Machine Learning Department
School of Computer Science
Carnegie Mellon University

Final Exam Review

Matt Gormley
Lecture 29
Dec 4, 2019

Reminders

- Homework 8: Learning Paradigms
  - Out: Mon, Nov. 25
  - Due: Wed, Dec. 4 at 11:59pm
  - Can only be submitted up to 3 days late, so we can return grades before final exam

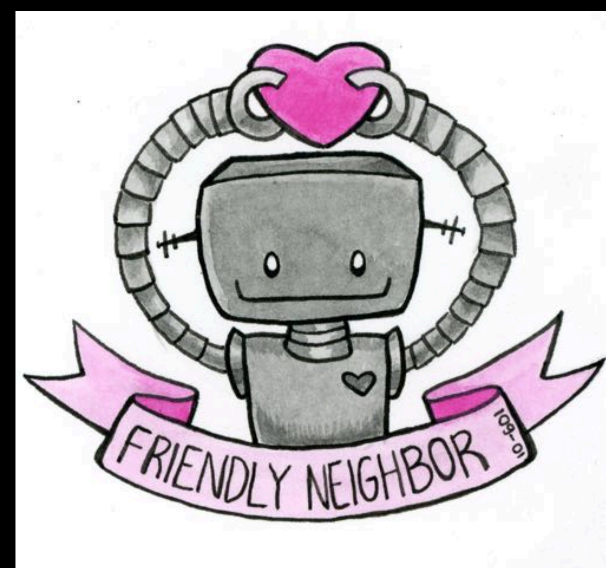
- Today's In-Class Poll
  - http://p29.mlcourse.org

Reminders

Congratulations to our top Piazza Question Answerers (2nd half)!

1. ba98959f457ec10d1272
2. 1465abbd2641a9a32459
3. 7636d8d965fd2e29626e
4. a3e3c79fc6310b5e54f6
5. 6112f1d4b2ad6ec178ff
6. c7b99972d87f77e0288f
7. 927e79510079b78549f4
8. 40ba2f9595a25edf584c
9. 1a2628b684e892154cf4
10. 73ab4e60182a6aa0ee40
11. 305fc04247ce71f3ba06
12. 9094a77492aa4fb6ec94

***Names passed through one-way crytographic hashing function (shake-256 with digest length 10) for FERPA compliance**



EXAM LOGISTICS

Final Exam

- **Time / Location**
  - **Time:** Registrar-scheduled Exam
    Mon, Dec 9 at 8:30am – 11:30am
  - **Room:** We will contact each student individually with **your room assignment.** The rooms are **not** based on section.
  - **Seats:** There will be **assigned seats.** Please arrive early.
  - Please watch Piazza carefully for announcements regarding room / seat assignments.
- **Logistics**
  - Format of questions:
    - Multiple choice
    - True / False (with justification)
    - Derivations
    - Short answers
    - Interpreting figures
    - Implementing algorithms on paper
  - No electronic devices
  - You are allowed to **bring** one 8½ x 11 sheet of notes (front and back)

Final Exam

- **How to Prepare**
  - Attend (or watch) this final exam review session
  - Review prior year's exams and solutions
    - We already posted these for the midterm
    - Disclaimer: This year's 10-601 is not the same as prior offerings, so review both midterm and final
  - Solve the "Final Exam **Worksheet 1**" and "Final Exam **Worksheet 2**" problems
  - Review this year's **homework problems**
  - Review the **poll questions** from each lecture
  - Consider whether you have achieved the **learning objectives** for each lecture / section
  - Attend the **Final Exam Office Hours**
    - New this fall!
    - Two small groups meeting in usual recitation lecture hall
    - Sign up for a slot (link on Piazza)
    - Bring questions for TAs

Final Exam

- **Advice (for during the exam)**
  - Solve the easy problems first
    (e.g. multiple choice before derivations)
    - if a problem seems extremely complicated you're likely missing something
  - Don't leave any answer blank!
  - If you make an assumption, write it down
  - If you look at a question and don't know the answer:
    - we probably haven't told you the answer
    - but we've told you enough to work it out
    - imagine arguing for some answer and see if you like it

Final Exam

- **Exam Contents**
  - ~30% of material comes from topics covered **before** Midterm Exam 2
  - ~70% of material comes from topics covered **after** Midterm Exam 2

Topics for Midterm 1

- Foundations
  - Probability, Linear Algebra, Geometry, Calculus
  - Optimization
- Important Concepts
  - Overfitting
  - Experimental Design
- Classification
  - Decision Tree
  - KNN
  - Perceptron
- Regression
  - Linear Regression

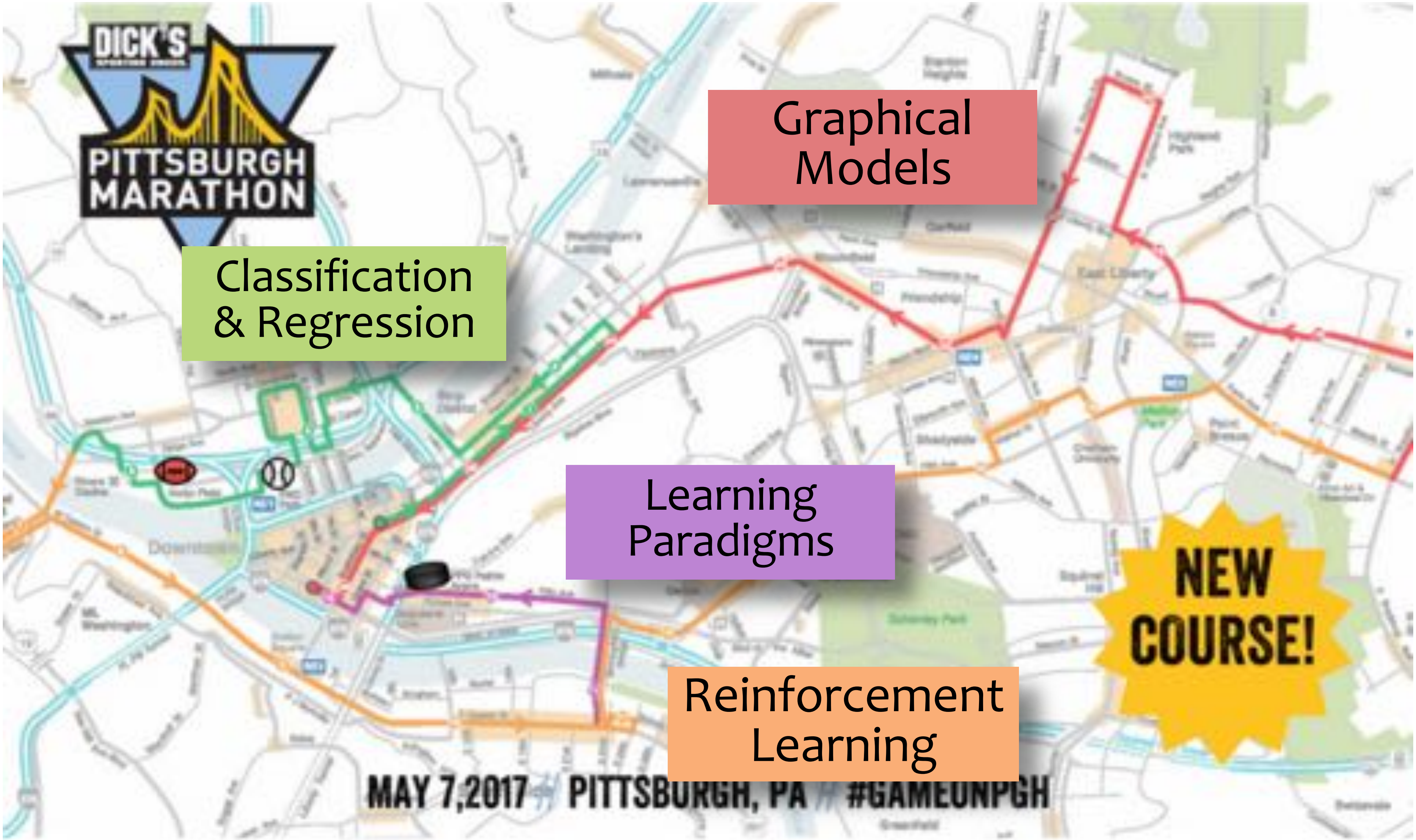
Topics for Midterm 2

- Classification
  - Binary Logistic Regression
  - Multinomial Logistic Regression
- Important Concepts
  - Regularization
  - Feature Engineering
- Feature Learning
  - Neural Networks
  - Basic NN Architectures
  - Backpropagation
- Reinforcement Learning
  - Value Iteration
  - Policy Iteration
  - Q-Learning
  - Deep Q-Learning
- Learning Theory
  - Information Theory

Topics for Final Exam

- Generative Models
  - Generative vs. Discriminative
  - MLE / MAP
  - Naïve Bayes
  - Bayes Framework
- Graphical Models
  - HMMs
  - Learning and Inference
  - Bayesian Networks
- Other Learning Paradigms
  - Ensemble Methods
  - Recommender Systems
  - SVM (large-margin)
  - PCA


DICK'S
SPORTING GOODS
PITTSBURGH
MARATHON


DICK'S
PITTSBURGH MARATHON
Graphical Models
Classification & Regression
Learning Paradigms
Reinforcement Learning
NEW COURSE!
MAY 7,2017 // PITTSBURGH, PA // #GAMEONPGH

