

Classical Planning:  
instantiated actions, state search, heuristics

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*15-887 – Planning, Execution, and Learning – Fall 2016*

## Outline

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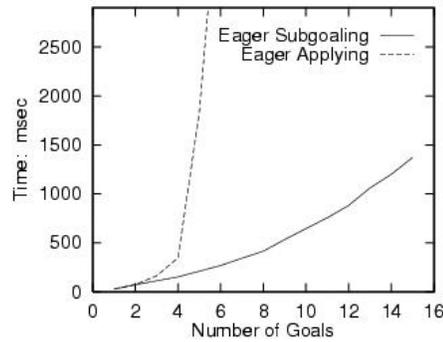
- State-space search
- GraphPlan
  - A type of state-space search
  - Fully instantiated operators
- (Satplan, FF)

## Impact of State-Space Search and MEA

Operator:  $A_i$   
 preconds:  $\{I_i\}$   
 adds:  $\{G_i\}$   
 deletes:  $\{I_j | j < i\}$

Example:

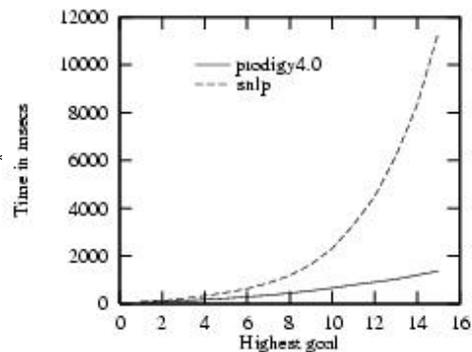
- Initial state:  $I_1, I_2, I_3$
- Goal:  $G_2, G_3, G_1$
- Plan:  $A_1, A_2, A_3$



## Impact of State-Space and MEA

operator $A_i$	operator $A_*$
preconds $g_*, g_{i-1}$	preconds $()$
adds $g_i$	adds $g_*$
deletes $g_*$	deletes $()$

Initial state:  $g_*$   
 Goal statement:  $g_*, g_5$   
 Plan:  $A_1, A_*, A_2, A_*, A_3, A_*, A_4, A_*$



## Example: One-Way Rocket Domain

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```
(OPERATOR LOAD-ROCKET
:preconds
?roc ROCKET
?obj OBJECT
?loc LOCATION
(and (at ?obj ?loc)
      (at ?roc ?loc))
:effects
add (inside ?obj ?roc)
del (at ?obj ?loc))

(OPERATOR UNLOAD-ROCKET
:preconds
?roc ROCKET
?obj OBJECT
?loc LOCATION
(and (inside ?obj ?roc)
      (at ?roc ?loc))
:effects
add (at ?obj ?loc)
del (inside ?obj ?roc))

