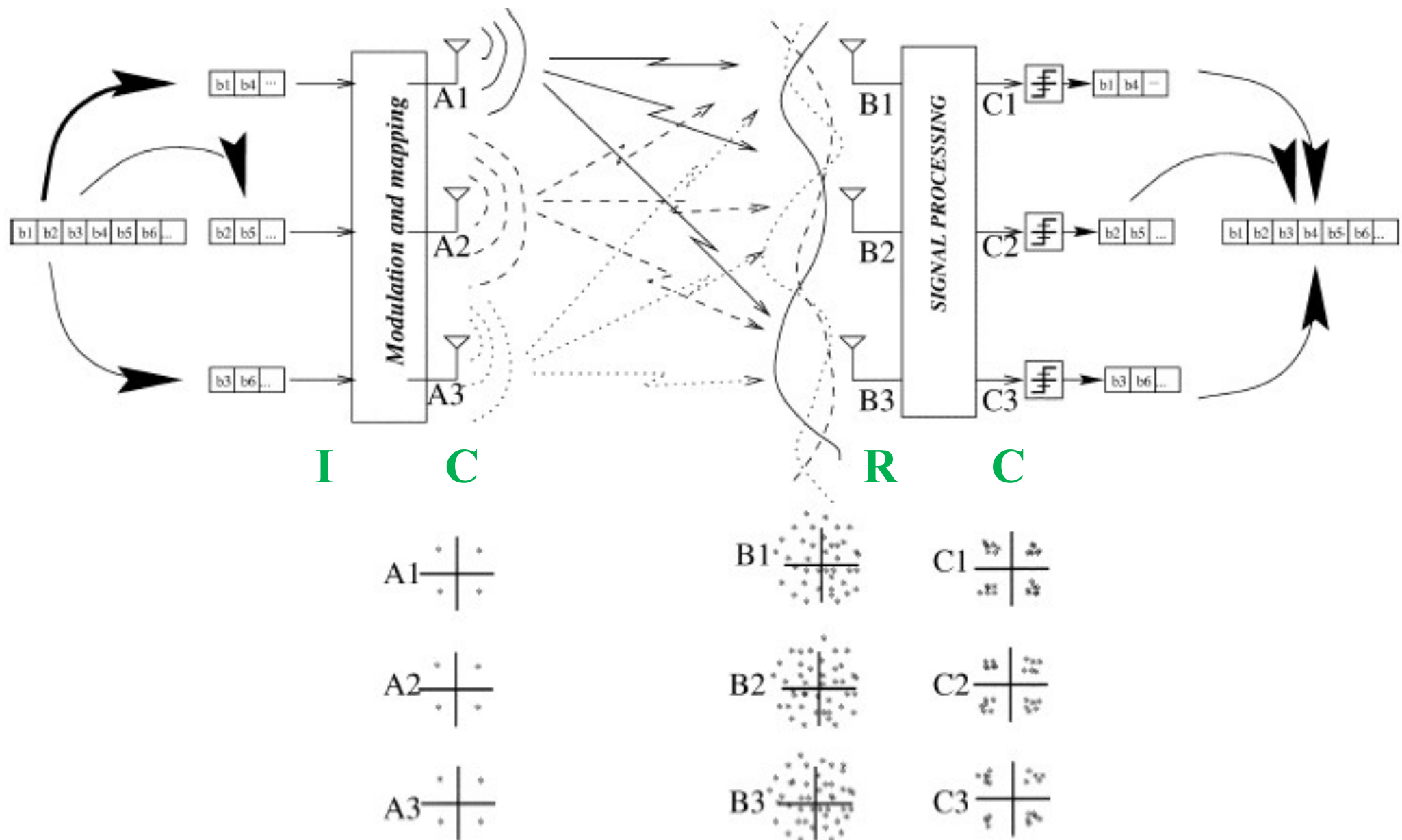
- Transmit and receive multiple data streams
- Coordinate the processing at the transmitter and receiver to overcome channel impairments
  - » Maximize throughput or minimize interference



- Combines previous techniques



# An Example of Space Coding



# Direct-Mapped NxM MIMO

## Only Receiver Processing ( $P_T=I$ )

Effect of transmission

$$\begin{matrix} \text{M} & \text{M} \times \text{N} & \text{N} & \text{M} \\ \vec{\mathbf{R}} = \mathbf{H} * \vec{\mathbf{C}} + \vec{\mathbf{N}} \end{matrix}$$

Decoding

$$\begin{matrix} \vec{\mathbf{O}} = \mathbf{P}_R * \vec{\mathbf{R}} & \vec{\mathbf{C}} = \vec{\mathbf{I}} \\ \text{D} & \text{D} \times \text{M} & \text{M} & \text{N} & \text{N} \end{matrix}$$

Results

$$\vec{\mathbf{O}} = \mathbf{P}_R * \mathbf{H} * \vec{\mathbf{I}} + \mathbf{P}_R * \vec{\mathbf{N}}$$

- How do we pick  $\mathbf{P}_R$  ? “Inverse” of  $\mathbf{H}$ :  $\mathbf{H}^{-1}$ 
  - » Equivalent of nulling the interfering signals (zero forcing)
  - » Only possible if the paths are completely independent
- Noise amplification is a concern if  $\mathbf{H}$  is non-invertible – its determinant will be small

# Direct MIMO

## Very Basic Example

$$\mathbf{O} = \mathbf{P}_R * \mathbf{H} * \mathbf{I} + \mathbf{P}_R * \mathbf{N}$$

