



# The Wolf Within

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# Outline

WORK IN PROGRESS

## I. MSR in brief

- Data Access Specification
- Dolev-Yao intruder

## II. DAS → DY Intruder

## III. Protocol Spec. → DAS



# Part I

MSR




# MSR

- Follows the Dolev-Yao abstraction
- Based on
  - Multiset rewriting, linear logic
  - Type theory
- Used to prove
  - Undecidability of protocol verification
  - Completeness of Dolev-Yao intruder
- Specifications
  - So many protocols ... so little time ...
- Related to CIL, strands, spi-calculus





# What's in MSR 2.0 ?

- Multiset rewriting with existentials
- Dependent types w/ subsorting 
- Memory predicates 
- Constraints 

# Roles

Role state pred.  
var. declarations

- Generic roles

$$\left[ \begin{array}{c} \exists L: \tau'_1(x_1) \times \dots \times \tau'_n(x_n) \\ \dots \\ \forall x:\tau. \text{ lhs} \rightarrow \exists y:\tau'. \text{ rhs} \\ \dots \\ \forall x:\tau. \text{ lhs} \rightarrow \exists y:\tau'. \text{ rhs} \end{array} \right] \forall A$$

Role  
owner

- Anchored roles

$$\left[ \begin{array}{c} \exists L: \tau'_1(x_1) \times \dots \times \tau'_n(x_n) \\ \dots \\ \forall x:\tau. \text{ lhs} \rightarrow \exists y:\tau'. \text{ rhs} \\ \dots \\ \forall x:\tau. \text{ lhs} \rightarrow \exists y:\tau'. \text{ rhs} \end{array} \right] A$$

# Rules

$\forall x_1: \tau_1.$

...

$\forall x_n: \tau_n.$

lhs

→

$\exists y_1: \tau'_1.$

...

$\exists y_{n'}: \tau'_{n'}.$

rhs

- $N(t)$  Network
- $L(t, \dots, t)$  Local state
- $M_A(t, \dots, t)$  Memory
- $\chi$  Constraints

- $N(t)$  Network
- $L(t, \dots, t)$  Local state
- $M_A(t, \dots, t)$  Memory

# NS Initiator

$A \rightarrow B: \{n_A, A\}_{k_B}$   
 $B \rightarrow A: \{n_A, n_B\}_{k_A}$   
 $A \rightarrow B: \{n_B\}_{k_B}$

$$\left( \begin{array}{l}
 \exists \textcolor{red}{L}: \text{princ} \times \text{princ}^{(B)} \times \text{pubK } B \times \text{nonce.} \\
 \\
 \forall B: \text{princ} \\
 \forall k_B: \text{pubK } B \quad \bullet \quad \rightarrow \quad \exists \textcolor{red}{n}_A: \text{nonce.} \quad \begin{array}{l} \textcolor{green}{L}(A, B, k_B, n_A) \\ N(\{n_A, A\}_{k_B}) \end{array} \\
 \\
 \forall \dots \\
 \forall k_A: \text{pubK } A \\
 \forall k'_A: \text{privK } k_A \\
 \forall n_A, n_B: \text{nonce} \quad \begin{array}{l} \textcolor{green}{L}(A, B, k_B, n_A) \\ N(\{n_A, n_B\}_{k_A}) \end{array} \rightarrow N(\{n_B\}_{k_B})
 \end{array} \right)^{\forall A}$$





# NS Responder

$A \rightarrow B: \{n_A, A\}_{k_B}$   
 $B \rightarrow A: \{n_A, n_B\}_{k_A}$   
 $A \rightarrow B: \{n_B\}_{k_B}$

$$\left( \begin{array}{l}
 \exists \mathcal{L}: \text{princ}^{(B)} \times \text{pubK } B^{(k_B)} \times \text{privK } k_B \times \text{nonce.} \\
 \\
 \forall k_B: \text{pubK } B \\
 \forall k'_B: \text{privK } k_B \\
 \forall A: \text{princ} \\
 \forall n_A: \text{nonce} \\
 \forall k_A: \text{pubK } A \\
 \\
 \forall \dots \\
 \forall n_B: \text{nonce}
 \end{array} \right) \forall B$$

$$\begin{array}{l}
 N(\{n_A, A\}_{k_B}) \rightarrow \exists n_B: \text{nonce.} \\
 \mathcal{L}(B, k_B, k'_B, n_B) \\
 N(\{n_A, n_B\}_{k_A}) \\
 \\
 \mathcal{L}(B, k_B, k'_B, n_B) \\
 N(\{n_B\}_{k_B}) \rightarrow \bullet
 \end{array}$$

# Type Checking

New

$\Sigma \vdash P$

$t$  has type  
 $\tau$  in  $\Gamma$

$\Gamma \vdash t : \tau$

$P$  is well-  
typed in  $\Sigma$

- Catches:

- Encryption with a nonce
- Transmission of a long term key
- Circular key hierarchies, ...



