

18-452/18-750  
**Wireless Networks and Applications**

**Lecture 7: Physical Layer**  
**Spread Spectrum and OFDM**

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<http://www.cs.cmu.edu/~prs/wirelessF18/>

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## Announcements

- Please form teams of two people for Project 1.
  - » Please use Canvas
  - » Separate teams on Pgh and SV campus
- We should have a video classroom for Friday recitations/lectures.
  - » Hopefully this will be ready by tomorrow
  - » I will keep you posted so please check for announcements

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## Outline

- RF introduction
- Modulation and multiplexing
- Channel capacity
- Antennas and signal propagation
- Modulation
- Diversity and coding
  - » Space, time and frequency diversity
- OFDM



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## Spread Spectrum

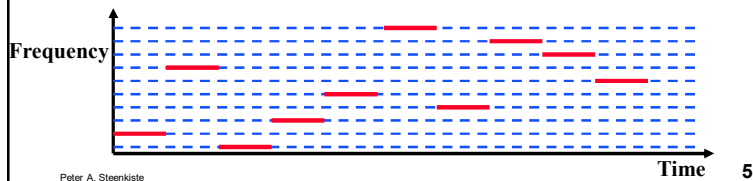
- Spread transmission over a wider bandwidth
  - » Don't put all your eggs in one basket!
- Also useful to minimize impact of a "bad" frequency in regular environments
- Good for military: jamming and interception becomes harder
- Drawback: you use more spectrum
- What can be gained from this apparent waste of spectrum?
  - » Immunity from various kinds of noise and multipath distortion
  - » Can be used for hiding and encrypting signals
  - » Several users can independently use the same higher bandwidth with very little interference

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## Frequency Hopping Spread Spectrum (FHSS)

- Have the transmitter hop between a seemingly random sequence of frequencies
  - » Each frequency has the bandwidth of the original signal
- Dwell time is the time spent using one frequency
- Spreading code determines the hopping sequence
  - » Must be shared by sender and receiver (e.g. standardized)



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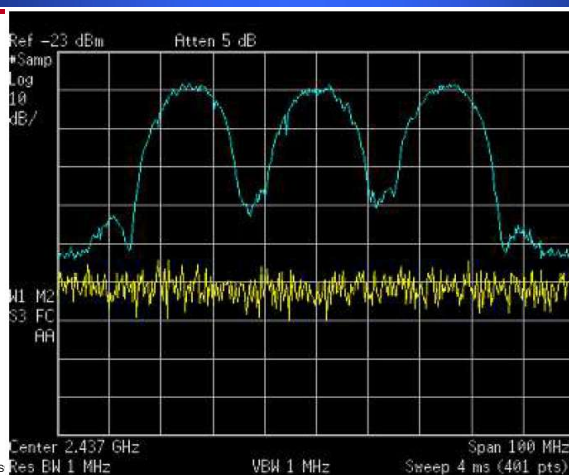
## Example: Bluetooth

- Uses frequency hopping spread spectrum in the 2.4 GHz ISM band
- Uses 79 frequencies with a spacing of 1 MHz
  - » Other countries use different numbers of frequencies
- Frequency hopping rate is 1600 hops/s
- Signal uses GFSK
  - » Minimum deviation is 115 KHz
- Maximum data rate is 1 MHz
- Also used in the original WiFi standard

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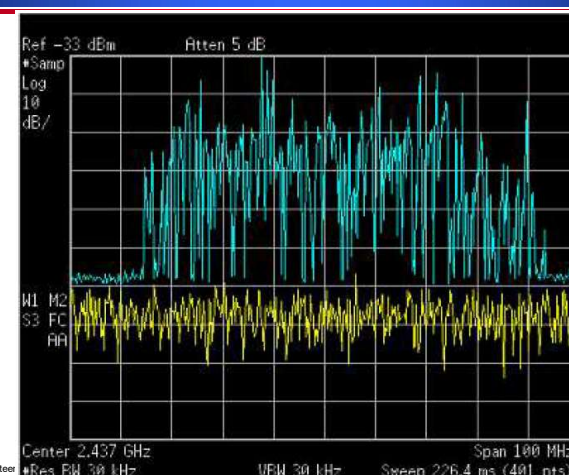
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## 802.11 Spectrogram



