Instructions:

• Verify your name and Andrew ID above.

- This exam contains 33 pages (including this cover page). The total number of points is 0.
- Clearly mark your answers in the allocated space. If you have made a mistake, cross out the invalid parts of your solution, and circle the ones which should be graded.
- Look over the exam first to make sure that none of the 33 pages are missing.
- No electronic devices may be used during the exam.
- Please write all answers in pen or darkly in pencil.
- You have N/A to complete the exam. Good luck!

Question	Points
1. Learning Theory	0
2. CNNs and RNNs	0
3. Language Modeling, Attention & Transformers	0
4. Pre-training, Fine-tuning & In-context Learning	0
5. k-means	0
6. Principal Component Analysis	0
7. Reinforcement Learning	0
8. Ensemble Methods	0
Total:	0

Instructions for Specific Problem Types

For "Select One" questions, please fill in the appropriate bubble completely:

Select One: Who taught this course?

- Matt Gormley
- O Marie Curie
- Noam Chomsky

If you need to change your answer, you may cross out the previous answer and bubble in the new answer:

Select One: Who taught this course?

- Henry Chai
- O Marie Curie
- Noam Chomsky

For "Select all that apply" questions, please fill in all appropriate squares completely:

Select all that apply: Which are instructors for this course?

- Matt Gormley
- Henry Chai
- □ I don't know

Again, if you need to change your answer, you may cross out the previous answer(s) and bubble in the new answer(s):

Select all that apply: Which are the instructors for this course?

- Matt Gormley
- Henry Chai
- I don't know

For questions where you must fill in a blank, please make sure your final answer is fully included in the given space. You may cross out answers or parts of answers, but the final answer must still be within the given space.

Fill in the blank: What is the course number?

10-601

10-8301

Learning Theory (0 points) 1

of D+1 data points.

1.1.	$\begin{array}{c} \text{poin} \\ S \end{array} \text{d}$	Consider a binary classification problem with an unknown distribution over data points D and an unknown target function $c^* : \mathcal{R}^d \mapsto \pm 1$. For any sample of points S drawn from D , answer whether the following statements are true or false, and provide a brief justification.					
	(a)	True or False: For a given hypothesis space \mathcal{H} , it is always possible to define a sufficient number of examples in S such that the true error is within a margin of ϵ of the sample error for all hypotheses $h \in H$ with a given probability.					
	(b)	True or False: The true error of any hypothesis h is an $upper$ bound on its training error on the sample S .					
1.2.		ort answer: Briefly describe the difference between the realizable case and ostic case of PAC learning.					
1.3.	Fill	in the Blanks: Complete the following sentence by circling one option in each					
	squa	are (options are separated by "/"s):					
		In order to prove that the VC-dimension of a hypothesis set \mathcal{H} is D , you must show that \mathcal{H} $\begin{bmatrix} \operatorname{can}/\operatorname{cannot} \end{bmatrix}$ shatter $\begin{bmatrix} \operatorname{any set}/\operatorname{some set}/\operatorname{multiple sets} \end{bmatrix}$					
		of D data points and $\frac{\text{can / cannot}}{\text{shatter}}$ shatter $\frac{\text{any set / some set / multiple sets}}{\text{shatter}}$					

- 1.4. Consider the hypothesis set \mathcal{H} consisting of all positive intervals in \mathbb{R} , i.e. all hypotheses of the form $h(x; a, b) = \begin{cases} +1 & \text{if } x \in [a, b] \\ -1 & \text{if } x \notin [a, b] \end{cases}$
 - (a) **Short Answer:** In 1-2 sentences, briefly justify why the VC dimension of \mathcal{H} is less than 3.

- (b) **Select one:** What is the VC dimension of \mathcal{H} ?
 - $\bigcirc 0$
 - \bigcirc 1
 - \bigcirc 2
- (c) Numerical Answer: Now, consider hypothesis sets \mathcal{H}_k indexed by k, such that \mathcal{H}_k consists of all hypotheses formed by k non-overlapping positive intervals in \mathbb{R} . Give an expression for the VC dimension of \mathcal{H}_k in terms of k.

Hint: Think about how to repeatedly apply the result you found in Part (b).

1.5. Your friend, who is taking an introductory ML course, is preparing to train a model for binary classification. Having just learned about PAC learning, she informs you that for her given model choice, \mathcal{H} , she is in the finite, agnostic case.