# Data Access Specification

New

$r$  is DAS-valid  
for  $A$  in  $\Gamma$

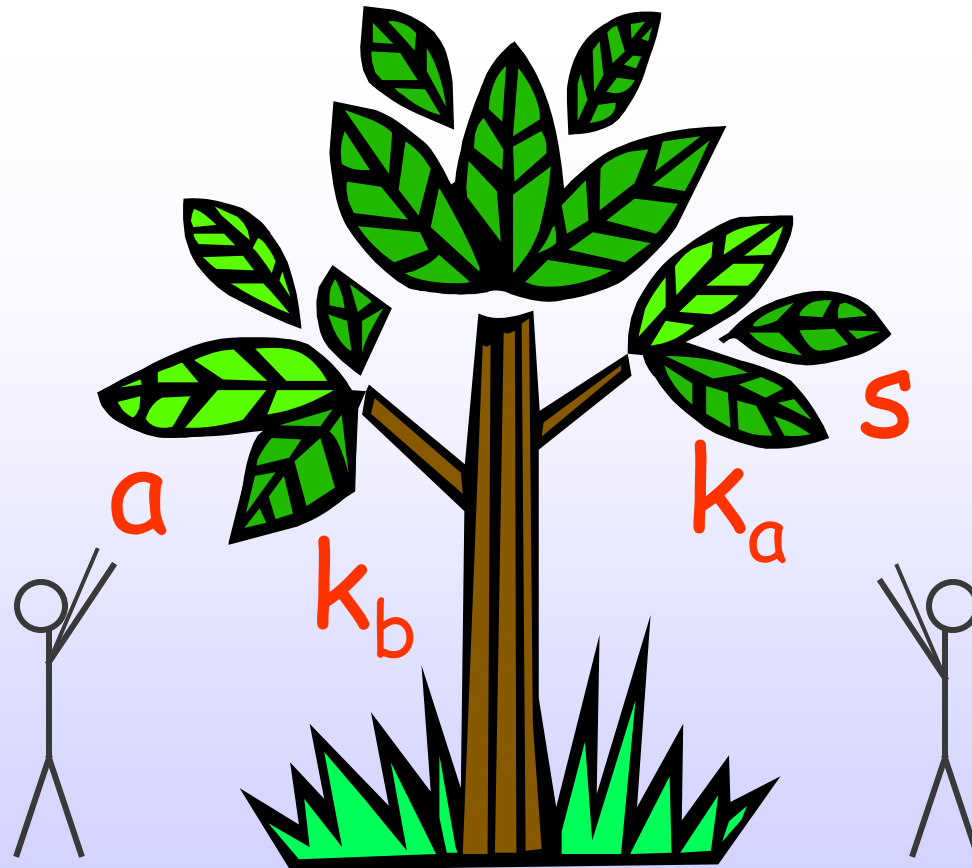
$\Sigma \Vdash P$

$\Gamma \Vdash_A r$

$P$  is DAS-  
valid in  $\Sigma$

- Catches
  - $A$  signing/encrypting with  $B$ 's key
  - $A$  accessing  $B$ 's private data, ...
- Static
- Decidable
- Gives meaning to Dolev-Yao intruder

