10-301/601: Introduction to Machine Learning Lecture 22 – Attention & Transformers

RNN Language Models: Pros & Cons

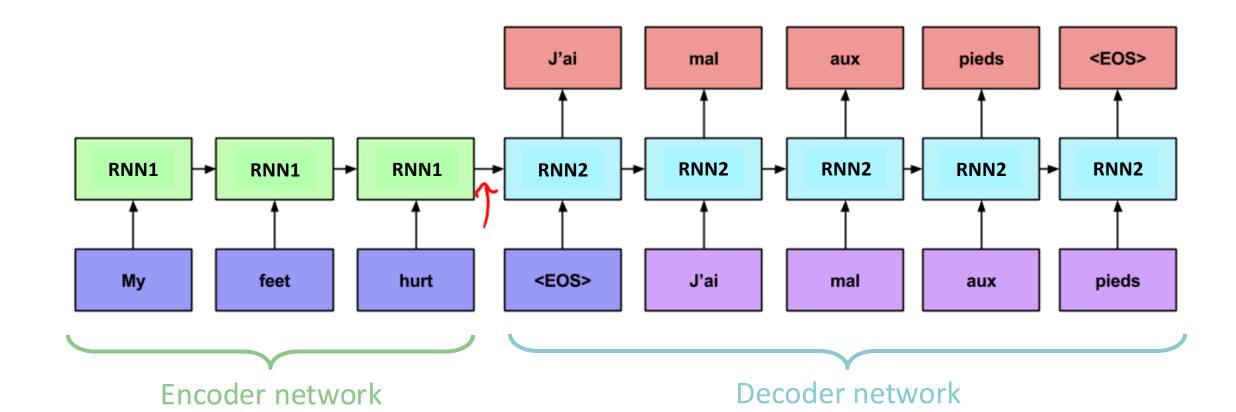
• Pros:

- Can handle arbitrary sequence lengths without having to increase model size (i.e., # of learnable parameters)
- Trainable via backpropagation
- Cons
 - Vanishing/exploding gradients
 - Does not consider information from later timesteps
 - Can be addressed by bidirectional RNNs
 - Computation is inherently sequential
 - "You can't cram the meaning of a whole %&!\$#
 sentence into a single \$&!#* vector!" Ray Mooney,
 UT Austin

RNN Language Models: Pros & Cons

• Pros:

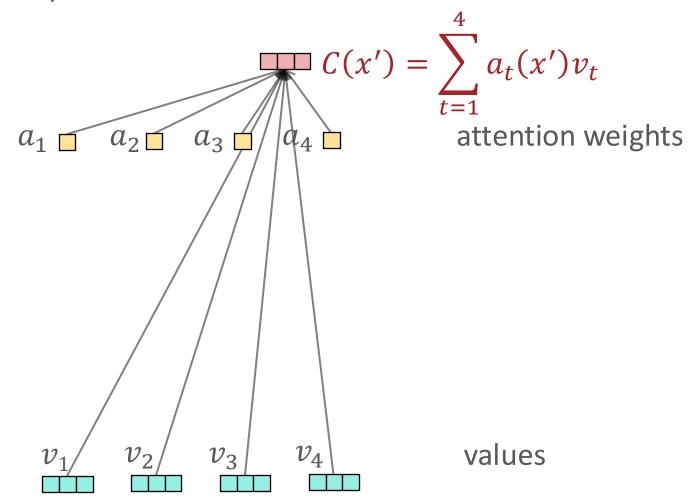
- Can handle arbitrary sequence lengths without having to increase model size (i.e., # of learnable parameters)
- Trainable via backpropagation
- Cons
 - Vanishing/exploding gradients
 - Does not consider information from later timesteps
 - Can be addressed by bidirectional RNNs
 - Computation is inherently sequential
 - The entire sequence up to some timestep is represented using just one vector