- $r_1 = (h_{11} \times i_1 + h_{12} \times i_2)$
- $r_2 = (h_{21} \times i_1 + h_{22} \times i_2)$
- $o_1 = p_{11} \times r_1 + p_{12} \times r_2$
- $o_2 = p_{21} \times r_1 + p_{22} \times r_2$
- Simple cases can be solved as set of linear equations
- Reality check!
  - » Above values are complex number (phase, amplitude)
  - » The channel state matrix  $\mathbf{H}$  changes with time and frequency – it can only be estimated
  - » The noise is not known
  - » The  $o_i$  values will not be identical to  $i_i$ !
- Simple examples
  - » What if all  $h_{ij} = 1$ ?
  - » What  $h_{12} = h_{21} = 1$  and  $h_{11} = h_{22} = 0$ ?
  - » Conclusion: MIMO benefits depend on the channel state matrix
    - Would like channels to be as uncorrelated as possible

# Precoded N x M MIMO

Effect of transmission

$$\begin{matrix} \text{M} & \text{M} \times \text{N} & \text{N} & \text{M} \\ \vec{\mathbf{R}} = \mathbf{H} * \vec{\mathbf{C}} + \vec{\mathbf{N}} \end{matrix}$$

Coding/decoding

$$\begin{matrix} \vec{\mathbf{O}} = \mathbf{P}_R * \vec{\mathbf{R}} \\ \text{D} \quad \text{D} \times \text{M} \quad \text{M} \end{matrix}$$

$$\begin{matrix} \vec{\mathbf{C}} = \mathbf{P}_T * \vec{\mathbf{I}} \\ \text{N} \quad \text{N} \times \text{D} \quad \text{D} \end{matrix}$$

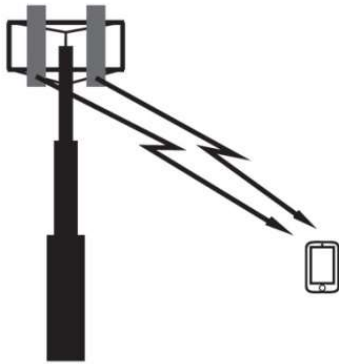
Results

$$\vec{\mathbf{O}} = \mathbf{P}_R * \mathbf{H} * \mathbf{P}_T * \vec{\mathbf{I}} + \mathbf{P}_R * \vec{\mathbf{N}}$$

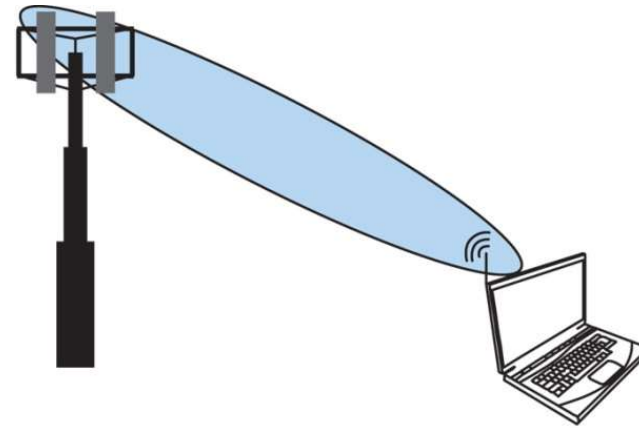
- How do we pick  $\mathbf{P}_R$  and  $\mathbf{P}_T$  ?
- Singular value decomposition of  $\mathbf{H} = \mathbf{U} * \mathbf{S} * \mathbf{V}$ 
  - » U and V are unitary matrices –  $\mathbf{U}^H * \mathbf{U} = \mathbf{V}^H * \mathbf{V} = \mathbf{I}$
  - » S is diagonal matrix

Identity matrix

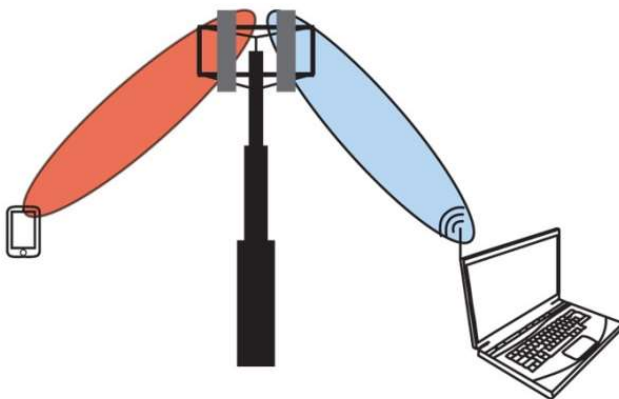
# Mechanisms Supported by MIMO



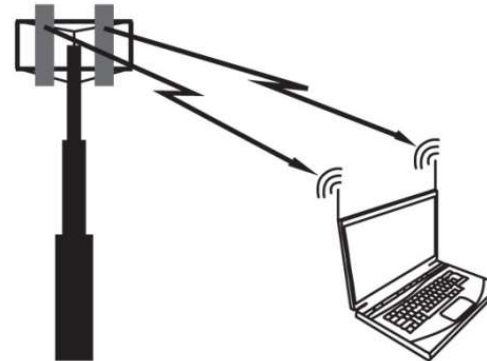
Diversity for improved system performance



Beam-forming for improved coverage  
(less cells to cover a given area)



Spatial division multiple access  
("MU-MIMO") for improved capacity  
(more user per cell)



Multilayer transmission  
("SU-MIMO") for higher data rates  
in a given bandwidth

# MIMO Discussion

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- **Need channel matrix  $H$ : use training with known signal**
- **So far we have ignored multi-path**
  - » Each channel is multiple paths with different properties
  - » Becomes even messier!
- **MIMO is used in 802.11n**
  - » Can use two adjacent non-overlapping “WiFi channels”
  - » Raises lots of compatibility issues
  - » Potential throughputs of 100s of Mbps
- **Focus is on maximizing throughput between two nodes**
  - » Is this always the right goal?

