



# 10-601 Introduction to Machine Learning

Machine Learning Department  
School of Computer Science  
Carnegie Mellon University

## Midterm Exam Review + Multinomial Logistic Reg. + Feature Engineering + Regularization

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Lecture 10  
Feb. 18, 2019

# Reminders

- **Homework 4: Logistic Regression**
  - Out: Fri, Feb 15
  - Due: Fri, Mar 1 at 11:59pm
- **Midterm Exam 1**
  - Thu, Feb 21, 6:30pm – 8:00pm
- **Today's In-Class Poll**
  - <http://p10.mlcourse.org>
- *Reading on Probabilistic Learning is reused later in the course for MLE/MAP*

# Outline

- Midterm Exam Logistics
- Sample Questions
- Classification and Regression:  
The Big Picture
- Q&A

# **MIDTERM EXAM LOGISTICS**

# Midterm Exam

- **Time / Location**
  - **Time:** Evening Exam  
**Thu, Feb. 21 at 6:30pm – 8:00pm**
  - **Room:** We will contact each student individually with **your room assignment**. The rooms are **not** based on section.
  - **Seats:** There will be **assigned seats**. Please arrive early.
  - Please watch Piazza carefully for announcements regarding room / seat assignments.
- **Logistics**
  - Covered material: Lecture 1 – Lecture 8
  - Format of questions:
    - Multiple choice
    - True / False (with justification)
    - Derivations
    - Short answers
    - Interpreting figures
    - Implementing algorithms on paper
  - No electronic devices
  - You are allowed to **bring** one 8½ x 11 sheet of notes (front and back)

# Midterm Exam

- **How to Prepare**

- Attend the midterm review lecture (right now!)
- Review prior year's exam and solutions (we'll post them)
- Review this year's homework problems
- Consider whether you have achieved the “learning objectives” for each lecture / section

# Midterm Exam

- **Advice (for during the exam)**
  - Solve the easy problems first  
(e.g. multiple choice before derivations)
    - if a problem seems extremely complicated you're likely missing something
  - Don't leave any answer blank!
  - If you make an assumption, write it down
  - If you look at a question and don't know the answer:
    - we probably haven't told you the answer
    - but we've told you enough to work it out
    - imagine arguing for some answer and see if you like it

# Topics for Midterm

- Foundations
  - Probability, Linear Algebra, Geometry, Calculus
  - Optimization
- Important Concepts
  - Overfitting
  - Experimental Design
- Classification
  - Decision Tree
  - KNN
  - Perceptron
- Regression
  - Linear Regression

# **SAMPLE QUESTIONS**

# Sample Questions

## 1.4 Probability

Assume we have a sample space  $\Omega$ . Answer each question with **T** or **F**.

(a) [1 pts.] **T or F:** If events  $A$ ,  $B$ , and  $C$  are disjoint then they are independent.

(b) [1 pts.] **T or F:**  $P(A|B) \propto \frac{P(A)P(B|A)}{P(A|B)}$ . (The sign ' $\propto$ ' means 'is proportional to')

# Sample Questions

## 5.2 Constructing decision trees

Consider the problem of predicting whether the university will be closed on a particular day. We will assume that the factors which decide this are whether there is a snowstorm, whether it is a weekend or an official holiday. Suppose we have the training examples described in the Table 5.2.

Snowstorm	Holiday	Weekend	Closed
T	T	F	F
T	T	F	T
F	T	F	F
T	T	F	F
F	F	F	F
F	F	F	T
T	F	F	T
F	F	F	T

Table 1: Training examples for decision tree

- **[2 points]** What would be the effect of the Weekend attribute on the decision tree if it were made the root? Explain in terms

# Sample Questions

## 4 K-NN [12 pts]

Now we will apply K-Nearest Neighbors using Euclidean distance to a binary classification task. We assign the class of the test point to be the class of the majority of the  $k$  nearest neighbors. A point can be its own neighbor.

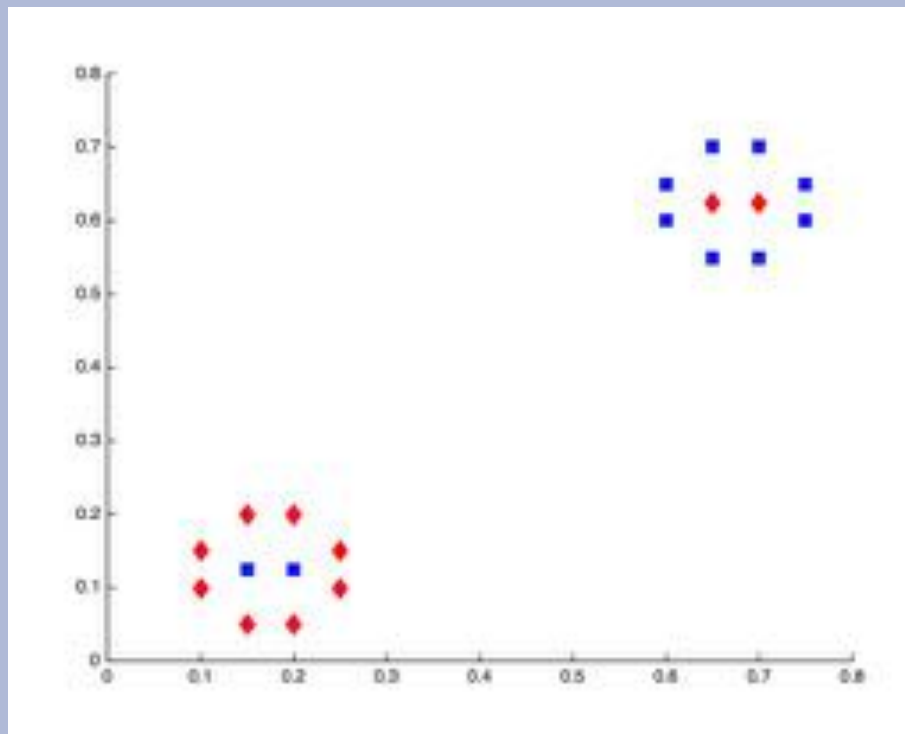


Figure 5

3. [2 pts] What value of  $k$  minimizes leave-one-out cross-validation error for the dataset shown in Figure 5? What is the resulting error?

# Sample Questions

## 4.1 True or False

Answer each of the following questions with **T** or **F** and **provide a one line justification**.