... pictorially

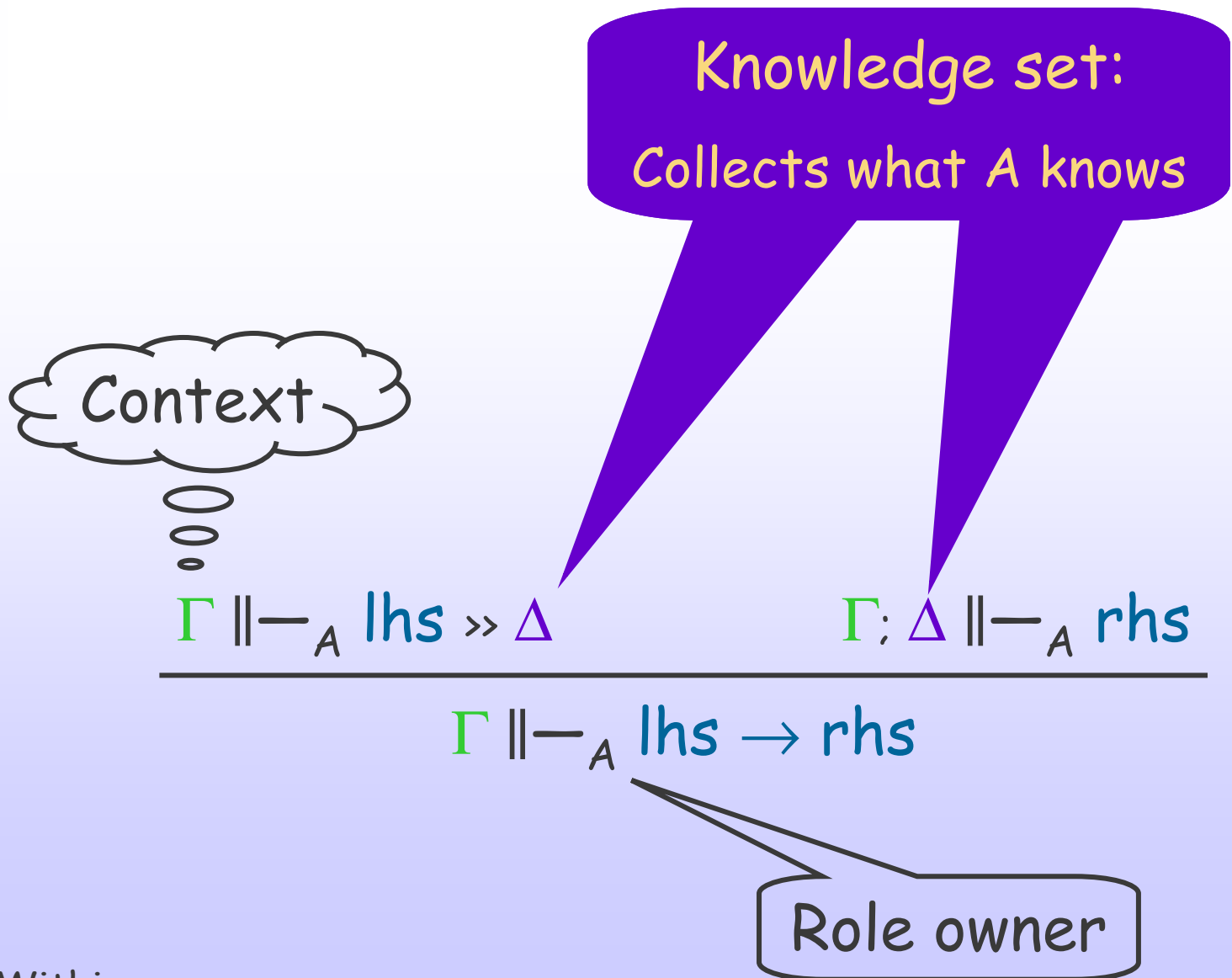




# An Overview of DAS

- Interpret incoming information
    - Collect received data
    - Access unknown data
  - Construct outgoing information
    - Generate data
    - Use known data
    - Access new data
- ... all along, verify access to data

# Verifying a Rule



# Processing Predicates on the LHS

- Network messages

$$\frac{\Gamma; \Delta \parallel -_A t \gg \Delta'}{\Gamma; \Delta \parallel -_A N(t) \gg \Delta'}$$

- Memory predicates

$$\frac{\Gamma; \Delta \parallel -_A t_1, \dots, t_n \gg \Delta'}{\Gamma; \Delta \parallel -_A M_A(t_1, \dots, t_n) \gg \Delta'}$$



# Interpreting Data on the LHS

- Pairs

$$\frac{\Gamma; \Delta \parallel -_A t_1, t_2 \gg \Delta'}{\Gamma; \Delta \parallel -_A (t_1, t_2) \gg \Delta'}$$

- Encrypted terms

$$\frac{\Gamma; \Delta \parallel -_A k \gg \Delta' \quad \Gamma; \Delta' \parallel -_A t \gg \Delta''}{\Gamma; \Delta \parallel -_A \{t\}_k \gg \Delta''}$$

- Elementary terms

$$\left\{ \begin{array}{l} \frac{}{\Gamma; (\Delta, x) \parallel -_A x \gg (\Delta, x)} \\ \frac{}{(\Gamma, x:\tau); \Delta \parallel -_A x \gg (\Delta, x)} \end{array} \right.$$





# Accessing Data on the LHS

- Shared keys

$$\left\{ \begin{array}{l} \hline \Gamma; (\Delta, k) \Vdash_A k \gg (\Delta, k) \\ \hline (\Gamma, x: \text{shK } A \ B); \Delta \Vdash_A x \gg (\Delta, x) \end{array} \right.$$

- Public keys

$$\left\{ \begin{array}{l} \hline (\Gamma, k: \text{pubK } A, k': \text{privK } k); (\Delta, k') \Vdash_A k \gg (\Delta, k') \\ \hline (\Gamma, k: \text{pubK } A, k': \text{privK } k); \Delta \Vdash_A k \gg (\Delta, k') \end{array} \right.$$