# 802.11n Overview

- **802.11n extends 802.11a for MIMO**
  - » Supports up to 4x4 MIMO
  - » Preamble that includes high throughput training field
- **Standardization was completed in Oct 2009, but early products had long been available**
  - » WiFi alliance started certification using draft in mid-2007
- **Supported in both the 2.4 and 5 GHz bands**
  - » Goal: typical indoor rates of 100-200 Mbps; max 600 Mbps
- **Use either 1 or 2 non-overlapping channels**
  - » Uses either 20 or 40 MHz - interoperability problems!
- **Supports frame aggregation to amortize overheads over multiple frames**
  - » Optimized version of 802.11e

# 802.11n

## Backwards Compatibility

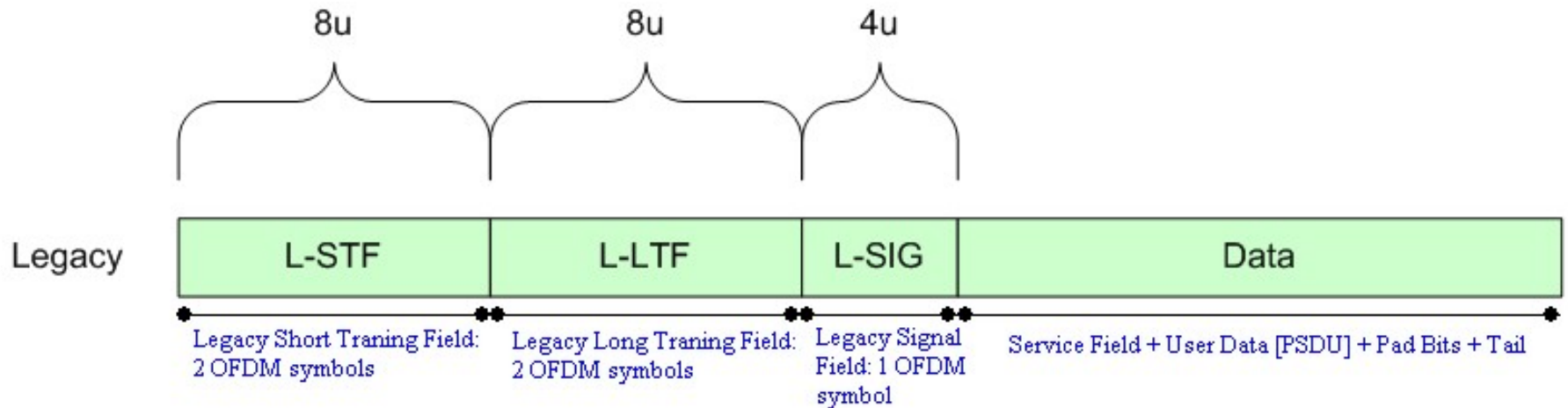
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- **802.11n can create interoperability problems for existing 802.11 devices (abg)**
  - » 802.11n does not sense their presence
  - » Legacy devices end up deferring and dropping in rate
- **Mixes Mode Format protection embeds an “n” frame in a “g” or “a” frame**
  - » Preamble is structured so legacy systems can decode header, but MIMO can achieve higher speed (training, cod/mod info)
  - » Works only for 20 MHz 802.11n use
  - » Only deals with interoperability with a and g – still need CTS protection for b
- **For 40 MHz 802.11n, we need CTS protection on both the 20 MHz channels – similar to g vs. b**
  - » Amortize over multiple transmissions



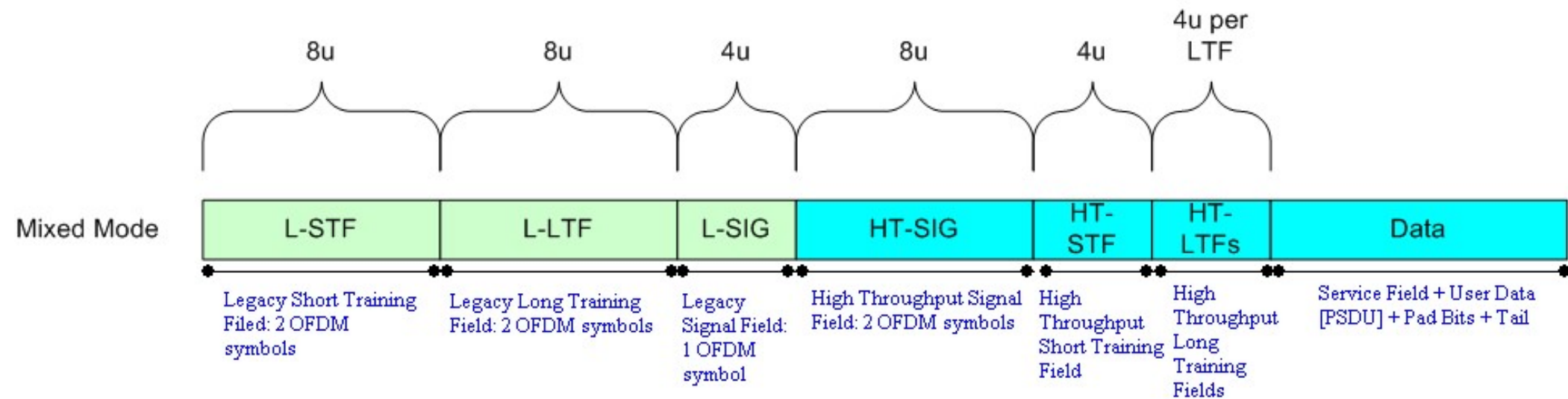
# Interoperability Uses PLCP in Three Modes

- **Legacy mode: use 802.11a/g OFDM format**
  - » The L-SIG field contains rate and length information
  - » Loses benefits of 802.11n!