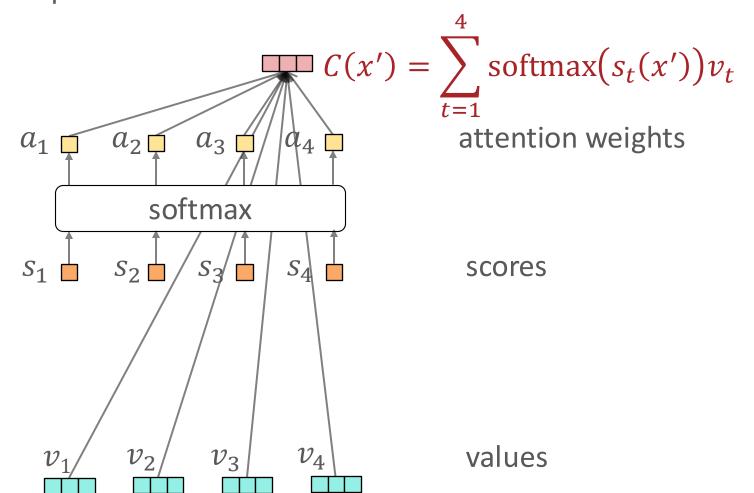
Encoder-Decoder Architectures (Sutskever et al., 2014)

- Approach: compute a representation of the input sequence for each token x' in the decoder
- Idea: allow the decoder to learn which tokens in the input to "pay attention to" i.e., put more weight on

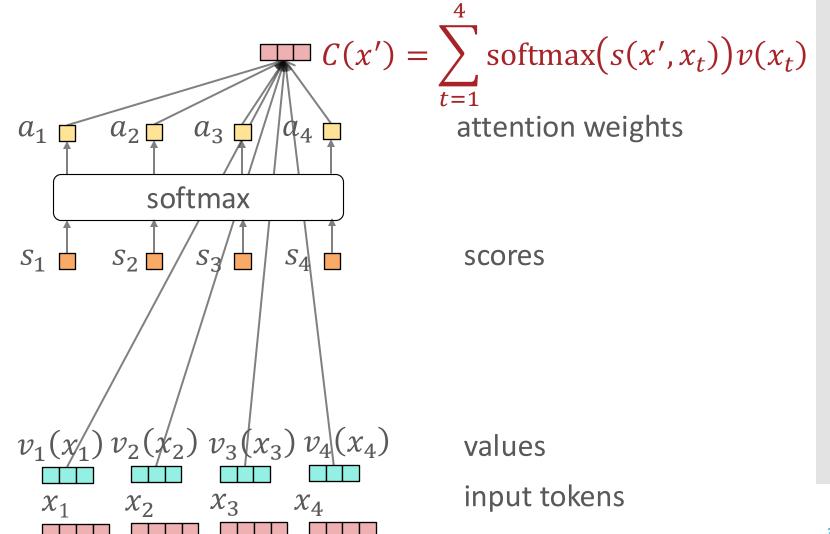
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• Approach: compute a representation of the input sequence for each token x' in the decoder

