

Deep Reinforcement Learning and Control

Function Approximation for Prediction

Lecture 6, CMU 10703

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Parts of slides borrowed from Russ Salakhutdinov, Rich Sutton, David Silver



Large-Scale Reinforcement Learning

- ▶ Reinforcement learning has been used to solve large problems, e.g.
 - Backgammon: 10^{20} states
 - Computer Go: 10^{170} states
 - Helicopter: continuous state space
- ▶ Tabular methods clearly do not work

Value Function Approximation (VFA)

- ▶ So far we have represented value function by a **lookup table**
 - Every **state** s has an entry $V(s)$, or
 - Every **state-action** pair (s,a) has an entry $Q(s,a)$
- ▶ Problem with large MDPs:
 - There are too many states and/or actions to store in memory
 - It is too slow to learn the value of each state individually
- ▶ Solution for large MDPs:
 - Estimate value function with **function approximation**

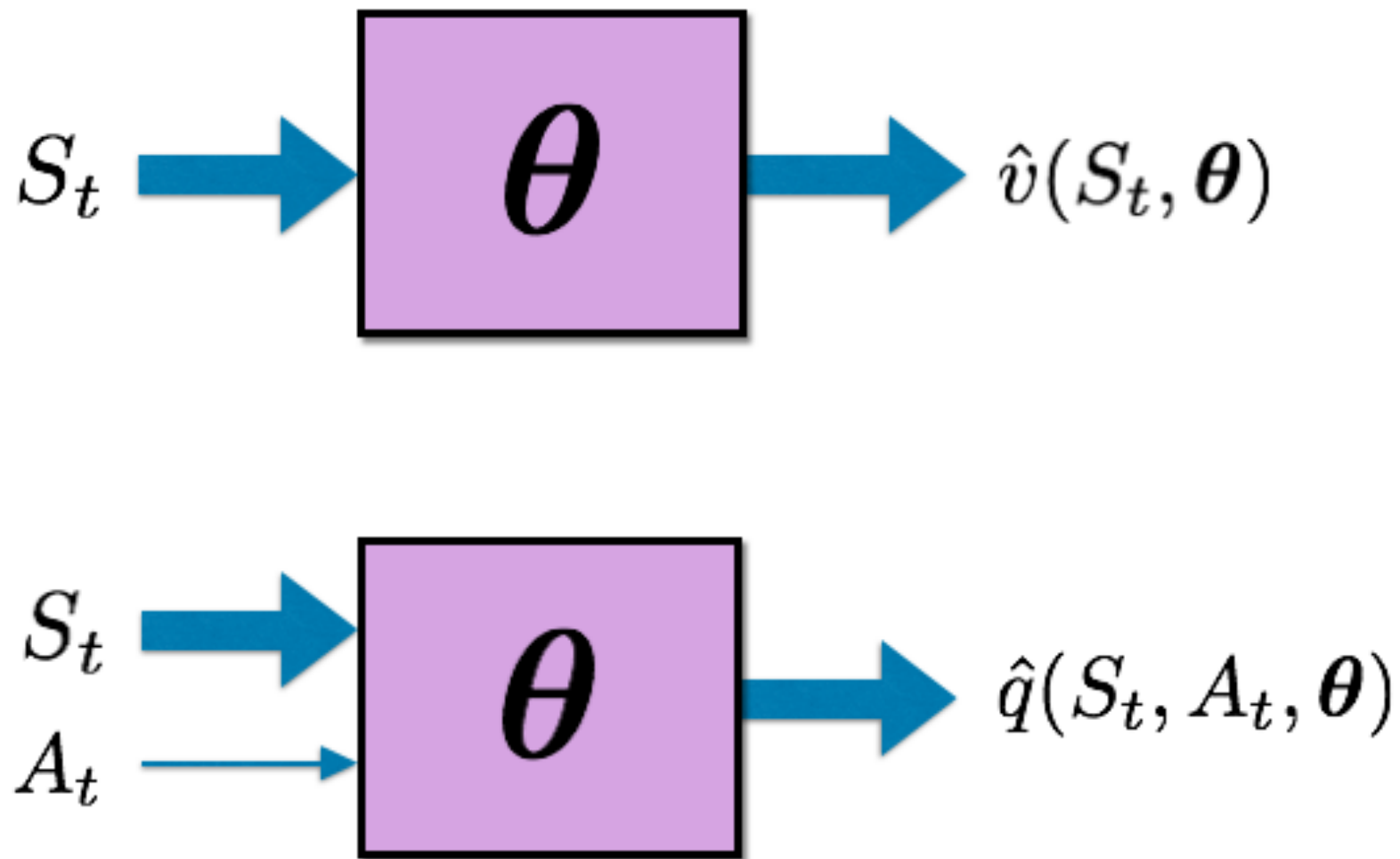
$$\hat{v}(s, \mathbf{w}) \approx v_{\pi}(s)$$

$$\text{or } \hat{q}(s, a, \mathbf{w}) \approx q_{\pi}(s, a)$$

- Generalize from seen states to unseen states

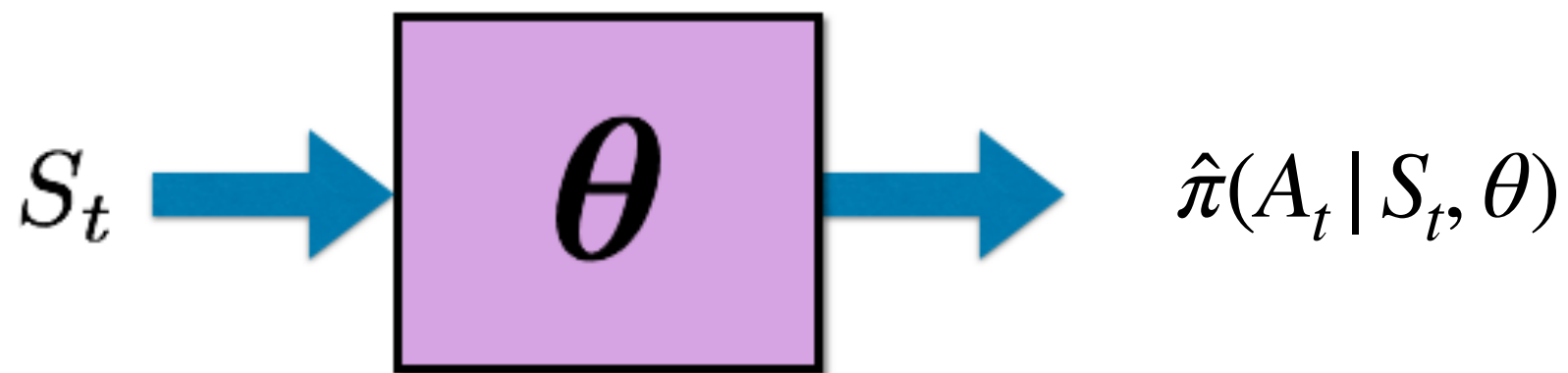
Value Function Approximation (VFA)

- Value function approximation (VFA) replaces the table with a general parameterized form:



Value Function Approximation (VFA)

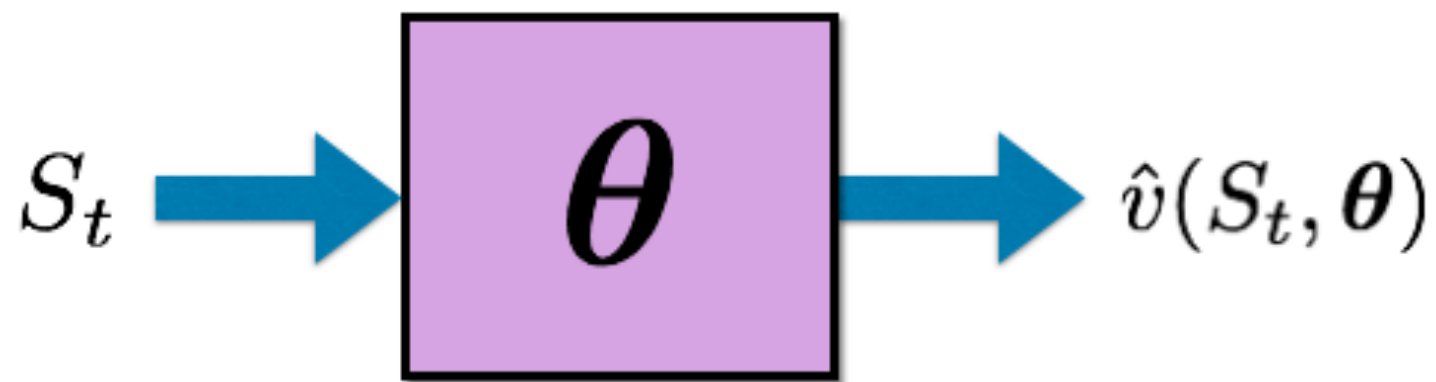
- ▶ Value function approximation (VFA) replaces the table with a general parameterized form:



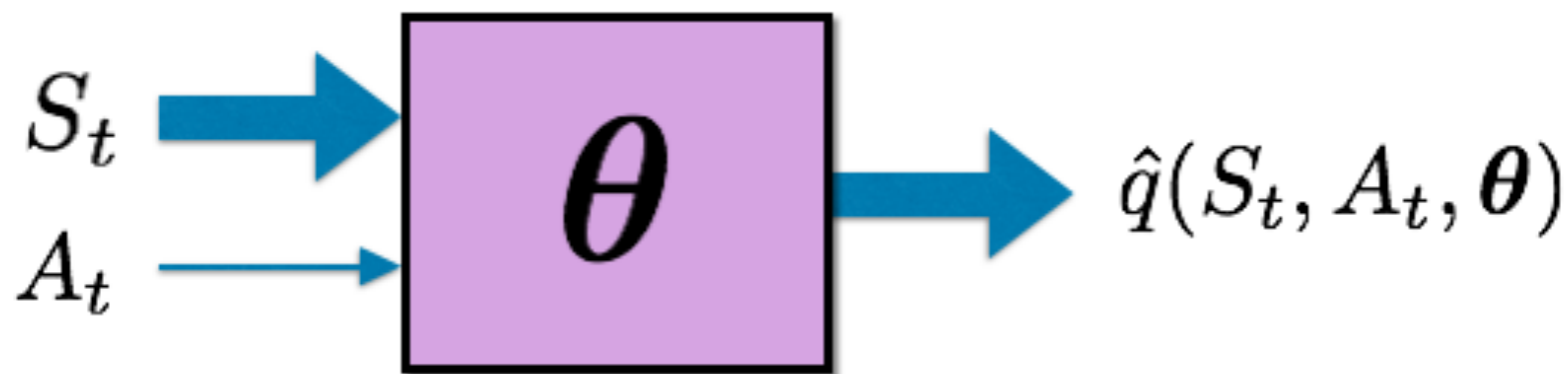
Next week: we will see policies to have such parametric form, also over continuous actions

Value Function Approximation (VFA)

- Value function approximation (VFA) replaces the table with a general parameterized form:



$$|\theta| \ll |\mathcal{S}|$$



When we update the parameters θ , the values of many states change simultaneously!

Which Function Approximation?

- ▶ There are many **function approximators**, e.g.
 - Linear combinations of features
 - Neural networks
 - Decision tree
 - Nearest neighbour
 - Fourier / wavelet bases
 - ...

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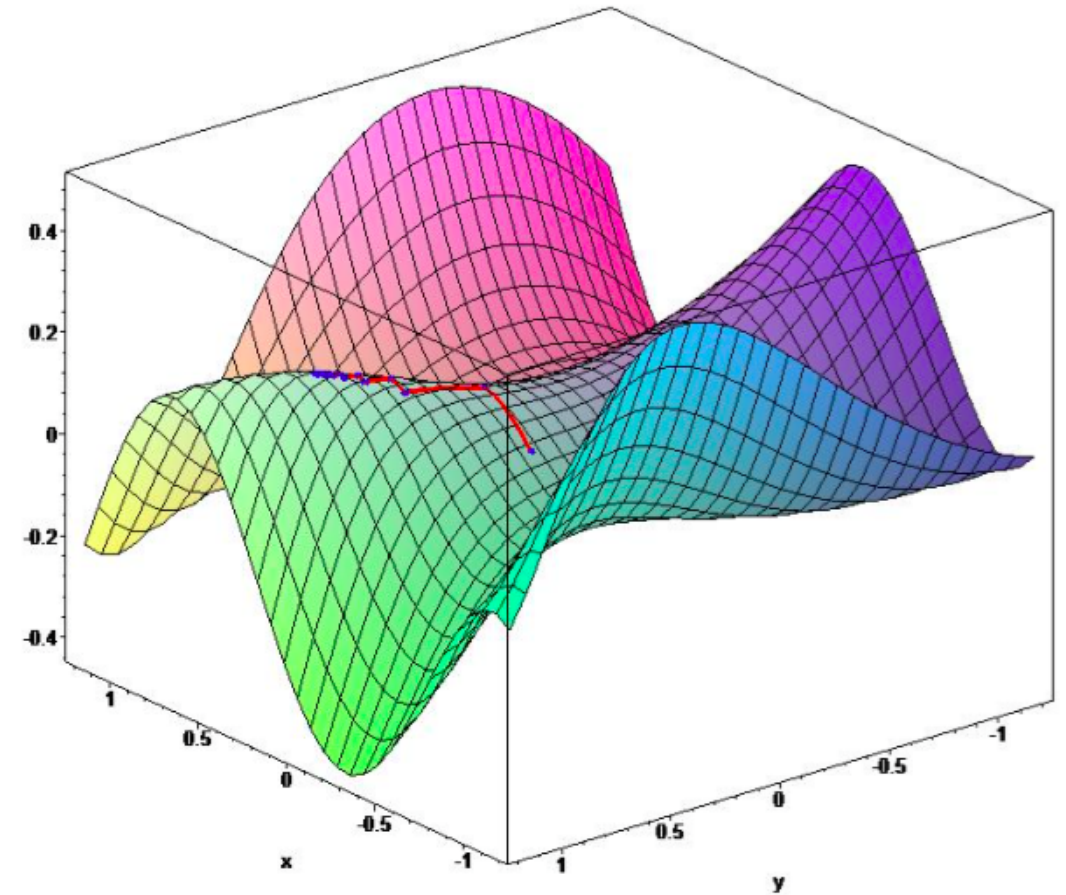
- **Linear combinations of features**
- **Neural networks**
- Decision tree
- Nearest neighbour
- Fourier / wavelet bases
- ...

► **differentiable function approximators**

Gradient Descent

- ▶ Let $J(\mathbf{w})$ be a **differentiable function** of parameter vector \mathbf{w}
- ▶ Define the gradient of $J(\mathbf{w})$ to be:

$$\nabla_{\mathbf{w}} J(\mathbf{w}) = \begin{pmatrix} \frac{\partial J(\mathbf{w})}{\partial \mathbf{w}_1} \\ \vdots \\ \frac{\partial J(\mathbf{w})}{\partial \mathbf{w}_n} \end{pmatrix}$$




Gradient Descent

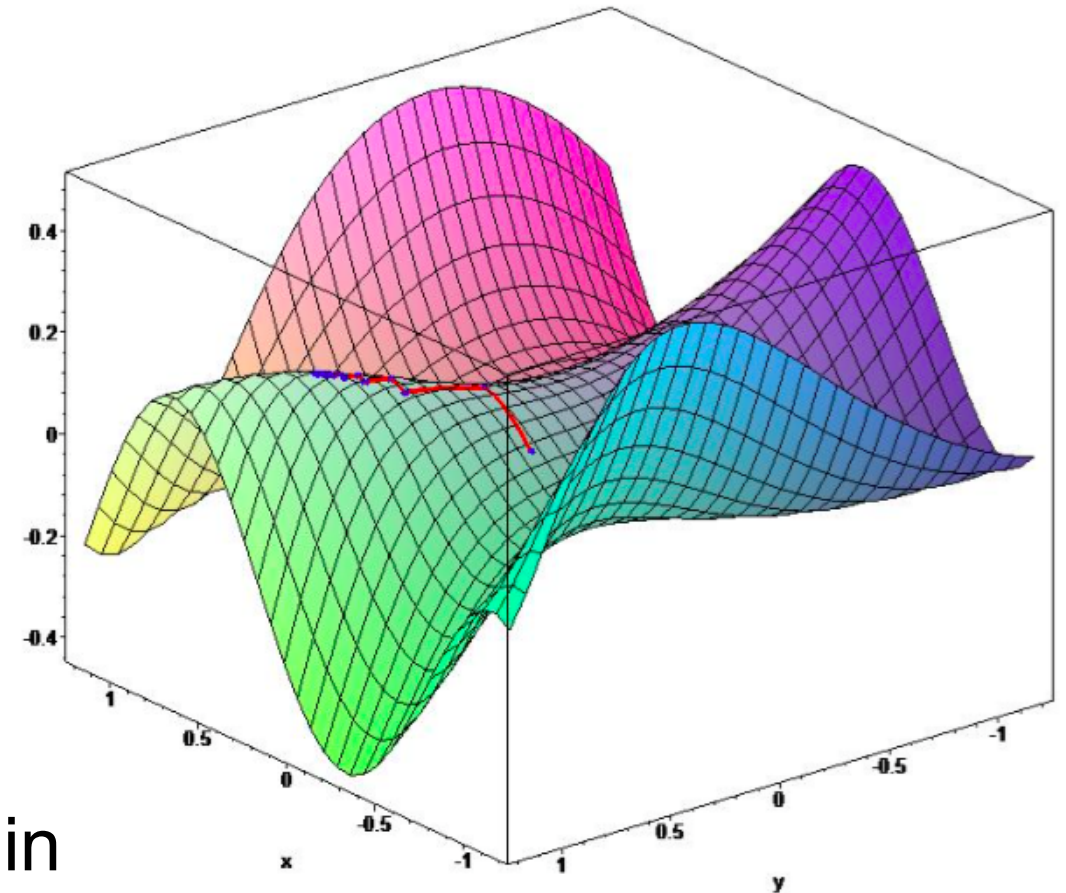
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- ▶ To find a local minimum of $J(\mathbf{w})$, adjust \mathbf{w} in direction of the **negative gradient**:

$$\Delta \mathbf{w} = -\frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w})$$