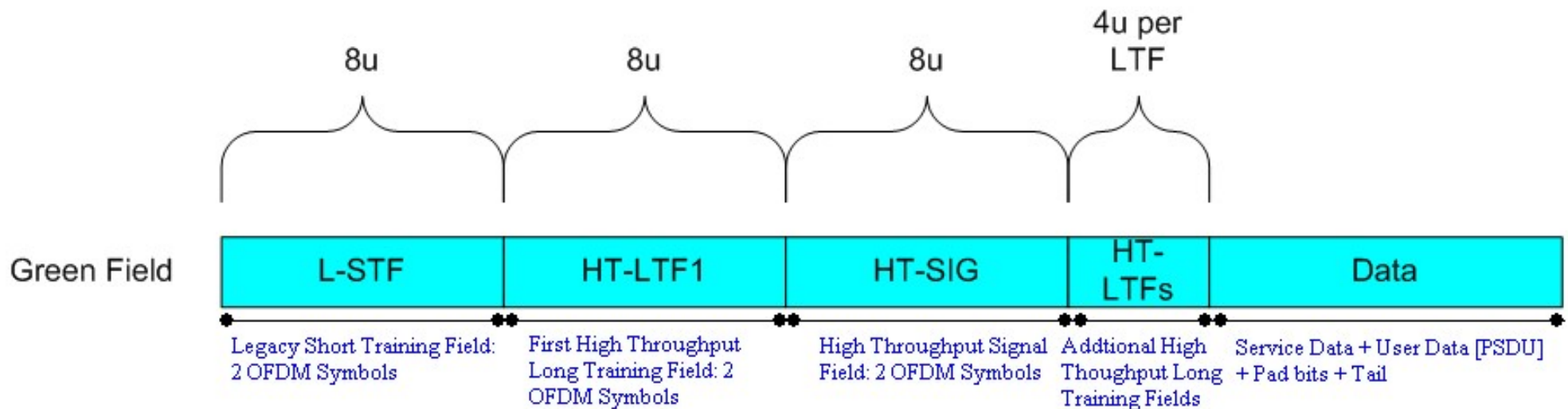


- **Mixed mode:**
  - » Include both an 802.11a/g and 802.11n PLC - next slide
  - » 802.11n devices can interpret green field, which includes the L-SIG field (rate and length information)