Now she wants to know how changing certain values will change the sample complexity i.e., the number of labeled training data points required to satisfy the PAC criterion:

$$P(|R(h) - \hat{R}(h)| \le \epsilon) \ge 1 - \delta \ \forall \ h \in \mathcal{H}$$

where R(h) and $\hat{R}(h)$ are the expected and empirical risks respectively.

For each of the following changes, determine whether the sample complexity will increase, decrease, or stay the same.

increase, decrease, or stay the same.
(a) Select one: Using a simpler model (decreasing $ \mathcal{H} $)
○ Sample complexity will increase
○ Sample complexity will decrease
○ Sample complexity will stay the same
(b) Select one: Choosing a new hypothesis set \mathcal{H}^* , such that $ \mathcal{H}^* = \mathcal{H} $
○ Sample complexity will increase
○ Sample complexity will decrease
○ Sample complexity will stay the same
(c) Select one: Decreasing δ
○ Sample complexity will increase
○ Sample complexity will decrease
○ Sample complexity will stay the same
(d) Select one: Decreasing ϵ

O Sample complexity will increase

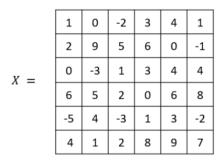
O Sample complexity will decrease

O Sample complexity will stay the same

2.1. Let's begin by considering some of the high-level components of a convolutional

2 CNNs and RNNs (0 points)

filte	er along with the basic motivation.
(a)	Short answer: What is a convolutional filter?
(b)	Short answer: Why do we need stride, and what benefits/tradeoffs might different values of stride have on the output?
(c)	Short answer: What functionality does padding add to the convolutional layer and why might we want to use it?



$$F = \begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

The shape of this particular Y is the result of using no padding and a stride of 1.

(a) **Numerical answer:** Suppose we decide that, instead of having our output shape be (4, 4), we want a slightly smaller, (3, 3) image as output. In order for this to happen, what is the smallest combination of stride and padding that would work?

(b) **Math:** Let's make this a bit more general. Suppose our original image has shape (a, a), and we want the shape of our final image to be (b, b), where $b \le a$. Furthermore the shape of the filter is (k, k), the stride length is s, and the padding is p. Express s in terms of all defined variables.

2.3.	Consider parameter sharing in a CNN.					
	(a)	Math: Consider the setup from 2.2.(b), with the same variables representing the same quantities. How many parameters do we learn with parameter sharing?				
	(b)	Math: Consider the setup from 2.2.(b), with the same variables representing the same quantities. How many parameters do we learn without parameter sharing?				
	(c)	Short answer: Suppose that this CNN is being used for a prediction task in a subject you have prior knowledge in - for instance, suppose you are being asked to classify images of cars, and you know that each image contains a side view of the car with the front of the car facing right and each car is roughly the same size. In this scenario, would parameter sharing be appropriate, disregarding computational constraints? Why or why not?				
2.4.		ort answer: What is the difference between upsampling and downsampling in Ns? What are the appropriate scenarios to use them?				

2.5.		I that apply: In which of the following settings is it more appropriate to NN over a CNN?
		Speech recognition
		Facial recognition
		Music composition
		Autocorrect system
		None of the above
2.6.		False : RNN's are helpful in analyzing time series data. Briefly justify wer in 1-2 sentences.
	\bigcirc	True
	\bigcirc	False

3 Language Modeling, Attention & Transformers (0 points)

3.1. Short answer: Your friend is painfully running a Transformer model on their a laptop, and their computer seems to be struggling with the large vocabulary size. To solve the problem, they try tokenizing letters instead of words: this way, the vocabulary only contains 26 tokens. Explain why this is not a good idea, and suggest an alternative method that would reduce vocabulary size.

3.2. Select one: Suppose a multi-head self-attention mechanism with 4 heads is applied to 20-token-long sequences where each token has an embedding dimensionality of 5. If we use scaled dot product attention with 10-dimensional keys and queries (so $d_k = d_q = 10$) and 3-dimensional values (so $d_v = 3$), what is the total dimensionality of the output for one sequence after concatenation?

$$\bigcirc$$
 4 * 20 * 3 = 240

$$\bigcirc$$
 4 * 20 * 10 = 800

$$\bigcirc$$
 4 * 20 * 5 = 400

$$\bigcirc 4 * 5 * 3 = 60$$

$$\bigcirc$$
 4 * 5 * 10 = 200

3.3. **Short answer:** In 1-2 concise sentences, briefly describe the importance of multihead attention over single head attention.