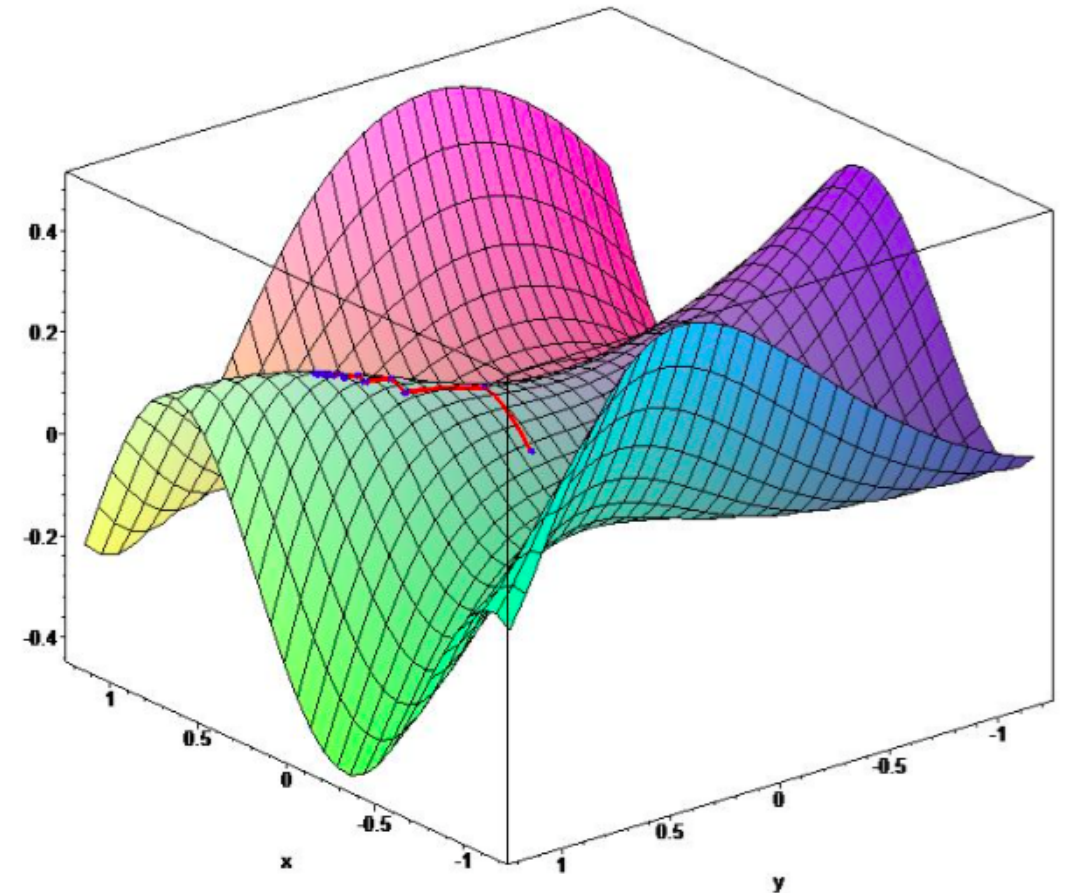

Step-size



Gradient Descent

- ▶ Let $J(\mathbf{w})$ be a **differentiable function** of parameter vector \mathbf{w}
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- ▶ Starting from a guess \mathbf{w}_0
- ▶ We consider the sequence $\mathbf{w}_0, \mathbf{w}_1, \mathbf{w}_2, \dots$ s.t. :

$$\mathbf{w}_{n+1} = \mathbf{w}_n - \frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w}_n)$$

- ▶ We then have $J(\mathbf{w}_0) \geq J(\mathbf{w}_1) \geq J(\mathbf{w}_2) \geq \dots$

Our objective

- ▶ **Goal**: find parameter vector \mathbf{w} minimizing mean-squared error between the true value function $v_{\pi}(S)$ and its approximation $\hat{v}(S, \mathbf{w})$

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Our objective

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$$J(\mathbf{w}) = \mathbb{E}_\pi \left[(v_\pi(S) - \hat{v}(S, \mathbf{w}))^2 \right]$$

Let $\mu(S)$ denote how much time we spend in each state s under policy π , then:

$$J(\mathbf{w}) = \sum_{n=1}^{|\mathcal{S}|} \mu(S) [v_\pi(S) - \hat{v}(S, \mathbf{w})]^2 \quad \sum_{s \in \mathcal{S}} \mu(S) = 1$$

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In contrast to:

$$J_2(\mathbf{w}) = \frac{1}{|\mathcal{S}|} \sum_{s \in \mathcal{S}} [v_\pi(S) - \hat{v}(S, \mathbf{w})]^2$$

Gradient Descent

- ▶ **Goal**: find parameter vector \mathbf{w} minimizing mean-squared error between the true value function $v_\pi(S)$ and its approximation $\hat{v}(S, \mathbf{w})$

$$J(\mathbf{w}) = \mathbb{E}_\pi \left[(v_\pi(S) - \hat{v}(S, \mathbf{w}))^2 \right]$$

- ▶ Gradient descent finds a local minimum:

$$\begin{aligned} \Delta \mathbf{w} &= -\frac{1}{2} \alpha \nabla_{\mathbf{w}} J(\mathbf{w}) \\ &= \alpha \mathbb{E}_\pi \left[(v_\pi(S) - \hat{v}(S, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S, \mathbf{w}) \right] \end{aligned}$$

Stochastic Gradient Descent

- ▶ **Goal**: find parameter vector \mathbf{w} minimizing mean-squared error between the true value function $v_\pi(S)$ and its approximation $\hat{v}(S, \mathbf{w})$

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- ▶ Stochastic gradient descent (SGD) samples the gradient:

$$\Delta \mathbf{w} = \alpha (v_\pi(S) - \hat{v}(S, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S, \mathbf{w})$$

No summation over all states! One example at a time!

Feature Vectors

- ▶ Represent state by a **feature vector**

$$\mathbf{x}(S) = \begin{pmatrix} \mathbf{x}_1(S) \\ \vdots \\ \mathbf{x}_n(S) \end{pmatrix}$$

- ▶ For example
 - Distance of robot from landmarks
 - Trends in the stock market
 - Piece and pawn configurations in chess

Linear Value Function Approximation (VFA)

- ▶ Represent **value function** by a linear combination of features

$$\hat{v}(S, \mathbf{w}) = \mathbf{x}(S)^\top \mathbf{w} = \sum_{j=1}^n \mathbf{x}_j(S) \mathbf{w}_j$$

- ▶ Objective function is **quadratic in parameters** \mathbf{w}

$$J(\mathbf{w}) = \mathbb{E}_\pi \left[(v_\pi(S) - \mathbf{x}(S)^\top \mathbf{w})^2 \right]$$

- ▶ Update rule is particularly simple

$$\nabla_{\mathbf{w}} \hat{v}(S, \mathbf{w}) = \mathbf{x}(S)$$

$$\Delta \mathbf{w} = \alpha (v_\pi(S) - \hat{v}(S, \mathbf{w})) \mathbf{x}(S)$$

- ▶ **Update** = step-size \times prediction error \times feature value
- ▶ Later, we will look at the neural networks as function approximators.

Incremental Prediction Algorithms

- ▶ We have assumed the **true value function** $v_\pi(s)$ is given by a supervisor
- ▶ But in RL there is no supervisor, only rewards
- ▶ In practice, we substitute a target for $v_\pi(s)$
- ▶ For MC, the target is the **return** G_t

$$\Delta \mathbf{w} = \alpha(\mathbf{G}_t - \hat{v}(S_t, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S_t, \mathbf{w})$$

- ▶ For TD(0), the target is the **TD target**: $R_{t+1} + \gamma \hat{v}(S_{t+1}, \mathbf{w})$

$$\Delta \mathbf{w} = \alpha(\mathbf{R}_{t+1} + \gamma \hat{v}(S_{t+1}, \mathbf{w}) - \hat{v}(S_t, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S_t, \mathbf{w})$$

Remember $\Delta \mathbf{w} = \alpha(v_\pi(S) - \hat{v}(S, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S, \mathbf{w})$

Monte Carlo with VFA

- ▶ Return G_t is an **unbiased**, noisy sample of true value $v_{\pi}(S_t)$
- ▶ Can therefore apply supervised learning to “**training data**”:

$$\langle S_1, G_1 \rangle, \langle S_2, G_2 \rangle, \dots, \langle S_T, G_T \rangle$$

- ▶ For example, using **linear Monte-Carlo policy evaluation**

$$\begin{aligned}\Delta \mathbf{w} &= \alpha(\mathbf{G}_t - \hat{v}(S_t, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S_t, \mathbf{w}) \\ &= \alpha(G_t - \hat{v}(S_t, \mathbf{w})) \mathbf{x}(S_t)\end{aligned}$$

- ▶ Monte-Carlo evaluation converges to a local optimum

Monte Carlo with VFA

Gradient Monte Carlo Algorithm for Approximating $\hat{v} \approx v_\pi$

Input: the policy π to be evaluated

Input: a differentiable function $\hat{v} : \mathcal{S} \times \mathbb{R}^n \rightarrow \mathbb{R}$

Initialize value-function weights $\boldsymbol{\theta}$ as appropriate (e.g., $\boldsymbol{\theta} = \mathbf{0}$)

Repeat forever:

 Generate an episode $S_0, A_0, R_1, S_1, A_1, \dots, R_T, S_T$ using π

 For $t = 0, 1, \dots, T - 1$:

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha [G_t - \hat{v}(S_t, \boldsymbol{\theta})] \nabla \hat{v}(S_t, \boldsymbol{\theta})$$

TD Learning with VFA

- ▶ The TD-target $R_{t+1} + \gamma \hat{v}(S_{t+1}, \mathbf{w})$ a **biased sample** of true value $v_{\pi}(S_t)$

- ▶ Can still apply supervised learning to “**training data**”:

$$\langle S_1, R_2 + \gamma \hat{v}(S_2, \mathbf{w}) \rangle, \langle S_2, R_3 + \gamma \hat{v}(S_3, \mathbf{w}) \rangle, \dots, \langle S_{T-1}, R_T \rangle$$

- ▶ For example, using **linear TD(0)**:

$$\begin{aligned} \Delta \mathbf{w} &= \alpha (\mathbf{R} + \gamma \hat{v}(S', \mathbf{w}) - \hat{v}(S, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(S, \mathbf{w}) \\ &= \alpha \delta \mathbf{x}(S) \end{aligned}$$

We ignore the dependence of the target on \mathbf{w} !