# Interoperability: High Throughput (HT) Modes

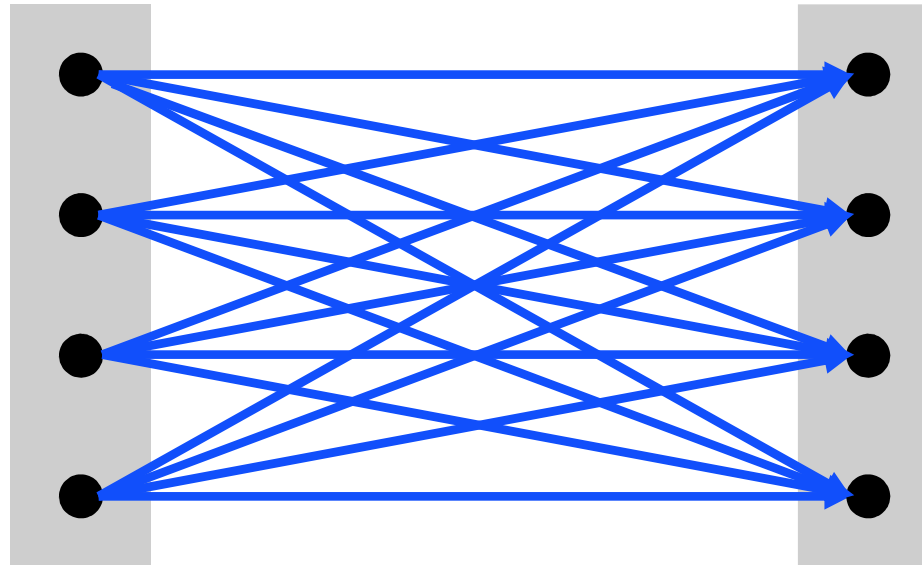


- **Green field mode: use 802.11n OFDM format**



# MIMO in a Network Context

**N transmit  
antennas**



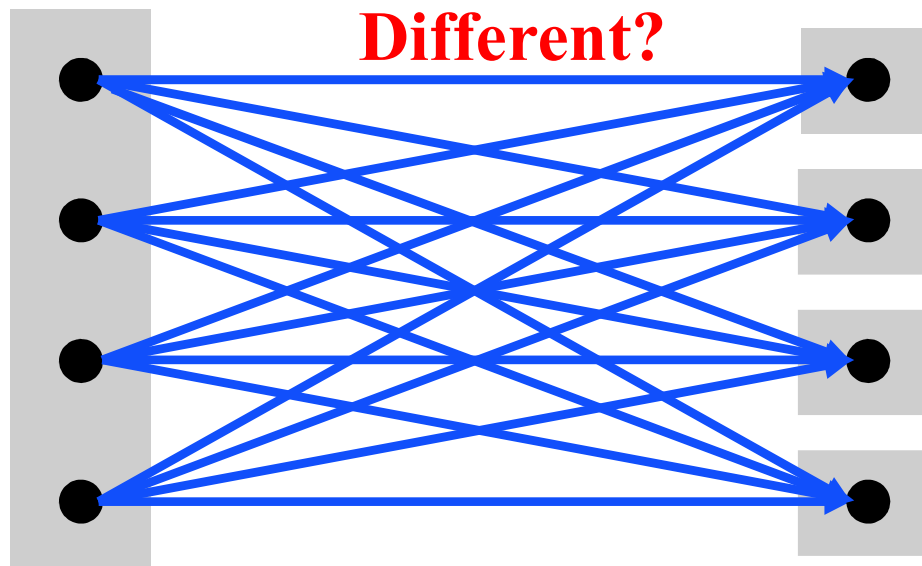
**M receive  
Antennas**

-

**1 receiver**

**How is this  
Different?**

**N transmit  
antennas**



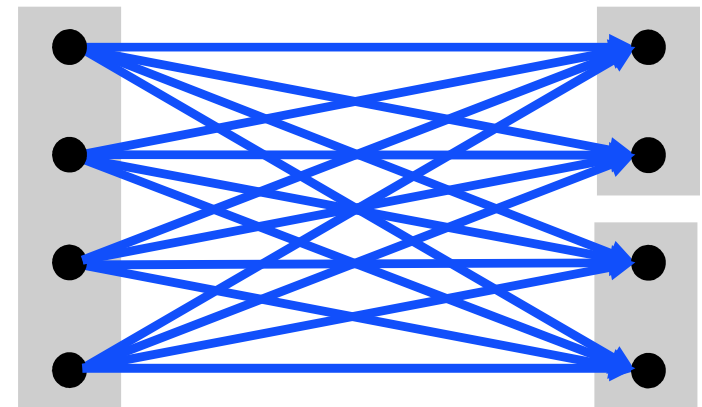
**M receive  
antennas**

-

**M receivers**

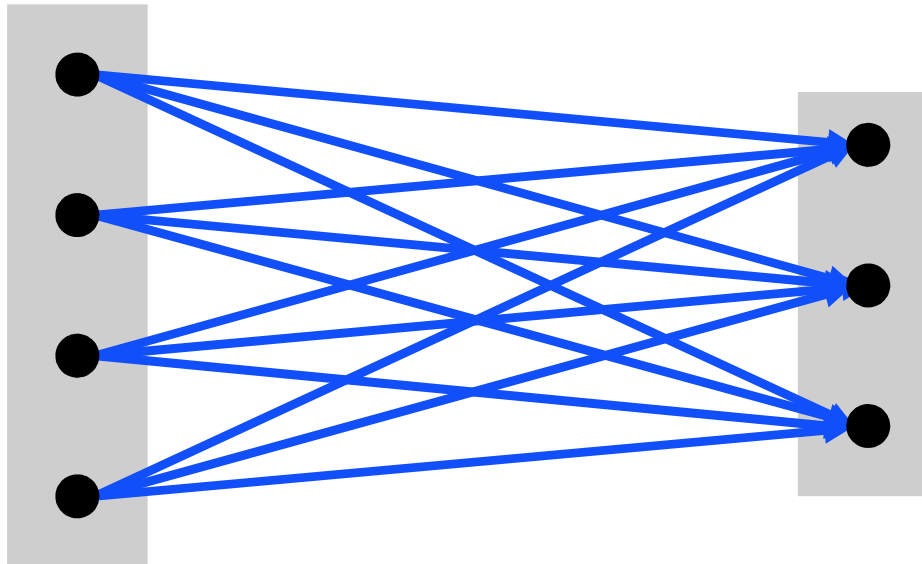
# Multi-User MIMO Discussion

- **Math is similar to MIMO, except for the receiver processing ( $P_R$ )**
  - » Receivers do not have access to the signals received by antennas on other nodes
  - » Cannot cancel interference – limits ability to extract useful data
  - » Can only do transmit-side preprocssing
- **MU-MIMO versus MIMO is really a tradeoff between TDMA and use of space diversity**
  - » MIMO: send packets to two destinations sequentially and efficiently
  - » MU-MIMO: send packet to destination simultaneously, but interference cancelation is more limited



# How about This?

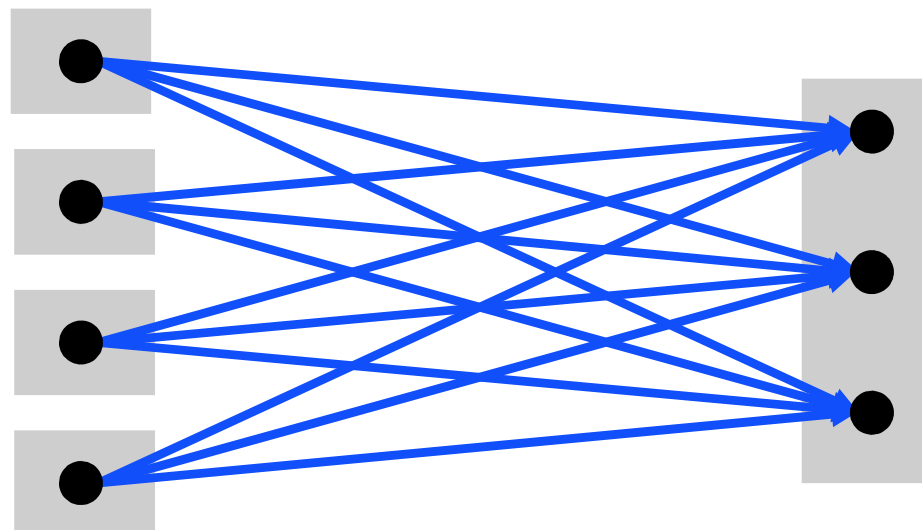
**N transmit  
antennas**



**M receive  
Antennas  
-  
1 receiver**

**How is this Different?**

**N transmit  
antennas**



**M receive  
antennas  
-  
M receivers**

# Multi-User MIMO

## Up versus Down Link

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- **Assume one AP with multiple clients**
- **Downlink: Broadcast Channel (BC)**
  - » Base station transmit separate data streams to multiple independent users
  - » Easier to do: close to the traditional CSMA-CA model of having each client receive a packet from the base station independently
- **Uplink: Multiple Access Channel (MAC)**
  - » Multiple clients transmit simultaneously to a single base station
  - » Requires fine grain clock coordination among clients on packet transmission – hard problem!
  - » Tricky for traditional CSMA-CA protocols