- (a) [2 pts.] Consider two datasets  $D^{(1)}$  and  $D^{(2)}$  where  $D^{(1)} = \{(x_1^{(1)}, y_1^{(1)}), \dots, (x_n^{(1)}, y_n^{(1)})\}$  and  $D^{(2)} = \{(x_1^{(2)}, y_1^{(2)}), \dots, (x_m^{(2)}, y_m^{(2)})\}$  such that  $x_i^{(1)} \in \mathbb{R}^{d_1}$ ,  $x_i^{(2)} \in \mathbb{R}^{d_2}$ . Suppose  $d_1 > d_2$  and  $n > m$ . Then the maximum number of mistakes a perceptron algorithm will make is higher on dataset  $D^{(1)}$  than on dataset  $D^{(2)}$ .

# Sample Questions

## 3.1 Linear regression

Consider the dataset  $S$  plotted in Fig. 1 along with its associated regression line. For each of the altered data sets  $S^{\text{new}}$  plotted in Fig. 3, indicate which regression line (relative to the original one) in Fig. 2 corresponds to the regression line for the new data set. Write your answers in the table below.

Dataset	(a)	(b)	(c)	(d)	(e)
Regression line					

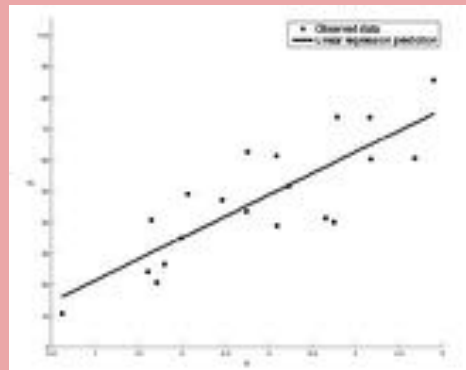


Figure 1: An observed data set and its associated regression line.







# Matching Game

**Goal:** Match the Algorithm to its Update Rule

1. SGD for Logistic Regression

$$h_{\theta}(\mathbf{x}) = p(y|x)$$

2. Least Mean Squares

$$h_{\theta}(\mathbf{x}) = \theta^T \mathbf{x}$$

3. Perceptron

$$h_{\theta}(\mathbf{x}) = \text{sign}(\theta^T \mathbf{x})$$

4.  $\theta_k \leftarrow \theta_k + (h_{\theta}(\mathbf{x}^{(i)}) - y^{(i)})$

5.  $\theta_k \leftarrow \theta_k + \frac{1}{1 + \exp \lambda(h_{\theta}(\mathbf{x}^{(i)}) - y^{(i)})}$

</

Q&A

# **MULTINOMIAL LOGISTIC REGRESSION**



# Multinomial Logistic Regression

## *Chalkboard*

- Background: Multinomial distribution
- Definition: Multi-class classification
- Geometric intuitions
- Multinomial logistic regression model
- Generative story
- Reduction to binary logistic regression
- Partial derivatives and gradients
- Applying Gradient Descent and SGD
- Implementation w/ sparse features

# Debug that Program!

## In-Class Exercise: *Think-Pair-Share*

Debug the following program which is (incorrectly) attempting to run SGD for multinomial logistic regression

### Buggy Program:

```
while not converged:
    for i in shuffle([1,...,N]):
        for k in [1,...,K]:
            theta[k] = theta[k] - lambda * grad(x[i], y[i],
theta, k)
```

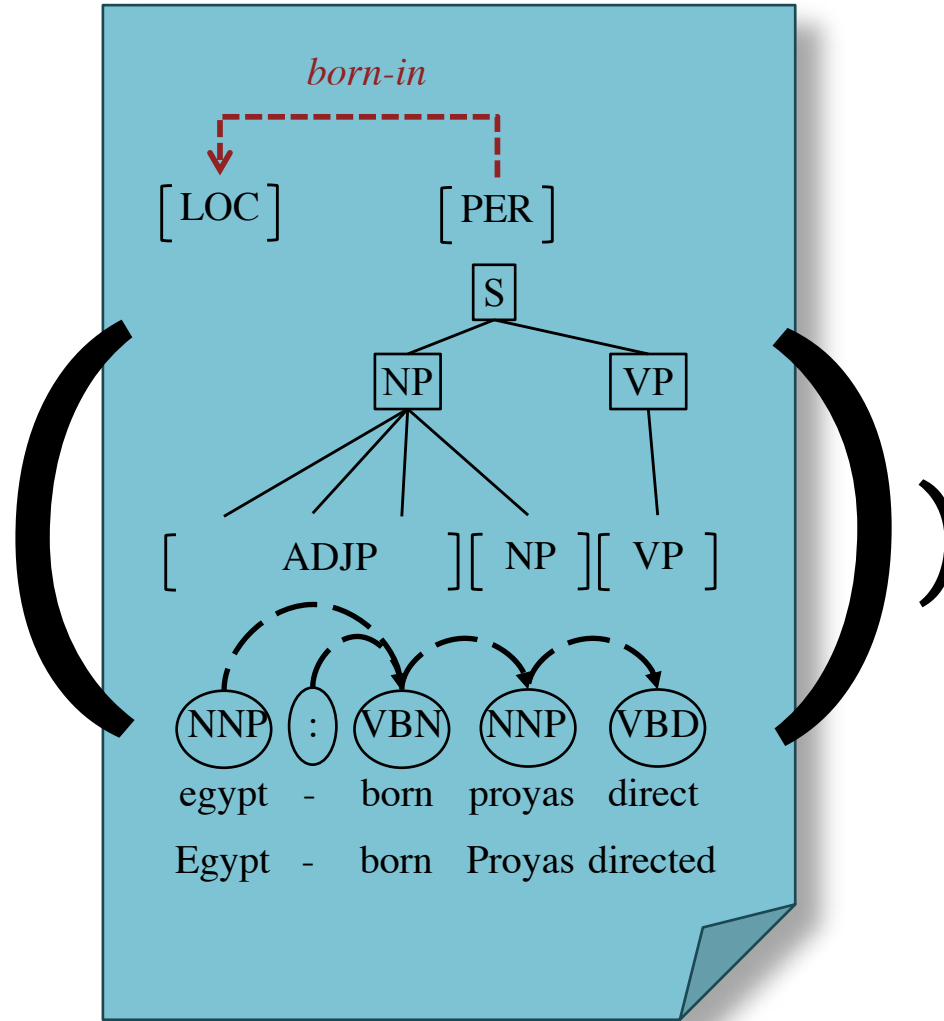
**Assume:** `grad(x[i], y[i], theta, k)` returns the gradient of the negative log-likelihood of the training example  $(x[i], y[i])$  with respect to vector `theta[k]`. `lambda` is the learning rate. `N` = # of examples. `K` = # of output classes. `M` = # of features. `theta` is a `K` by `M` matrix.