RICHARD S. CALIGUIRI
CITY OF PITTSBURGH

Great Race

Learning as Memorization

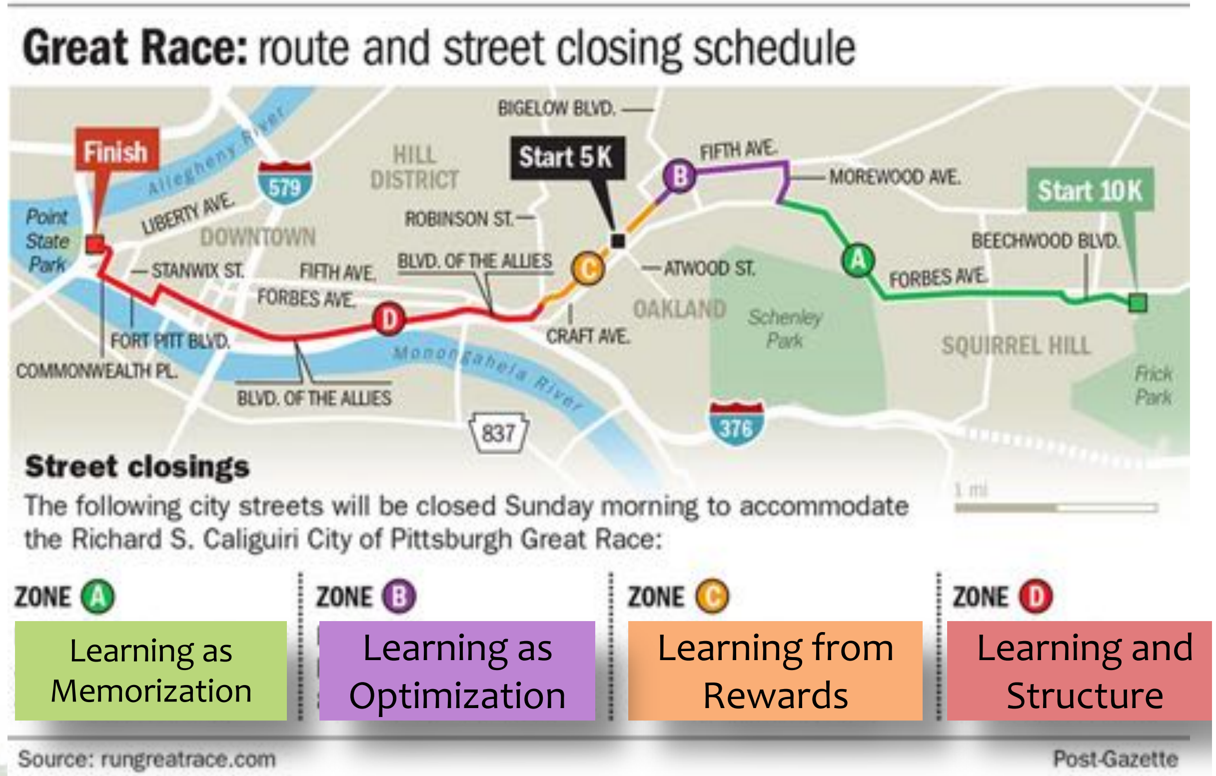
Learning as Optimization

Learning from Rewards

Learning and Structure

A new **combined** course…

…with the best (uphill climbs) from both



Material Covered **Before** Midterm Exam 2

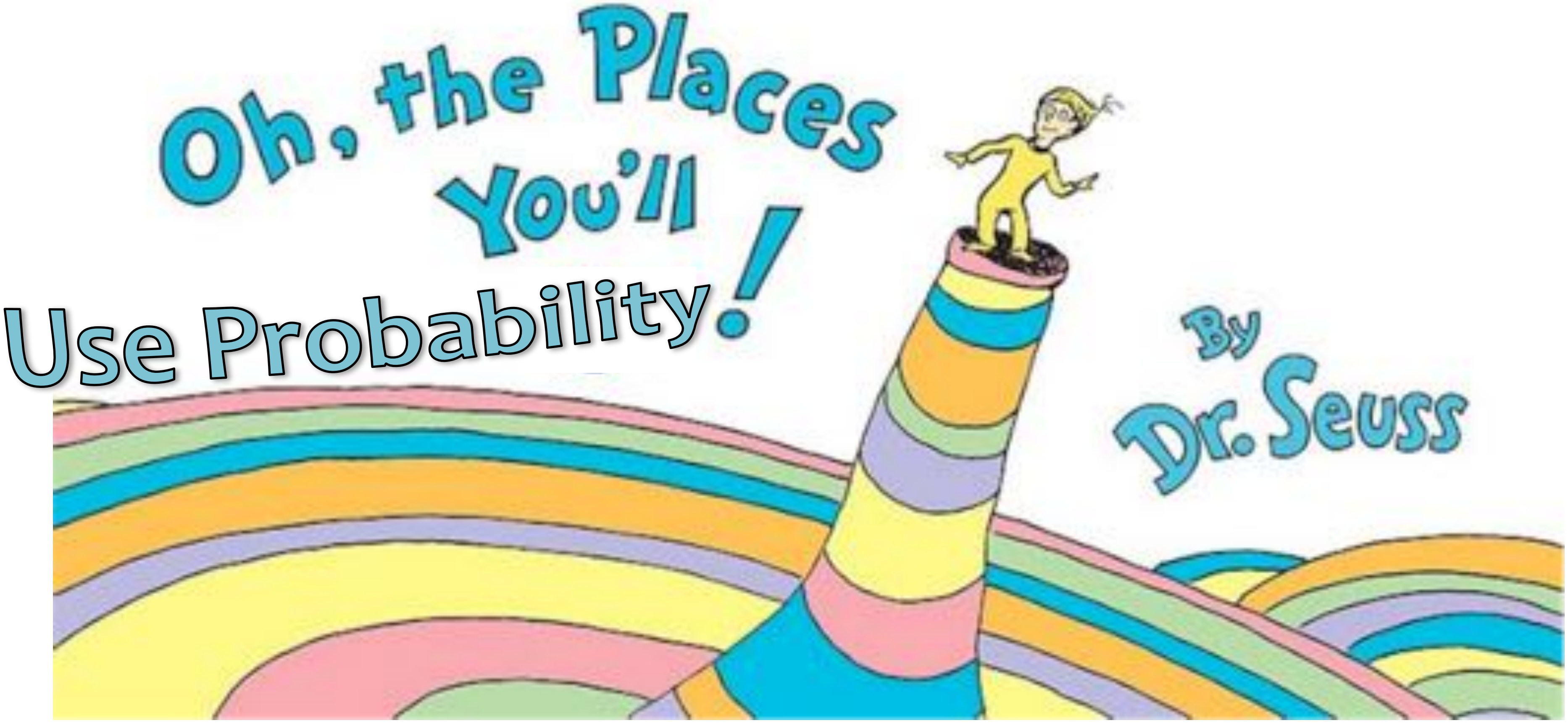
SAMPLE QUESTIONS

Matching Game

Goal: Match the Algorithm to its Update Rule

1. SGD for Logistic Regression $h_{\boldsymbol{\theta}}(\mathbf{x}) = p(y\|x)$	**4.** $\theta_k \leftarrow \theta_k + (h_{\boldsymbol{\theta}}(\mathbf{x}^{(i)}) - y^{(i)})$
2. Least Mean Squares $h_{\boldsymbol{\theta}}(\mathbf{x}) = \boldsymbol{\theta}^T \mathbf{x}$	**5.** $\theta_k \leftarrow \theta_k + \frac{1}{1 + \exp \lambda(h_{\boldsymbol{\theta}}(\mathbf{x}^{(i)}) - y^{(i)})}$
3. Perceptron (next lecture) $h_{\boldsymbol{\theta}}(\mathbf{x}) = \text{sign}(\boldsymbol{\theta}^T \mathbf{x})$	**6.** $\theta_k \leftarrow \theta_k + \lambda(h_{\boldsymbol{\theta}}(\mathbf{x}^{(i)}) - y^{(i)})x_k^{(i)}$

A. 1=5, 2=4, 3=6
B. 1=5, 2=6, 3=4
C. 1=6, 2=4, 3=4
D. 1=5, 2=6, 3=6
E. 1=6, 2=6, 3=6


Oh, the Places You'll
Use Probability!
By Dr. Seuss

Sample Questions

1.4 Probability

Assume we have a sample space Ω. Answer each question with **T** or **F**.

(a) [1 pts.] **T or F:** If events A, B, and C are disjoint then they are independent.

(b) [1 pts.] **T or F:** $P(A|B) \propto \frac{P(A)P(B|A)}{P(A|B)}$. (The sign '$\propto$' means 'is proportional to')

Species	Sepal Length	Sepal Width	Petal Length	Petal Width
0	4.3	3.0	1.1	0.1
0	4.9	3.6	1.4	0.1
0	5.3	3.7	1.5	0.2
1	4.9	2.4	3.3	1.0
1	5.7	2.8	4.1	1.3
1	6.3	3.3	4.7	1.6
1	6.7	3.0	5.0	1.7

Sample Questions

4 K-NN [12 pts]

Now we will apply K-Nearest Neighbors using Euclidean distance to a binary classification task. We assign the class of the test point to be the class of the majority of the k nearest neighbors. A point can be its own neighbor.

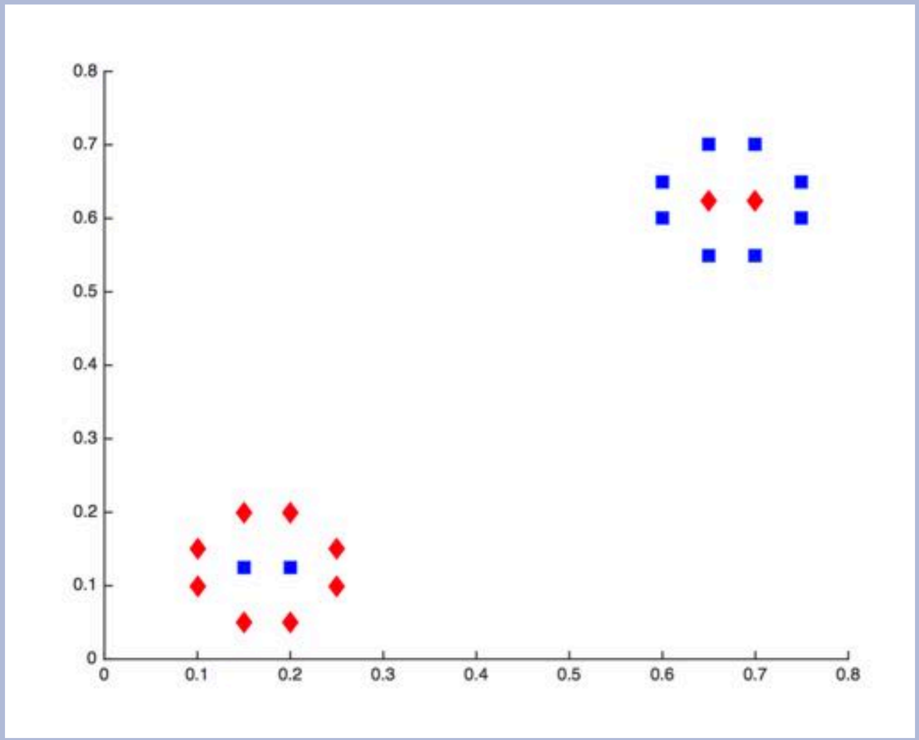


Figure 5

3. **[2 pts]** What value of k minimizes leave-one-out cross-validation error for the dataset shown in Figure 5? What is the resulting error?

Sample Questions

3.1 Linear regression

Consider the dataset S plotted in Fig. 1 along with its associated regression line. For each of the altered data sets S^{new} plotted in Fig. 3, indicate which regression line (relative to the original one) in Fig. 2 corresponds to the regression line for the new data set. Write your answers in the table below.

Dataset	(a)	(b)	(c)	(d)	(e)
Regression line					

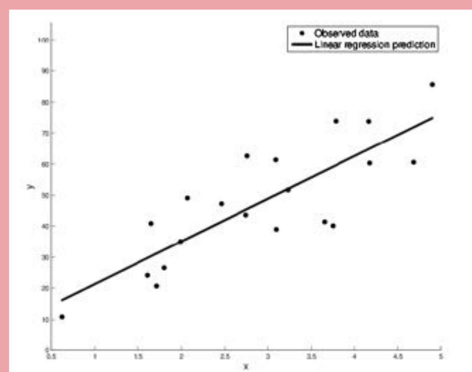
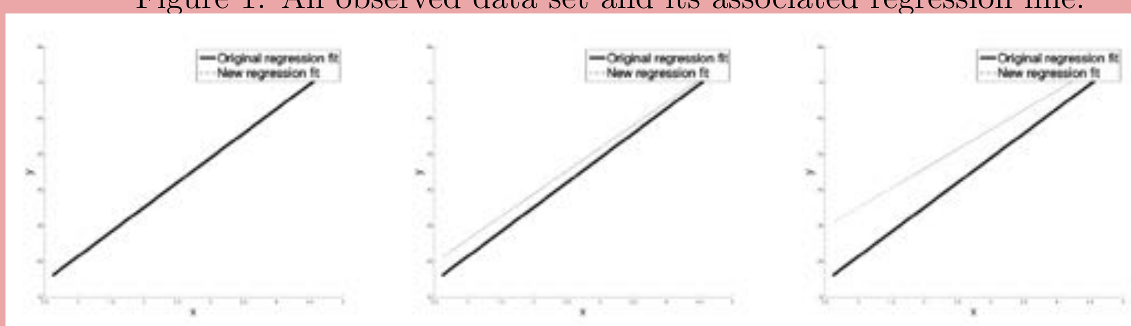


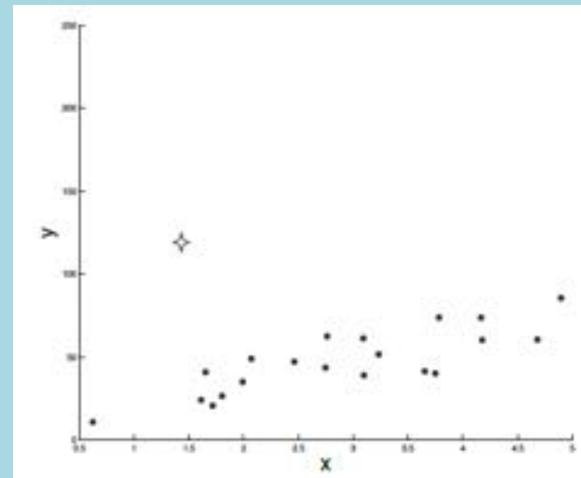
Figure 1: An observed data set and its associated regression line.



(a) Old and new regression lines. (b) Old and new regression lines. (c) Old and new regression lines.

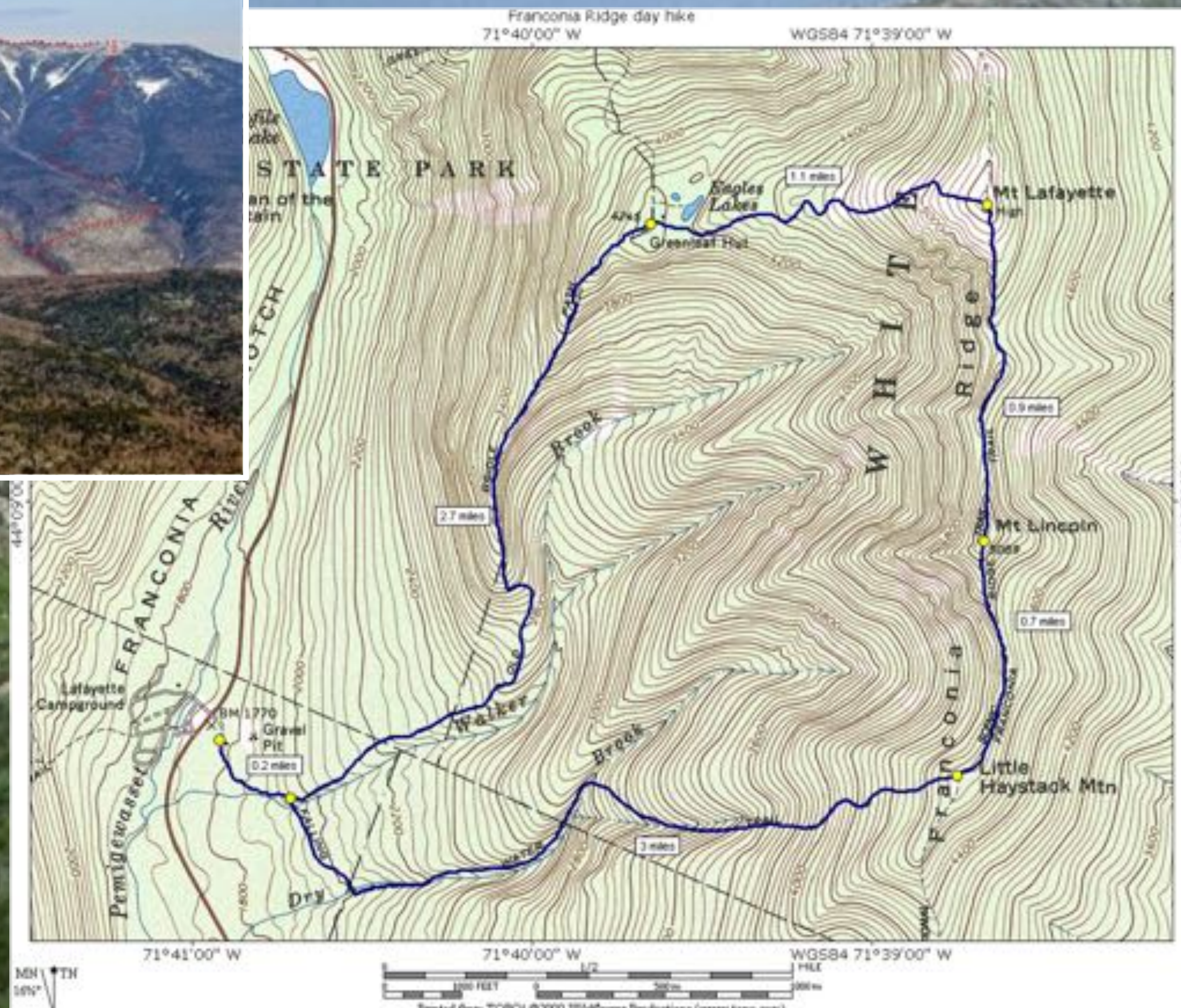
Figure 2: New regression lines for altered data sets S^{new}.

Dataset



(a) Adding one outlier to the original data set.