# 802.11ac

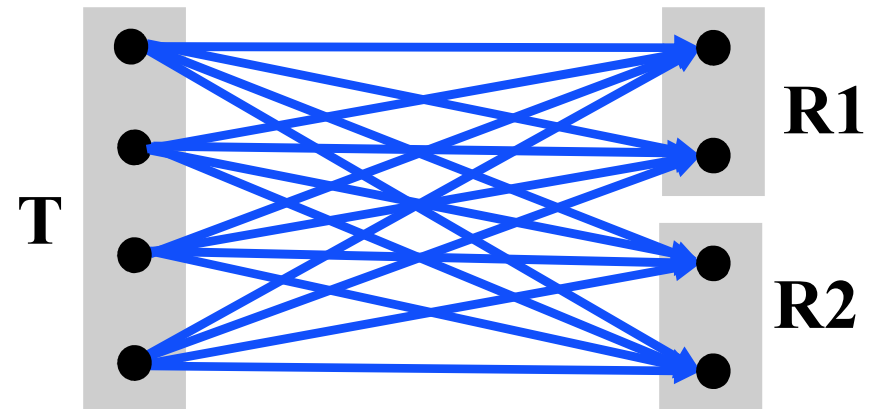
## Multi-user MIMO

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- **Extends beyond 802.11n**
  - » MIMO: up to 8 x 8 channels (vs. 4 x 4)
  - » More bandwidth: up to 160 MHz by bonding up to 8 channels (vs. 40 MHz)
  - » More aggressive signal coding: up to 256 QAM (vs. 64 QAM); both use 5/6 coding rate (data vs. total bits)
  - » Uses RTS-CTS for clear channel assessment
  - » Multi-gigabit rates (depends on configuration)
- **Support for multi-user MIMO on the downlink**
  - » Can support different frames to multiple clients at the same time
  - » Especially useful for smaller devices, e.g., smartphones
  - » Besides beam forming to target signal to device, requires also nulling to limit interference

# Challenges in 802.11ac

- You must have traffic for multiple receivers!
- Channels to the receivers be “orthogonal”



$$\text{R1: } \mathbf{O}_1 = \mathbf{P}_{\text{R1}} * \mathbf{H}_1 * \mathbf{P}_T * \mathbf{I} + \mathbf{P}_{\text{R1}} * \mathbf{N}$$

$$\text{R2: } \mathbf{O}_2 = \mathbf{P}_{\text{R2}} * \mathbf{H}_2 * \mathbf{P}_T * \mathbf{I} + \mathbf{P}_{\text{R2}} * \mathbf{N}$$

- » The signal that you create with the packet for one destination should have a “null” for the other destination(s)
- » Important since the other receivers cannot cancel out that signal
- Becomes a scheduling problem: for each “packet” transmission, identify the destinations that have traffic waiting and that are “the most” orthogonal



# 802.11ad

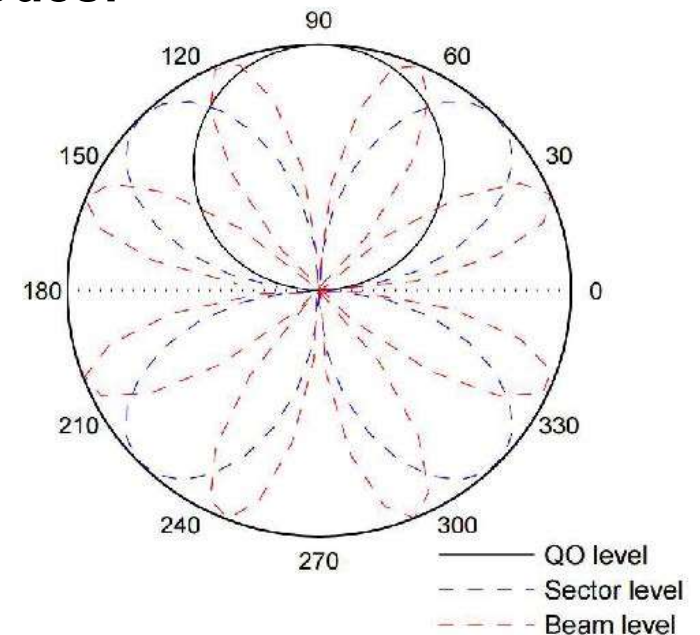
## 60 GHz WiFi

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- **Uses a new physical layer definition specifically for 60 GHz band**
  - » Very different signal propagation properties
  - » Does not penetrate walls, but does work with reflections
  - » Shorter distances; up to 7 Gbps
  - » 6 channels of 2.16 GHz
- **Compatible with 802.11 in 2.4 / 5 GHz bands**
  - » Backwards compatible MAC (not PHY!)
  - » E.g., mobile devices can switch between bands
- **Has been used for point-point links for a while**
  - » Set top box to TV screen,
  - » Combined with other 802.11 versions

# Optimizing Communication in 802.11ad

- **Transmission range in 60 GHz is limited**
- **Must use directional antennas to direct energy to the receiver**
  - » Increases range and throughput (high signal strength)
  - » Also reduces interference at other nodes!
- **Good news: antenna size scales with wave length**
  - » Small antennas and narrow beams
- **Bad news: how do nodes find each other?**
  - » Use iterative algorithm, starting with wider beams