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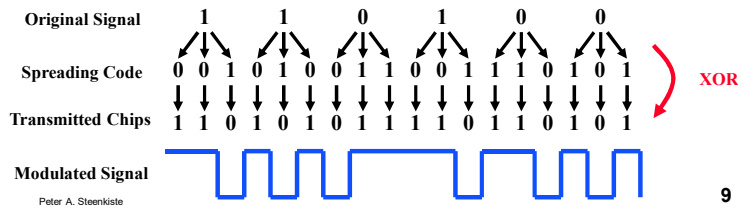
## Frequency Hopping Spectrogram



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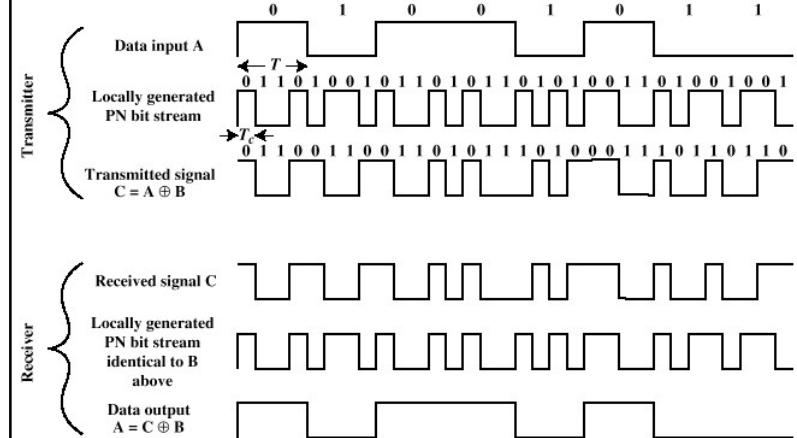
## Direct Sequence Spread Spectrum (DSSS)

- Each bit in original signal is represented by multiple bits (chips) in the transmitted signal
- Spreading code spreads signal across a wider frequency band
  - » Spread is in direct proportion to number of bits used
  - » E.g. exclusive-OR of the bits with the spreading code
- The resulting bit stream is used to modulate the signal

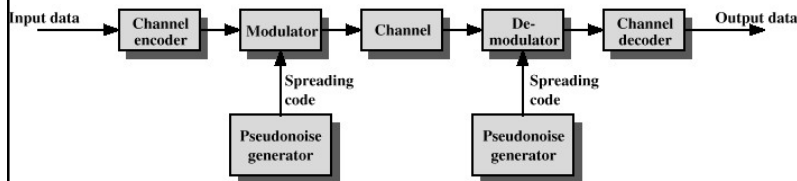


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## Direct Sequence Spread Spectrum



## Spread Spectrum



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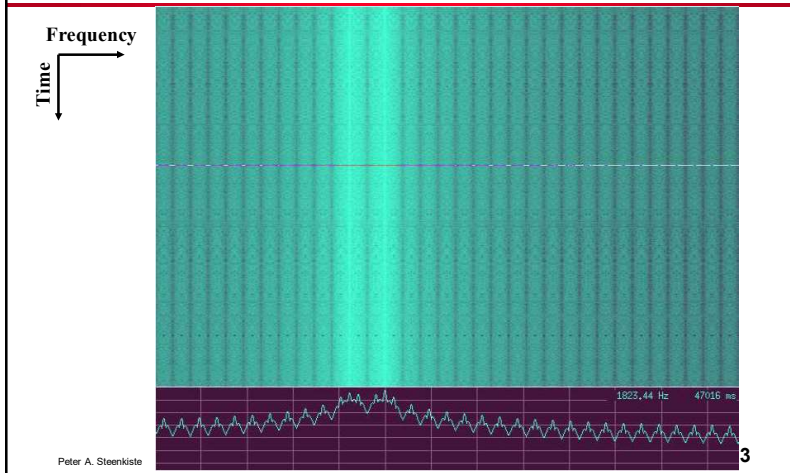
## Example: Original 802.11 Standard (DSSS)