We call it semi-gradient methods

TD Learning with VFA

Semi-gradient TD(0) for estimating $\hat{v} \approx v_\pi$

Input: the policy π to be evaluated

Input: a differentiable function $\hat{v} : \mathcal{S}^+ \times \mathbb{R}^n \rightarrow \mathbb{R}$ such that $\hat{v}(\text{terminal}, \cdot) = 0$

Initialize value-function weights $\boldsymbol{\theta}$ arbitrarily (e.g., $\boldsymbol{\theta} = \mathbf{0}$)

Repeat (for each episode):

 Initialize S

 Repeat (for each step of episode):

 Choose $A \sim \pi(\cdot | S)$

 Take action A , observe R, S'

$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha [R + \gamma \hat{v}(S', \boldsymbol{\theta}) - \hat{v}(S, \boldsymbol{\theta})] \nabla \hat{v}(S, \boldsymbol{\theta})$

$S \leftarrow S'$

 until S' is terminal

Control with VFA

- ▶ Policy evaluation **Approximate** policy evaluation: $\hat{q}(\cdot, \cdot, \mathbf{w}) \approx q_\pi$
- ▶ Policy improvement ϵ -greedy policy improvement

Action-Value Function Approximation

- ▶ Approximate the **action-value function**

$$\hat{q}(S, A, \mathbf{w}) \approx q_{\pi}(S, A)$$

- ▶ Minimize **mean-squared error** between the true action-value function $q_{\pi}(S, A)$ and the approximate action-value function:

$$J(\mathbf{w}) = \mathbb{E}_{\pi} [(q_{\pi}(S, A) - \hat{q}(S, A, \mathbf{w}))^2]$$

- ▶ Use **stochastic gradient descent** to find a local minimum

$$-\frac{1}{2} \nabla_{\mathbf{w}} J(\mathbf{w}) = (q_{\pi}(S, A) - \hat{q}(S, A, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S, A, \mathbf{w})$$

$$\Delta \mathbf{w} = \alpha (q_{\pi}(S, A) - \hat{q}(S, A, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S, A, \mathbf{w})$$

Linear Action-Value Function Approximation

- ▶ Represent state and action by a **feature vector**

$$\mathbf{x}(S, A) = \begin{pmatrix} \mathbf{x}_1(S, A) \\ \vdots \\ \mathbf{x}_n(S, A) \end{pmatrix}$$

- ▶ Represent action-value function by **linear combination of features**

$$\hat{q}(S, A, \mathbf{w}) = \mathbf{x}(S, A)^\top \mathbf{w} = \sum_{j=1}^n \mathbf{x}_j(S, A) \mathbf{w}_j$$

- ▶ **Stochastic gradient descent** update

$$\nabla_{\mathbf{w}} \hat{q}(S, A, \mathbf{w}) = \mathbf{x}(S, A)$$

$$\Delta \mathbf{w} = \alpha (q_\pi(S, A) - \hat{q}(S, A, \mathbf{w})) \mathbf{x}(S, A)$$

Incremental Control Algorithms

- ▶ Like prediction, we must substitute a target for $q_{\pi}(S,A)$
- ▶ For MC, the target is the return G_t

$$\Delta \mathbf{w} = \alpha(\mathbf{G}_t - \hat{q}(S_t, A_t, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S_t, A_t, \mathbf{w})$$

- ▶ For TD(0), the target is the TD target: $R_{t+1} + \gamma Q(S_{t+1}, A_{t+1})$

$$\Delta \mathbf{w} = \alpha(\mathbf{R}_{t+1} + \gamma \hat{q}(S_{t+1}, A_{t+1}, \mathbf{w}) - \hat{q}(S_t, A_t, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S_t, A_t, \mathbf{w})$$

Incremental Control Algorithms

Episodic Semi-gradient Sarsa for Estimating $\hat{q} \approx q_*$

Input: a differentiable function $\hat{q} : \mathcal{S} \times \mathcal{A} \times \mathbb{R}^n \rightarrow \mathbb{R}$

Initialize value-function weights $\boldsymbol{\theta} \in \mathbb{R}^n$ arbitrarily (e.g., $\boldsymbol{\theta} = \mathbf{0}$)

Repeat (for each episode):

$S, A \leftarrow$ initial state and action of episode (e.g., ε -greedy)

 Repeat (for each step of episode):

 Take action A , observe R, S'

 If S' is terminal:

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha [R - \hat{q}(S, A, \boldsymbol{\theta})] \nabla \hat{q}(S, A, \boldsymbol{\theta})$$

 Go to next episode

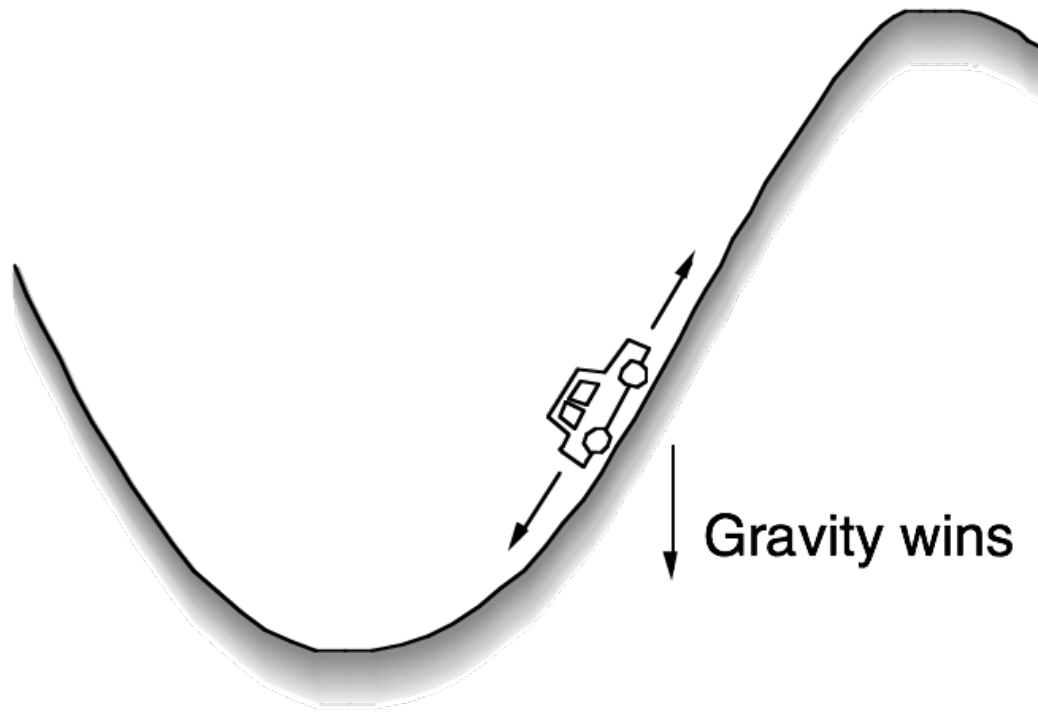
 Choose A' as a function of $\hat{q}(S', \cdot, \boldsymbol{\theta})$ (e.g., ε -greedy)

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha [R + \gamma \hat{q}(S', A', \boldsymbol{\theta}) - \hat{q}(S, A, \boldsymbol{\theta})] \nabla \hat{q}(S, A, \boldsymbol{\theta})$$