3.4. Ordering: In lecture, we saw that a transformer consists of many components/steps.

• ____ Layer Norm

• ____ Multi-Head Attention

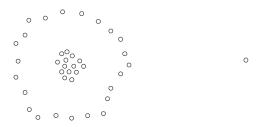
• ____ Positional Encoding

4 Pre-training, Fine-tuning & In-context Learning (0 points)

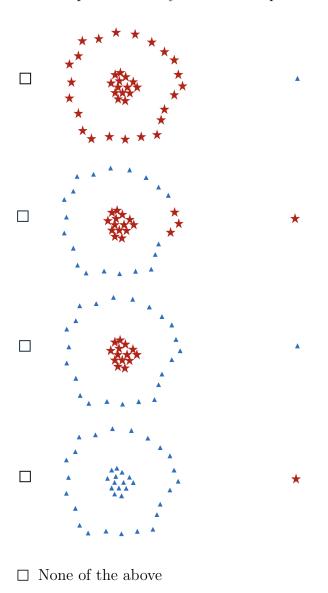
	Short answer: Why is unsupervised pre-training considered a plausible approach to improving the training of deep neural networks? Briefly explain its underlying intuition.				
	True or False: In-context learning selects a subset of the training data points to make a prediction on some test data point and adjusts the LLM's parameters to maximize the likelihood of the selected subset.				
	O True				
	○ False				
4.3.	Short answer: A pre-trained language model is to be deployed for two tasks: medical report analysis and sentiment classification of a product review. For medical report analysis, the user will ask the model follow-up questions about a report it is prompted with. For sentiment classification, the model is prompted with a review for a product and must classify the review as either {positive, negative or neutral}. For each task, decide whether fine-tuning or in-context learning would be more appropriate and justify your choice with specific reasons related to the nature of each task.				

5 k-means (0 points)

5.1. Select all that apply: Consider performing k-means clustering using Lloyd's method on the following dataset with k = 2 (note the outlier on the far right):



Which of the following could be the final clustering at convergence? In the options below, cluster membership is denoted by color and shape: red stars or blue triangles.



- 5.2. Answer whether the following statements are true or false and if space is provided, provide a brief justification.
 - (a) True or False: k-means can always converge to the global optimum.

○ True

O False

(b) True or False: k-means is sensitive to outliers.

O True

O False

- (c) Consider the following generalized version of the k-means++ algorithm:
 - Choose \mathbf{c}_1 at random.
 - For $j = 2, \dots, K$
 - Pick \mathbf{c}_j among $\mathbf{x}^{(1)}, \cdots, \mathbf{x}^{(N)}$ according to the distribution

$$P(\mathbf{c}_j = \mathbf{x}^{(i)}) \propto \min_{j' < j} \|\mathbf{x}^{(i)} - \mathbf{c}_{j'}\|^{\alpha}$$

True or False: The version of k-means++ presented in lecture is equivalent to this version with $\alpha = 2$.

O True

O False

5.3. In k-means, random initialization of the cluster centers tends to lead to a local optimum with poor performance. To alleviate this issue, instead of initializing all of the centers completely randomly, we decide to use k-means++:

Given: Data set $x^{(i)}, i = 1, \dots, N$ Initialize:

$$\mu^{(1)} \sim \text{Uniform}(\{x^{(i)}\}_{i=1}^N)$$

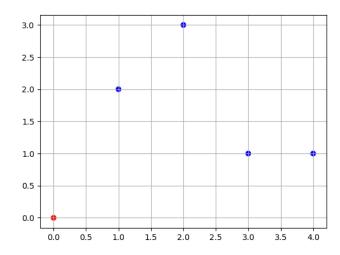
For $j = 2, \dots, k$

Computing probabilities of selecting each point

$$p_i = \frac{\min_{j' < j} \|\mu^{(j')} - x^{(i)}\|_2^2}{\sum_{i'=1}^N \min_{j' < j} \|\mu^{(j')} - x^{(i')}\|_2^2}$$

Select next center given the appropriate probabilities $\mu^{(j)} \sim \text{Categorical}(\{x^{(i)}\}_{i=1}^N, \mathbf{p}_{1:N})$

Suppose we have 5 data points: (0, 0), (1, 2), (2, 3), (3, 1), (4, 1) and (0, 0) is randomly chosen to be the center of cluster 1 (shown in red in the figure below):