# Generating Data on the RHS

- Nonces

$$\frac{(\Gamma, x:\text{nonce}); (\Delta, x) \Vdash_A \text{rhs}}{\Gamma; \Delta \Vdash_A \exists x:\text{nonce}. \text{rhs}}$$

# Constructing Terms on the RHS

- Pairs

$$\frac{\Gamma; \Delta \Vdash_A t_1 \quad \Gamma; \Delta \Vdash_A t_2}{\Gamma; \Delta \Vdash_A (t_1, t_2)}$$

- Shared-key encryptions

$$\frac{\Gamma; \Delta \Vdash_A t \quad \Gamma; \Delta \Vdash_A k}{\Gamma; \Delta \Vdash_A \{t\}_k}$$



# Accessing Data on the RHS

- Principal

$$\frac{}{\Gamma, B:\text{princ} \parallel -_A B}$$

- Shared key

$$\frac{}{\Gamma, B:\text{princ}, k:\text{shK } A \ B \parallel -_A k}$$

- Public key

$$\frac{}{\Gamma, B:\text{princ}, k:\text{pubK } B \parallel -_A k}$$

- Private key

$$\frac{}{\Gamma, k:\text{pubK } A, k':\text{privK } k \parallel -_A k'}$$





## Part II

Data Access Specification



Dolev-Yao Intruder

# The Dolev-Yao Intruder Model

- Interpret incoming information
  - Collect received data
  - Access unknown data
- Construct outgoing information
  - Generate data
  - Use known data
  - Access new data
- Same operations as DAS!

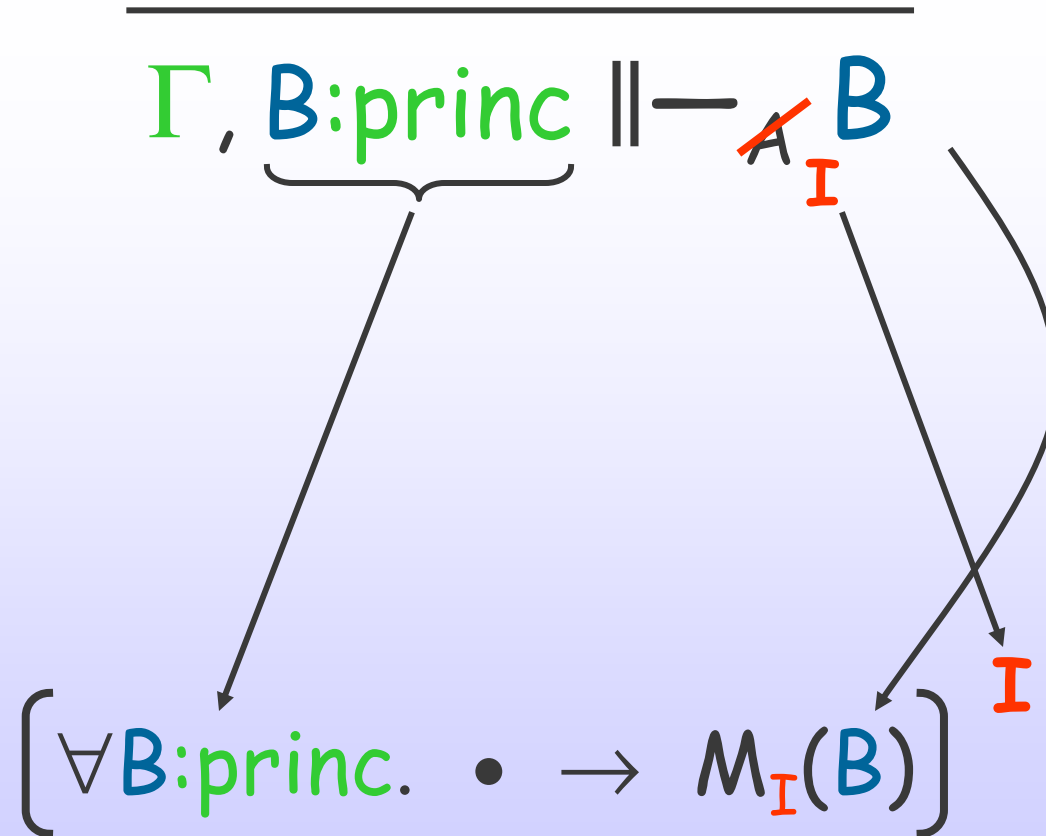




# DAS $\Rightarrow$ DY

- Interpret messages on LHS
- Access data (keys) on LHS
- Generate data on RHS
- Construct messages on RHS
- Access data on RHS