Topographical Maps



Sample Questions

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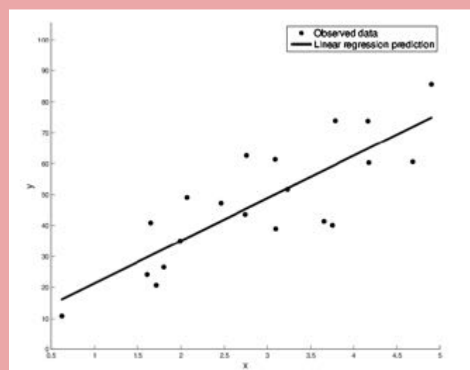

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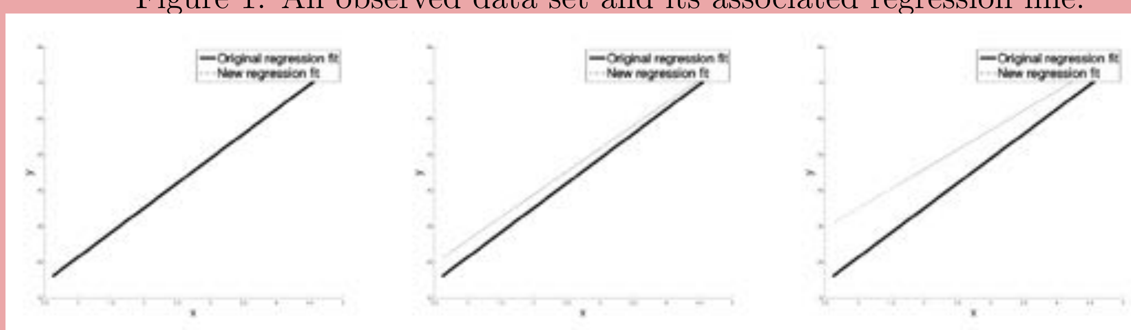

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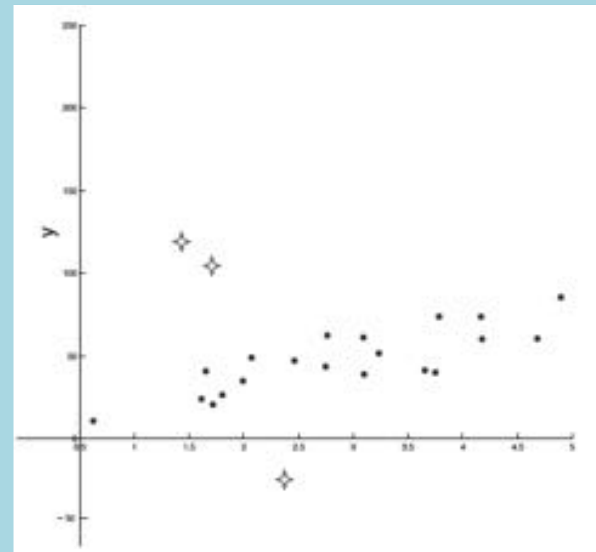
Dataset



(c) Adding three outliers to the original data set. Two on one side and one on the other side.

Sample Questions

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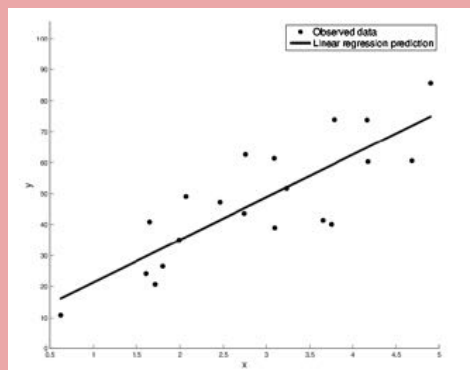

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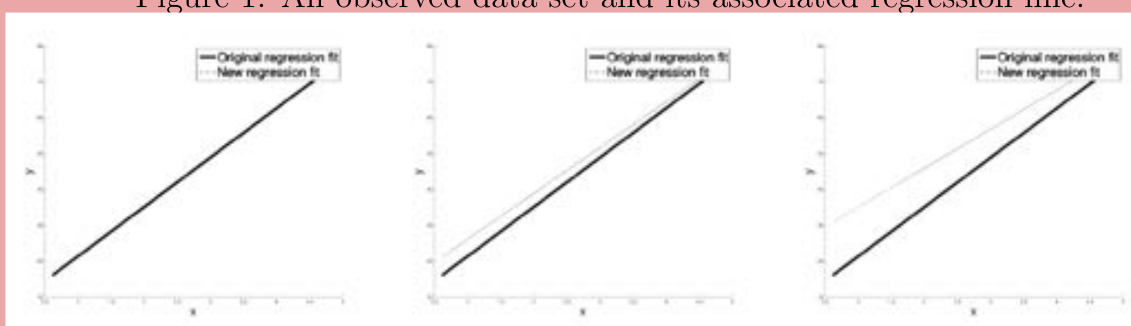

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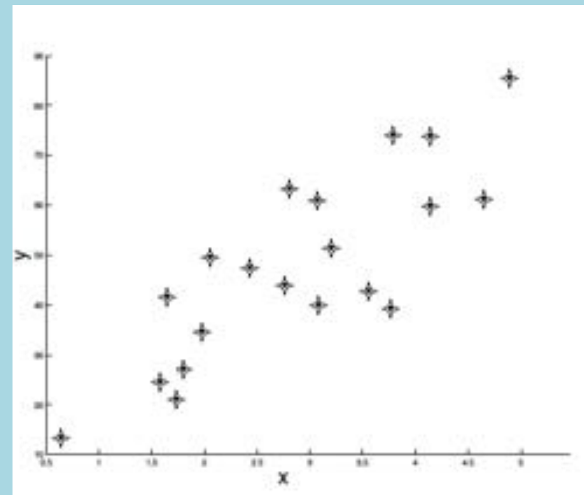
Dataset



(d) Duplicating the original data set.

Sample Questions

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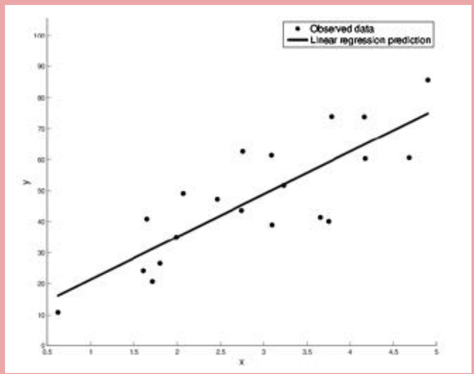

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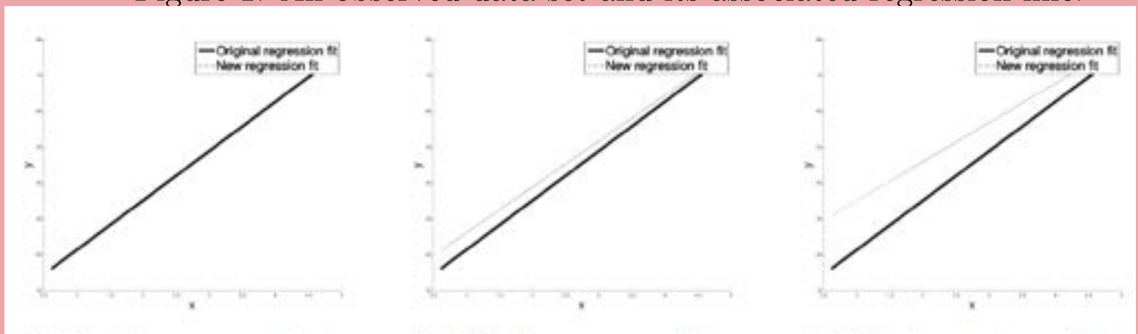

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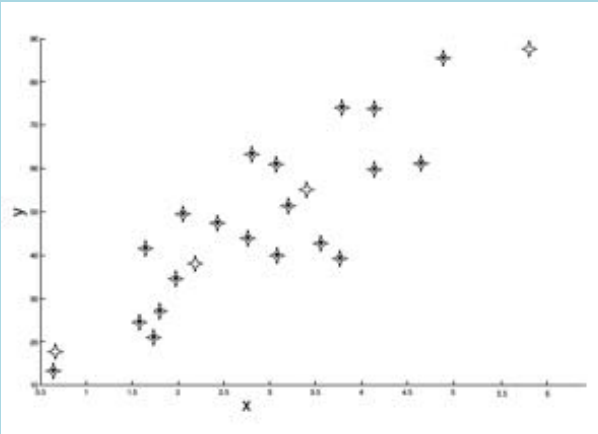
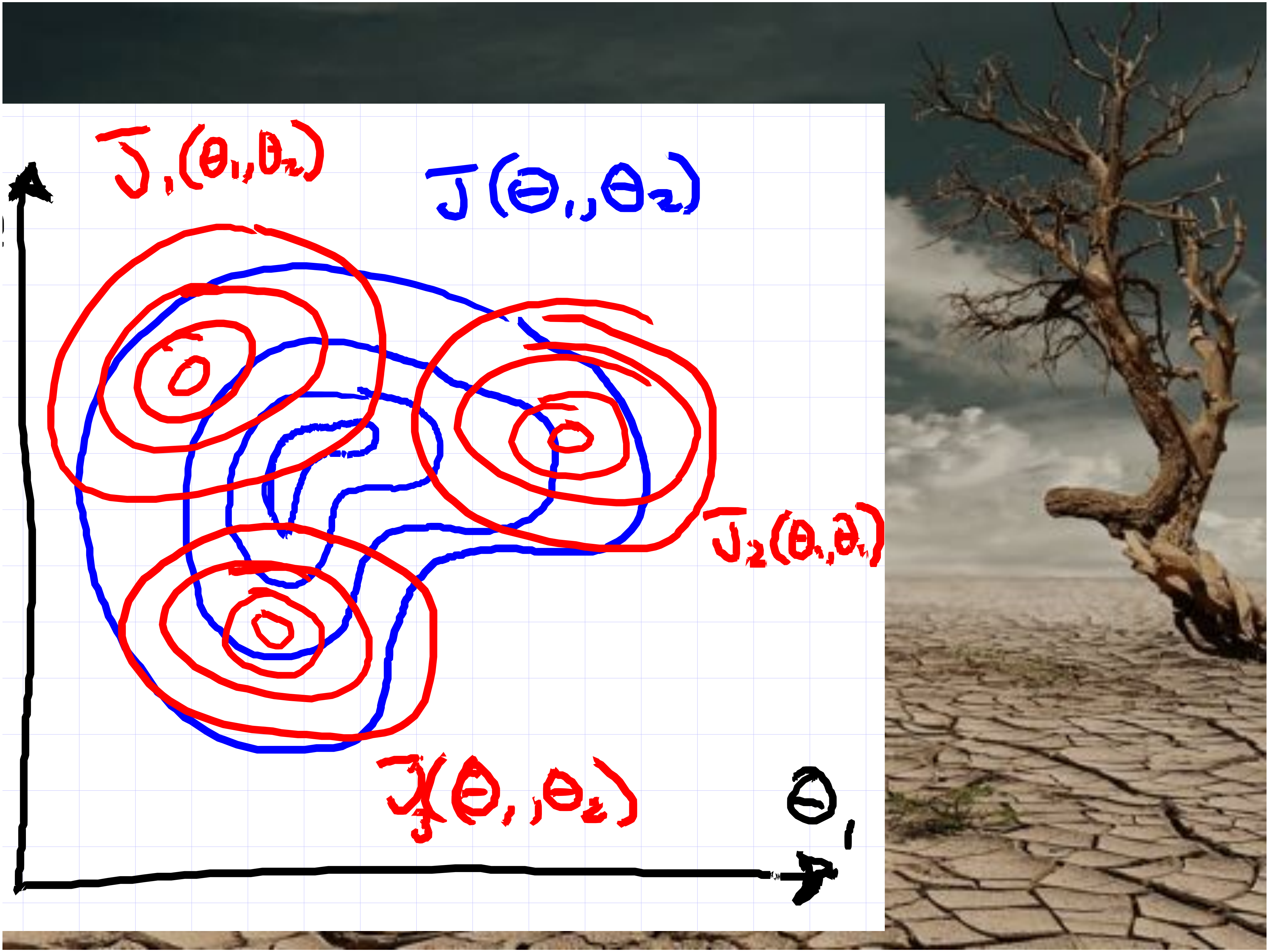


(e) Duplicating the original data set and adding four points that lie on the trajectory of the original regression line.



$J_1(\theta_1,\theta_2)$
$J(\theta_1,\theta_2)$
$J_2(\theta_1,\theta_2)$
$J_3(\theta_1,\theta_2)$
θ_1

Robotic Farming

	Deterministic	**Probabilistic**
Classification (binary output)	Is this a picture of a wheat kernel?	Is this plant drought resistant?
Regression (continuous output)	How many wheat kernels are in this picture?	What will the yield of this plant be?