# **FEATURE ENGINEERING**

# Handcrafted Features

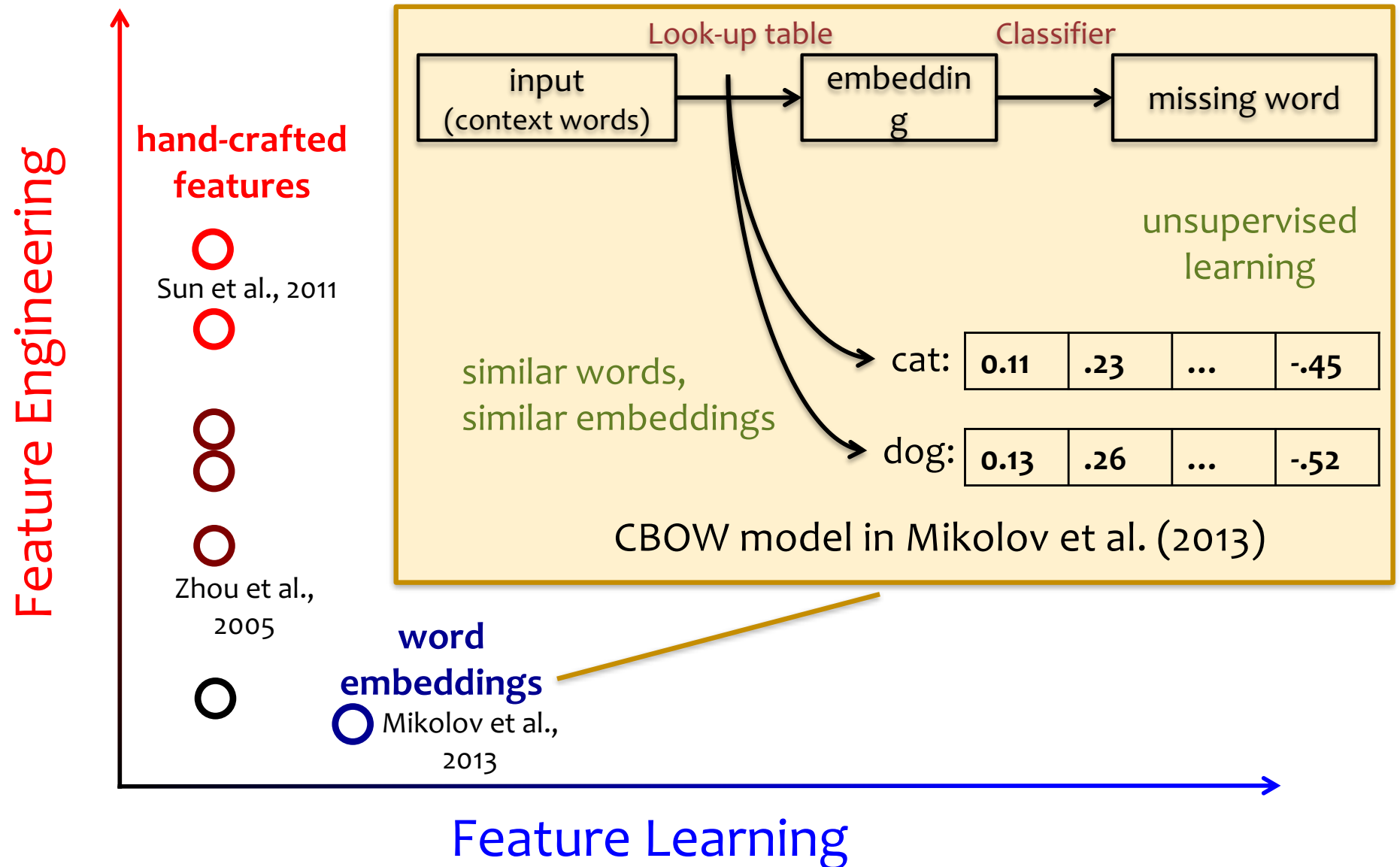
$$p(y|x) \propto$$

$$\exp(\Theta_y \cdot f$$