- The DS PHY uses a 1 Msymbol/s rate with an 11-to-1 spreading ratio and a Barker chipping sequence
  - » Barker sequence has low autocorrelation properties – why?
  - » Uses about 22 MHz
- Receiver decodes by counting the number of “1” bits in each word
  - » 6 “1” bits correspond to a 0 data bit
- Chips were transmitted using DBPSK modulation
  - » Resulting data rate is 1 Mbps (i.e. 11 Mchips/sec)
  - » Extended to 2 Mbps by using a DQPSK modulation
    - Requires the detection of a ¼ phase shift

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## Spectrogram: DSSS-encoded Signal



## DSSS Properties

- Since each bit is sent as multiple chips, you need more bps bandwidth to send the signal.
  - » Number of chips per bit is called the spreading ratio
- Given the Nyquist and Shannon results, you need more spectral bandwidth to do this.
  - » Spreading the signal over the spectrum
- Advantage is that is transmission is more resilient.
  - » Effective against noise and multi-path
  - » DSSS signal will look like noise in a narrow band
  - » Can lose some chips in a word and recover easily
- Multiple users can share bandwidth (easily).
  - » Follows directly from Shannon (capacity is there)
  - » E.g., Code Division Multiple Access - next

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## Code Division Multiple Access

- Users use a spectrum band at the same time, but they use different codes to spread their data over the frequency
  - » DSSS where users use different spreading sequences
  - » Use spreading sequences that are orthogonal, i.e. they have minimal overlap
- The signal of other users will appear as noise
  - » But since the each user uses a lot of spectrum their signal is very robust
- Offers an easy way to share spectrum
  - » Adding users will increase the noise for each user
  - » This will reduce their throughput – sharing!

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## CDMA Principle

- Basic Principles of CDMA
  - »  $D$  = rate of data signal
  - » Break each bit into  $k$  chips - user-specific fixed pattern
  - » Chip data rate of new channel =  $kD$
- If  $k=6$  and code is a sequence of 1s and -1s
  - » For a '1' bit, A sends code as chip pattern
    - $\langle c1, c2, c3, c4, c5, c6 \rangle$
  - » For a '0' bit, A sends complement of code
    - $\langle -c1, -c2, -c3, -c4, -c5, -c6 \rangle$
- Receiver knows sender's code and performs electronic decode function

$$S_u(d) = d1 \times c1 + d2 \times c2 + d3 \times c3 + d4 \times c4 + d5 \times c5 + d6 \times c6$$

- $\langle d1, d2, d3, d4, d5, d6 \rangle$  = received chip pattern
- $\langle c1, c2, c3, c4, c5, c6 \rangle$  = sender's code

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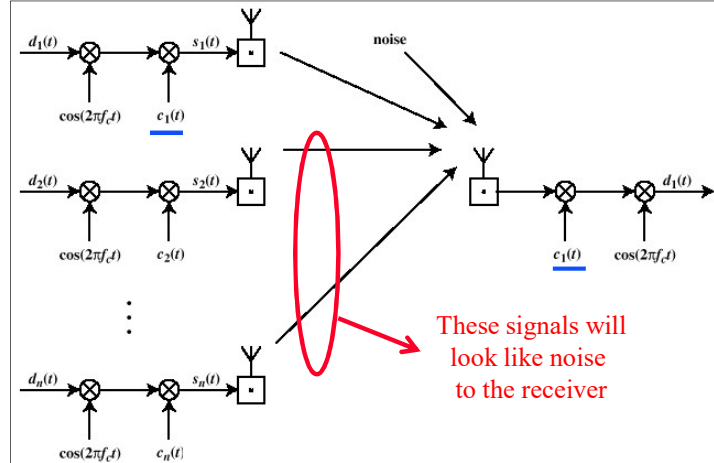
## CDMA Example