(a) **Numerical answer:** What is the probability of every data point being chosen as the center for cluster 2? Your answer should contain 5 probabilities, one for each data point.

$$\bigcirc$$
 $(0,0)$

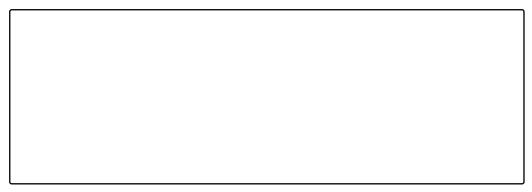
$$\bigcirc$$
 $(1, 2)$

$$\bigcirc$$
 (2, 3)

$$\bigcirc$$
 (3, 1)

$$\bigcirc$$
 (4, 1)

(c) **Numerical answer:** Assume the center for cluster 2 is chosen to be the most likely one. What is the probability of every data point being chosen as the center for cluster 3? Your answer should again contain 5 probabilities, one for each data point.



5.4. **Select one:** Consider a dataset with seven points $\{x_1, \ldots, x_7\}$. Given below are the distances between all pairs of points.

	x_1	x_2	x_3	x_4	x_5	x_6	x_7
x_1	0	5	3	1	6	2	3
x_2	5	0	4	6	1	7	8
x_3	3	4	0	4	3	5	6
x_4	1	6	4	0	7	1	2
x_5	6	1	3	7	0	8	9
x_6	2	7	5	1	8	0	1
x_7	3	8	6	2	9	1	0

Assume that k = 2, and the cluster centers are initialized to x_3 and x_6 . Which of the following shows the two clusters formed at the end of the first iteration of k-means?

$$\bigcirc \{x_1, x_2, x_3, x_4\}, \{x_5, x_6, x_7\}$$

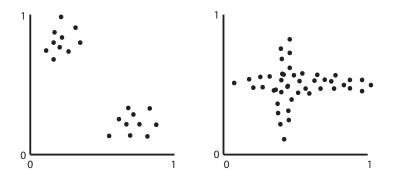
$$\bigcirc \{x_2, x_3, x_5\}, \{x_1, x_4, x_6, x_7\}$$

$$\bigcirc \{x_1, x_2, x_3, x_5\}, \{x_4, x_6, x_7\}$$

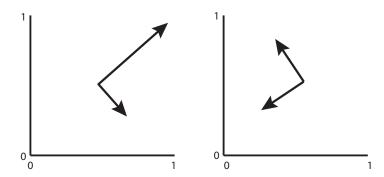
$$\bigcirc \{x_2, x_3, x_4, x_7\}, \{x_1, x_5, x_6\}$$

6 Principal Component Analysis (0 points)

6.1. (a) **Drawing:** Consider the following two plots of data. Draw arrows from the mean of the data to denote the direction and relative magnitudes of the principal components.



(b) **Drawing:** Now consider the following two plots, where we have drawn only the principal components. Draw the data ellipse or place data points that could yield the given principal components for each plot. Note that for the right hand plot, the principal components are of equal magnitude.



(a) **Select one:** Now suppose that you add an extra data point to \mathcal{D} so that \mathcal{D}' consists of N+1 data points and D features. You once again use PCA to project \mathcal{D}' to d < D dimensions: let E' be the squared reconstruction error of this new projection. How do E and E' relate to one another?

$$\bigcirc E < E'$$

$$\bigcirc E \leq E'$$

$$\bigcirc E = E'$$

$$\bigcirc E \ge E'$$

$$\bigcirc E > E'$$

(b) **Select one:** Now suppose that you use PCA to project the original dataset \mathcal{D} down to (d+1) < D dimensions instead of d dimensions: let E' be the squared reconstruction error of this new projection. How do E and E' relate to one another?

$$\bigcirc E < E'$$

$$\bigcirc E \leq E'$$

$$\bigcirc E = E'$$

$$\bigcirc E \ge E'$$

$$\bigcirc E > E'$$

7 Reinforcement Learning (0 points)

Lord Farquaad is hoping to evict all fairytale creatures from his kingdom of Duloc, and has one final ogre to evict: Shrek. Unfortunately all his previous attempts to catch the crafty ogre have fallen short, and he turns to you, with your knowledge of Markov Decision Processes (MDP's) to help him catch Shrek once and for all.