# Outline

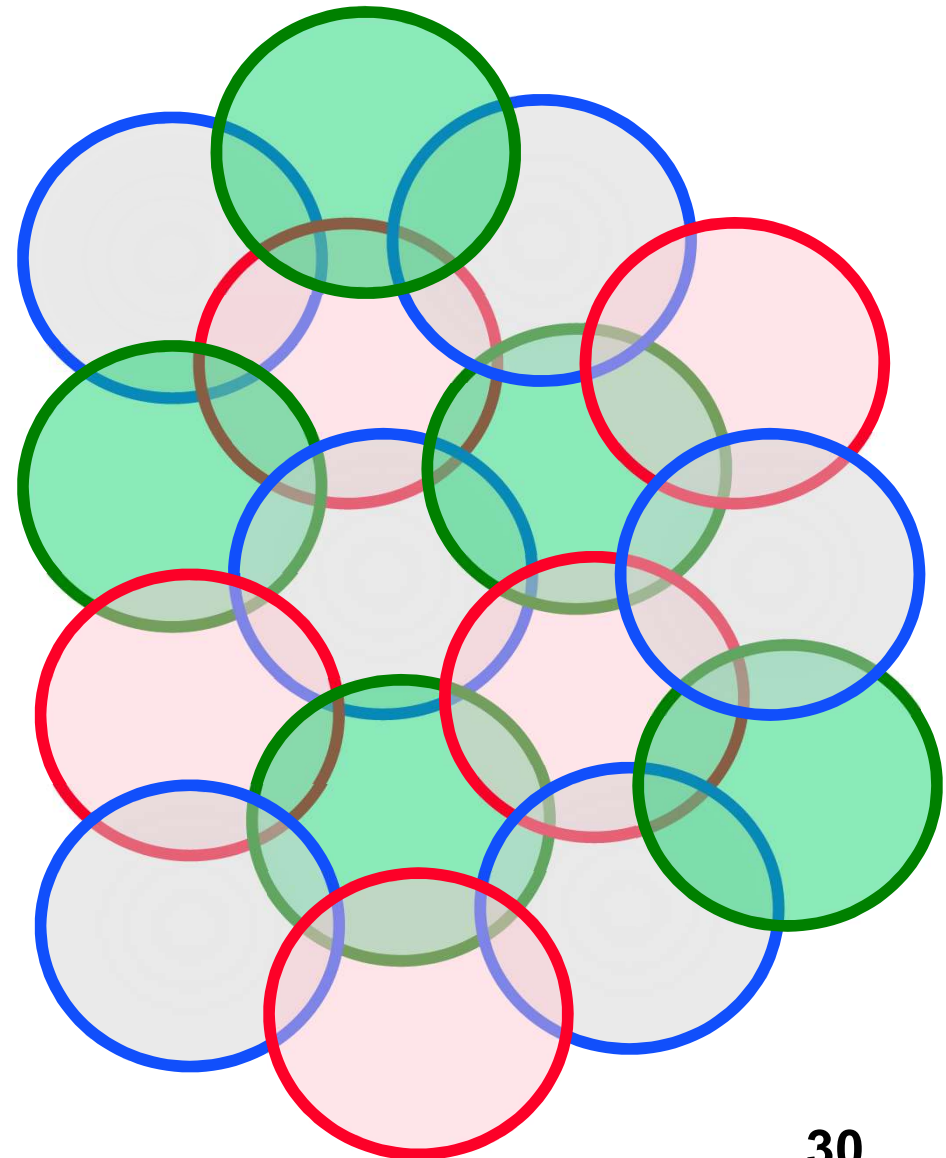
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  - » MIMO basics
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  - » Millimeter wave: 802.11ad
- **WiFi deployments**
  - » Planning
  - » Channel selection
  - » Rate adaptation

# Infrastructure Deployments

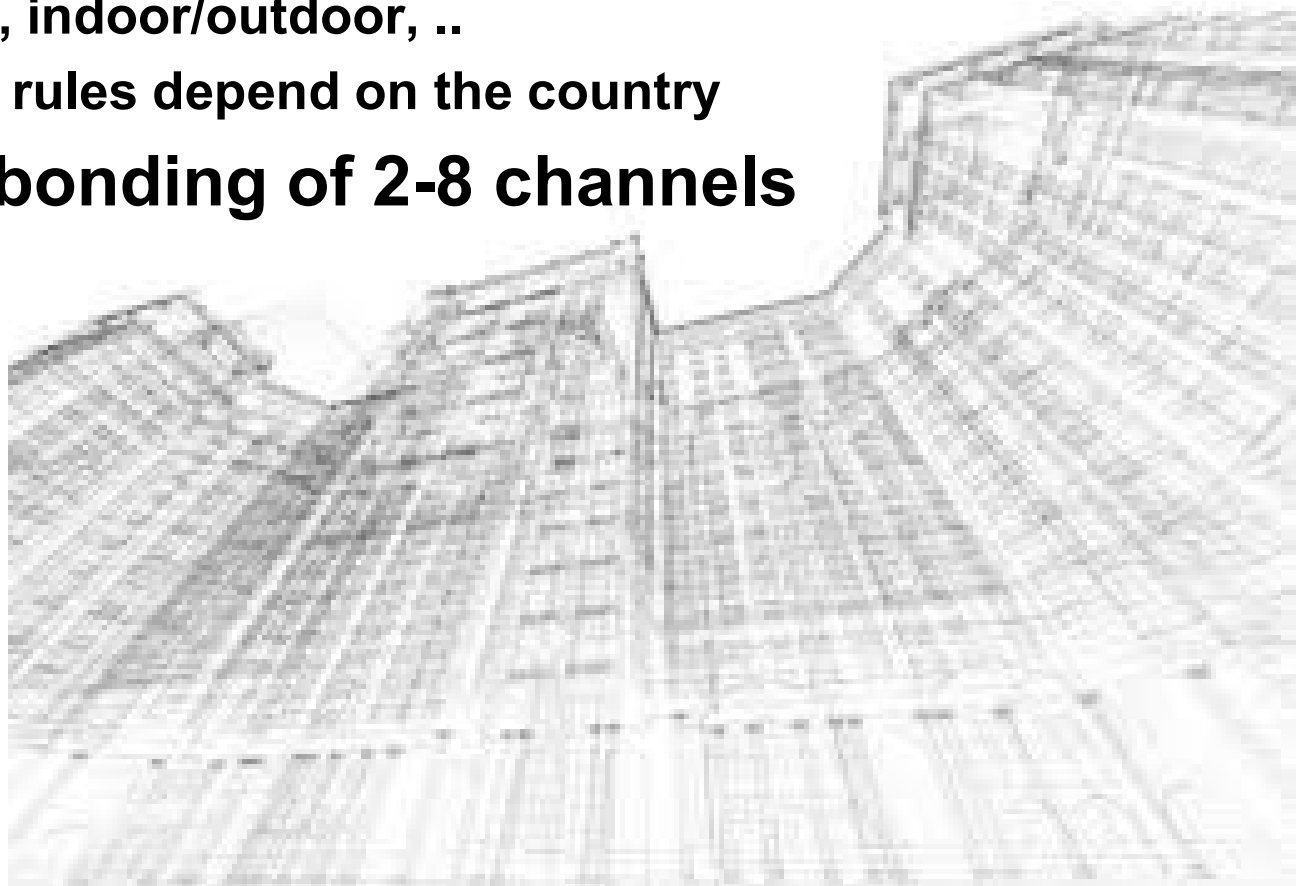
## Frequency Reuse in Space

- **Set of cooperating cells with a base stations must cover a large area**
- **Cells that reuse frequencies should be as distant as possible to minimize interference and maximize capacity**
  - » Hidden and exposed terminals are also a concern