- **User A code =  $\langle 1, -1, -1, 1, -1, 1 \rangle$** 
  - » To send a 1 bit =  $\langle 1, -1, -1, 1, -1, 1 \rangle$
  - » To send a 0 bit =  $\langle -1, 1, 1, -1, 1, -1 \rangle$
- **User B code =  $\langle 1, 1, -1, -1, 1, 1 \rangle$** 
  - » To send a 1 bit =  $\langle 1, 1, -1, -1, 1, 1 \rangle$
- **Receiver receiving with A's code**
  - » (A's code) x (received chip pattern)
    - User A '1' bit: 6  $\rightarrow$  1
    - User A '0' bit: -6  $\rightarrow$  0
    - User B '1' bit: 0  $\rightarrow$  unwanted signal ignored

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## CDMA for Direct Sequence Spread Spectrum



## CDMA Discussion

- **CDMA does not assign a fixed bandwidth but a user's bandwidth depends on the traffic load**
  - » More users results in more "noise" and less throughput for each user, e.g. more information lost due to errors
  - » How graceful the degradation is depends on how orthogonal the codes are
  - » TDMA and FDMA have a fixed channel capacity
- **Weaker signals may be lost in the clutter**
  - » This will systematically put the same node pairs at a disadvantage – not acceptable
  - » The solution is to add power control, i.e. nearby nodes use a lower transmission power than remote nodes

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## CDMA Example

- **CDMA cellular standard**
  - » 3G standard
  - » Used in the US, e.g. Sprint
- **Allocates 1.228 MHz for base station to mobile communication**
  - » Shared by 64 "code channels"
  - » Used for voice (55), paging service (8), and control (1)
- **Provides a lot error coding to recover from errors**
  - » Voice data is 8550 bps
  - » Coding and FEC increase this to 19.2 kbps
  - » Then spread out over 1.228 MHz using DSSS; uses QPSK

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## Summary

- Spread spectrum achieves robustness by spreading out the signal over a wide channel
  - » Sending different data blocks on different frequencies, or
  - » Spreading all data across the entire channel
- CDMA builds on the same concept by allowing multiple senders to simultaneously use the same channel
  - » Sender and receiver must coordinate so receiver can decode the data

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## Outline

- RF introduction
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- OFDM

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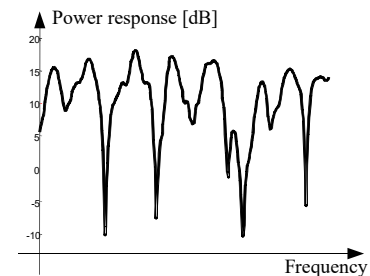
## How Do We Increase Rates?

- Two challenges related to multipath:
- Frequency selective fading starts to have a bigger impact because there is less redundancy in the signal
- As rates increase, symbol times shrink and the effects of inter-symbol interference becomes more pronounced
  - » See earlier examples
- We would like an encoding and modulation solution that has longer symbol times and allows us to fight frequency selective fading more effectively

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## Frequency-Selective Radio Channel

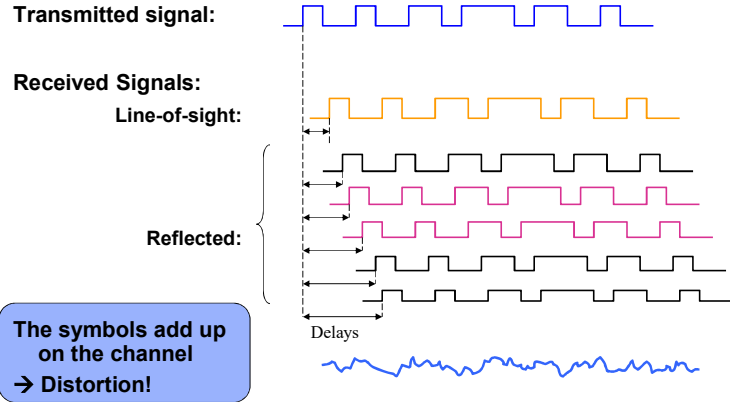


- Interference of reflected and LOS radio waves results in frequency dependent fading
- Impact is reduced for narrow channels