# Accessing Principal Names





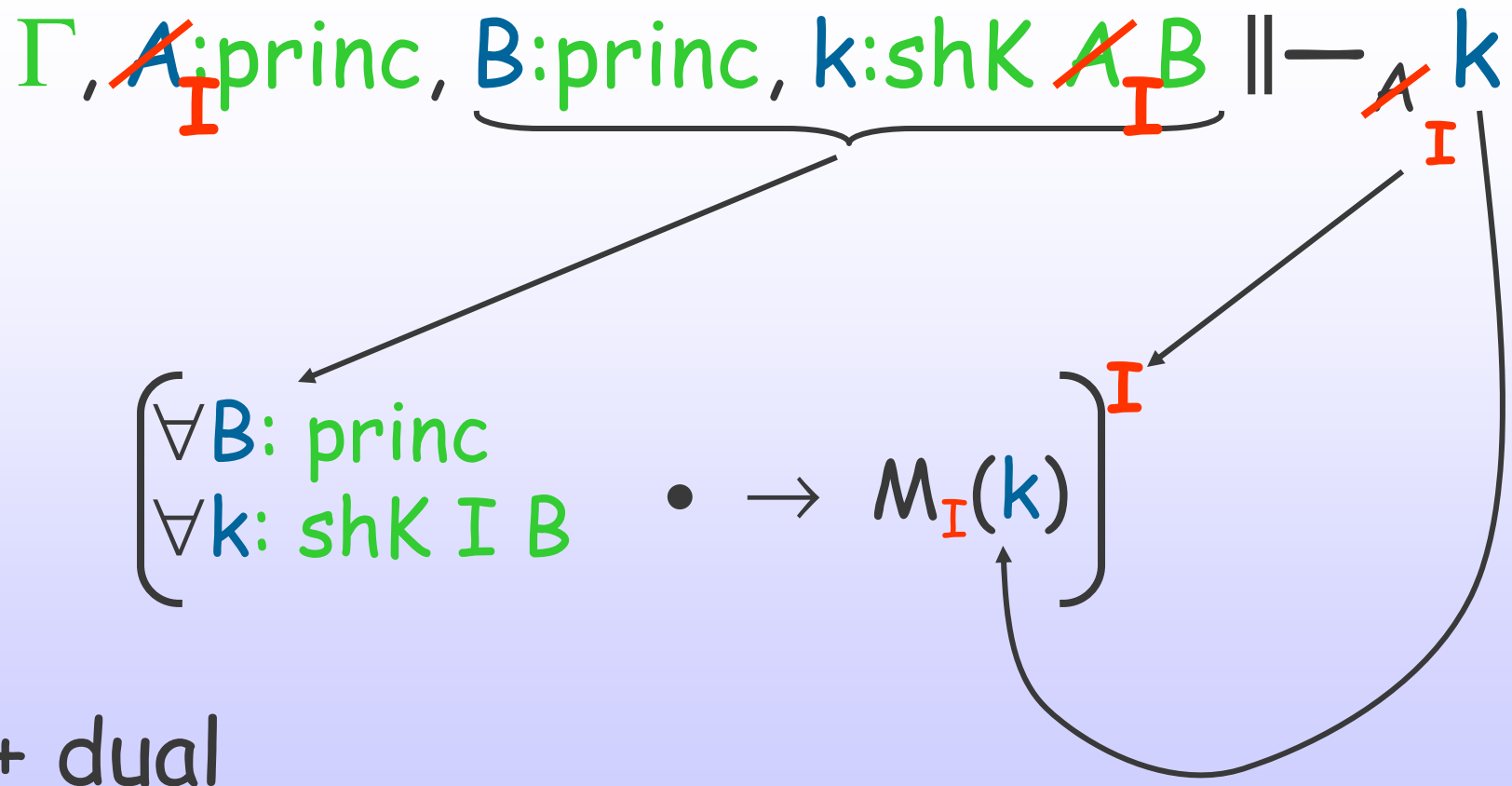
# What did we do?