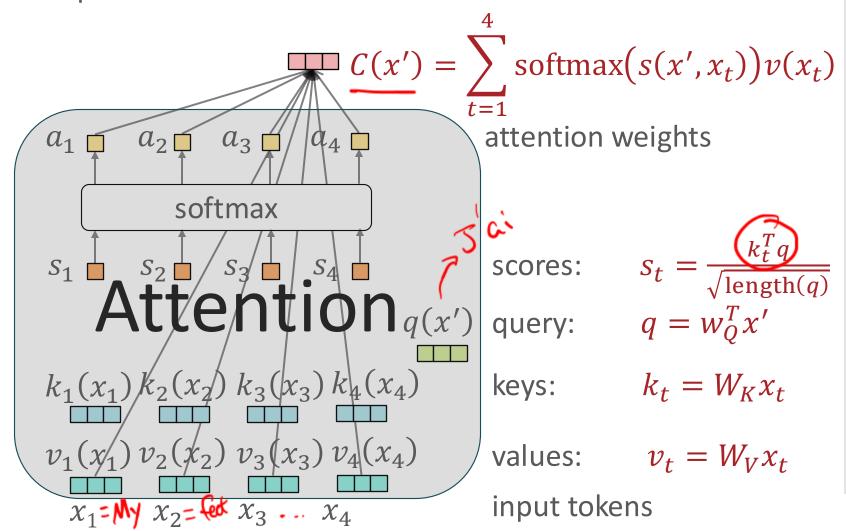


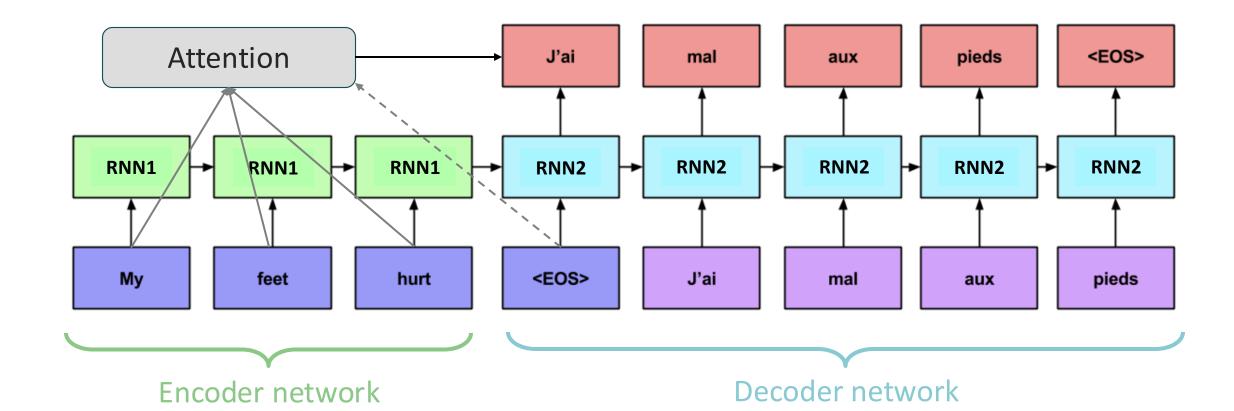
• Approach: compute a representation of the input sequence for each token x' in the decoder



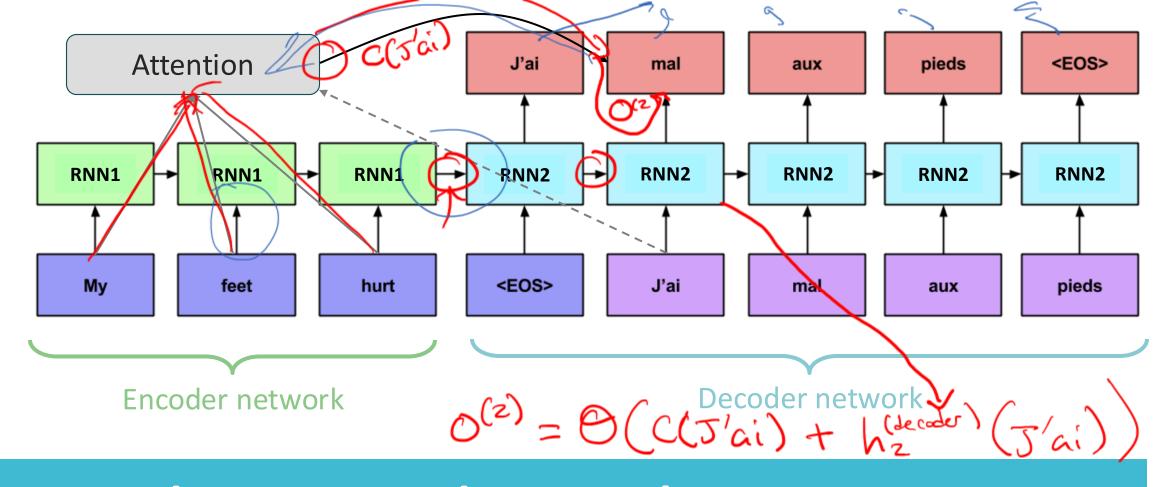
Scaled Dot-product Attention

• Approach: compute a representation of the input sequence for each token x' in the decoder