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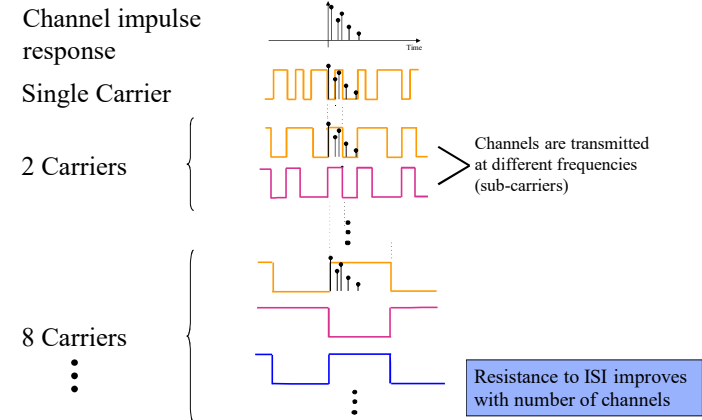
## Inter-Symbol-Interference



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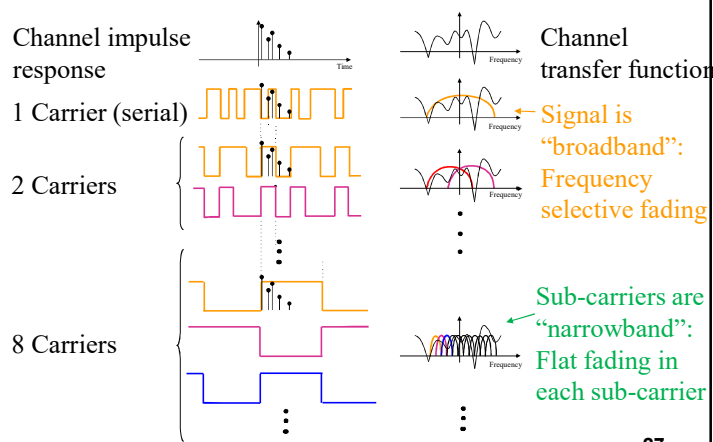
## Distributing Bits over Subcarriers



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## Benefits of Narrow Band Channels