$S \leftarrow S'$

$A \leftarrow A'$

Example: The Mountain-Car problem



Minimum-Time-to-Goal Problem

SITUATIONS:

car's position and velocity

ACTIONS:

three thrusts: forward, reverse, none

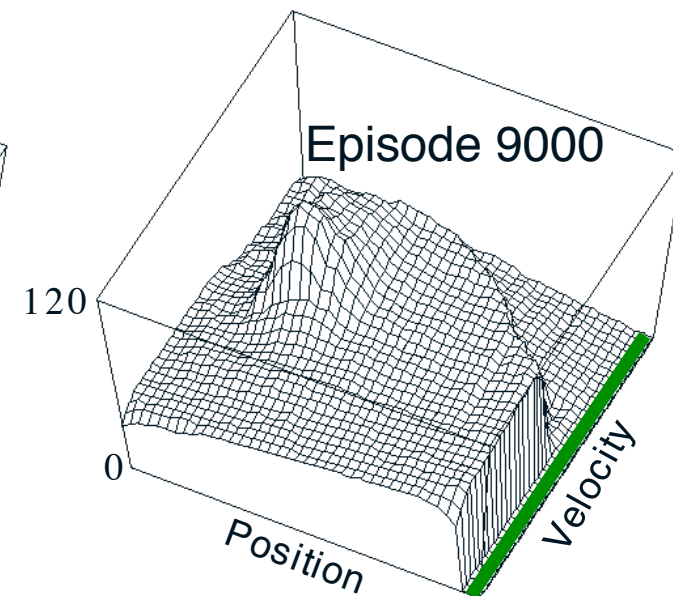
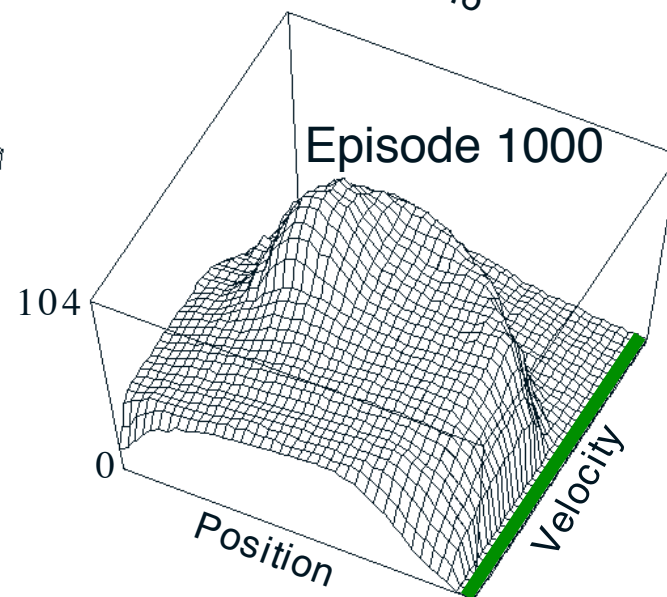
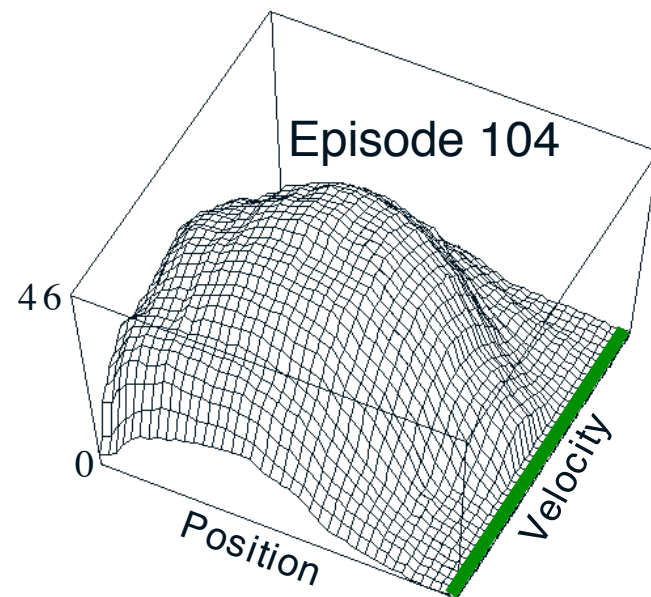
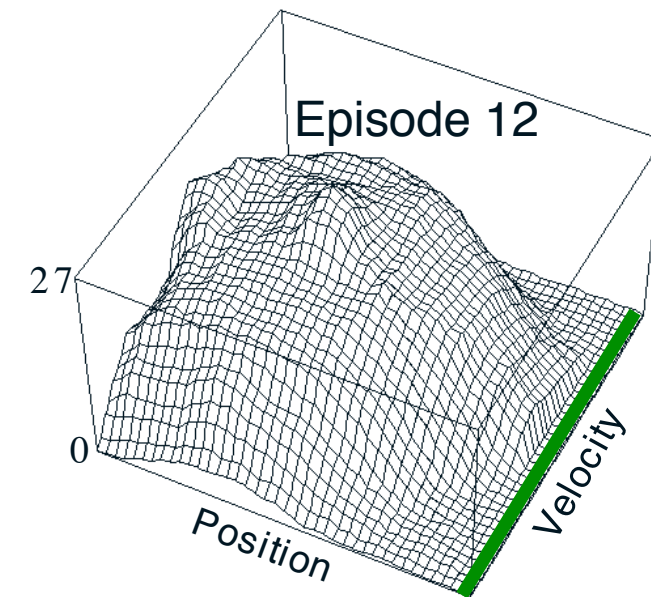
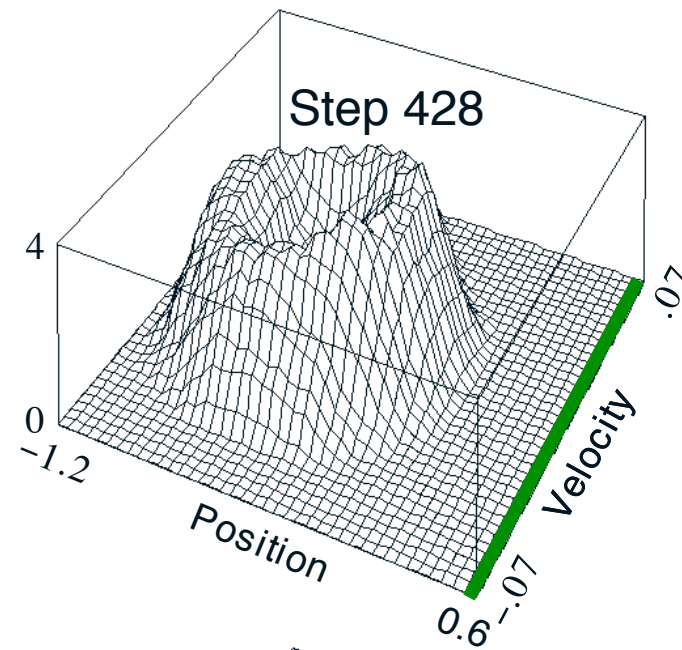
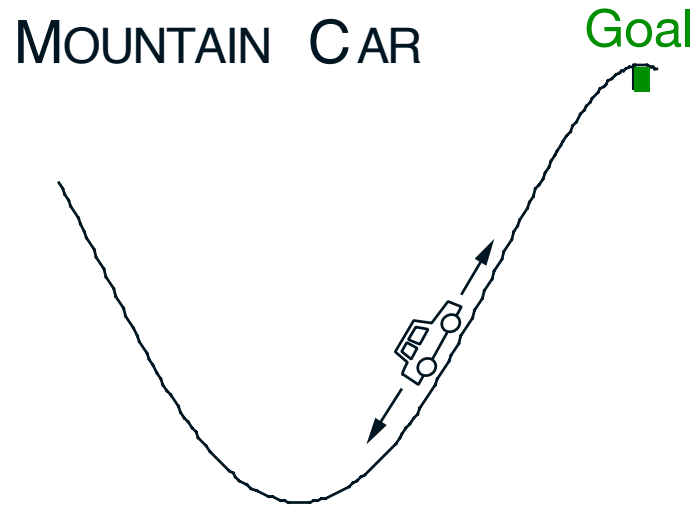
REWARDS:

always -1 until car reaches the goal

Episodic, No Discounting, $\gamma=1$

Example: The Mountain-Car problem

$$- \max_a \hat{q}(s, a, \theta)$$



Batch Reinforcement Learning

- ▶ Gradient descent is simple and appealing
- ▶ But it is not **sample efficient**
- ▶ Batch methods seek to find the best fitting value function
- ▶ Given the agent's **experience** (“training data”)

Least Squares Prediction

▶ Given **value function approximation**: $\hat{v}(s, \mathbf{w}) \approx v_\pi(s)$

▶ And **experience** \mathcal{D} consisting of $\langle \text{state}, \text{value} \rangle$ pairs

$$\mathcal{D} = \{ \langle s_1, v_1^\pi \rangle, \langle s_2, v_2^\pi \rangle, \dots, \langle s_T, v_T^\pi \rangle \}$$

▶ Find parameters \mathbf{w} that give the best fitting value function $v(s, \mathbf{w})$?

▶ Least squares **algorithms** find parameter vector \mathbf{w} minimizing sum-squared error between $v(s_t, \mathbf{w})$ and target values v_t^π :

$$\begin{aligned} LS(\mathbf{w}) &= \sum_{t=1}^T (v_t^\pi - \hat{v}(s_t, \mathbf{w}))^2 \\ &= \mathbb{E}_{\mathcal{D}} [(v^\pi - \hat{v}(s, \mathbf{w}))^2] \end{aligned}$$

SGD with Experience Replay

- ▶ Given **experience** consisting of $\langle \text{state}, \text{value} \rangle$ pairs

$$\mathcal{D} = \{ \langle s_1, v_1^\pi \rangle, \langle s_2, v_2^\pi \rangle, \dots, \langle s_T, v_T^\pi \rangle \}$$

- ▶ Repeat

- Sample state, value from experience

$$\langle s, v^\pi \rangle \sim \mathcal{D}$$

- Apply stochastic gradient descent update

$$\Delta \mathbf{w} = \alpha (v^\pi - \hat{v}(s, \mathbf{w})) \nabla_{\mathbf{w}} \hat{v}(s, \mathbf{w})$$

- ▶ Converges to least squares solution

- ▶ We will look at Deep Q-networks later.

Which Function Approximation?