Multinomial Logistic Regression

Sample Questions

3.2 Logistic regression

Given a training set $\{(x_i, y_i), i = 1, \ldots, n\}$ where $x_i \in \mathbb{R}^d$ is a feature vector and $y_i \in \{0, 1\}$ is a binary label, we want to find the parameters $\hat{w}$ that maximize the likelihood for the training set, assuming a parametric model of the form

$$p(y = 1|x; w) = \frac{1}{1 + \exp(-w^T x)}.$$

The conditional log likelihood of the training set is

$$\ell(w) = \sum_{i=1}^{n} y_i \log p(y_i, |x_i; w) + (1 - y_i) \log(1 - p(y_i, |x_i; w)),$$

and the gradient is

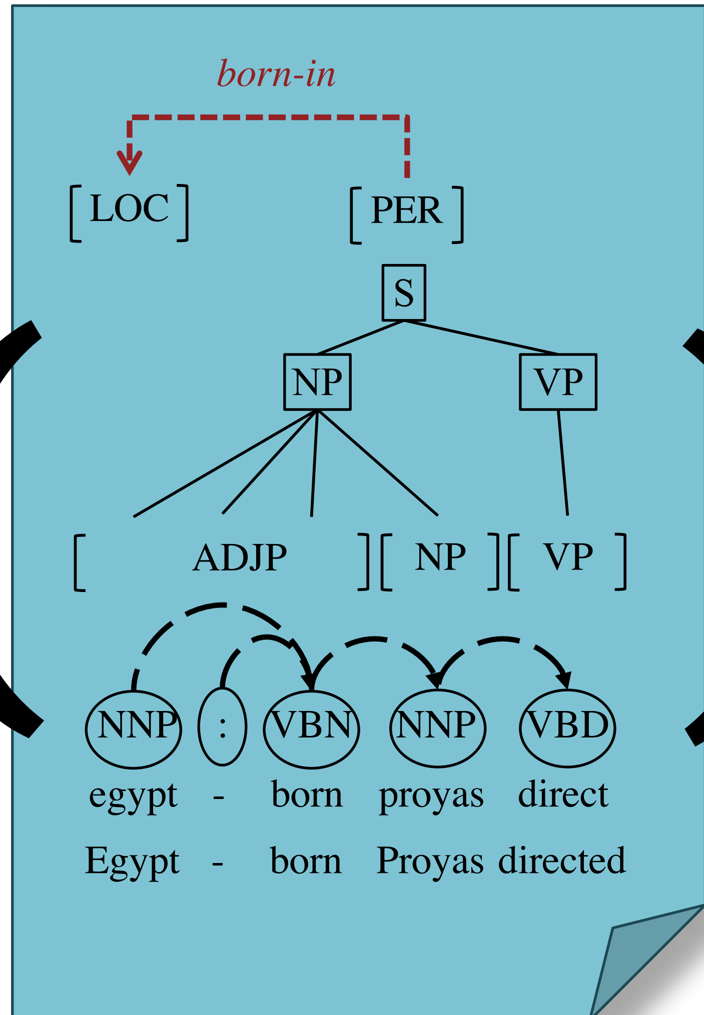
$$\nabla \ell(w) = \sum_{i=1}^{n} (y_i - p(y_i|x_i; w)) x_i.$$

(b) [5 pts.] What is the form of the classifier output by logistic regression?

(c) [2 pts.] **Extra Credit:** Consider the case with binary features, i.e, $x \in \{0, 1\}^d \subset \mathbb{R}^d$, where feature x_1 is rare and happens to appear in the training set with only label 1. What is $\hat{w}_1$? Is the gradient ever zero for any finite w? Why is it important to include a regularization term to control the norm of $\hat{w}$?

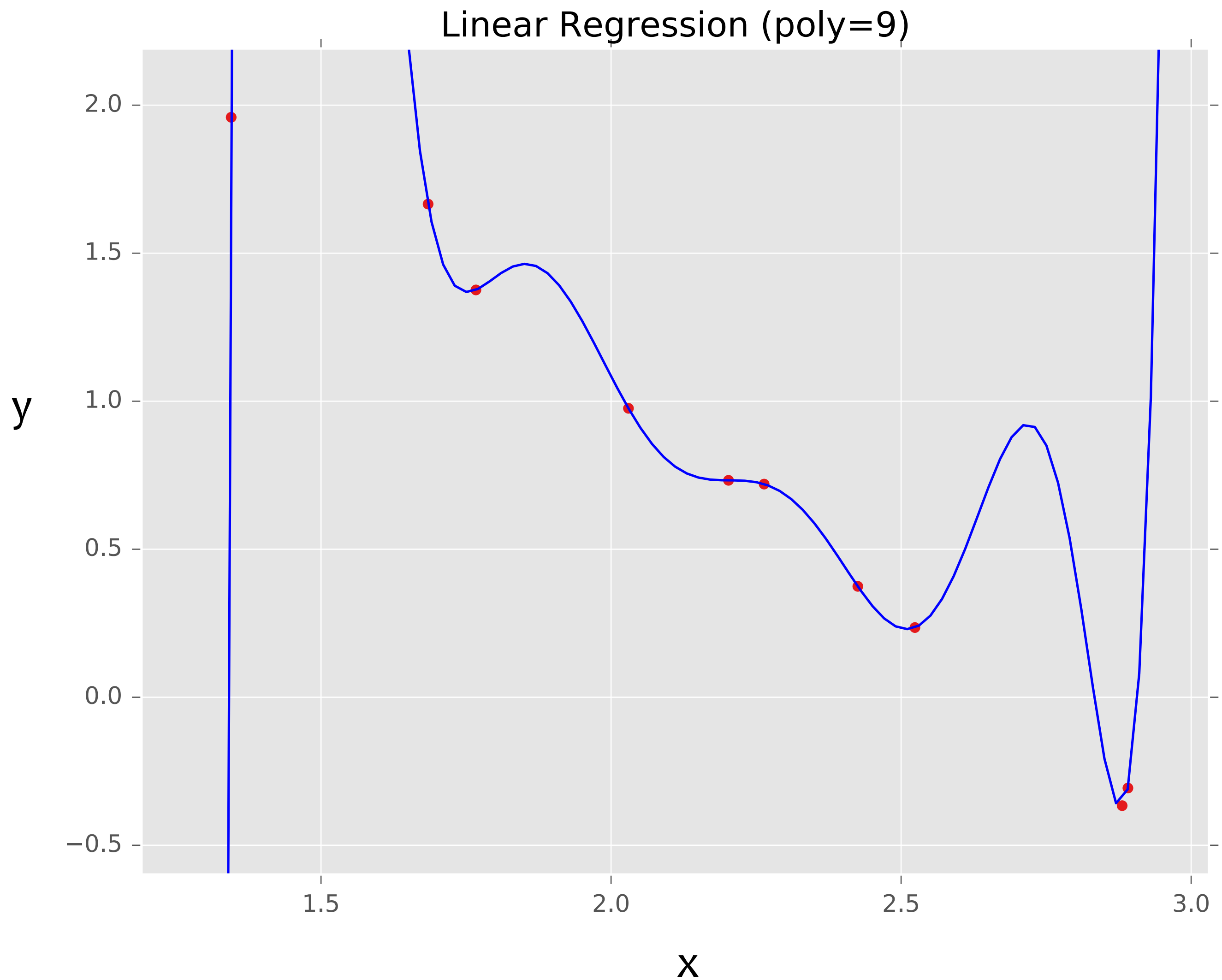
Handcrafted Features

$$p(y|x) \propto \exp(\Theta_y \bullet f(\ \cdot\ ))$$



Example: Linear Regression

Goal: Learn y = $\mathbf{w}^T f(\mathbf{x}) + b$
where f(.) is a polynomial
basis function



true “unknown” target function is linear with negative slope and gaussian noise

Samples Questions

2.1 Train and test errors

In this problem, we will see how you can debug a classifier by looking at its train and test errors. Consider a classifier trained till convergence on some training data $\mathcal{D}^{\text{train}}$, and tested on a separate test set $\mathcal{D}^{\text{test}}$. You look at the test error, and find that it is very high. You then compute the training error and find that it is close to 0.

1. **[4 pts]** Which of the following is expected to help? Select all that apply.

   (a) Increase the training data size.

   (b) Decrease the training data size.

   (c) Increase model complexity (For example, if your classifier is an SVM, use a more complex kernel. Or if it is a decision tree, increase the depth).

   (d) Decrease model complexity.

   (e) Train on a combination of $\mathcal{D}^{\text{train}}$ and $\mathcal{D}^{\text{test}}$ and test on $\mathcal{D}^{\text{test}}$

   (f) Conclude that Machine Learning does not work.

Samples Questions

2.1 Train and test errors

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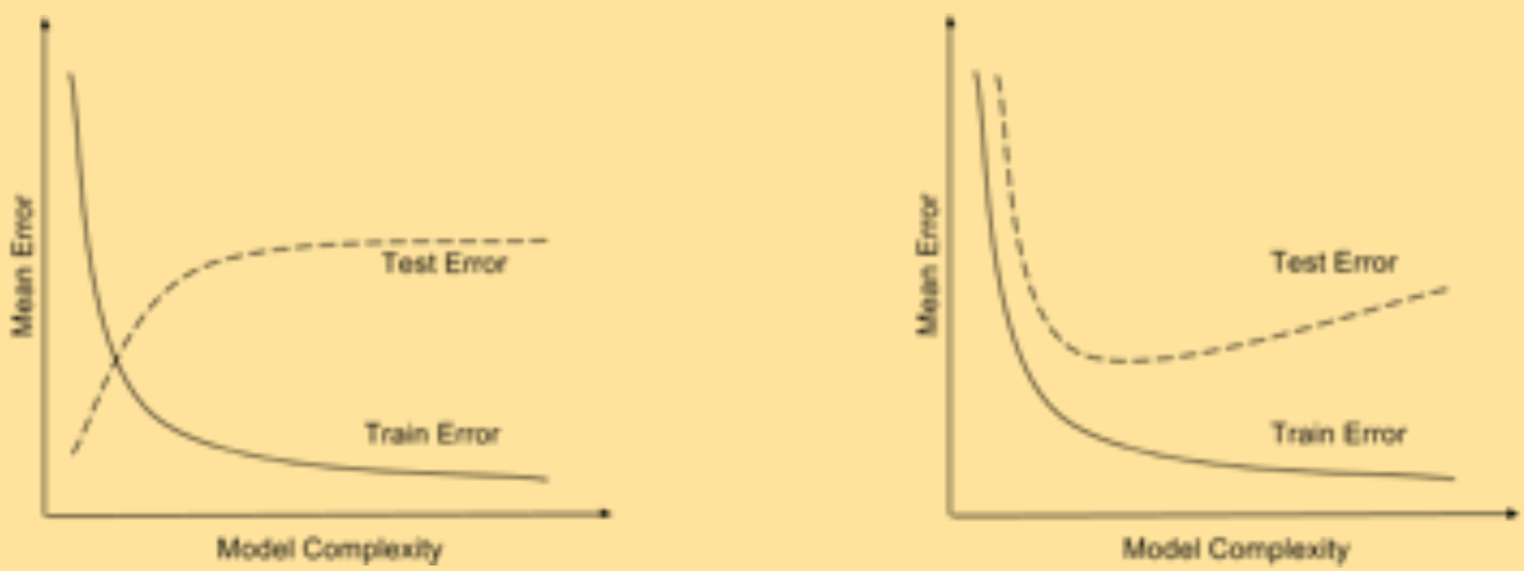
4. **[1 pts]** Say you plot the train and test errors as a function of the model complexity. Which of the following two plots is your plot expected to look like?



(a) (b)

Sample Questions

4.1 True or False

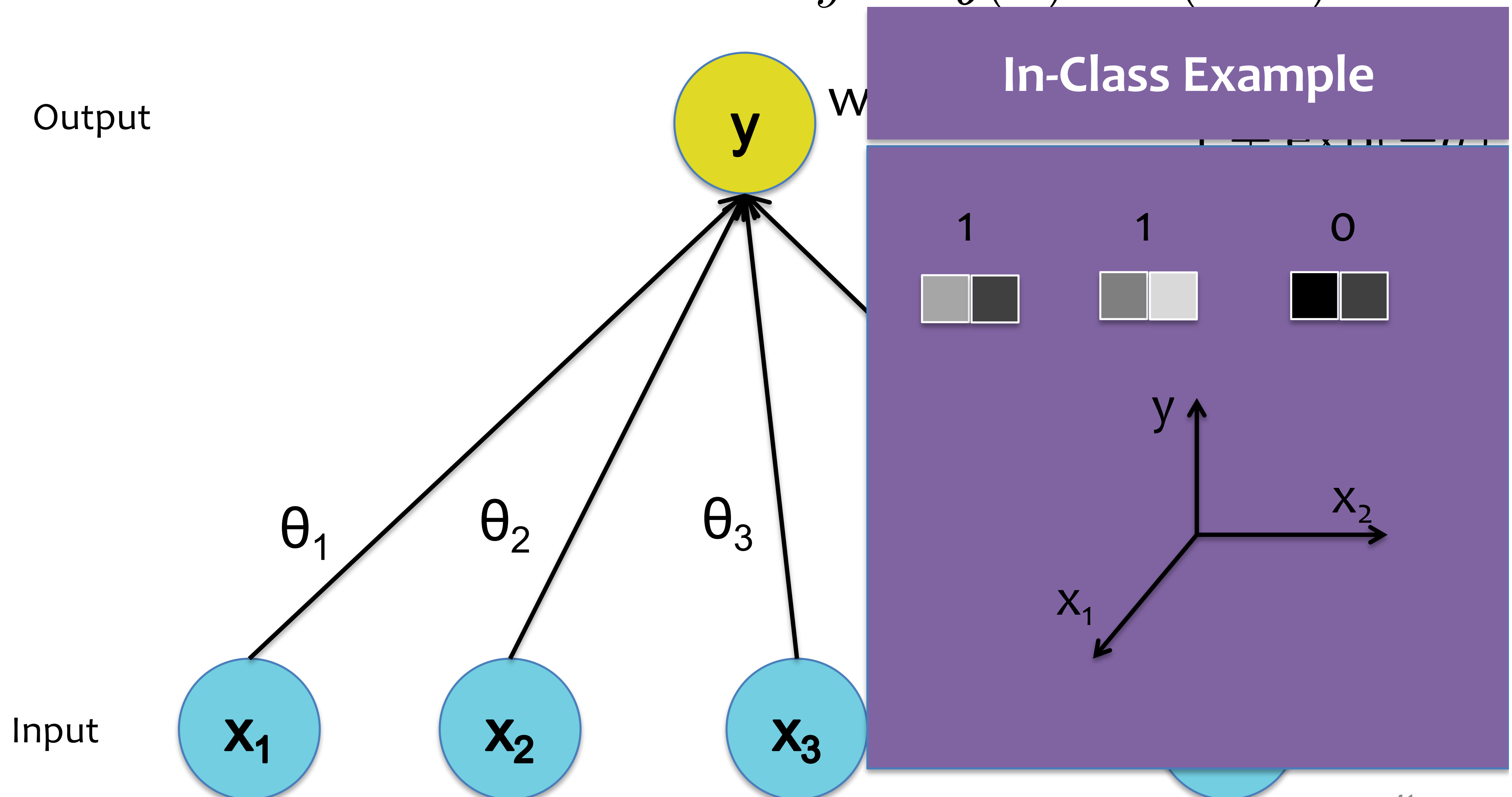
Answer each of the following questions with **T** or **F** and **provide a one line justification**.