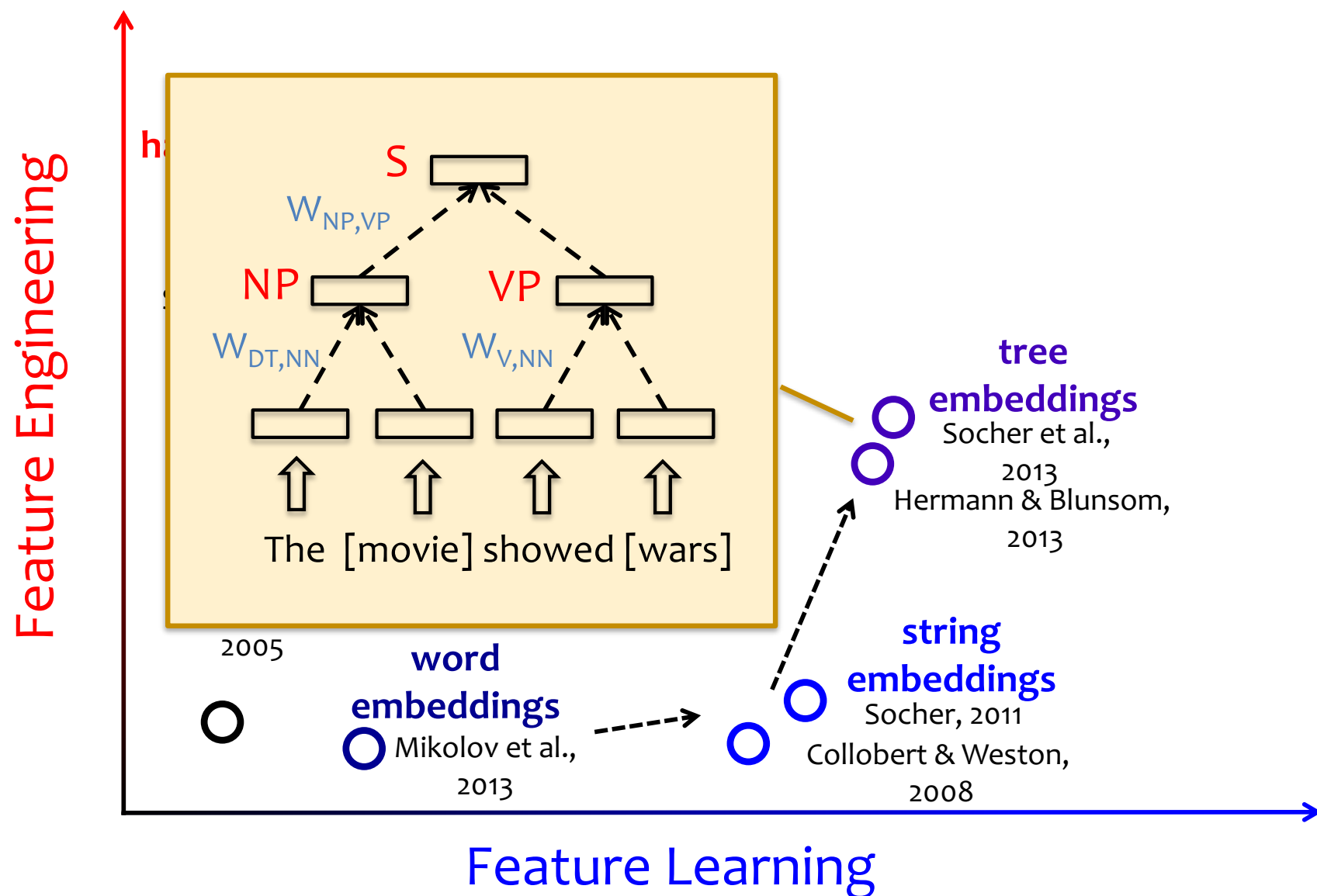


# Where do features come from?





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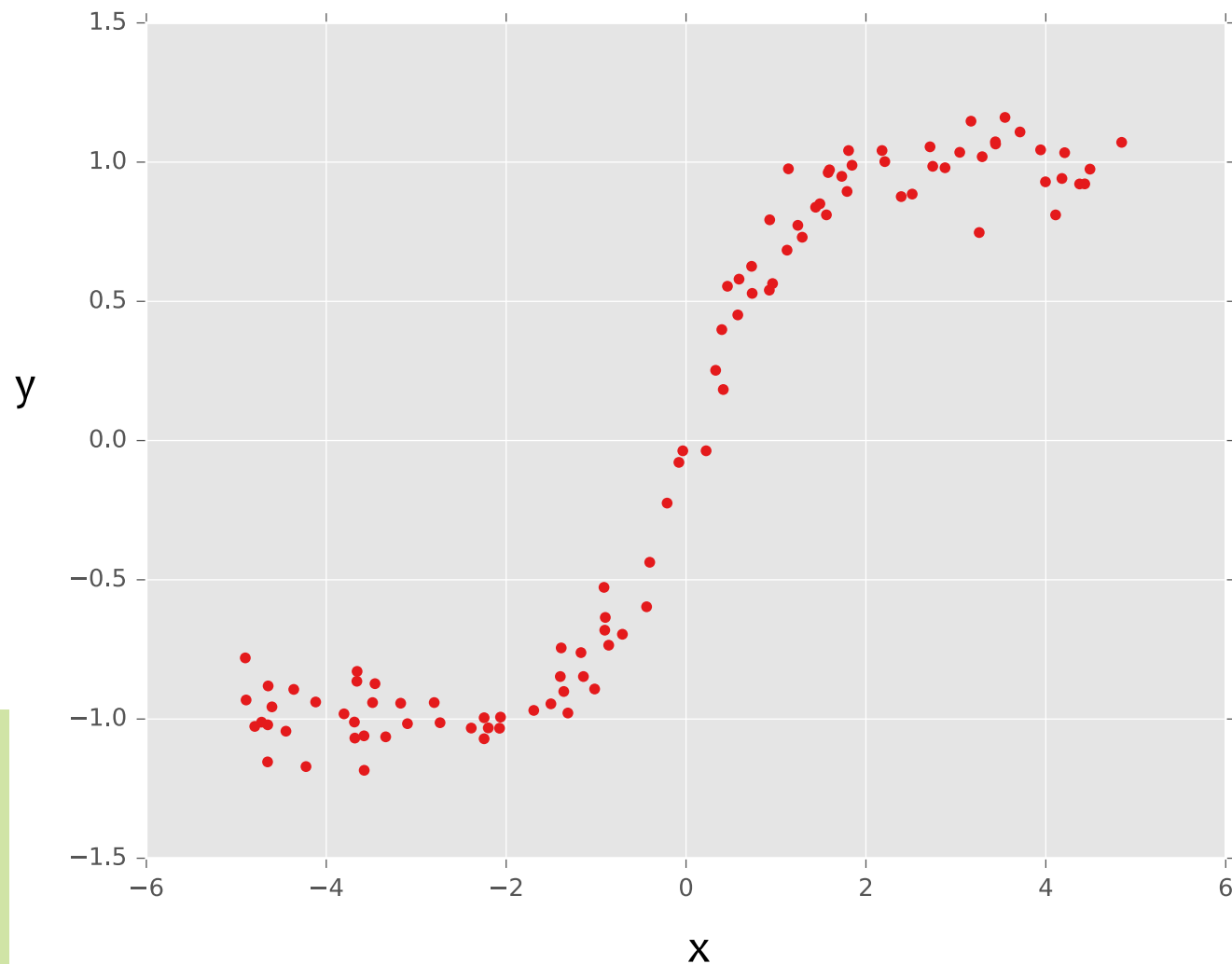