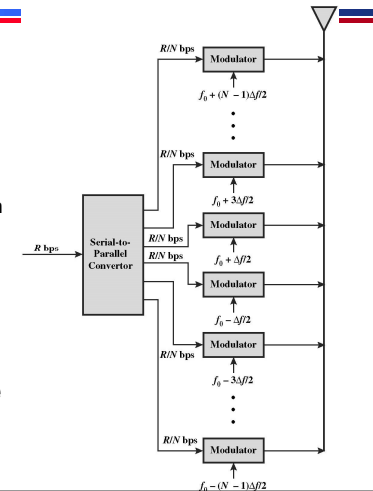


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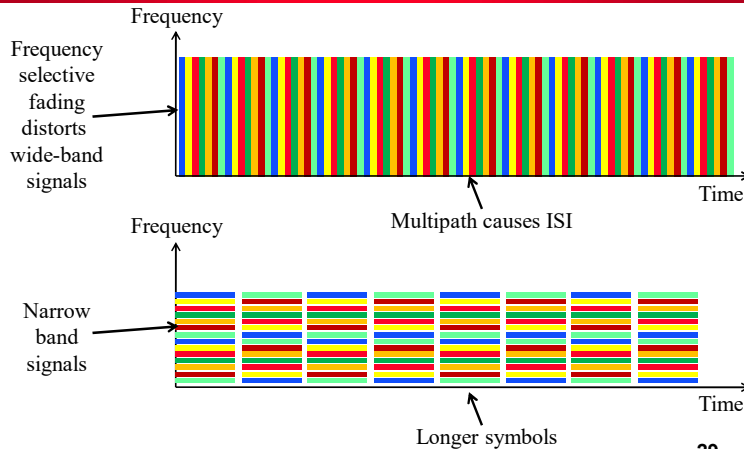
## OFDM - Orthogonal Frequency Division Multiplexing

- **Distribute bits over N subcarriers that use different frequencies in the band B**
  - » Multi-carrier modulation
  - » Each signal uses  $\sim B/N$  bandwidth
- **Since each subcarrier only encodes  $1/N$  of the bit stream, each symbol takes N times longer in time**
- **Since signals are narrower, fighting frequency selective fading is easier**



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## OFDM Transmission



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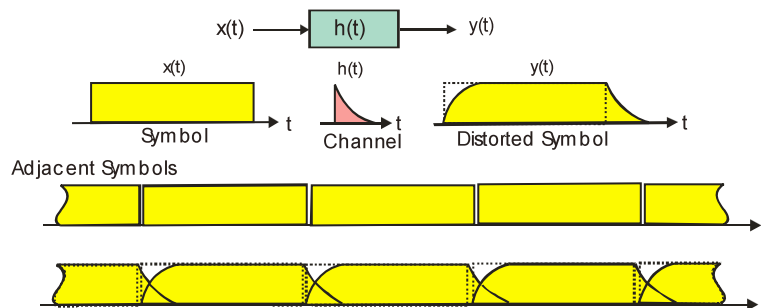
## Fighting ISI

- Frequency selective fading will only affects some subcarriers
  - » May be able to simply amplify affected subcarriers
  - » No need for complex dynamic equalizer
    - Become less effective with shorter symbols
- Further reduce ISI effects by sending a “cyclic prefix” before every burst of symbols
  - » Can be used to absorb delayed copies of real symbols, without affecting the symbols in the next burst
  - » Prefix is a copy of the tail of the symbol burst to maintain a smooth symbol
  - » E.g. a cyclic prefix of 64 symbols and data bursts of 256 symbols using QPSK modulation

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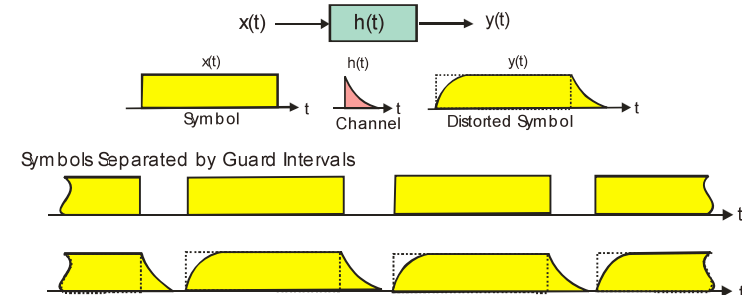
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## Adjacent Symbol Interference (ASI) Symbol Smearing Due to Channel



Slide Prof Harris, SDSU 31

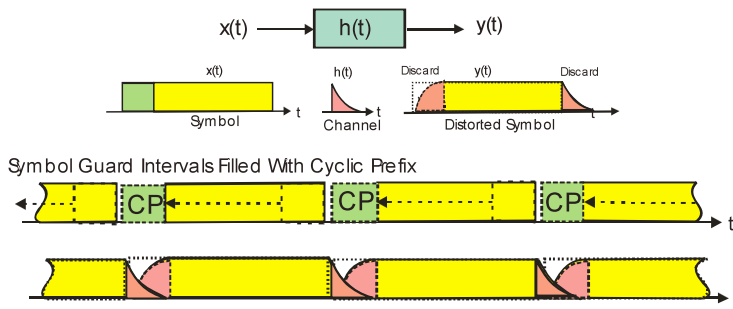
## Guard Interval Inserted Between Adjacent Symbols to Suppress ASI