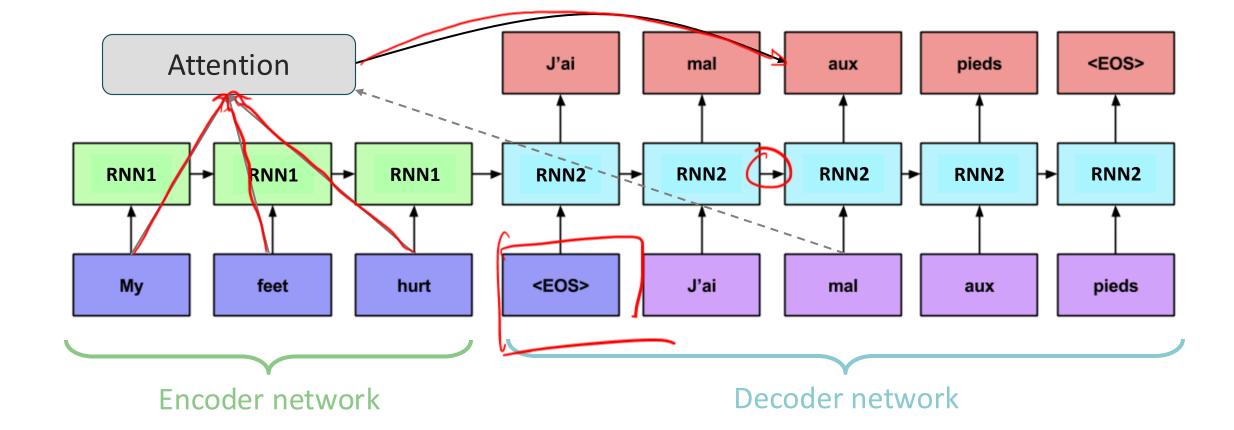




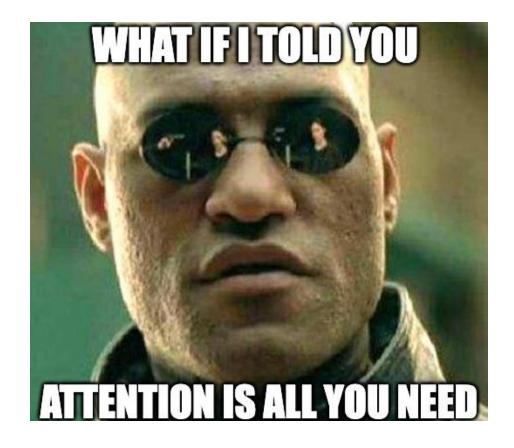
Encoder-Decoder Architectures with Attention



Encoder-Decoder Architectures with Attention



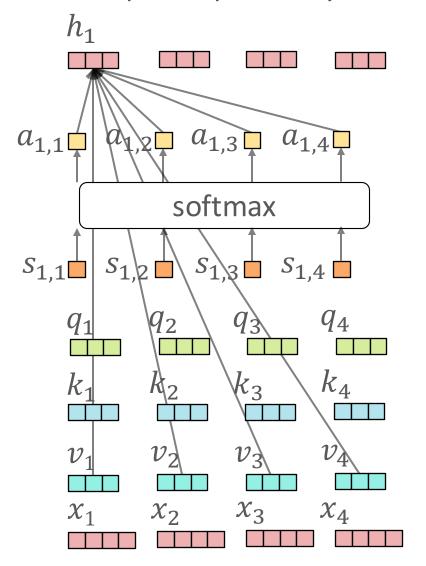
Encoder-Decoder Architectures with Attention



Encoder-Decoder Architectures with Attention (Vaswani et al., 2017)

Scaled Dot-product Self-attention

 Approach: compute a representation for each token in the *input sequence* by attending to all the input tokens