(OPERATOR MOVE-ROCKET
:preconds
?roc ROCKET
?from-l LOCATION
?to-l LOCATION
(and (at ?roc ?from-l)
      (has-fuel ?roc))
:effects
add (at ?roc ?to-l)
del (at ?roc ?from-l)
del (has-fuel ?roc))
```

## Graphplan

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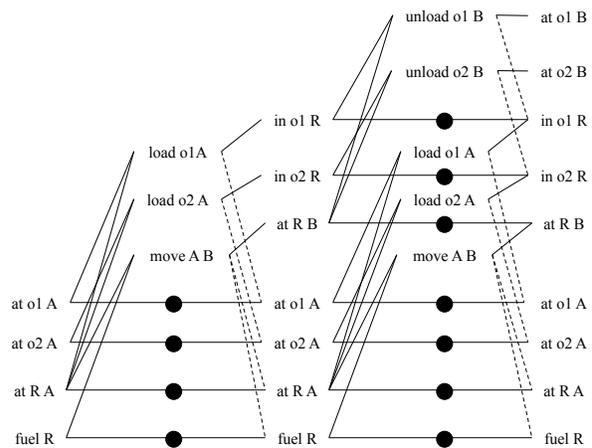
*Blum & Furst 95*

- Preprocessing before engaging in search.
- Forward search combined with backward search.
- Construct a *planning graph* to reveal constraints
- Two stages:
  - **Extend**: One time step in the planning graph.
  - **Search**: Find a valid plan in the planning graph.
- Graphplan finds a plan or proves that no plan has fewer “time steps.”

## Plan Graph

### One-Way Rocket Example

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## Extending a Planning Graph - Actions

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- To create an action-level  $i$ :
  - Add each instantiated operator, for which all of its preconditions are present at proposition-level  $i$  AND *no two of its preconditions are exclusive*.
  - Add all the no-op actions.
- Determine the **exclusive** actions.

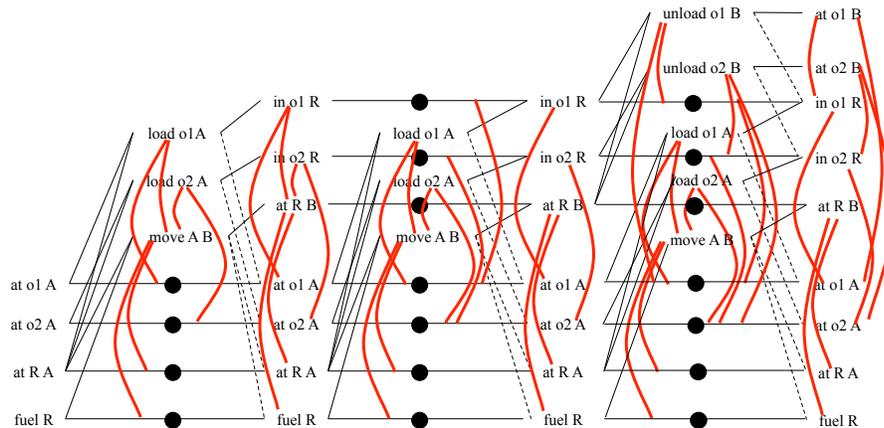
## Extending a Planning Graph – Propositions

- To create a proposition-level  $i + 1$ :
  - Add all the effects of the inserted actions at action-level  $i$  - distinguishing add and delete effects.
- Determine the **exclusive** actions.

## Planning Graphs

- A literal may exist at level  $i + 1$  if it is an Add-Effect of some action in level  $i$ .
- Two propositions  $p$  and  $q$  are **exclusive** in a proposition-level if ALL actions that add  $p$  are exclusive of ALL actions that add  $q$ .
- Actions A and B are **exclusive** at action-level  $i$ , if:
  - **Interference**: A (or B) deletes a precondition or an Add-Effect of B (or A).
  - **Competing Needs**:  $p$  is a precondition of A and  $q$  is a precondition of B, and  $p$  and  $q$  are exclusive in proposition-level  $i - 1$ .

## Mutex Exclusivity Relations One-Way Rocket Example



## Exclusivity Examples

- Exclusive Actions: (Move A B) deletes a precondition of (Load o1 A). Therefore exclusive (existence of threats).
- Exclusive Propositions: (at R A) and (at R B) at time 2 are exclusive. (at R A) is added by a no-op and (at R B) is added by (Move A B) and no-op and (Move A B) are exclusive actions.
- Exclusive Actions: Then (Load o1 A) and (Load o2 B) are exclusive because (at R A) and (at R B) are exclusive.
- Propositions can be exclusive in some time step and not in others: If (at o1 A) and (at R A) at time 1, then (in o1 A) and (at R B) are exclusive at time 2, but not at time 3.

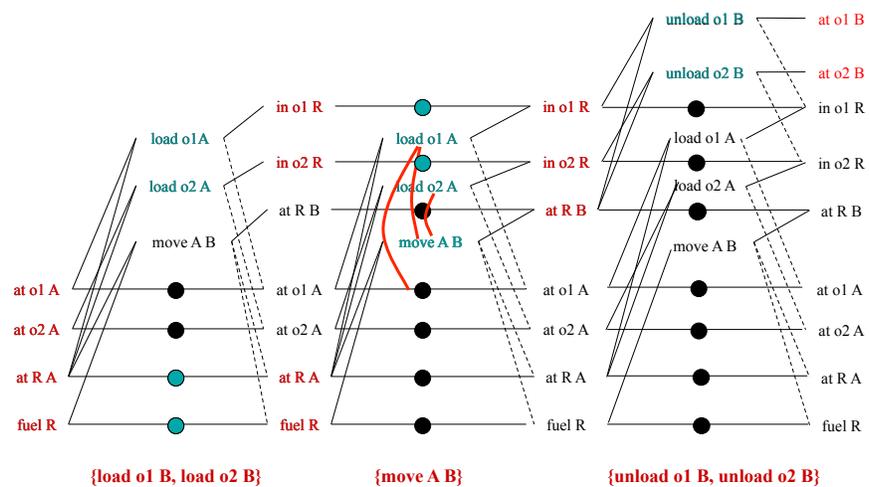
## Searching a Planning Graph

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- Level-by-level backward-chaining approach to use the exclusivity constraints.