(a) [2 pts.] Consider two datasets $D^{(1)}$ and $D^{(2)}$ where $D^{(1)} = \{(x_1^{(1)}, y_1^{(1)}), ..., (x_n^{(1)}, y_n^{(1)})\}$ and $D^{(2)} = \{(x_1^{(2)}, y_1^{(2)}), ..., (x_m^{(2)}, y_m^{(2)})\}$ such that $x_i^{(1)} \in \mathbb{R}^{d_1}$, $x_i^{(2)} \in \mathbb{R}^{d_2}$. Suppose $d_1 > d_2$ and $n > m$. Then the maximum number of mistakes a perceptron algorithm will make is higher on dataset $D^{(1)}$ than on dataset $D^{(2)}$.

Decision Functions

Logistic Regression

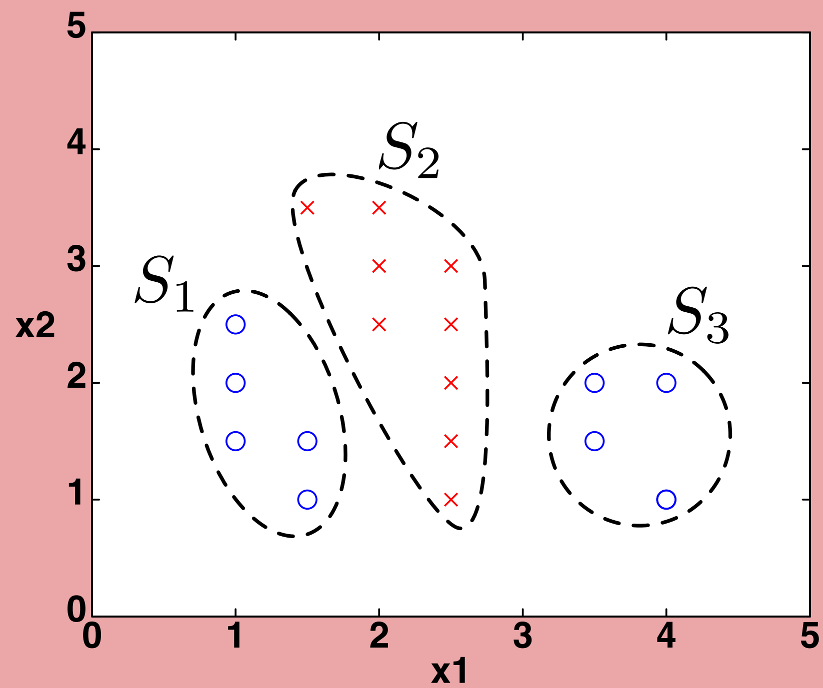
$$y = h_{\boldsymbol{\theta}}(\boldsymbol{x}) = \sigma(\boldsymbol{\theta}^T \boldsymbol{x})$$



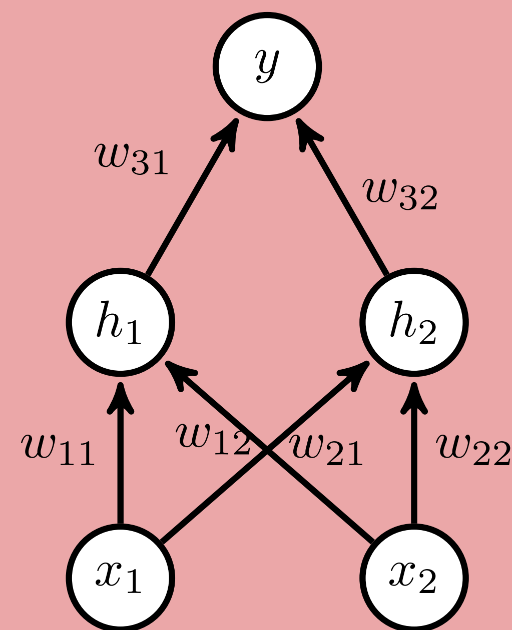
Sample Questions

Neural Networks

Can the neural network in Figure (b) correctly classify the dataset given in Figure (a)?



(a) The dataset with groups S_1, S_2, and S_3.

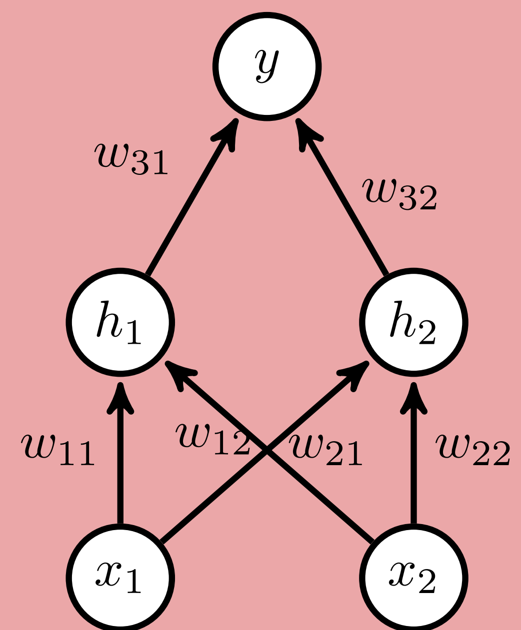


(b) The neural network architecture

Sample Questions

Neural Networks

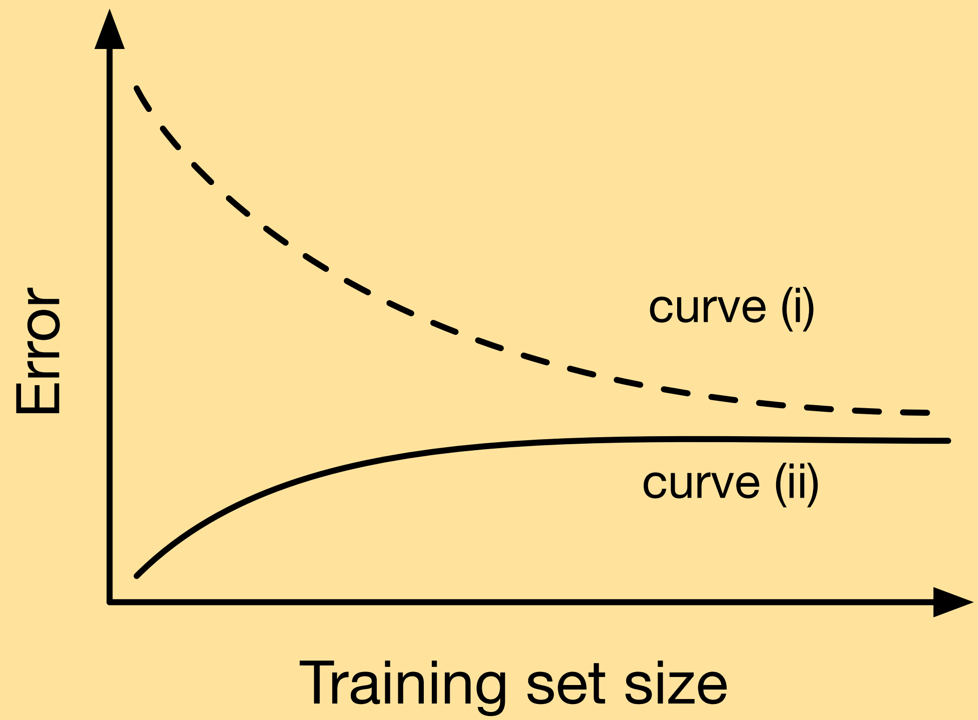
Apply the backpropagation algorithm to obtain the partial derivative of the mean-squared error of y with the true value y^* with respect to the weight w_{22} assuming a sigmoid nonlinear activation function for the hidden layer.



(b) The neural network architecture

Samples Questions

2.2 Training Sample Size



(a) [8 pts.] Which curve represents the training error? **Please provide 1–2 sentences of justification**.

(b) [4 pt.] In one word, what does the gap between the two curves represent?

Example: Path Planning

Sample Questions

7.1 Reinforcement Learning

3. (1 point) **Please select one statement that is true for reinforcement learning and supervised learning.**

   ◯ Reinforcement learning is a kind of supervised learning problem because you can treat the reward and next state as the label and each state, action pair as the training data.

   ◯ Reinforcement learning differs from supervised learning because it has a temporal structure in the learning process, whereas, in supervised learning, the prediction of a data point does not affect the data you would see in the future.

4. (1 point) **True or False:** Value iteration is better at balancing exploration and exploitation compared with policy iteration.

   ◯ True

   ◯ False

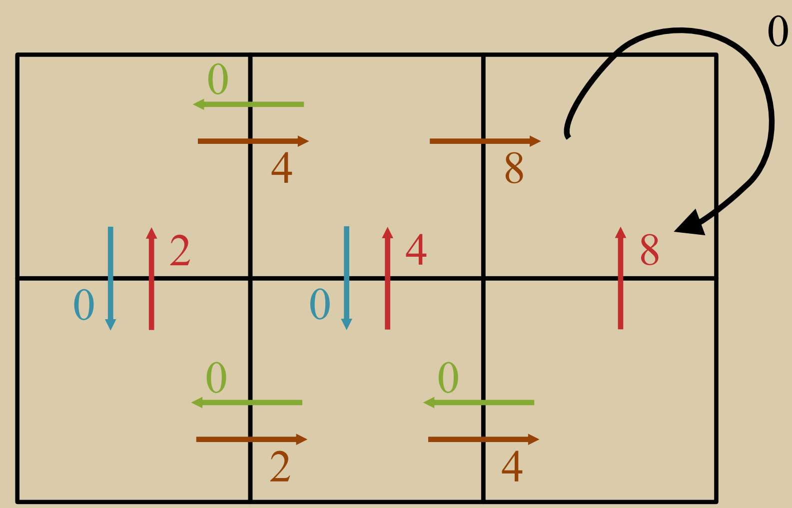
Sample Questions

7.1 Reinforcement Learning

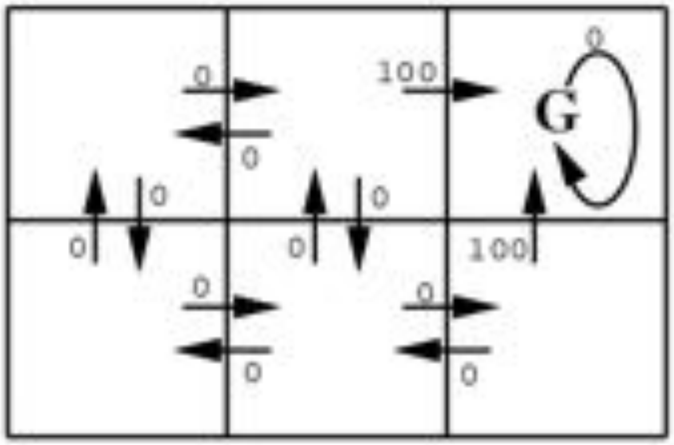
1. For the R(s,a) values shown on the arrows below, what is the corresponding optimal policy? Assume the discount factor is 0.1

2. For the R(s,a) values shown on the arrows below, which are the corresponding V*(s) values? Assume the discount factor is 0.1

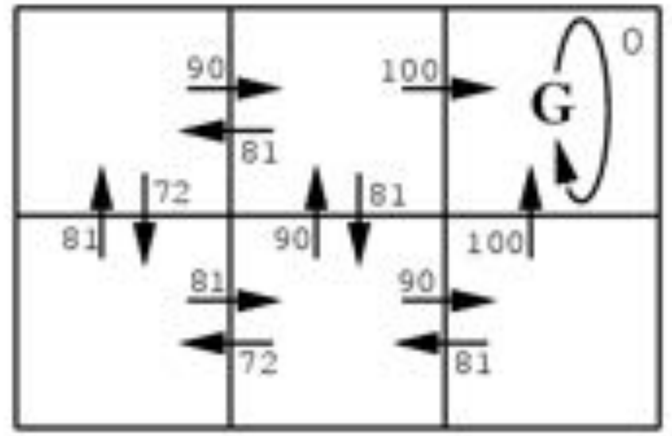
3. For the R(s,a) values shown on the arrows below, which are the corresponding Q*(s,a) values? Assume the discount factor is 0.1



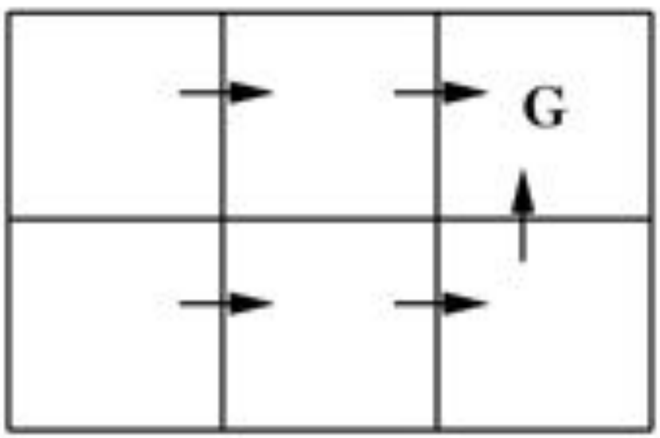
Example: Robot Localization



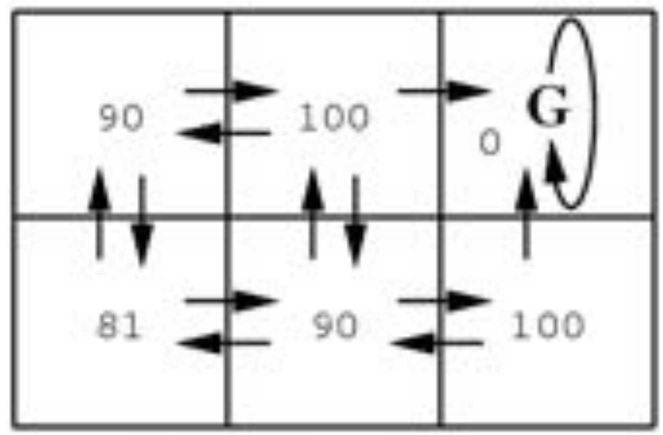
$r(s, a)$ (immediate reward) values



$Q(s, a)$ values



One optimal policy



$V^*(s)$ values

Figure from Tom Mitchell

Material Covered **After** Midterm Exam 2

SAMPLE QUESTIONS

Sample Questions

1.2 Maximum Likelihood Estimation (MLE)

Assume we have a random sample that is Bernoulli distributed $X_1, \ldots, X_n \sim \text{Bernoulli}(\theta)$. We are going to derive the MLE for θ. Recall that a Bernoulli random variable X takes values in $\{0, 1\}$ and has probability mass function given by

$$P(X; \theta) = \theta^X (1 - \theta)^{1-X}.$$

(a) [2 pts.] Derive the likelihood, $L(\theta; X_1, \ldots, X_n)$.