RHS data access:

- Instantiate acting principal to **I**
- Accessed data → Intruder knowledge
- Meta-variables → Rule variables
- Context provides types



# Checking it out: Shared Keys



# Getting Confident: Pub./Priv. Keys

---


$$\Gamma, \underbrace{B:\text{princ}, k:\text{pubK } B}_{\text{I}} \parallel -_{\cancel{A} \text{I}} k$$

$$\left[ \begin{array}{l} \forall B: \text{princ} \\ \forall k: \text{pubK } B \end{array} \bullet \rightarrow M_{\text{I}}(k) \right]_{\text{I}}$$

---


$$\Gamma, \underbrace{\cancel{A}:\text{princ}, \cancel{k}:\text{pubK } \cancel{A}, k':\text{privK } k}_{\text{I}} \parallel -_{\cancel{A} \text{I}} k'$$

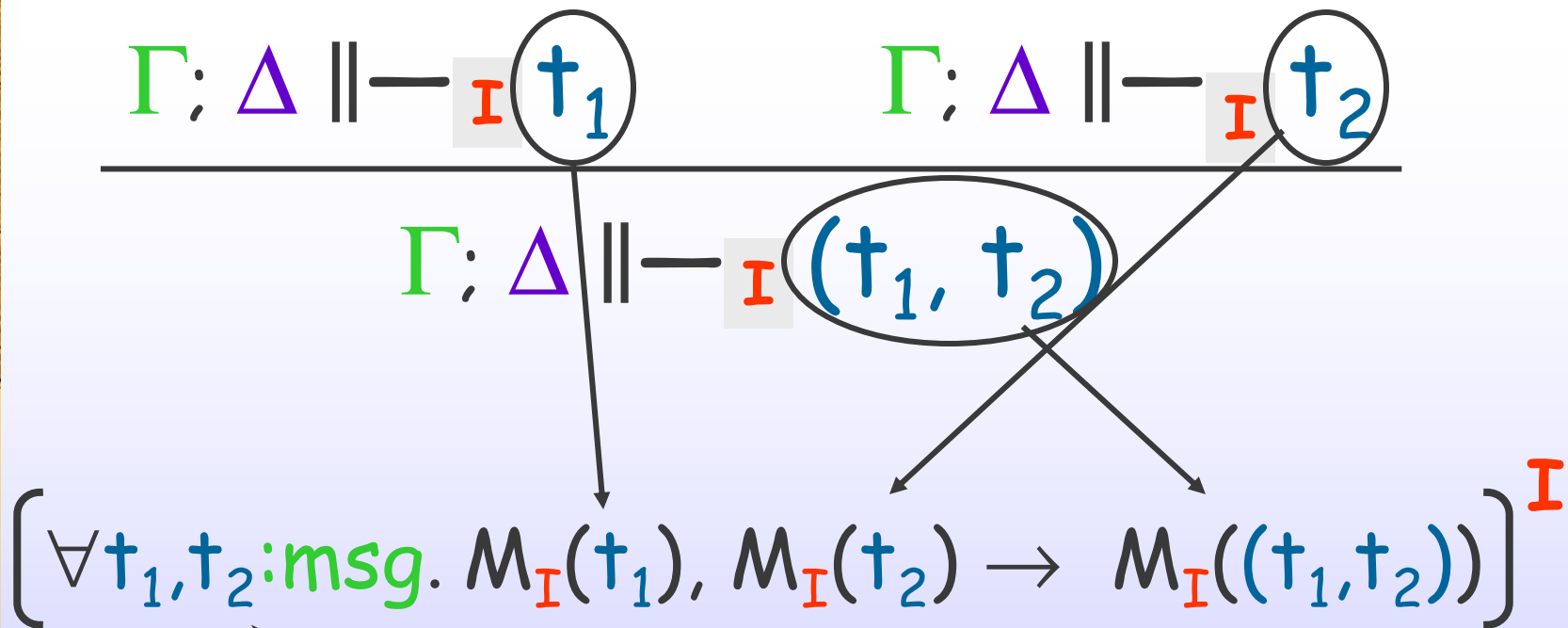
$$\left[ \begin{array}{l} \forall k: \text{pubK } \text{I} \\ \forall k': \text{privK } k \end{array} \bullet \rightarrow M_{\text{I}}(k') \right]_{\text{I}}$$



# DAS $\Rightarrow$ DY

- Interpret messages on LHS
- Access data (keys) on LHS
- Generate data on RHS
- Construct messages on RHS
- Access data on RHS

# Constructing Messages: Pairs



$$\frac{\Gamma \vdash t_1 : \textcolor{brown}{msg} \quad \Gamma \vdash t_2 : \textcolor{brown}{msg}}{\Gamma \vdash (t_1, t_2) : \textcolor{brown}{msg}}$$


# Now, what did we do?

## RHS message construction:

- Instantiate acting principal to  $I$
- Meta-variables  $\rightarrow$  Rule variables
- Premises  $\rightarrow$  antecedent
- Conclusion  $\rightarrow$  consequent
- Types from auxiliary typing derivation