# Frequencies are Precious

- **2.4 Ghz: 3 non-overlapping channels**
  - » Plus lots of competition: microwaves and other devices
- **5 GHz: 20+ channels, but with constraints**
  - » Power constraints, indoor/outdoor, ..
  - » Exact number and rules depend on the country
- **802.11n and ac: bonding of 2-8 channels**
- **And the world is not flat!**



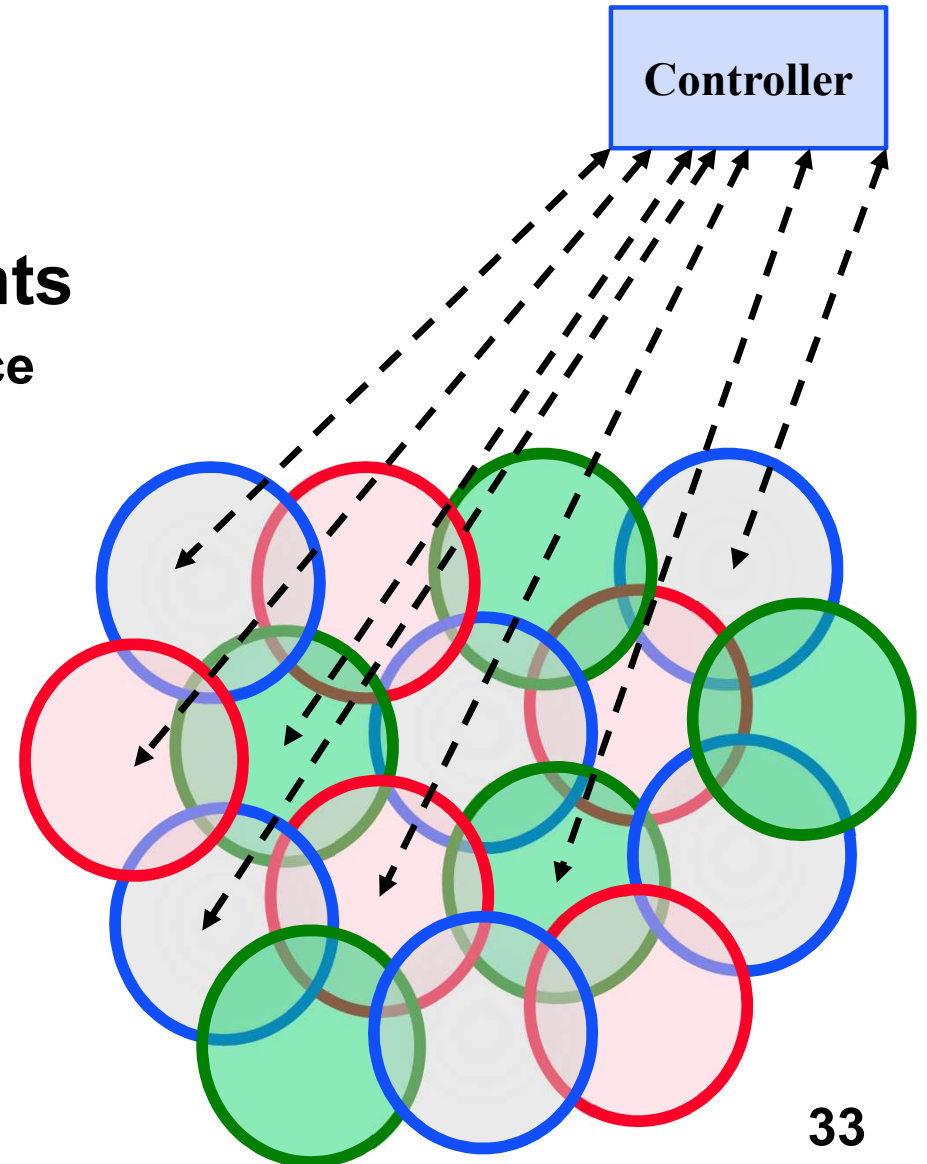
# Frequency Planning

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- **Campus-style WiFi deployments are very carefully planned:**
- **A lot of measurements to determine where to place the AP**
  - » What is the coverage area?
  - » What set of APs has good coverage with few “dead spots”
  - » What level of interference can we expect between cells
  - » What traffic loads can we expect, e.g., auditorium vs office
- **Frequencies are very carefully assigned**
  - » Can use the above measurements
- **Must periodically re-evaluate infrastructure**
  - » Furniture is moved, remodeling, ...

# Centralized Control

- **Many WiFi deployments have centralized control**
- **APs report measurements**
  - » Signal strengths, interference from other cells, load, ...
- **Controller makes adjustments**
  - » Changes frequency bands
  - » Adjusts power
  - » Redistributes load
  - » Can switch APs on/off
  - » Very sophisticated!



# Monitoring the Spectrum

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- **FCC (in the US) controls spectrum use**
  - » Rules for unlicensed spectrum, licenses for other spectrum, what technologies can be used, ...
- **... but there is an special clause for campuses**
  - » They have significant control over unlicensed spectrum use on the campus
  - » They can even use some “licensed” spectrum if it does not interfere with the license holder
- **Network management involves carefully monitoring for performance and security**
  - » Shut down rogue APs – interference, security
  - » Non-approved equipment - interference
  - » Discourages outdated standards - inefficient



# How about Small Networks?

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- **Most WiFi networks are small and (largely) unmanaged**
  - » Home networks, hotspots, ...
- **Traditional solution: user-chosen frequency of their AP or a factory set default**
  - » How well does that work?
- **Today, APs pick a channel automatically in a smart way**
  - » Monitors how busy channels are or how strong the signals are and then picks the best channel
  - » Can periodically check for better channels