(c) **Extra Credit:** [2 pts.] Derive the following formula for the MLE: $\hat{\theta} = \frac{1}{n} \left(\sum_{i=1}^{n} X_i\right)$.

Sample Questions

1.3 MAP vs MLE

Answer each question with **T** or **F** and **provide a one sentence explanation of your answer**:

(a) [2 pts.] **T or F:** In the limit, as n (the number of samples) increases, the MAP and MLE estimates become the same.

Sample Questions

1.1 Naive Bayes

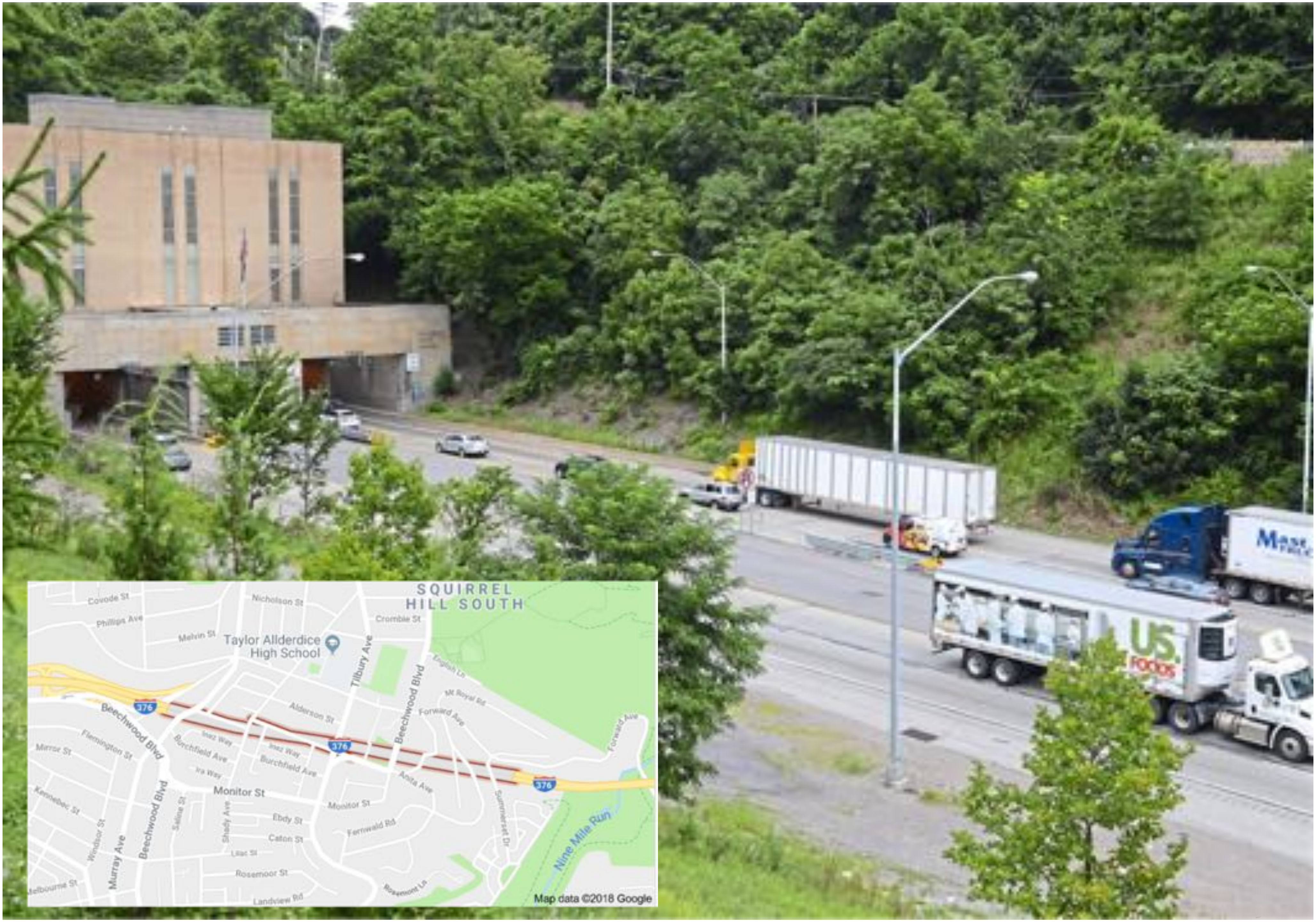
You are given a data set of 10,000 students with their sex, height, and hair color. You are trying to build a classifier to predict the sex of a student, so you randomly split the data into a training set and a testing set. Here are the specifications of the data set:

- sex $\in$ {male,female}
- height $\in$ [0,300] centimeters
- hair $\in$ {brown, black, blond, red, green}
- 3240 men in the data set
- 6760 women in the data set

Under the assumptions necessary for Naive Bayes (not the distributional assumptions you might naturally or intuitively make about the dataset) answer each question with **T** or **F** and **provide a one sentence explanation of your answer**:

(a) [2 pts.] **T or F:** As height is a continuous valued variable, Naive Bayes is not appropriate since it cannot handle continuous valued variables.

(c) [2 pts.] **T or F:** $P(\texttt{height}|\texttt{sex}, \texttt{hair}) = P(\texttt{height}|\texttt{sex})$.



SQUIRREL
HILL SOUTH
Taylor Allderdice
High School
Covode St
Nicholson St
Phillips Ave
Crombie St
Melvin St
Tilbury Ave
Beechwood Blvd
English Ln
Mt Royal Rd
Alderson St
Forward Ave
376
Beechwood Blvd
Flemington St
Inez Way
Burchfield Ave
Mirror St
Ira Way
Anita Ave
Monitor St
Kennebec St
Windsor St
Murray Ave
Saline St
Shady Ave
Ebdy St
Caton St
Lilac St
Fernwald Rd
Summerset Dr
Nine Mile Run
Rosemoor St
Melbourne St
Landview Rd
Rosemont Ln
Map data ©2018 Google
US.
FOODS

Sample Questions

(a) [2 pts.] Write the expression for the joint distribution.

5 Graphical Models [16 pts.]

We use the following Bayesian network to model the relationship between studying (S), being well-rested (R), doing well on the exam (E), and getting an A grade (A). All nodes are binary, i.e., $R, S, E, A \in \{0, 1\}$.

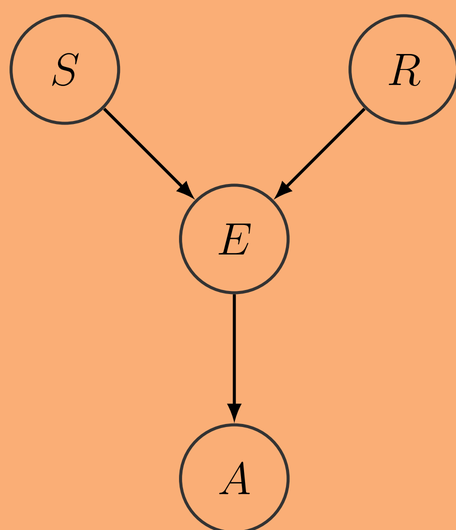


Figure 5: Directed graphical model for problem 5.

Sample Questions

(b) [2 pts.] How many parameters, i.e., entries in the CPT tables, are necessary to describe the joint distribution?

5 Graphical Models [16 pts.]

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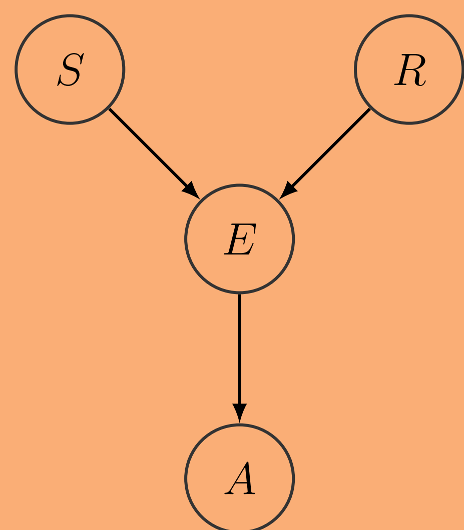


Figure 5: Directed graphical model for problem 5.

Sample Questions

(d) [2 pts.] Is S marginally independent of R? Is S conditionally independent of R given E? Answer yes or no to each questions and provide a brief explanation why.

5 Graphical Models [16 pts.]

We use the following Bayesian network to model the relationship between studying (S), being well-rested (R), doing well on the exam (E), and getting an A grade (A). All nodes are binary, i.e., $R, S, E, A \in \{0, 1\}$.

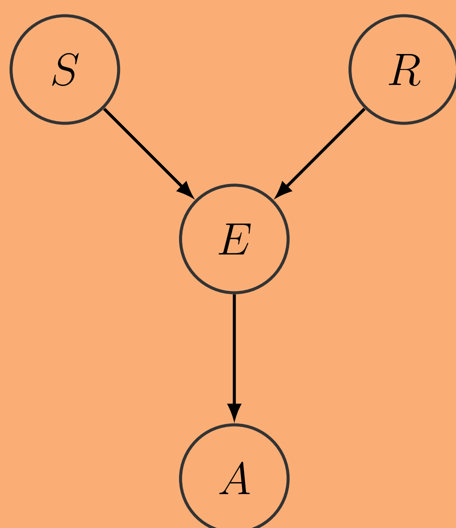


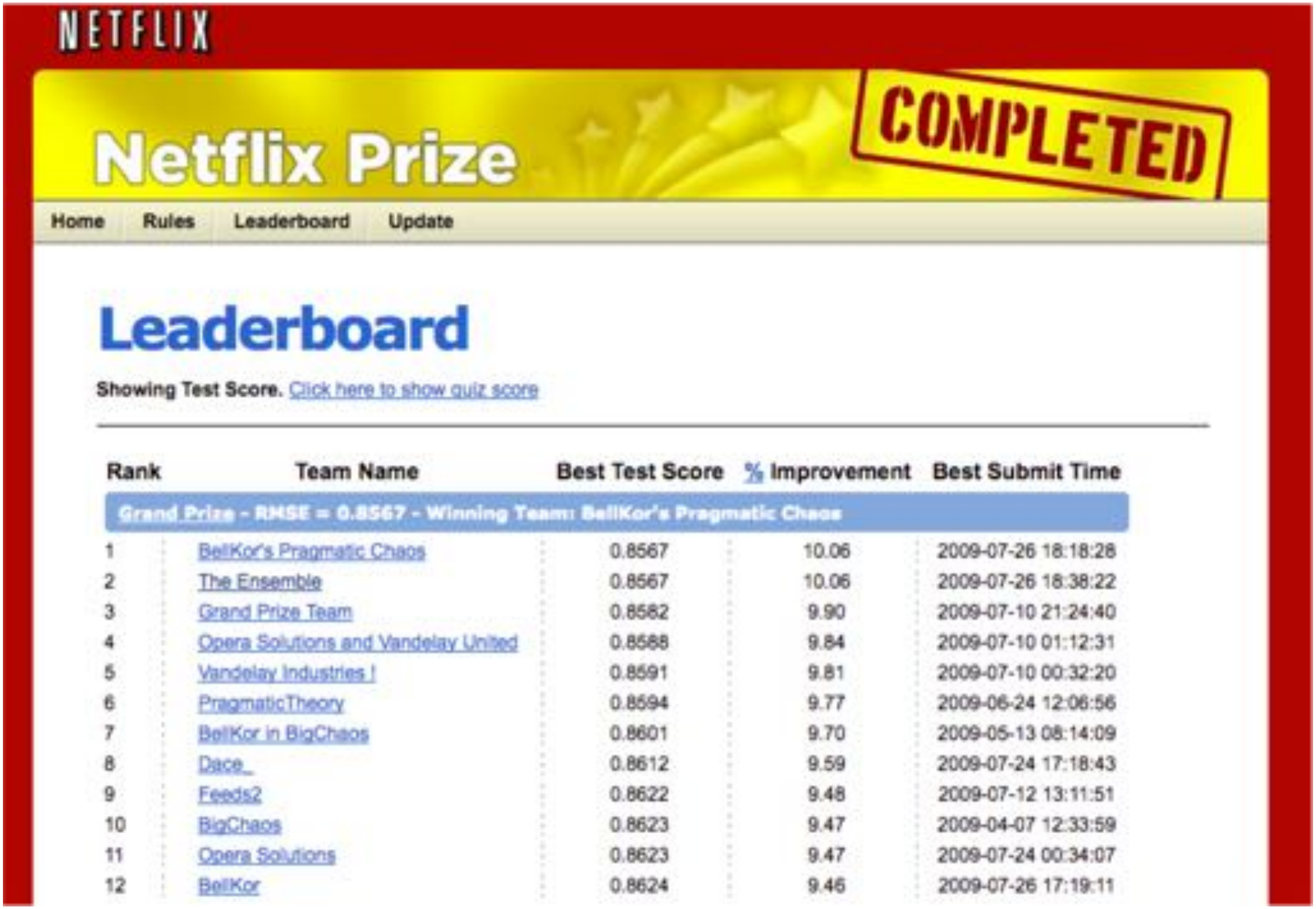
Figure 5: Directed graphical model for problem 5.