Consider the following MDP environment where the agent is Lord Farquaad:

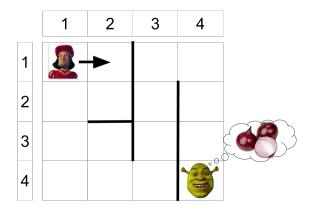


Figure 1: Kingdom of Duloc, circa 2001

Here's how we will define this MDP:

- S (state space): a set of states the agent can be in. In this case, the agent (Farquaad) can be in any location (row, col) and also in any orientation $\in \{N, E, S, W\}$. Therefore, state is represented by a three-tuple (row, col, dir), and S = all possible of such tuples. Farquaad's start state is (1, 1, E).
- A (action space): a set of actions that the agent can take. Here, we will have just three actions: turn right, turn left, and move forward (turning does not change row or col, just dir). So our action space is $\{R, L, M\}$. Note that Farquaad is debilitatingly short, so he cannot travel through (or over) the walls. Moving forward when facing a wall results in no change in state (but counts as an action).
- R(s, a) (reward function): In this scenario, Farquaad gets a reward of 5 by moving into the swamp (the cell containing Shrek), and a reward of 0 otherwise.
- p(s'|s,a) (transition probabilities): We'll use a deterministic environment, so this will be 1 if s' is reachable from s and by taking a, and 0 if not.

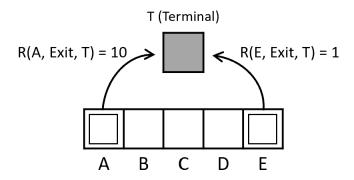
7.1.	Numerical answer: What are $ S $ and $ A $ (size of state space and size of action space)?
7.2.	Short answer: Why is it called a "Markov" decision process? (Hint: what is the assumption made with p ?)
7.3.	Numerical answer: What are the following transition probabilities?
	p((1,1,N) (1,1,N),M) =
	p((1, 1, N) (1, 1, E), L) =
	p((2,1,S) (1,1,S),M) =
	p((2,1,E) (1,1,S),M) =
	Fix $\gamma = 0.5$ for following problems.
7.4.	Given a start position of $(1, 1, E)$, what is the expected discounted future reward from $a = R$? For $a = L$?
7.5.	Short answer: Farquaad's chief strategist (Vector from Despicable Me) suggests that using $\gamma = 0.9$ will result in a different optimal policy. Is he right? Why or why not?

7.6.	Short answer: Vector then suggests the following setup: $R(s,a) = 0$ when moving into the swamp, and $R(s,a) = -1$ otherwise. Will this result in a different set of optimal policies? Why or why not?				
7.7.	Vector now suggests the following setup: $R(s,a) = 5$ when moving into the swamp, and $R(s,a) = 0$ otherwise, but with $\gamma = 1$. Could this result in a different optimal policy? Why or why not?				
7.8.	Numerical answer: Surprise! Elsa from Frozen suddenly shows up. Vector hypnotizes her and forces her to use her powers to turn the ground into ice. The environment is now stochastic: since the ground is now slippery, when choosing the action M , with a 0.2 chance, Farquaad will slip and move two squares instead of one. What is the expected future-discounted total reward from $s = (2, 4, S)$?				

7.9.	Select all that apply: Which of the following environment characteristics would increase the computational complexity per iteration for a value iteration algorithm?
	☐ Large Action Space
	☐ A Stochastic Transition Function
	□ Large State Space
	☐ Unknown Reward Function
	□ None of the Above
7.10.	Select all that apply: Which of the following environment characteristics would increase the computational complexity per iteration for a policy iteration algorithm?
	☐ Large Action Space
	\square A Stochastic Transition Function
	□ Large State Space
	☐ Unknown Reward Function
	\square None of the Above
7.11.	Select one: Let $V_k(s)$ indicate the value of state s at iteration k in (synchronous) value iteration. What is the relationship between $V_{k+1}(s)$ and $\sum_{s' \in S} P(s' s,a)[R(s,a,s') + \gamma V_k(s')]$, for any $a \in A$? Indicate the most restrictive relationship that applies. For example, if $x < y$ always holds, use $<$ instead of \le . Selecting ? means it's not possible to assign any true relationship. Assume $R(s,a,s') \ge 0 \ \forall s,s' \in S,\ a \in A$.
	$V_{k+1}(s) \square \sum_{s'} P(s' s,a) [R(s,a,s') + \gamma V_k(s')]$
	\bigcirc =
	\bigcirc <
	\bigcirc >
	$\bigcirc \leq$
	$\bigcirc \ge$
	\bigcirc ?