# Carrying on: Shared-Key Encrypt.


$$\frac{\Gamma; \Delta \parallel -_{\mathbf{I}} t \qquad \Gamma; \Delta \parallel -_{\mathbf{I}} k}{\Gamma; \Delta \parallel -_{\mathbf{I}} \{t\}_k}$$

$$\left[ \begin{array}{l} \forall A, B: \text{princ} \\ \forall k: \text{shK } A \ B \ M_{\mathbf{I}}(t), M_{\mathbf{I}}(k) \rightarrow M_{\mathbf{I}}(\{t\}_k) \\ \forall t: \text{msg} \end{array} \right]_{\mathbf{I}}$$

Similar for public-key encryption



# DAS $\Rightarrow$ DY

- Interpret messages on LHS
- Access data (keys) on LHS
- **Generate data on RHS**
- **Construct messages on RHS**
- **Access data on RHS**



# Generating Nonces



$$\frac{(\Gamma, x:\text{nonce}); (\Delta, \textcircled{x}) \Vdash_{\mathbf{I}} \text{rhs}}{\Gamma; \Delta \Vdash_{\mathbf{I}} \underbrace{\exists x:\text{nonce}. \text{rhs}}}$$

Diagram illustrating the generation of nonces. The top line shows a typing context  $(\Gamma, x:\text{nonce})$  and a derivation  $(\Delta, \textcircled{x}) \Vdash_{\mathbf{I}} \text{rhs}$ , where  $x$  is circled in red. A horizontal line separates this from the bottom line, which shows the result  $\Gamma; \Delta \Vdash_{\mathbf{I}} \exists x:\text{nonce}. \text{rhs}$ . A bracket under the existential quantifier in the bottom line has two arrows pointing to the expression  $\left[ \bullet \rightarrow \exists x:\text{nonce}. M_{\mathbf{I}}(x) \right]^{\mathbf{I}}$ . A black arrow points from the bracket to the  $\exists$  quantifier, and a red arrow points from the circled  $x$  in the top line to the  $x$  in  $M_{\mathbf{I}}(x)$ .

Similarly for other generated data

# Now, what did we do?

## Data generation on the RHS:

- Instantiate acting principal to **I**
- Auxiliary typing derivation gives types
- Remember generated object
- Follow knowledge acquisition flow






# DAS $\Rightarrow$ DY

- Interpret messages on LHS
- Access data (keys) on LHS
- Generate data on RHS
- Construct messages on RHS
- Access data on RHS

# Accessing Shared Keys on the LHS



$$(\Gamma, k:shK \text{ I } B); \Delta \parallel - \text{ I } k \gg (\Delta, k)$$

$$\left( \begin{array}{l} \forall B: \text{ princ} \\ \forall k: shK \text{ I } B \end{array} \bullet \rightarrow M_{\text{ I }}(k) \right)^{\text{ I }}$$

Similarly for other keys

# Now, what did we do?

## LHS data access:

- Instantiate acting principal to  $I$
- Meta-variables  $\rightarrow$  Rule variables
- Types from auxiliary typing derivation
- Follow knowledge acquisition flow
- Remember generated object