Sample Questions

5 Graphical Models

(f) [3 pts.] Give two reasons why the graphical models formalism is convenient when compared to learning a full joint distribution.

Recommender Systems

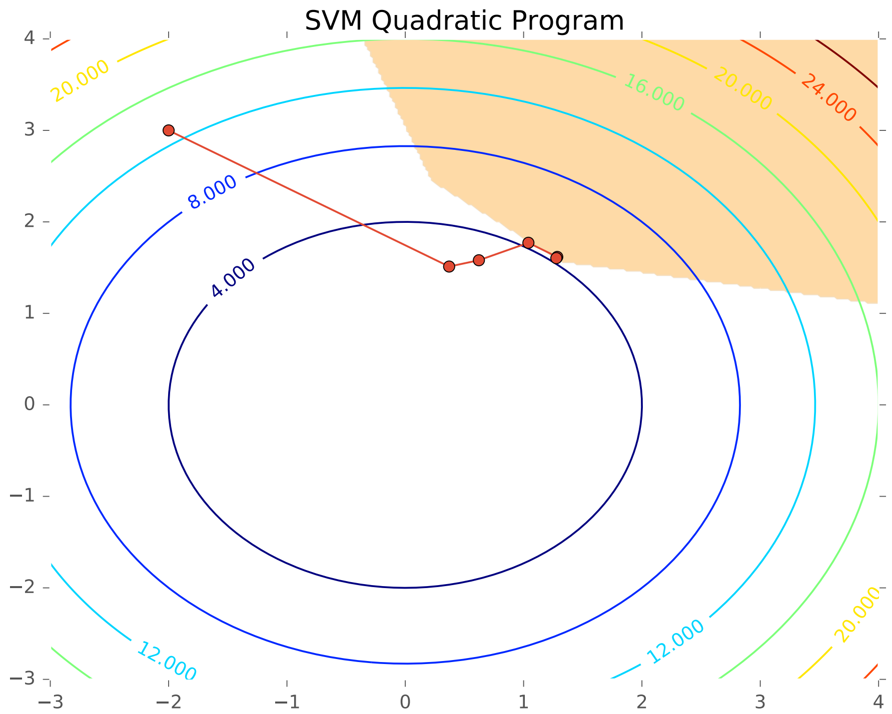


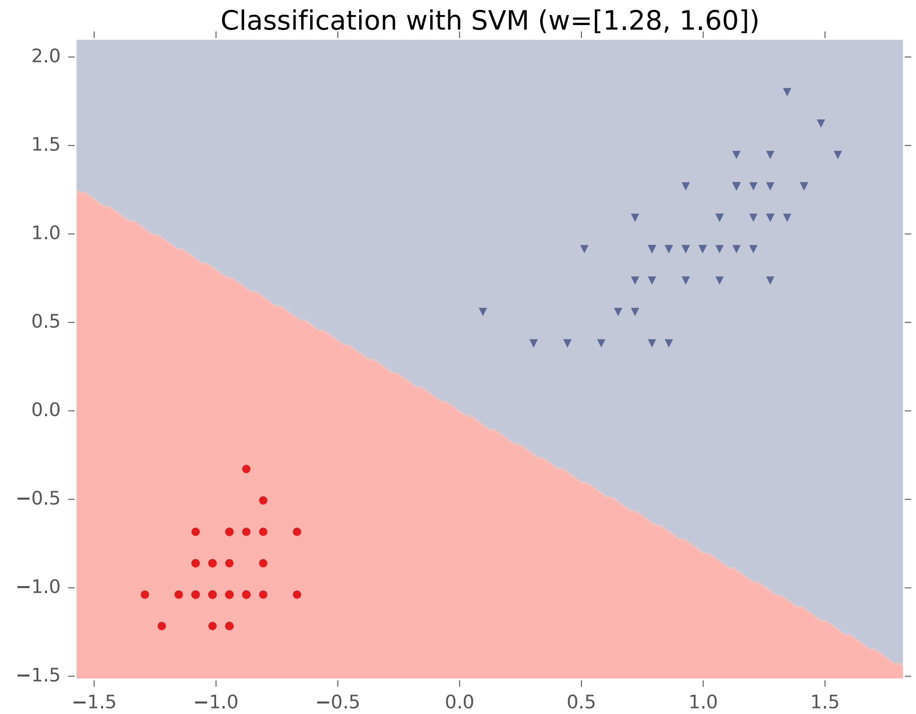
Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos				
1	BellKor's Pragmatic Chaos	0.8567	10.06	2009-07-26 18:18:28
2	The Ensemble	0.8567	10.06	2009-07-26 18:38:22
3	Grand Prize Team	0.8582	9.90	2009-07-10 21:24:40
4	Opera Solutions and Vandelay United	0.8588	9.84	2009-07-10 01:12:31
5	Vandelay Industries !	0.8591	9.81	2009-07-10 00:32:20
6	PragmaticTheory	0.8594	9.77	2009-06-24 12:06:56
7	BellKor in BigChaos	0.8601	9.70	2009-05-13 08:14:09
8	Dace_	0.8612	9.59	2009-07-24 17:18:43
9	Feeds2	0.8622	9.48	2009-07-12 13:11:51
10	BigChaos	0.8623	9.47	2009-04-07 12:33:59
11	Opera Solutions	0.8623	9.47	2009-07-24 00:34:07
12	BellKor	0.8624	9.46	2009-07-26 17:19:11

Example: Building a Canal

https://www.flickr.com/photos/hereistom/10438848375

SVM QP


SVM Quadratic Program
4.000
8.000
12.000
16.000
20.000
24.000


Classification with SVM (w=[1.28, 1.60])

Sample Questions

(c) [4 pts.] **Extra Credit:** Consider the dataset in Fig. 4. Under the SVM formulation in section 4.2(a),

(1) Draw the decision boundary on the graph.

(2) What is the size of the margin?

(3) Circle all the support vectors on the graph.

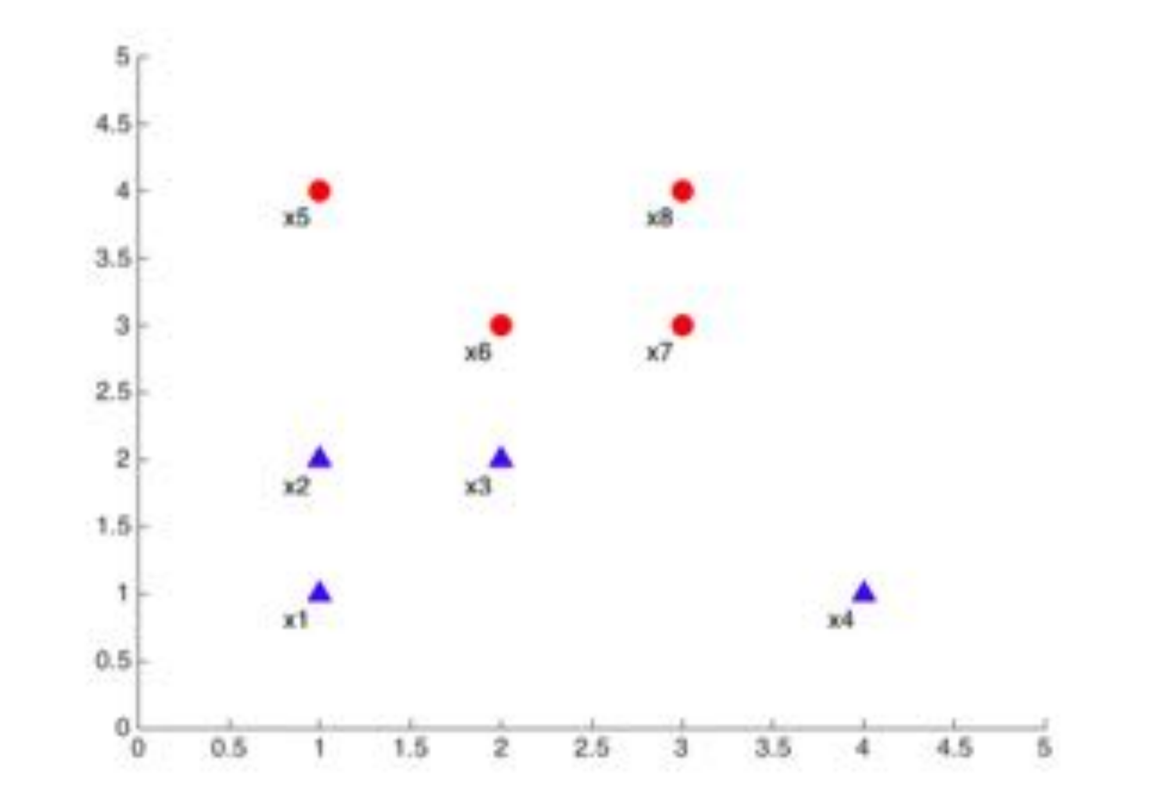


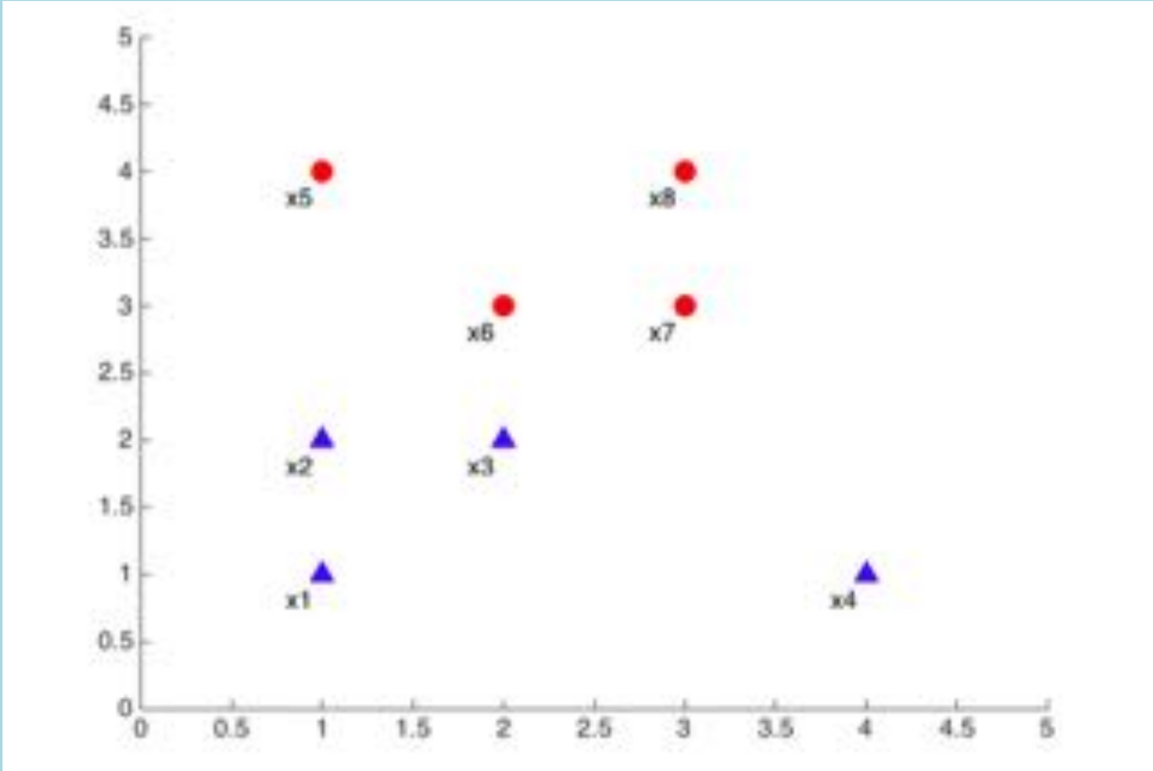
Figure 4: SVM toy dataset

Sample Questions

4.2 Multiple Choice

(a) [3 pt.] If the data is linearly separable, SVM minimizes $\|w\|^2$ subject to the constraints $\forall i, y_i w \cdot x_i \geq 1$. In the linearly separable case, which of the following may happen to the decision boundary if one of the training samples is removed? **Circle all that apply.**

- Shifts toward the point removed
- Shifts away from the point removed
- Does not change



Sample Questions

3. **[Extra Credit: 3 pts.]** One formulation of soft-margin SVM optimization problem is:

$$\min_{\mathbf{w}} \frac{1}{2}\|\mathbf{w}\|_2^2 + C\sum_{i=1}^{N}\xi_i$$

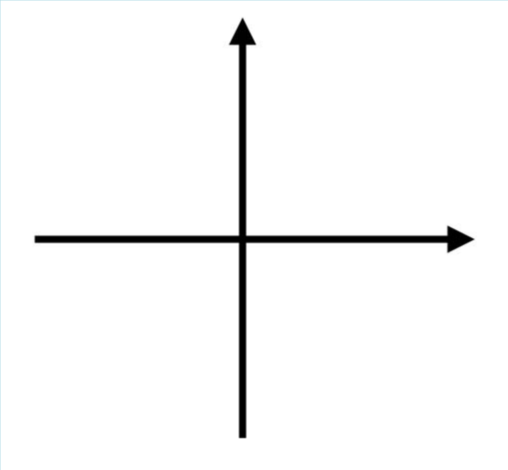
$$\text{s.t. } y_i(\mathbf{w}^\top x_i) \geq 1 - \xi_i \quad \forall i = 1, ..., N$$

$$\xi_i \geq 0 \quad \forall i = 1, ..., N$$

$$C \geq 0$$

where (x_i, y_i) are training samples and $\mathbf{w}$ defines a linear decision boundary.