Slide Prof Harris, SDSU 32



## Cyclic Prefix Inserted in Guard Interval to Suppress Adjacent Channel Interference (ACI)

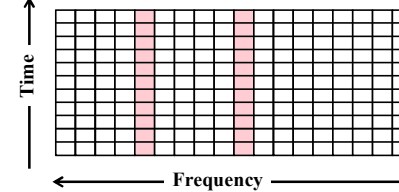


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## Use of Redundancy in OFDM

- OFDM uses error coding as described earlier
  - » Degree of error coding depends on channel conditions
- OFDM offers frequency and diversity
  - » Frequency: data is spread out over multiple subcarriers
  - » Time: data spread out over multiple time slots



- Combining OFDM with MIMO adds space diversity (discussed later in course)

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## Implementing OFDM

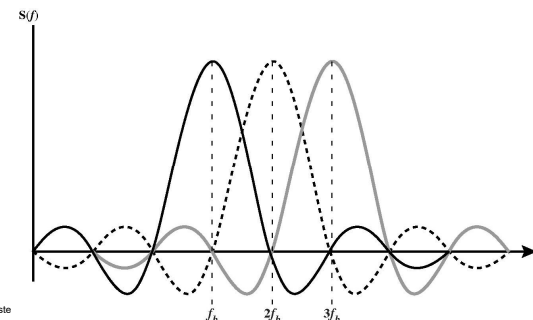
- This is great, but OFDM looks very complicated!
- How many radios do I need? 48?
- How do I get 48 (or more) subcarriers packed very densely?
- Do I need guard bands between the subcarriers, and if so, how wide?
  - » Looks like a lot of wasted spectrum

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## Subcarriers are "Orthogonal"

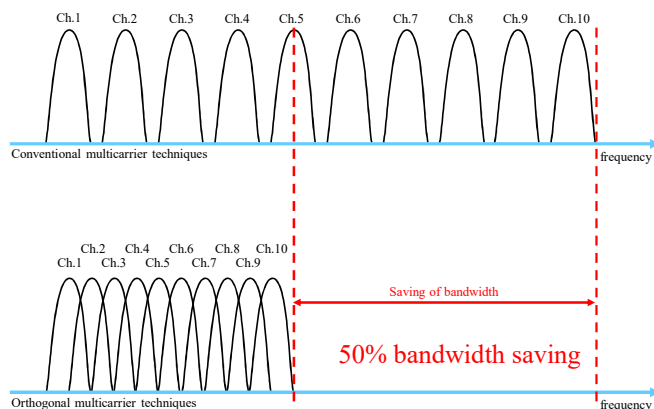
- Peaks of spectral density of each carrier coincide with the zeros of the other carriers
  - » Carriers can be packed very densely with minimal interference
  - » Requires very good control over frequencies



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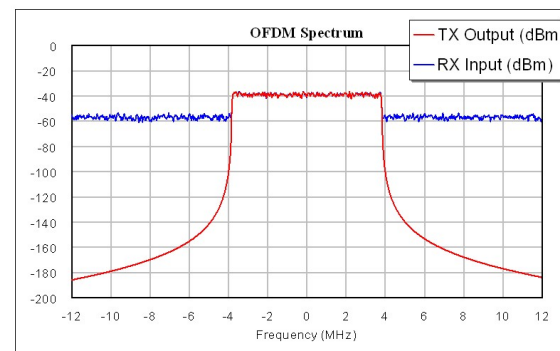
## Densely Packing OFDM Channels