- ▶ There are many **function approximators**, e.g.
 - Linear combinations of features
 - Neural networks
 - Decision tree
 - **Nearest neighbour**
 - Fourier / wavelet bases
 - ...

Nearest neighbors

- ▶ Save training examples in memory as they arrive $(s, v(s))$. (state, value)
- ▶ Then, given a new state s' , retrieve closest state examples from the memory and average their values based on similarity:

$$v(s') = \sum_{i=1}^K k(h_{s'}, h_{s_i}) v(s_i)$$

- ▶ Accuracy improves as more data accumulates.
- ▶ Agent's experience has an **immediate affect** on value estimates in the neighborhood of its environment's current state.
- ▶ Parametric methods need to incrementally adjust parameters of a global approximation.

Neural Episodic Control

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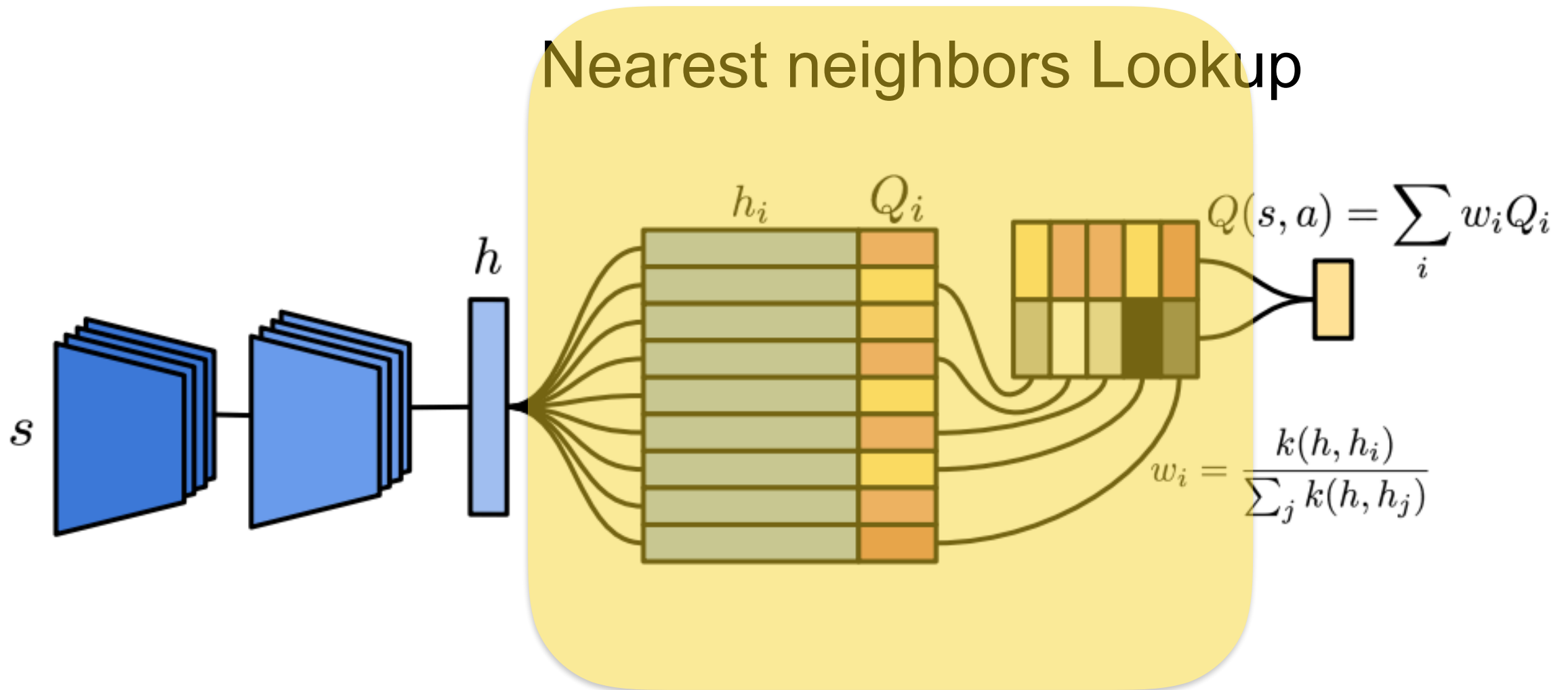
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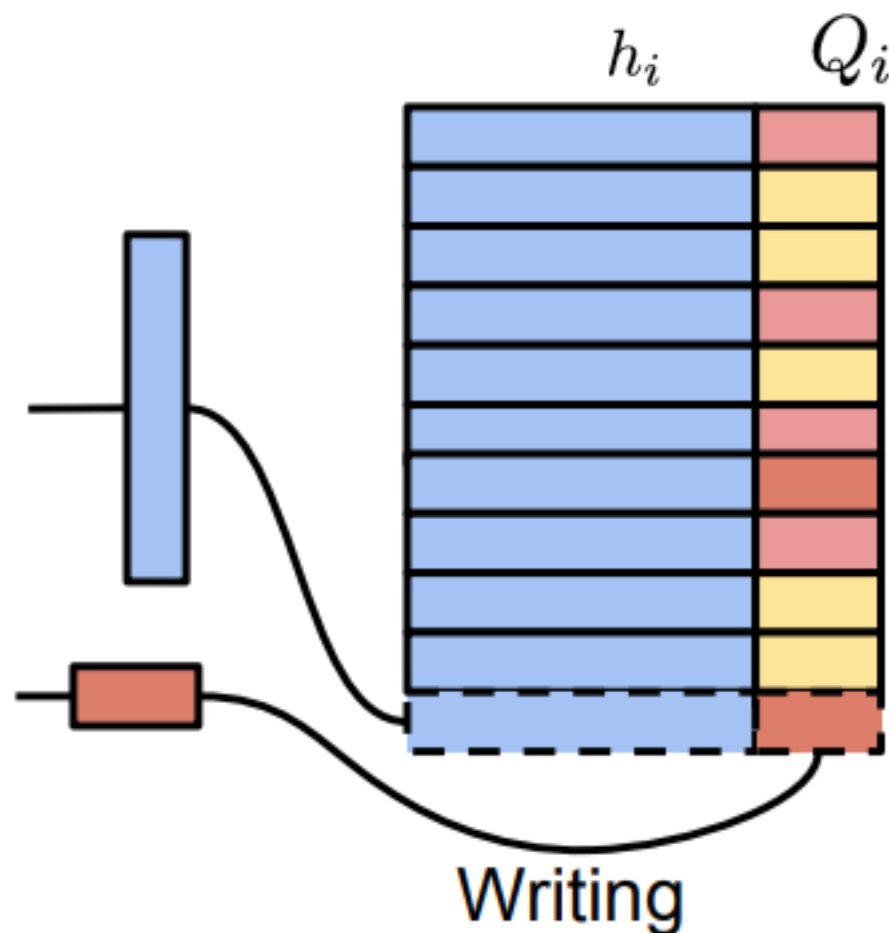
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Nearest neighbors Lookup



Writing in the memory

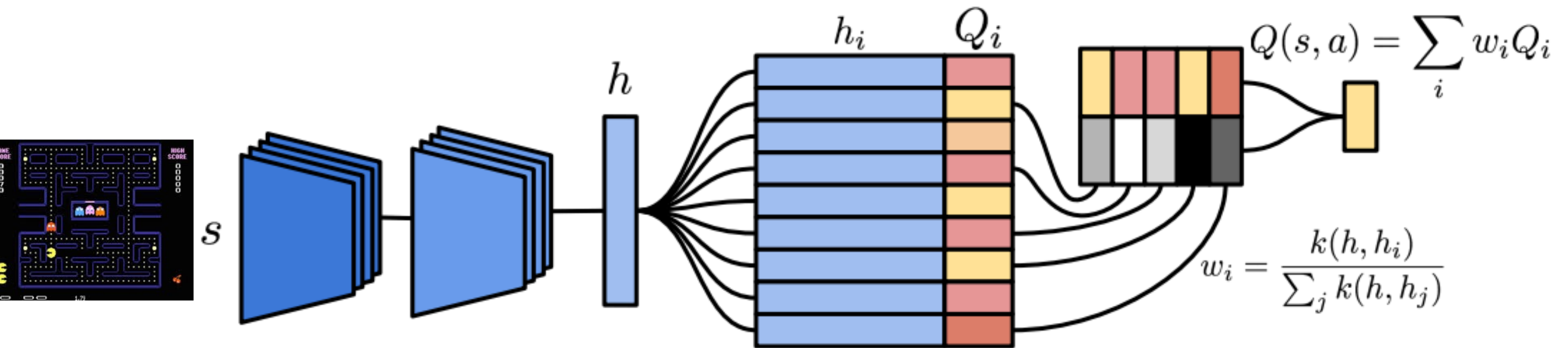


$$Q^{(N)}(s_t, a) = \sum_{j=0}^{N-1} \gamma^j r_{t+j} + \gamma^N \max_{a'} Q(s_{t+N}, a')$$

If identical key h present:

$$Q_i \leftarrow Q_i + \alpha(Q^{(N)}(s, a) - Q_i)$$

Else add row $(h, Q^N(s, a))$ to the memory



Algorithm 1 Neural Episodic Control

\mathcal{D} : replay memory.

M_a : a DND for each action a .

N : horizon for N -step Q estimate.

for each episode **do**

for $t = 1, 2, \dots, T$ **do**

 Receive observation s_t from environment with embedding h .