$$h_1 = \sum_{j=1}^{4} \operatorname{softmax}(s_{1,j}) v_j$$

attention weights

scores:
$$S_{1,j} = \frac{k_j^T q_1}{\sqrt{\operatorname{length}(k_j)}}$$

queries: $q_t = W_Q x_t$

keys: $k_t = W_K x_t$

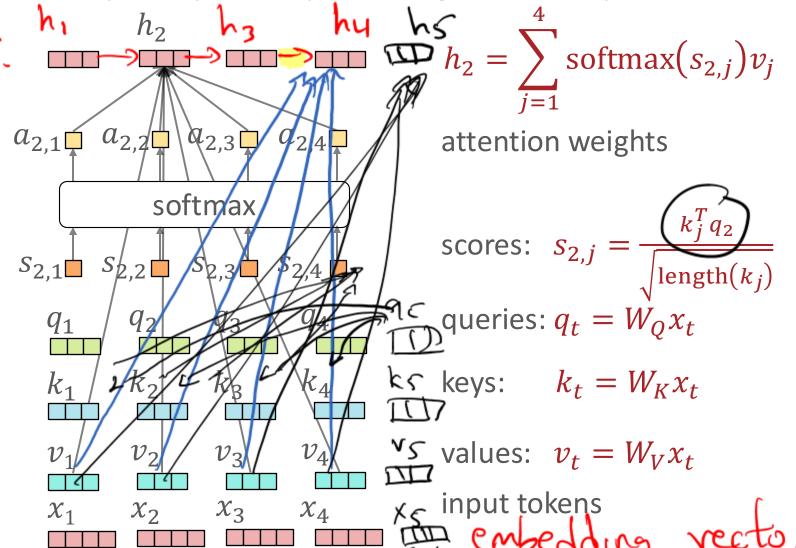
values: $v_t = W_V x_t$

input tokens

 Approach: compute a representation for each token in the *input sequence* by attending to all the input tokens

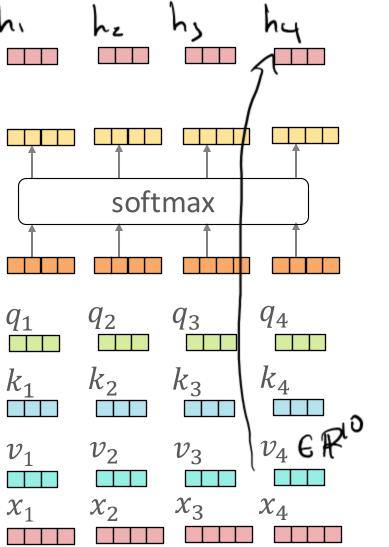
computes.

Scaled
Dot-product
Self-attention



Scaled Dot-product Self-attention: Matrix Form

 Approach: compute a representation for each token in the *input sequence* by attending to all the input tokens



$$H = \operatorname{softmax}(S)V$$

attention weights

scores:
$$S = \frac{QK^T}{\sqrt{d_k}}$$

queries:
$$Q = XW_Q$$

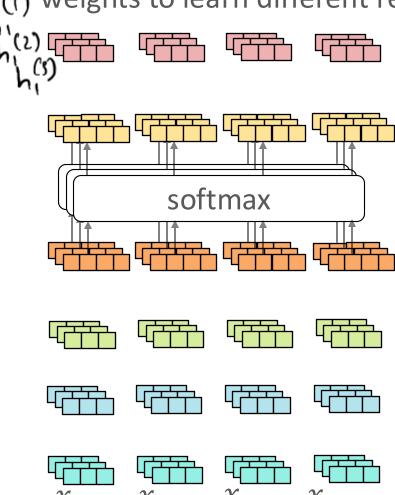
keys:
$$K = XW_K$$

values:
$$V = XW_V$$

design matrix: X

Multi-head Scaled Dot-product Self-attention

Idea: just like we might want multiple convolutional filters in a convolutional layer, we might want multiple attention
(1) weights to learn different relationships between tokens!



$$H^{(h)} = \operatorname{softmax}(S^{(h)})V^{(h)}$$

attention weights

scores:
$$S^{(h)} = \frac{Q^{(h)}K^{(h)}}{\sqrt{d_k^{(h)}}}$$

queries:
$$Q^{(h)} = XW_Q^{(h)}$$

keys:
$$K^{(h)} = XW_K^{(h)}$$

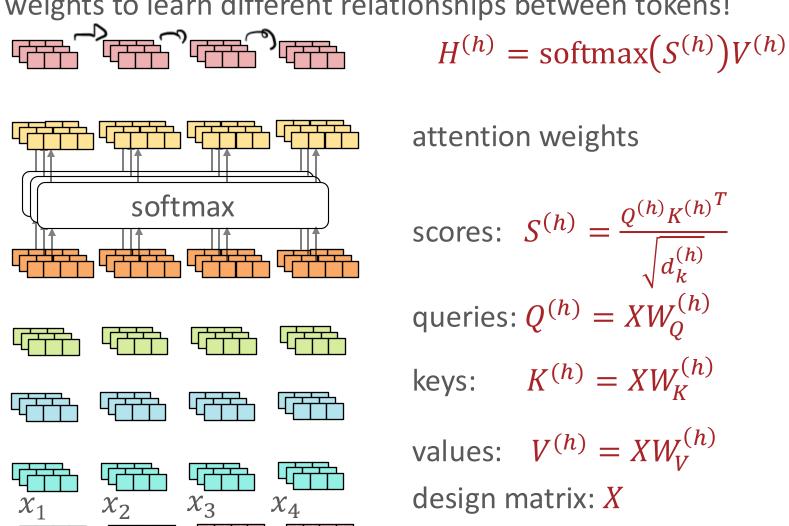
values:
$$V^{(h)} = XW_V^{(h)}$$

design matrix: X

Key Takeaway: All of this computation is

- 1. differentiable
- 2. highly parallelizable!