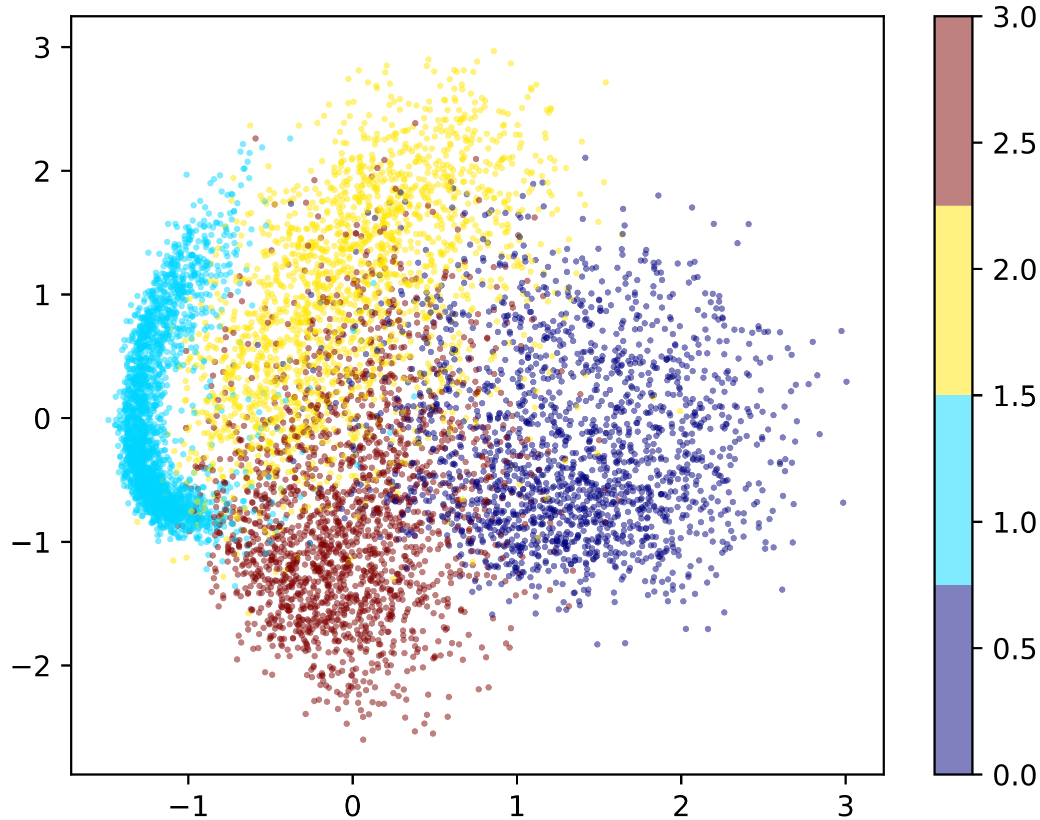
Derive a formula for ξ_i when the objective function achieves its minimum (No steps necessary). Note it is a function of $y_i\mathbf{w}^\top x_i$. Sketch a plot of ξ_i with $y_i\mathbf{w}^\top x_i$ on the x-axis and value of ξ_i on the y-axis. What is the name of this function?



Projecting MNIST digits

Task Setting:

1. Take 25x25 images of digits and project them down to 2 components
2. Plot the 2 dimensional points



Sample Questions

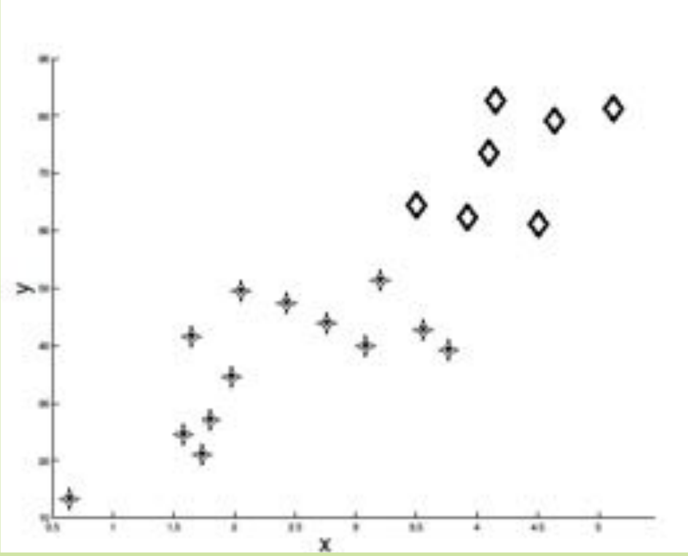
4 Principal Component Analysis [16 pts.]

(a) In the following plots, a train set of data points X belonging to two classes on $\mathbb{R}^2$ are given, where the original features are the coordinates (x, y). For each, answer the following questions:

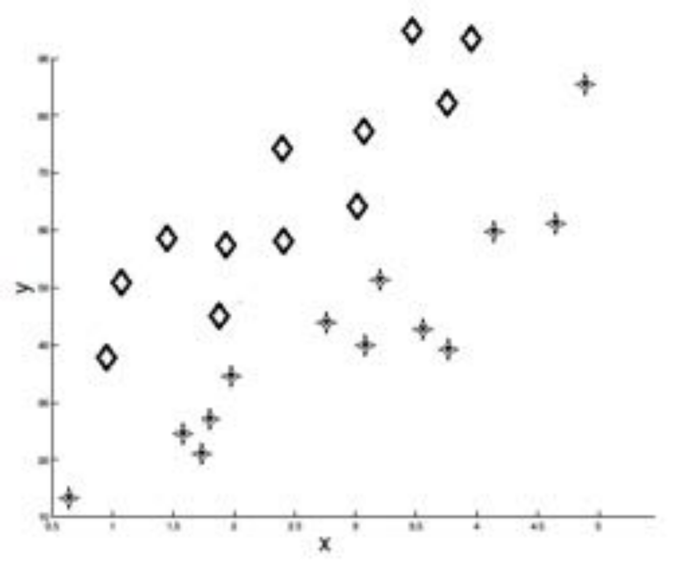
(i) [3 pt.] Draw all the principal components.

(ii) [6 pts.] Can we correctly classify this dataset by using a threshold function after projecting onto one of the principal components? If so, which principal component should we project onto? If not, explain in 1–2 sentences why it is not possible.

Dataset 1:



Dataset 2:



Sample Questions

4 Principal Component Analysis

(i) **T or F** The goal of PCA is to interpret the underlying structure of the data in terms of the principal components that are best at predicting the output variable.

(ii) **T or F** The output of PCA is a new representation of the data that is always of lower dimensionality than the original feature representation.

(iii) **T or F** Subsequent principal components are always orthogonal to each other.

Sample Questions

1 Topics before Midterm

8. **[2 pts]** With an infinite supply of training data, the trained Naïve Bayes classifier is an optimal classifier.

   Circle one: True False

   One line justification (only if False):

Sample Questions

1 Topics before Midterm

(a) [2 pts.] **T or F**: Naive Bayes can only be used with MLE estimates, and not MAP estimates.

(b) [2 pts.] **T or F**: Logistic regression cannot be trained with gradient descent algorithm.

(d) [2 pts.] **T or F**: Leaving out one training data point will always change the decision boundary obtained by perceptron.

Crowdsourcing Exam Questions

In-Class Exercise

1. Select one of lecture-level learning objectives
   http://mlcourse.org/slides/10601-objectives.pdf
2. Write a question that assesses that objective
3. Adjust to avoid 'trivia style' question

Answer Here:

The Big Picture

MACHINE LEARNING

Learning Paradigms

Paradigm	**Data**	
Supervised	$\mathcal{D} = \{\mathbf{x}^{(i)}, y^{(i)}\}_{i=1}^N$	$\mathbf{x} \sim p^*(\cdot)$ and $y = c^*(\cdot)$
↪ Regression	$y^{(i)} \in \mathbb{R}$	
↪ Classification	$y^{(i)} \in \{1, \ldots, K\}$	
↪ Binary classification	$y^{(i)} \in \{+1, -1\}$	
↪ Structured Prediction	$\mathbf{y}^{(i)}$ is a vector	

Learning Paradigms

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Online	$\mathcal{D} = \{(\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), (\mathbf{x}^{(3)}, y^{(3)}), \ldots\}$

Learning Paradigms

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Learning Paradigms

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Active Learning	$\mathcal{D} = \{\mathbf{x}^{(i)}\}_{i=1}^{N}$ and can query $y^{(i)} = c^*(\cdot)$ at a cost
Imitation Learning	$\mathcal{D} = \{(s^{(1)}, a^{(1)}), (s^{(2)}, a^{(2)}), \ldots\}$
Reinforcement Learning	$\mathcal{D} = \{(s^{(1)}, a^{(1)}, r^{(1)}), (s^{(2)}, a^{(2)}, r^{(2)}), \ldots\}$

Machine Learning: The Big Picture

Whiteboard

- **Decision Rules / Models** (probabilistic generative, probabilistic discriminative, perceptron, SVM, regression, MDP, graphical models)
- **Objective Functions** (likelihood, conditional likelihood, hinge loss, mean squared error)
- **Regularization** (L1, L2, priors for MAP)
- **Update Rules** (SGD, perceptron)
- **Nonlinear Features** (preprocessing, kernel trick)

ML Big Picture

Learning Paradigms:

What data is available and when? What form of prediction?

- supervised learning
- unsupervised learning
- semi-supervised learning
- reinforcement learning
- active learning
- imitation learning
- domain adaptation
- online learning
- density estimation
- recommender systems
- feature learning
- manifold learning
- dimensionality reduction
- ensemble learning
- distant supervision
- hyperparameter optimization

Problem Formulation:

What is the structure of our output prediction?

boolean	Binary Classification
categorical	Multiclass Classification
ordinal	Ordinal Classification
real	Regression
ordering	Ranking
multiple discrete	Structured Prediction
multiple continuous	(e.g. dynamical systems)
both discrete & cont.	(e.g. mixed graphical models)

Application Areas

Key challenges?

NLP, Speech, Computer Vision, Robotics, Medicine, Search

Theoretical Foundations:

What principles guide learning?

- ❑ probabilistic
- ❑ information theoretic
- ❑ evolutionary search
- ❑ ML as optimization

Facets of Building ML Systems:

How to build systems that are robust, efficient, adaptive, effective?

1. *Data prep*
2. *Model selection*
3. *Training (optimization / search)*
4. *Hyperparameter tuning on validation data*
5. *(Blind) Assessment on test data*

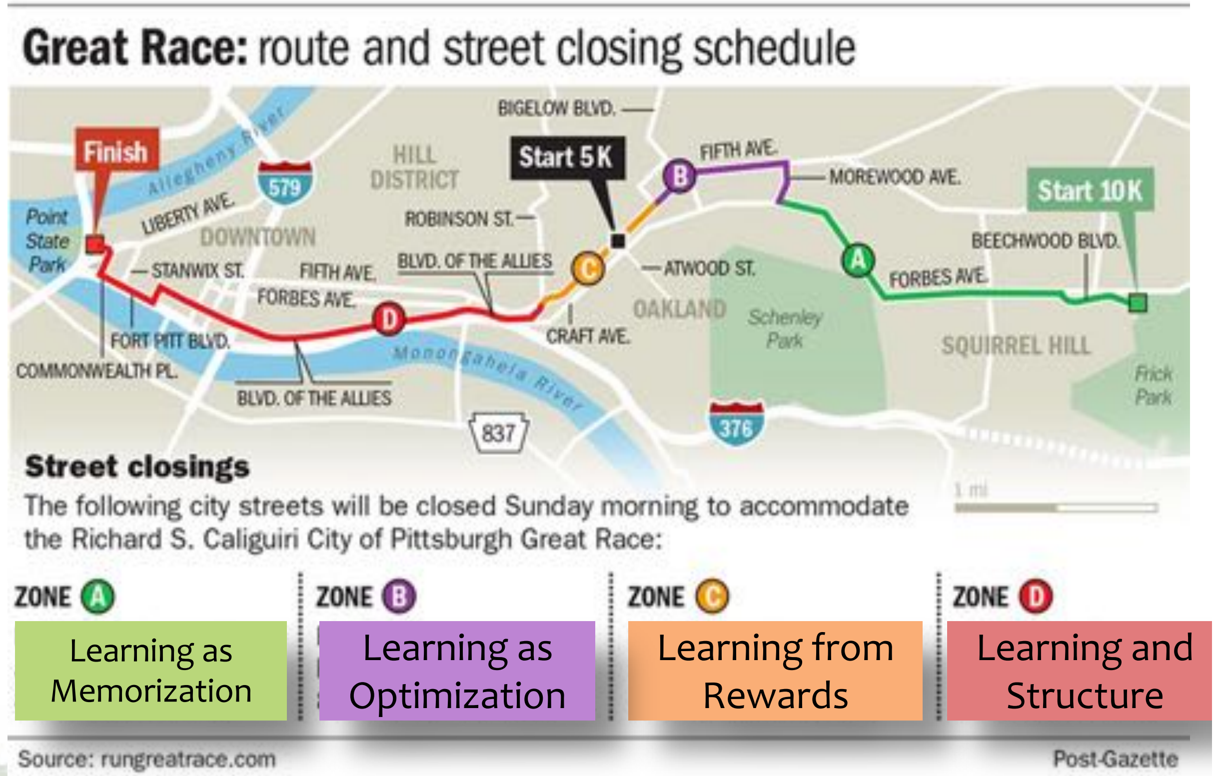
Big Ideas in ML:

Which are the ideas driving development of the field?

- *inductive bias*
- *generalization / overfitting*
- *bias-variance decomposition*
- *generative vs. discriminative*
- *deep nets, graphical models*
- *PAC learning*
- *distant rewards*

A new **combined** course…

…with the best (uphill climbs) from both



Course Level Objectives

You should be able to…

1. Implement and analyze existing learning algorithms, including well-studied methods for classification, regression, structured prediction, clustering, and representation learning
2. Integrate multiple facets of practical machine learning in a single system: data preprocessing, learning, regularization and model selection
3. Describe the the formal properties of models and algorithms for learning and explain the practical implications of those results
4. Compare and contrast different paradigms for learning (supervised, unsupervised, etc.)
5. Design experiments to evaluate and compare different machine learning techniques on real-world problems
6. Employ probability, statistics, calculus, linear algebra, and optimization in order to develop new predictive models or learning methods
7. Given a description of a ML technique, analyze it to identify (1) the expressive power of the formalism; (2) the inductive bias implicit in the algorithm; (3) the size and complexity of the search space; (4) the computational properties of the algorithm: (5) any guarantees (or lack thereof) regarding termination, convergence, correctness, accuracy or generalization power.

Q&A