# **NON-LINEAR FEATURES**



# Example: Linear Regression

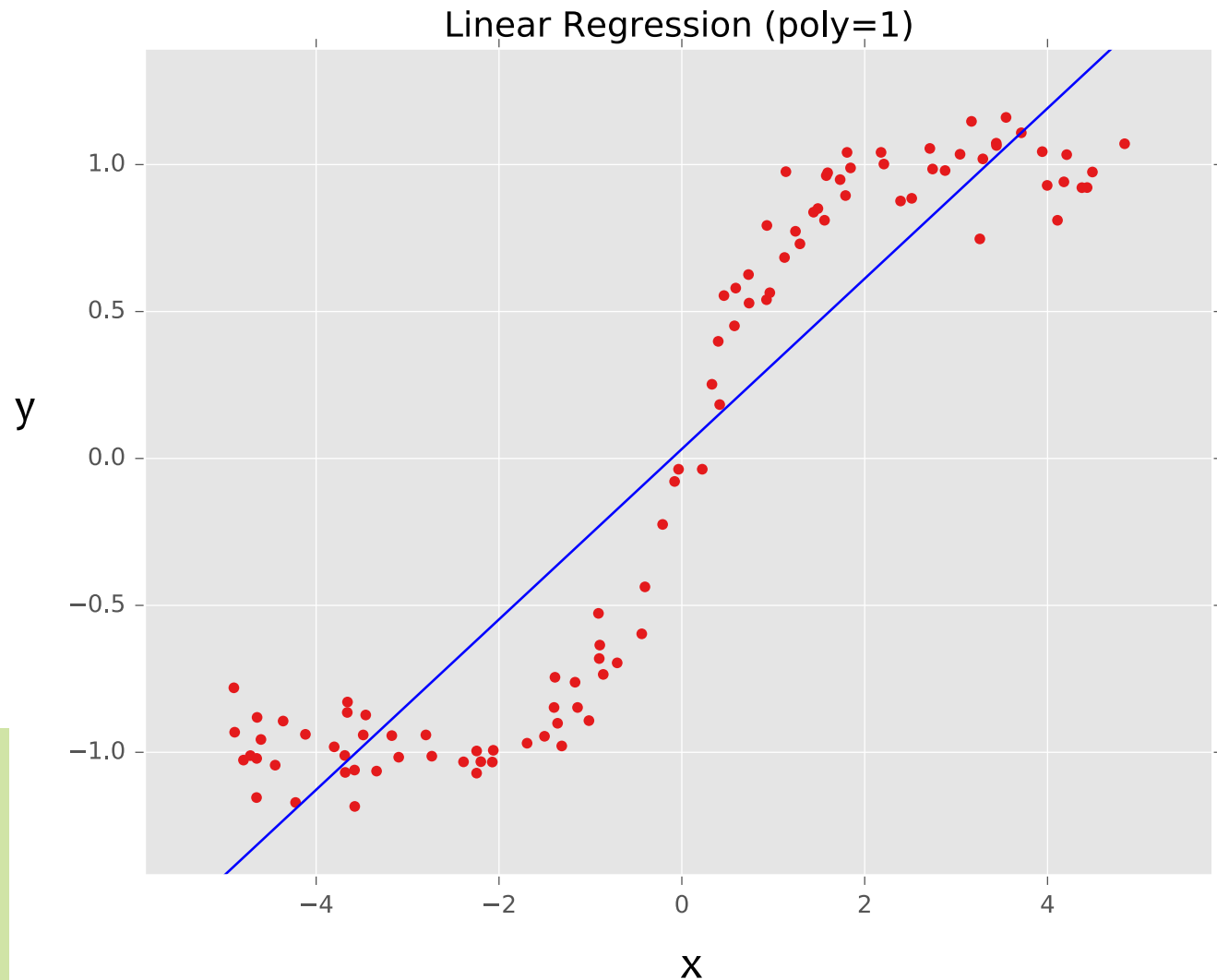
**Goal:** Learn  $y = \mathbf{w}^T \mathbf{f}(\mathbf{x}) + b$   
where  $\mathbf{f}(\cdot)$  is a polynomial  
basis function