Same target rules as for RHS data access

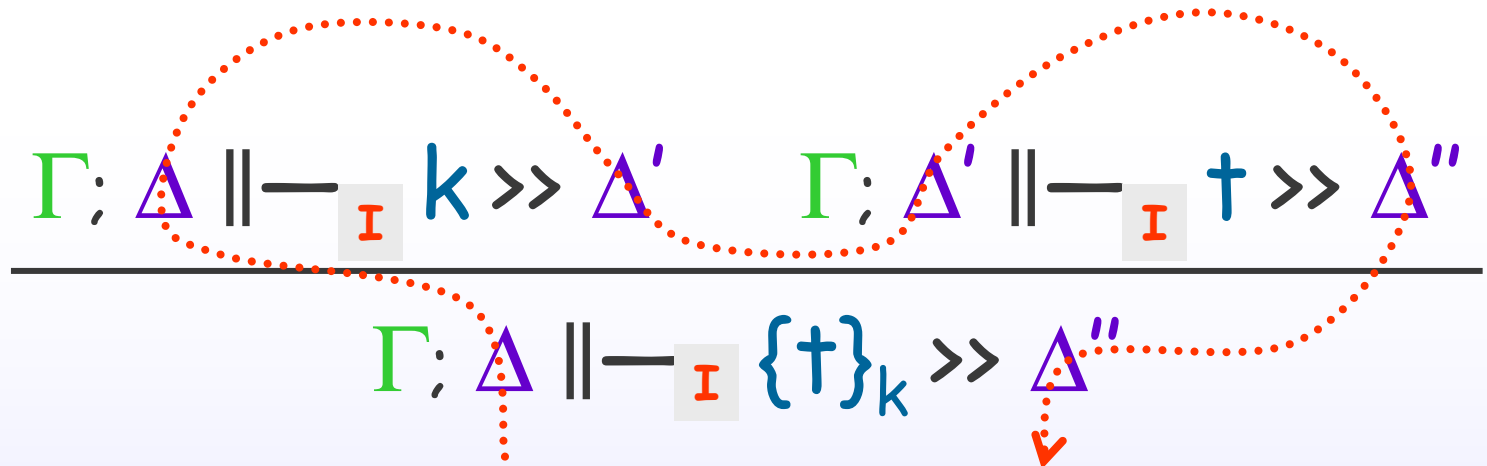




# DAS $\Rightarrow$ DY

- Interpret messages on LHS
- Access data (keys) on LHS
- Generate data on RHS
- Construct messages on RHS
- Access data on RHS

# Interpreting Shared-Key Encrypt.



$$\left[ \begin{array}{l} \forall A, B: \text{princ} \\ \forall k: \text{shK } A \ B \quad M_{\mathbf{I}}(\{t\}_k), M_{\mathbf{I}}(k) \rightarrow M_{\mathbf{I}}(t) \\ \forall t: \text{msg} \end{array} \right]^{\mathbf{I}}$$

Similar for public-key encryption and pairing

# Now, what did we do?

## LHS message interpretation

- Instantiate acting principal to  $I$
- Meta-variables  $\rightarrow$  Rule variables
- Types from auxiliary typing derivation
- Follow knowledge acquisition flow
- Conclusion  $\rightarrow$  antecedant
- "Last" premises  $\rightarrow$  consequent





# Network Rules

$$\frac{\Gamma; \Delta \parallel -_A \textcolor{teal}{t} \gg \Delta'}{\Gamma; \Delta \parallel -_A \textcolor{teal}{N(t)} \gg \Delta'}$$

LHS

$$\left[ \forall \textcolor{teal}{t}:\textcolor{teal}{msg}. \textcolor{teal}{N(t)} \rightarrow M_{\textcolor{red}{I}}(\textcolor{teal}{t}) \right]^{\textcolor{red}{I}}$$

RHS

$$\frac{\Gamma; \Delta \parallel -_A \textcolor{teal}{t}}{\Gamma; \Delta \parallel -_A \textcolor{teal}{N(t)}}$$

$$\left[ \forall \textcolor{teal}{t}:\textcolor{teal}{msg}. M_{\textcolor{red}{I}}(\textcolor{teal}{t}) \rightarrow \textcolor{teal}{N(t)} \right]^{\textcolor{red}{I}}$$

## ... Other Rules?

Either

- redundant, or

$$\left[ \forall t:msg. N(t) \rightarrow N(t) \right]^I$$

- or, innocuous (but sensible)

$$\left[ \forall t_1, \dots, t_n :msg. M'_I(t_1, \dots, t_n) \rightarrow M_I(t_1), \dots, M_I(t_n) \right]^I$$





## Part III

Protocol Spec.



Data Access Spec. Rules

# Automating DAS Rule Design?

- One size does not fit all
- Look at protocol
  - Typed MSR spec.
  - Usage of constructs
- Involve construct declarations
  - Not sufficient
  - Use annotations



# Generating DAS rules from use

## Constructors atoms

- Interpret message components on LHS
- Access data (keys) on LHS
- Generate data on RHS
- Construct messages on RHS
- Access data on RHS



# Accessing data

- Annotate the type of freely accessible data

anybody can access

`princ: +type`

- Make it conditional for dep. types

`pubK: *princ -> +type`

doesn't  
matter

`privK:  $\Pi A$ : +princ. +pubK A -> +type`

owner

# Generating data

- Again, annotate types

can be generate


nonce: !type

shK: +princ -> +princ -> !type

shK: +princ -> +princ -> !type

# Pattern-matching constructors

- Mark *arguments* as input or output



output

input

```
_,_ : -msg -> -msg -> msg
```

```
{_}_ : -msg -> ΠA:+princ. ΠB:+princ.+shK A B -> msg
```

```
{{_}}_ : -msg -> ΠA:+princ. Πk:+pubK A.+privK k -> msg
```

```
hash: +msg -> msg
```

```
[_]_ : +msg -> ΠA:*princ. Πk:*sigK A.*verK k -> msg
```

+ or -



# Annotating Declarations

- Integrates semantics of types and constructors
- "Trimmed down" version of DAS
- Allows constructing DAS rules
  - ... and Dolev-Yao intruder





... alternatively

Compute DAS rules from protocol

- There are finitely many annotations
- Check protocol against each of them
- Keep the most restrictive ones that validate the protocol

Exponential!

More efficient algorithms?

# Further Questions ...

- Relationship to “intruder-less” languages
  - E.g. Spi-calculus