 Idea: just like we might want multiple convolutional filters in a convolutional layer, we might want multiple attention weights to learn different relationships between tokens!



$$H^{(h)} = \operatorname{softmax}(S^{(h)})V^{(h)}$$

attention weights

scores:
$$S^{(h)} = \frac{Q^{(h)}K^{(h)}}{\sqrt{d_k^{(h)}}}$$

queries:
$$Q^{(h)} = XW_Q^{(h)}$$

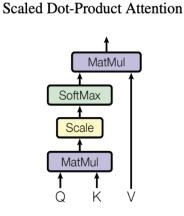
keys:
$$K^{(h)} = XW_K^{(h)}$$

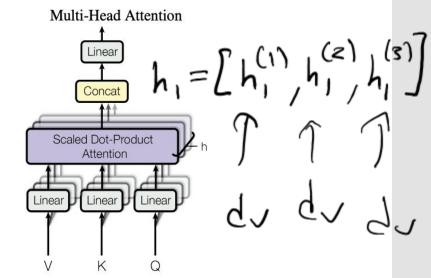
values:
$$V^{(h)} = XW_V^{(h)}$$

design matrix: X

Multi-head Scaled Dot-product Self-attention

• Idea: just like we might want multiple convolutional filters in a convolutional layer, we might want multiple attention weights to learn different relationships between tokens!

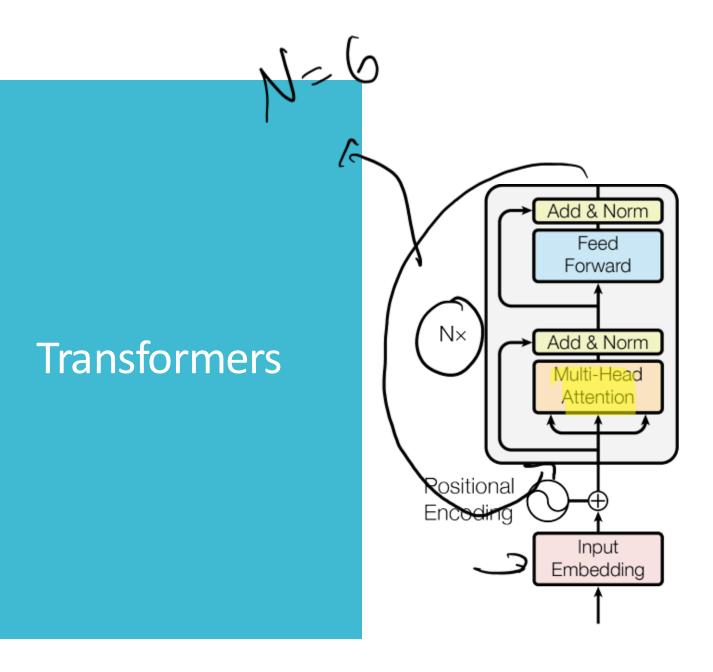




 The outputs from all the attention heads are concatenated together to get the final representation