- Given a set of goals at time  $t$ , identify all the sets of actions (including no-ops) at time  $t - 1$  who add those goals and are not exclusive. The preconditions of these actions are new goals for  $t - 1$ .

## Searching a Planning Graph

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## Recursive Search

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- For each goal at time  $t$  in some arbitrary order:
  - Select some action at time  $t - 1$  that achieves that goal and it is not exclusive with any other action already selected.
  - Do this recursively for all the goals at time  $t - 1$  - do not add new action, but use the ones already selected if they add another goal.
  - If recursion returns failure, then select a different action.
- The new goal set is the set of all the preconditions of the selected actions.

## Enhancements

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- Forward-checking - for the goals ahead, check if all the actions that add it are exclusive with the selected action.
- Memoization - when a set of goals is not solvable at some time  $t$ , then this is recorded and hashed. If back at time  $t$ , the hash table is checked and search proceeds backing up right away.

## Planning as Satisfiability

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- One interpretation: ‘‘first-order deductive theorem-proving does not scale well.’’
- One solution: ‘‘propositional satisfiability’’
- Uniform clausal representation for goals and operators.
- Stochastic local search is a powerful technique for planning.

## SatPlan

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- Assume the plan has  $n$  (time-parallel) steps. (*strong assumption*)
- **Initial state:** completely specified at time 0.  
 $at-o1-A_0 \wedge at-o2-A_0 \wedge at-R-A_0$
- **Goal:** specified at time  $2n$ .  
 $at-o1-B_6 \wedge at-o2-B_6$
- **Actions:** specified at *odd* times; An action implies its preconditions and effects.  
 $(\neg load-o1-A_1 \vee at-o1-A_0) \wedge (\neg load-o1-A_1 \vee at-R-A_0) \wedge$   
 $(\neg load-o1-A_1 \vee in-R-A_2) \wedge (\neg load-o1-A_1 \vee \neg at-o1-A_2)$

## “FF”

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- A\* search with heuristic values from:
  - *Relaxed* planning graph – only add effects

## Summary

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- **Planning:** selecting one sequence of actions (operators) that transform (apply to) an initial state to a final state where the goal statement is true.
- **Means-ends analysis:** identify and reduce, as soon as possible, *differences* between state and goals.
- **Linear planning:** backward chaining with means-ends analysis using a stack of goals - potentially efficient, possibly unoptimal, incomplete; GPS, STRIPS.
- **Nonlinear planning with means-ends analysis:** backward chaining using a set of goals; reason about *when* “to reduce the differences;” Prodigy4.0.
- **Graphplan**
  - Expand (forward) and search (backwards)
- **SATPlan, FF**