true “unknown”  
target function is  
 $y = \tanh(x) + \text{noise}$

# Example: Linear Regression

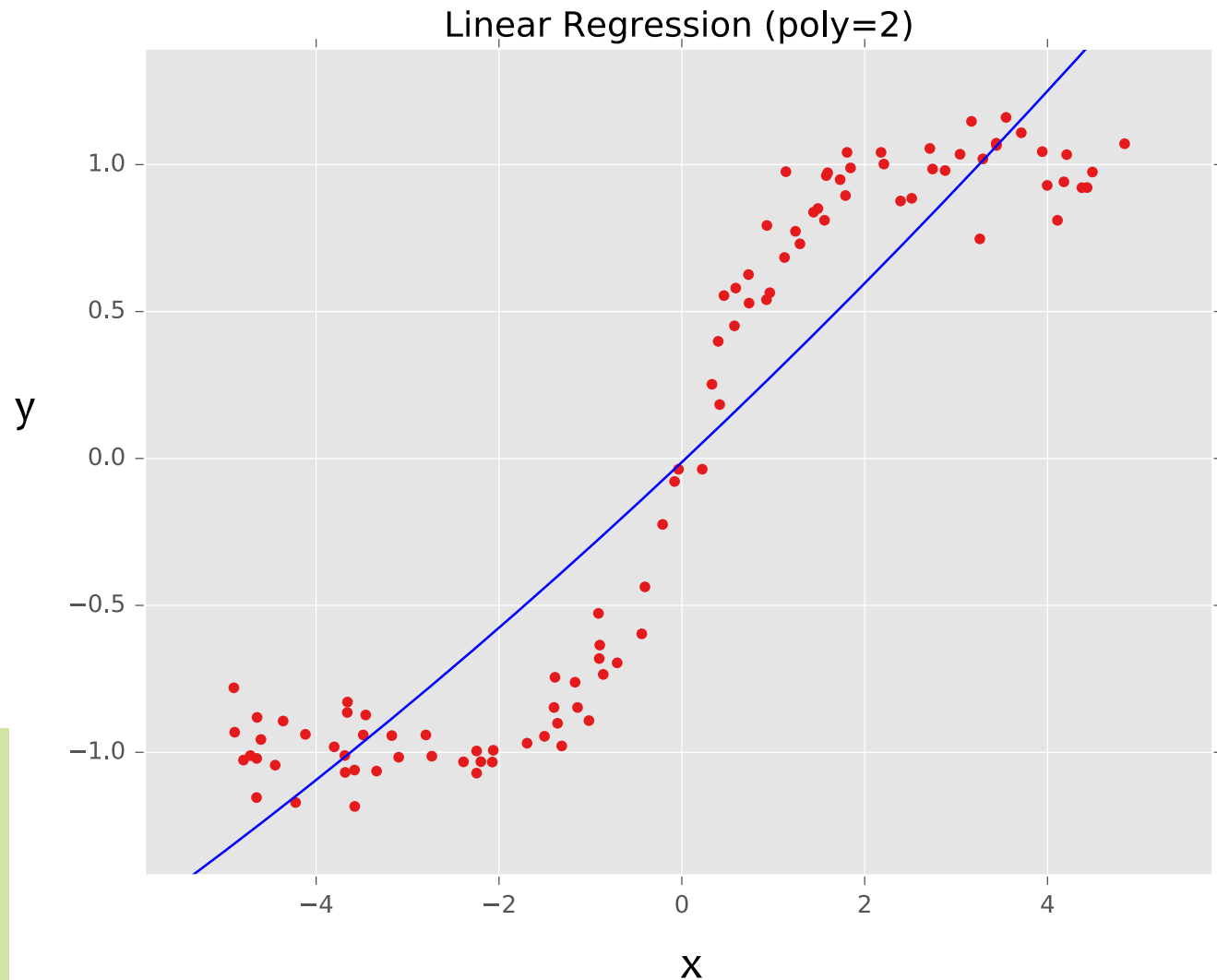
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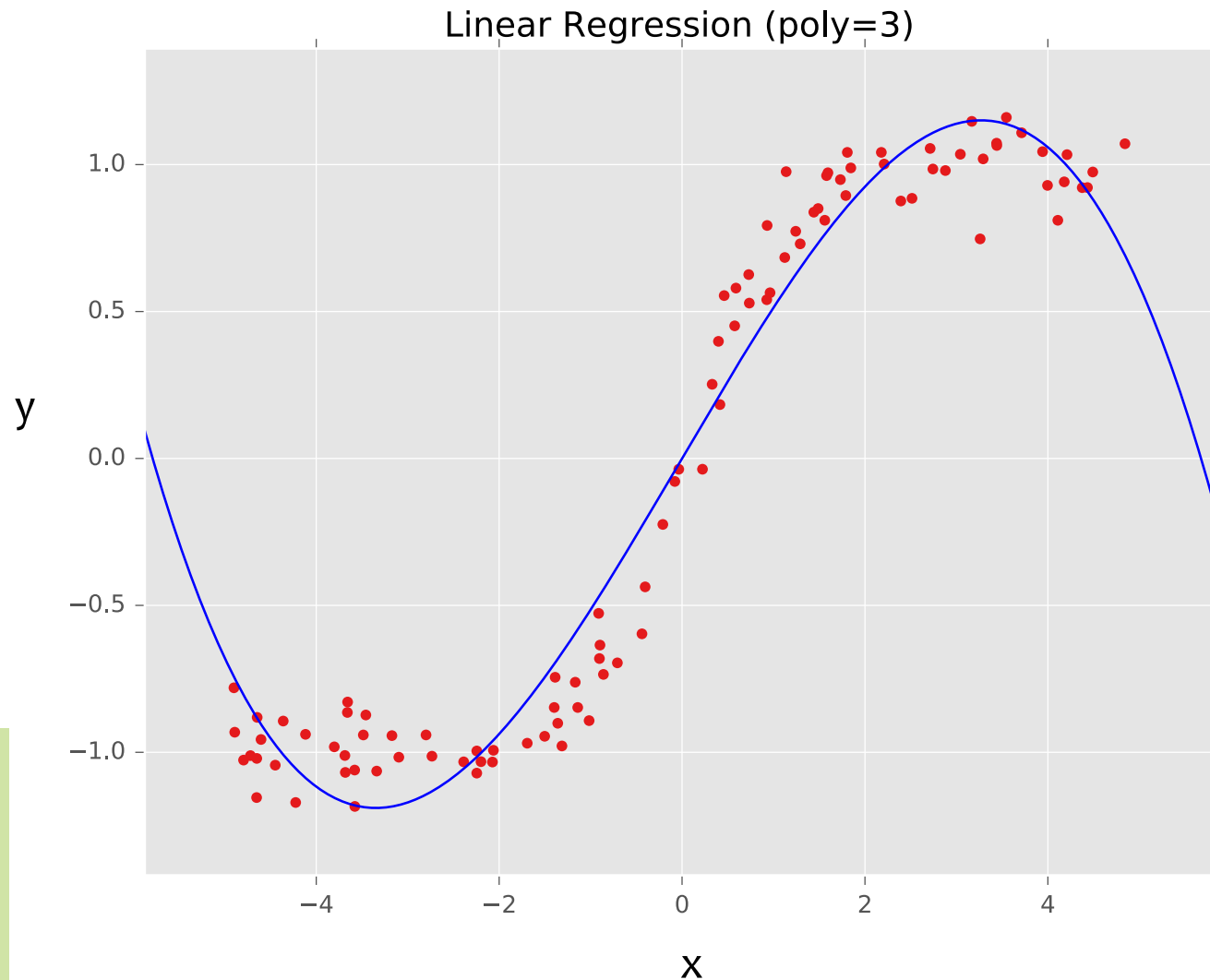