 Estimate $Q(s_t, a)$ for each action a via (1) from M_a

$a_t \leftarrow \epsilon$ -greedy policy based on $Q(s_t, a)$

 Take action a_t , receive reward r_{t+1}

 Append $(h, Q^{(N)}(s_t, a_t))$ to M_{a_t} .

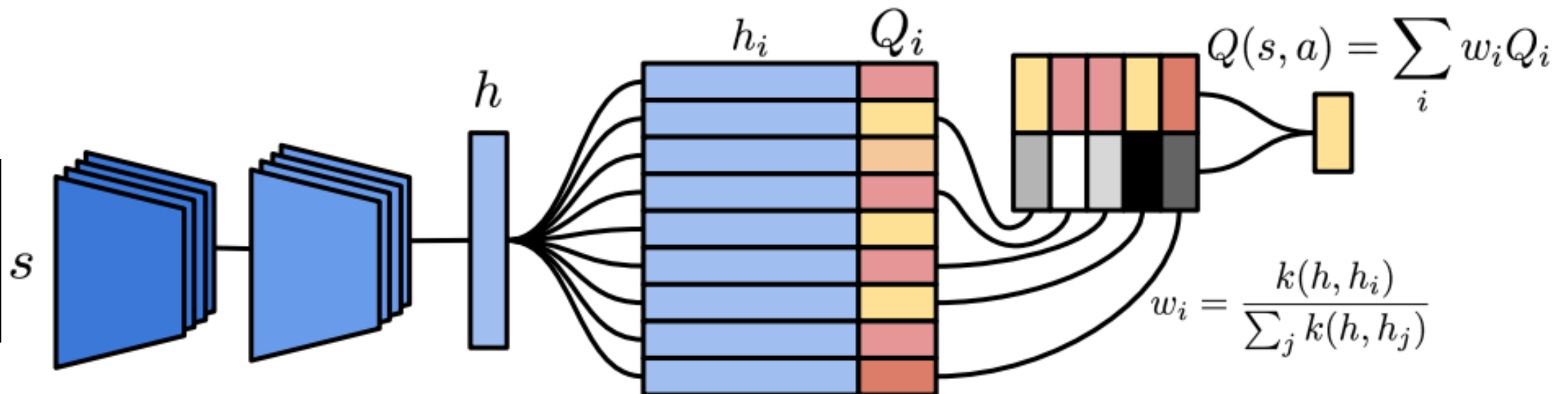
 Append $(s_t, a_t, Q^{(N)}(s_t, a_t))$ to \mathcal{D} .

 Train on a random minibatch from \mathcal{D} .

end for

end for

$$Q^{(N)}(s_t, a) = \sum_{j=0}^{N-1} \gamma^j r_{t+j} + \gamma^N \max_{a'} Q(s_{t+N}, a')$$



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Append $(h, Q^{(N)}(s_t, a_t))$ to M_{a_t} .

Append $(s_t, a_t, Q^{(N)}(s_t, a_t))$ to \mathcal{D} .

Train on a random minibatch from \mathcal{D} .

end for

end for

$$Q^{(N)}(s_t, a) = \sum_{j=0}^{N-1} \gamma^j r_{t+j} + \gamma^N \max_{a'} Q(s_{t+N}, a')$$

$$-\frac{1}{2} \nabla_{\mathbf{w}} J(\mathbf{w}) = (q_{\pi}(S, A) - \hat{q}(S, A, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S, A, \mathbf{w})$$

$$\Delta \mathbf{w} = \alpha (q_{\pi}(S, A) - \hat{q}(S, A, \mathbf{w})) \nabla_{\mathbf{w}} \hat{q}(S, A, \mathbf{w})$$

Deep Reinforcement Learning and Control

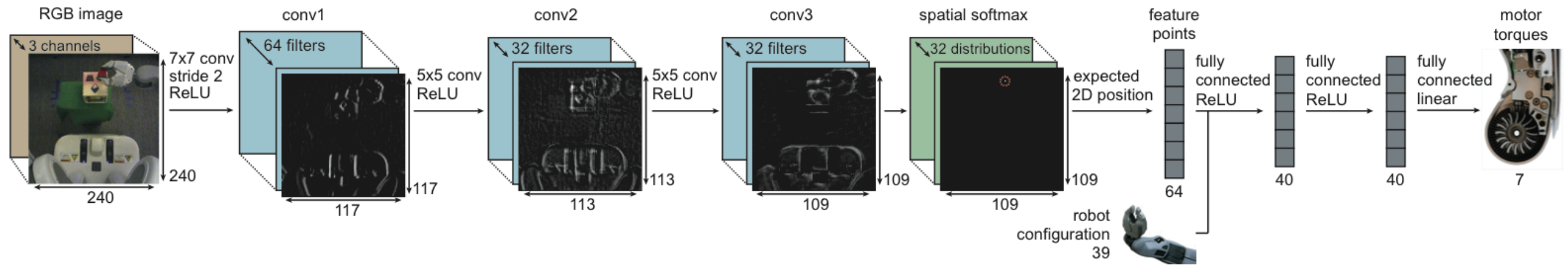
Neural Networks Architectures for RL

CMU 10703

Katerina Fragkiadaki

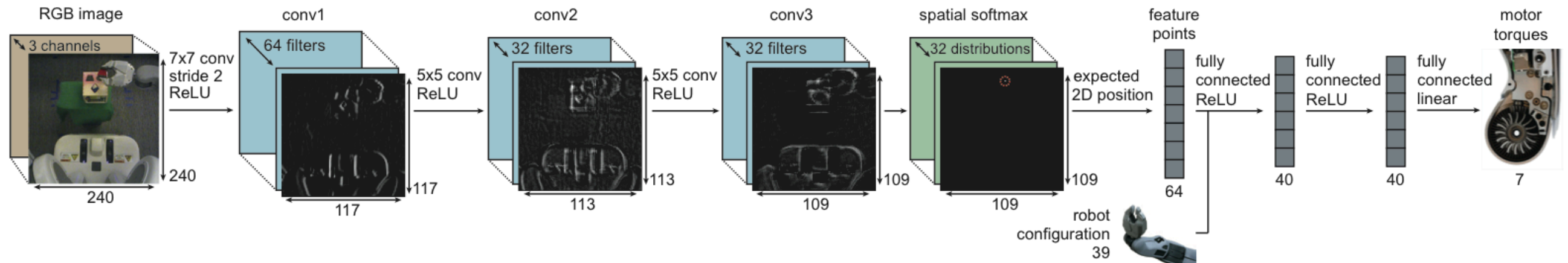


Spatial Softmax



End-to-end learning of visuomotor policies, Levine et al. 2015

Spatial Softmax

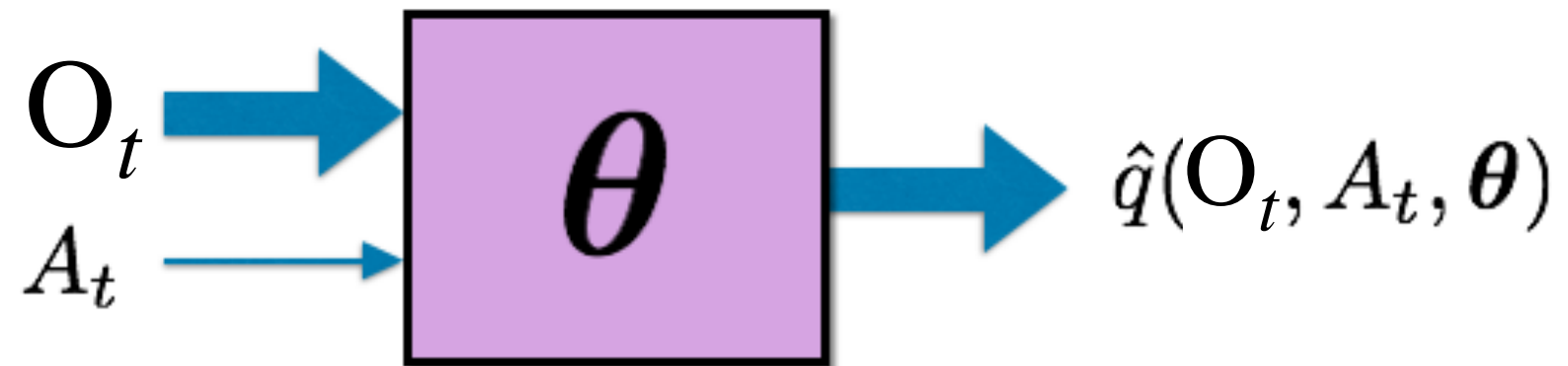
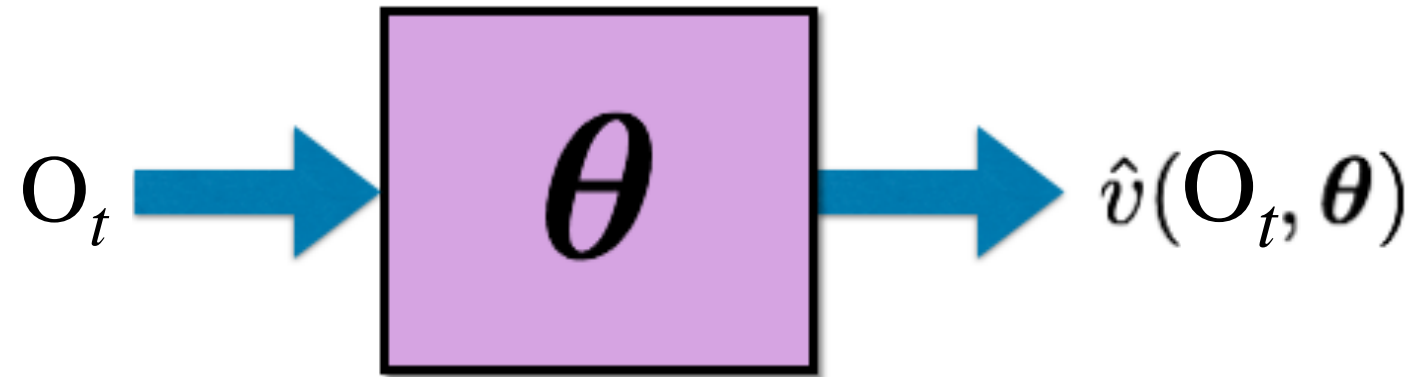


End-to-end learning of visuomotor policies, Levine et al. 2015

- For each feature map, “flatten” it and compute a softmax
- Then take X and Y grid coordinates and compute the corresponding weighted averages
- Imposes a very tight bottleneck and avoids overfitting

End-to-End RL

- **End-to-end RL methods** replace the hand-designed state representation with raw observations.