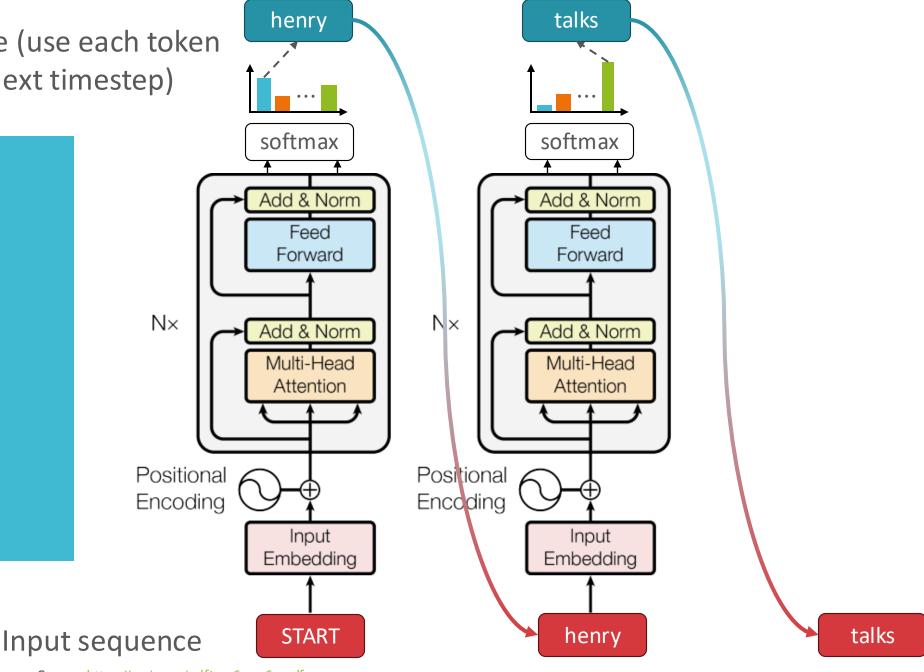
$$H = [H^{(1)}, H^{(2)}, \dots, H^{(h)}]$$

• Common architectural choice: $d_v = D/h \rightarrow |H| = D$



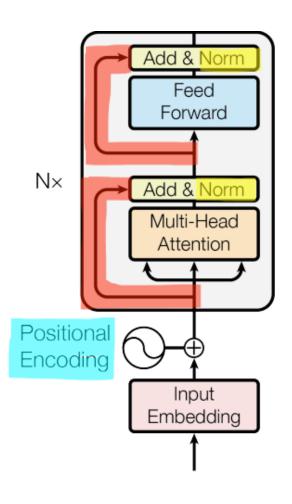
Generated sequence (use each token as the input to the next timestep)

Transformer Language Models



Source: https://arxiv.org/pdf/1706.03762.pdf

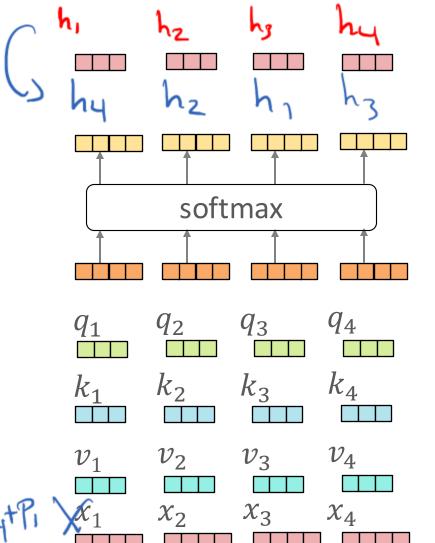
Transformers



- In addition to multi-head attention, transformer architectures use
 - 1. Positional encodings
 - 2. Layer normalization
 - 3. Residual connections
 - 4. A fully-connected feed-forward network

Scaled Dot-product Self-attention: Matrix Form

• Issue: if all tokens attend to every token in the sequence, then how does the model infer the order of tokens?



$$H = \operatorname{softmax}(S)V \in \mathbb{R}^{N \times d_v}$$

attention weights

$$S := \frac{QK^T}{\sqrt{d_k}} \in \mathbb{R}^{N \times N}$$

queries:
$$Q = XW_Q \in \mathbb{R}^{N \times d_k}$$

keys:
$$K = XW_K \in \mathbb{R}^{N \times d_k}$$

values:
$$V = XW_V \in \mathbb{R}^{N \times d_v}$$

design matrix:
$$X \in \mathbb{R}^{N \times D}$$

Positional Encodings

- Issue: if all tokens attend to every token in the sequence, then how does the model infer the order of tokens?
- Idea: add a position-specific embedding p_t to the token embedding x_t

$$x_t' = x_t + p_t$$

- Positional encodings can be
 - fixed i.e., some predetermined function of t or learned alongside the token embeddings
 - absolute i.e., only dependent on the token's location in the sequence or *relative* to the query token's location

Key Takeaways

- Attention allows information to directly pass between every pair of tokens
 - Attention can be used in conjunction with RNNs/LSTMs
 - However, (self-)attention can also be used in isolation
- Transformers consist of multi-head attention layers with residual connections, layer normalization and fullyconnected layers