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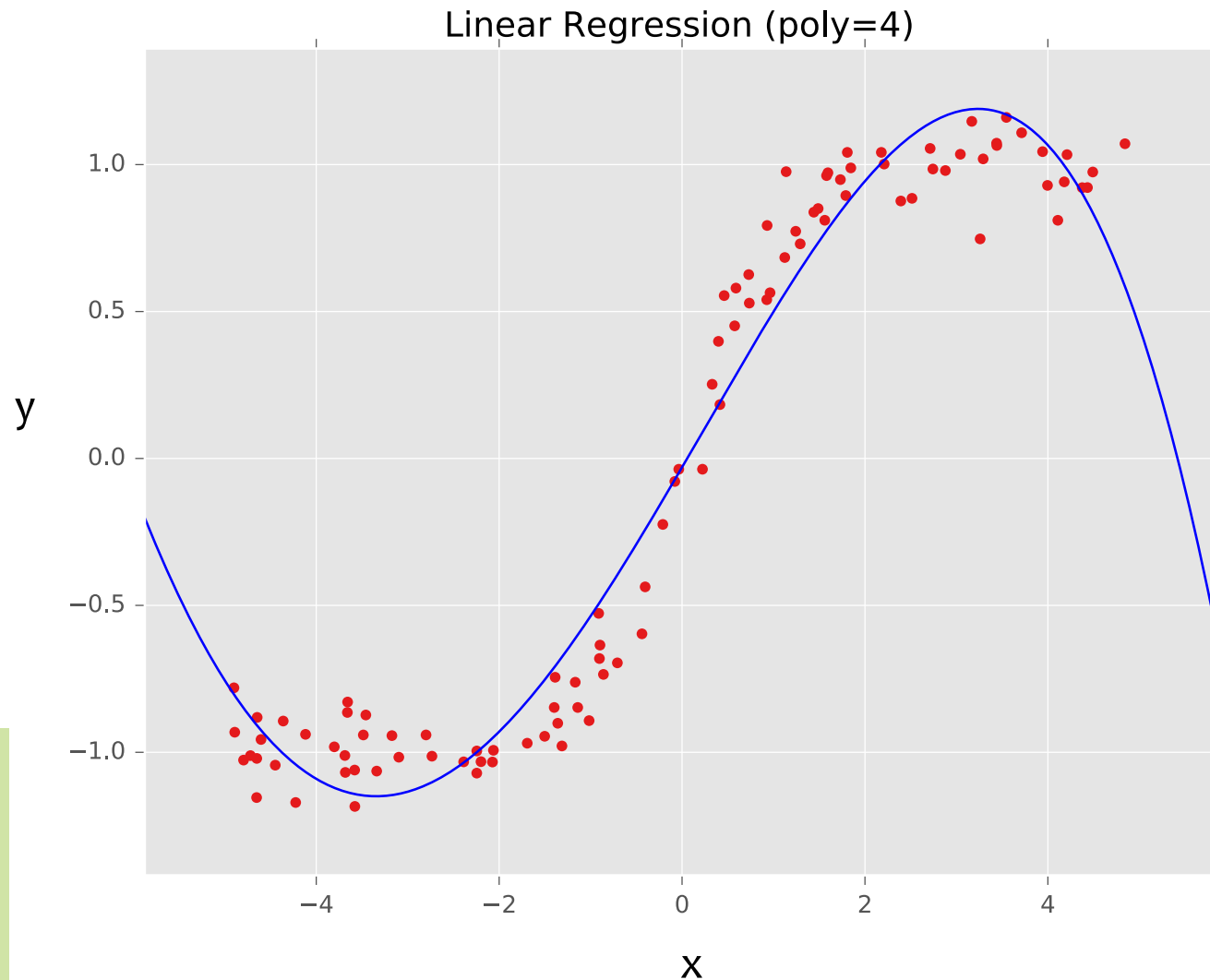
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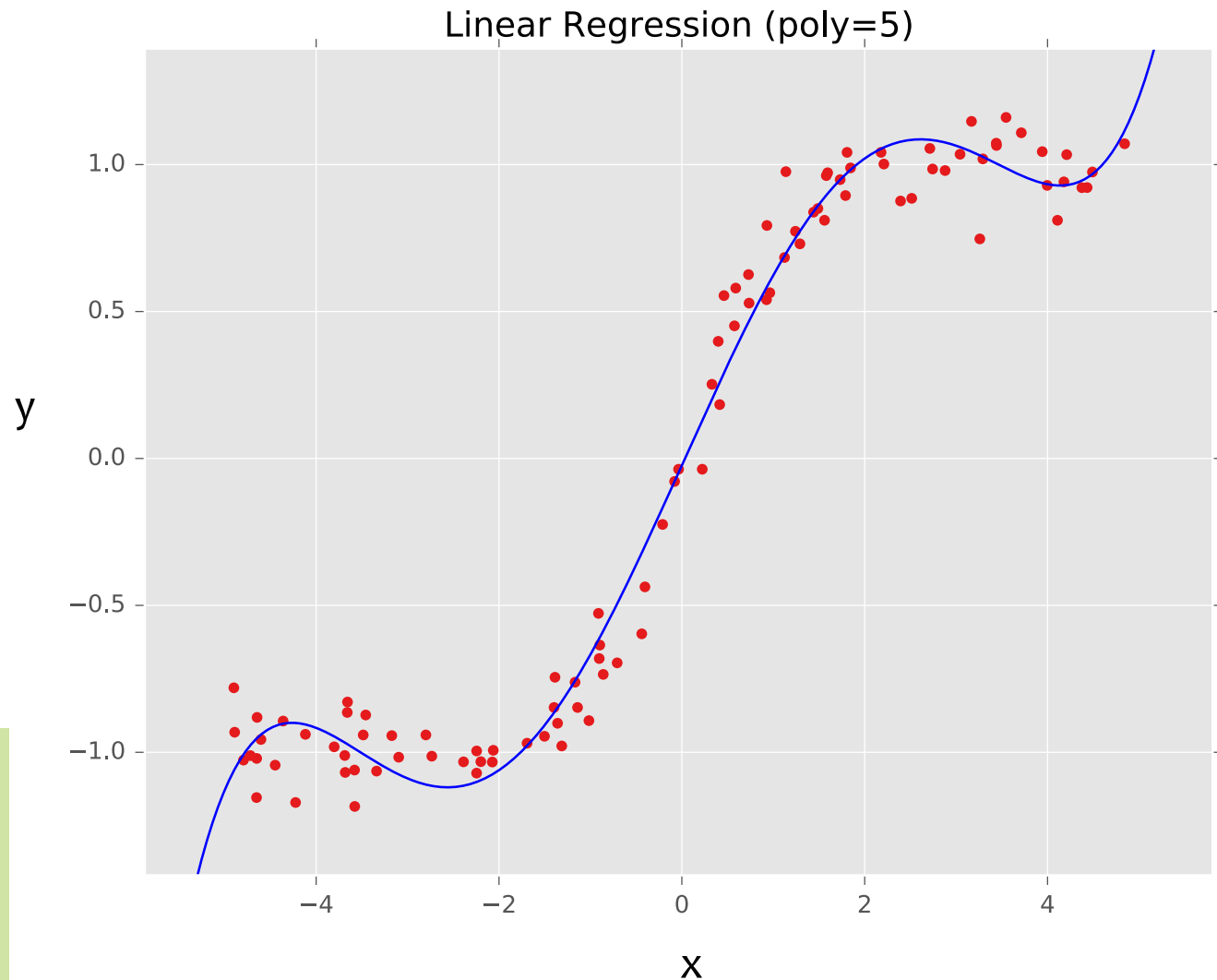
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# Example: Linear Regression