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## OFDM Spectrum Use



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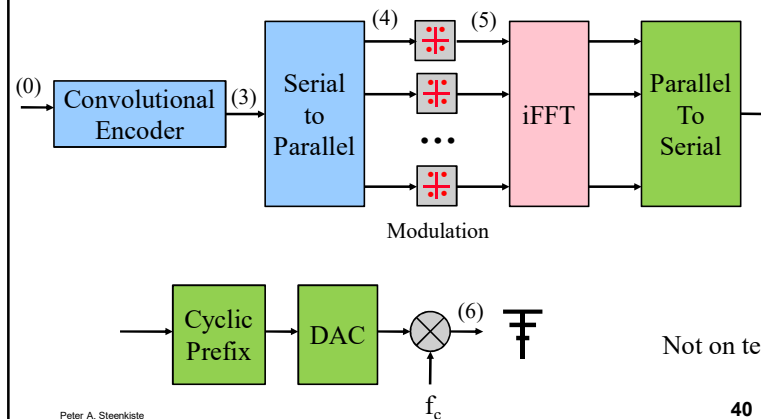
## Implementing OFDM

- **The naïve approach is to modulate individual subcarriers and move them each to the right frequency**
  - » Not practical: the subcarriers are packed very densely and their spacing must be very precise
  - » Also complicated: lots of signals to deal with!
- **How it works: Radio modulates the subcarriers and combines them in the digital domain and then converts the signal to the analog domain**
  - » The details do not matter for this course

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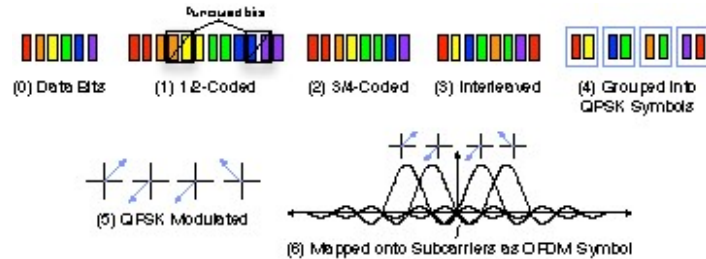
## OFDM Transmitter



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## OFDM in 802.11



- Uses punctured code: add redundancy and then drop some bits to reach a certain level of redundancy

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## OFDM in WiFi

- OFDM is used in all “post b” WiFi standard
- Example: 802.11a
- 20 MHz band, with a signal of 16.6 MHz
- 52 subcarriers: 48 for data, 4 pilots
- Modulations: BPSK, QPSK, 16-QAM, 64-QAM
- 4 microsec symbol duration, including a 0.8 microsec guard interval
- Modulation and coding scheme determines the bit rates

» Next slide

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## MCS for 802.11a

MCS index	RATE bits	Modulation type	Coding rate	Data rate (Mbit/s)
13	1101	BPSK	1/2	6
16	1111	BPSK	3/4	9
5	0101	QPSK	1/2	12
7	0111	QPSK	3/4	18
9	1001	16-QAM	1/2	24
11	1011	16-QAM	3/4	36
1	0001	64-QAM	2/3	48
3	0011	64-QAM	3/4	54

Symbol rate is 12 Msymbols/sec

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## Discussion

- OFDM is very effective in fighting frequency selective fading and ISI
- Finally a free lunch?
- No – you introduce some overhead
  - » Frequency: you need space between the sub carriers
  - » Time: You need to insert prefixes
- You also add complexity
  - » How do you create many, closely spaced subcarriers?
  - » The OFDM signal is fairly flat in the frequency domain, so it is very variable in the time domain
    - High peak-to-average Power ratio (PAPR)
    - Can be a problem for simple, mobile devices

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## Summary

- **OFDM fights frequency selective fading and inter-symbol interference to increase rates**
  - » Both become more significant at higher rates
  - » It modules a large number of narrow-band signals (subcarriers) instead of a single wide channel
  - » Cyclic prefixes are used to separate symbols
- **It uses time and frequency diversity, combined with coding (FEC) to reduce the effect of fading**
  - » Can “pick” the right bit rate for the observed channel conditions by adjusting both the modulation and coding parameters