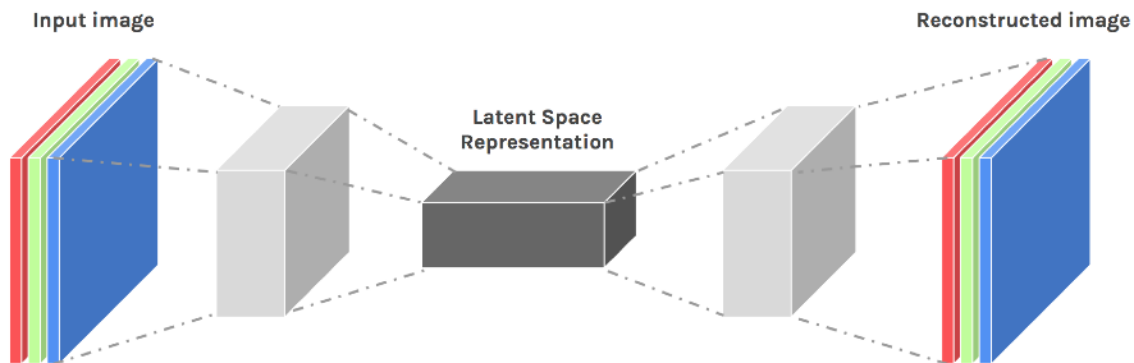
- We get rid of manual design of state representations :-)
- We need tons of data to train the network since O_t usually WAY more high dimensional than hand-designed S_t :-)
- We can pre-train or jointly train with additional losses (auxiliary tasks) :-) **For example?**

Unsupervised Losses / Pretraining

- We can always fine-tune from weights trained on a supervised visual task.
- We can use auxiliary tasks, e.g., autoencoders
- We can use prediction of gripper key points (we know where they are using forward kinematics and camera calibration)
- We can use inverse model learning

Autoencoders

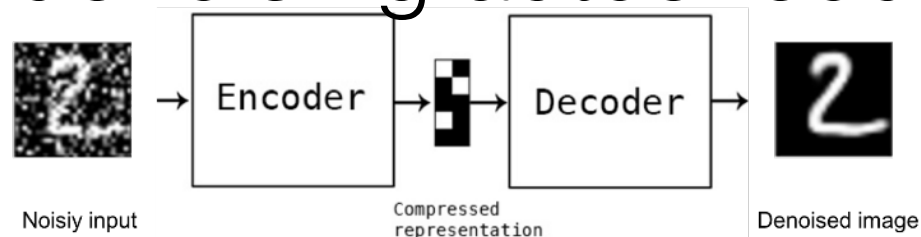
autoencoder



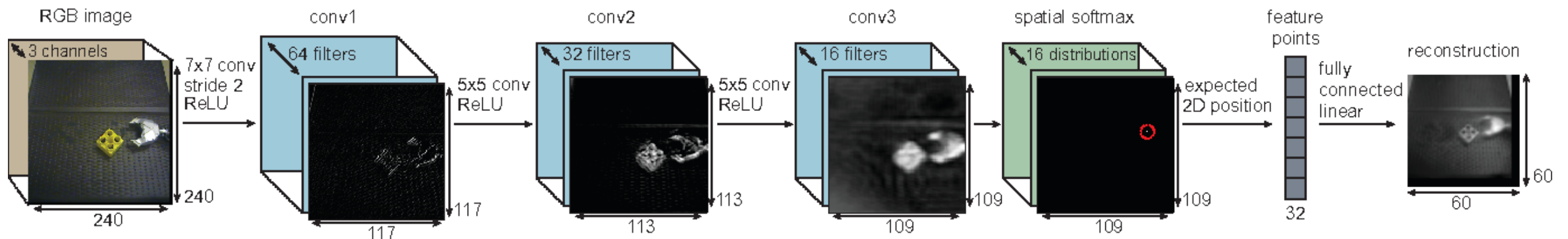
Autoencoders are trained to reconstruct the input (e.g., L2 pixel loss) after they pass through a tight bottleneck layer (the state representation)

What can go wrong?

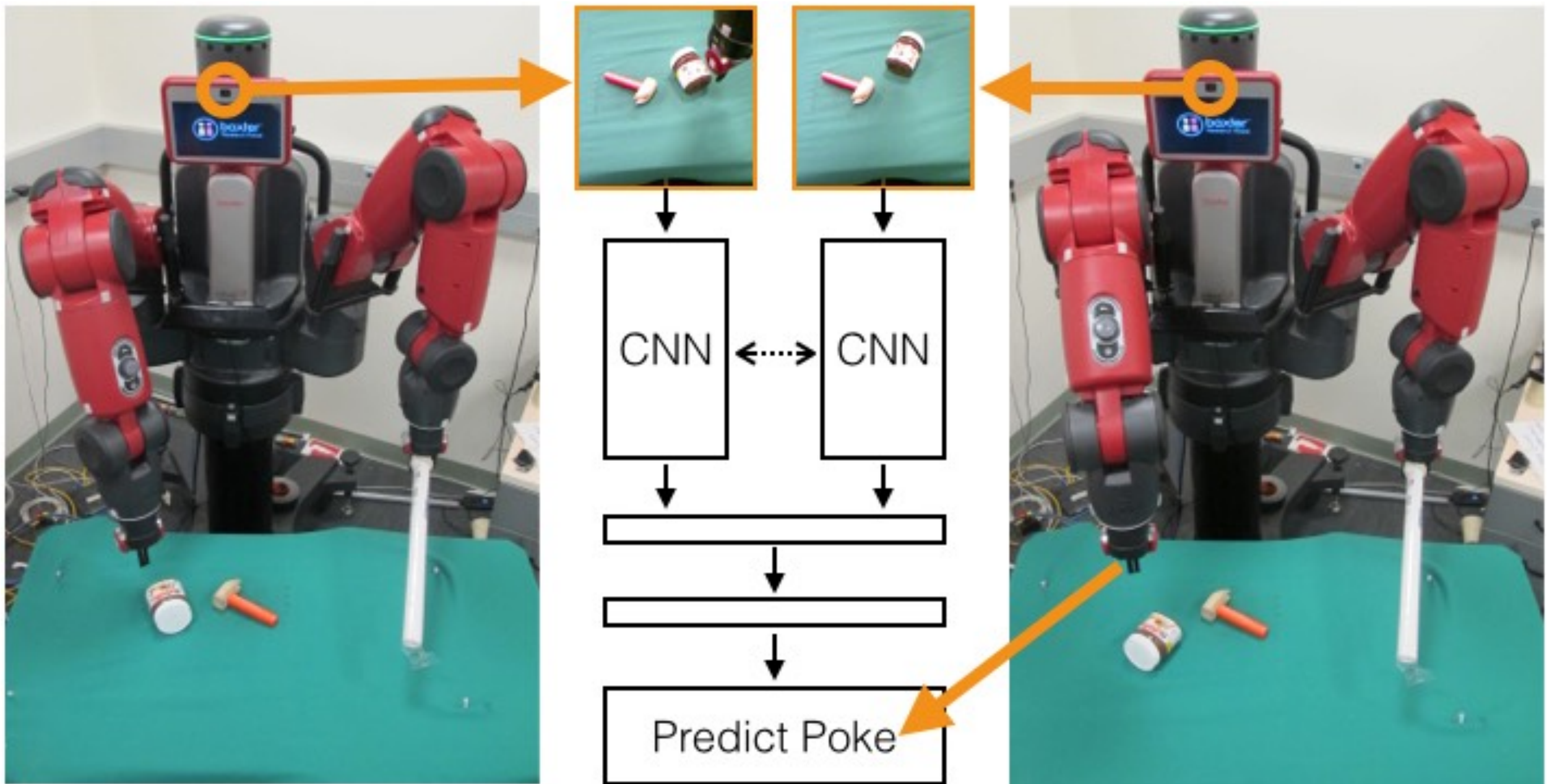
denoising autoencoder



what/where autoencoder



Train to predict the robotic action



Learning to poke by poking, Agrawal et al., 2015