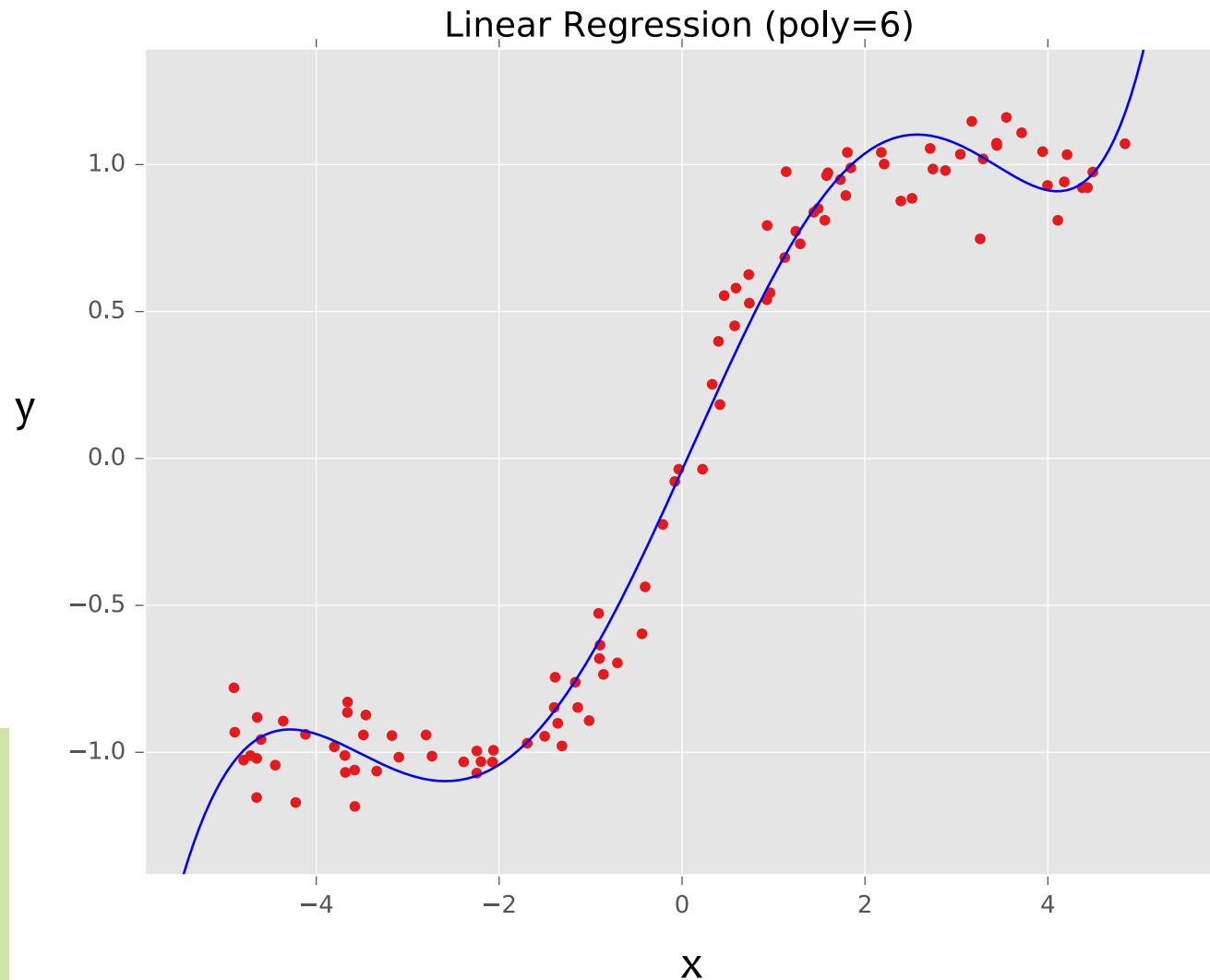
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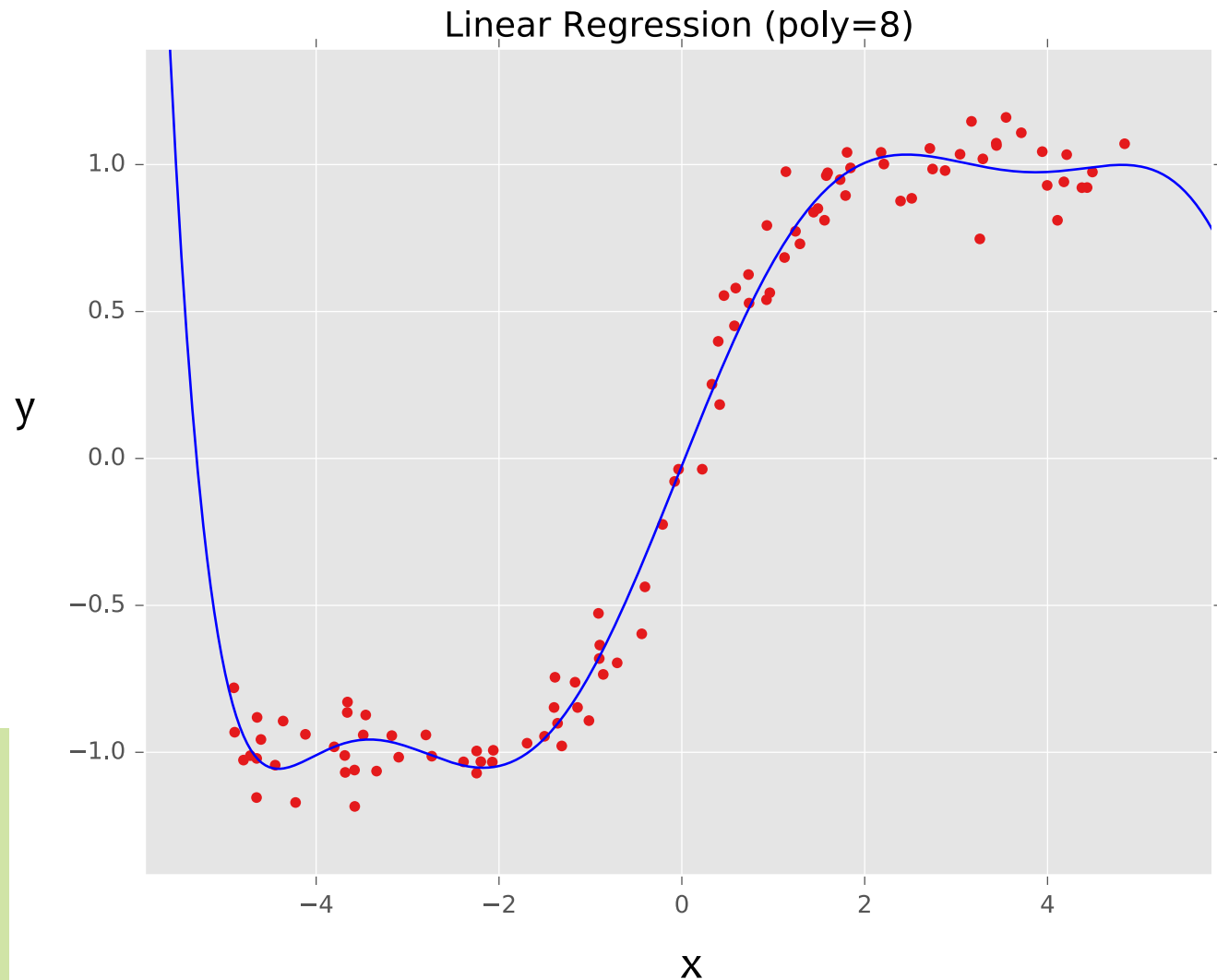


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# Example: Linear Regression

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# **REGULARIZATION**







# Regularization

## *Chalkboard*

- L2, L1, L0 Regularization
- Example: Linear Regression











# Example: Logistic Regression

Training  
Data







