7.13.	Select one: Let $Q(s,a)$ indicate the estimated Q-value of state-action pair $(s,a) \in S \times A $ at some point during Q-learning. Suppose you receive reward r after taking action a at state s and arrive at state s' . Before updating the Q values based on this experience, what is the relationship between $Q(s,a)$ and $r + \gamma \max_{a' \in A} Q(s',a')$?
	Indicate the most restrictive relationship that applies. For example, if $x < y$ always holds, use $<$ instead of \le . Selecting ? means it's not possible to assign any true relationship.
	$Q(s,a) \square r + \gamma \max_{a'} Q(s',a')$
	\bigcirc =
	O <
	>
	\bigcirc \leq
	$\bigcirc \ge$
	\bigcirc ?
7.14.	Select one: During tabular Q-learning, you get a reward r after taking action $North$ from state A and arrive at state B . You compute the sample $r+\gamma Q(B,South)$ where $South = \arg\max_a Q(B,a)$.
	Which of the following Q-values are updated during this step?
	$\bigcirc Q(A, North)$
	\bigcirc Q(A, South)
	$\bigcirc Q(B, North)$
	\bigcirc Q(B, South)
7.15.	In general, for tabular Q-Learning to converge to the optimal Q function, which of the following are true?
	True or False: It is necessary that every state-action pair is visited infinitely often.
	O True
	○ False
	True or False: It is necessary that the discount γ is less than 0.5.
	O True
	○ False
	True or False: It is necessary that actions get chosen according to $\arg \max_a Q(s,a)$.
	○ True
	False

7.16. Consider training a robot to navigate the following grid-based MDP environment.



- There are six states, A, B, C, D, E, and a terminal state T.
- Valid actions in states B, C, and D are Left and Right.
- The only action from states A and E is Exit, which lead deterministically to the terminal state

The reward function is as follows:

- R(A, Exit, T) = 10
- R(E, Exit, T) = 1
- The reward for any other tuple (s, a, s') equals -1

Assume the discount factor is 1. When taking action Left, with probability 0.8, the robot will successfully move one space to the left, and with probability 0.2, the robot will move one space in the opposite direction. When taking action Right, with probability 0.8, the robot will successfully move one space to the right, and with probability 0.2, the robot will move one space in the opposite direction. Run synchronous value iteration on this environment for two iterations. Begin by initializing the value of all states to zero.

Write the value of each state after the first and the second iterations. Write your values as a comma-separated list of 6 numerical expressions in the alphabetical order of the states, specifically V(A), V(B), V(C), V(D), V(E), V(T). Each of the six entries may be a number or an expression that evaluates to a number. Do not include any max operations in your response.

- 8.1. Random forests reduce the variance of single decision trees by introducing randomness at different stages of the algorithm: what are the places where we introduce this randomness? For each assertion below, indicate whether it is true or false and briefly justify your answer in 1-2 concise sentences.
 - (a) True or False: Bootstrap Aggregation we choose N random examples without replacement from the dataset every time we train a decision tree in the forest. Doing so ensures that every tree looks at a different set of examples and thus, the forest as a whole will not overfit to the dataset.
 - (b) True or False: Bagging Take N random examples with replacement from the dataset every time we train a decision tree in the forest. Doing so and then combining the hypothesis of all trees (by taking majority) reduces variance while still holding the trends and statistical properties of the original dataset.

(c) **True or False:** Feature Split Randomization - Every tree starts with a random subset of features and uses ID3 to split them. This ensures that all trees are not dependent on the same set of features and the forest is robust

(d) **True or False:** Hypothesis Combination/Aggregation - We take the majority vote from a random subset of the decision trees at the end. This means that not all decision trees contribute to the final prediction, so the aggregated model

Tree	Sample Number	Prediction	Actual
DT1	6	No	Yes
DT1	7	No	Yes
DT2	2	No	No
DT3	1	No	No
DT3	2	Yes	No
DT3	4	Yes	Yes
DT4	2	Yes	No
DT4	7	No	Yes
DT5	3	Yes	Yes
DT5	5	No	No

(a)	Numerical answer:	What is the OOB	error of the	above random	forest	clas-
	sifier?					

(b) **Select one:** To reduce the error of each individual decision tree, Neural uses all the features to train each tree instead of using split-feature randomization. How would this impact the generalization error of the random forest?

\bigcirc	The generalization	error	would	${\it decrease}$	as	${\rm each}$	${\rm tree}$	has	lower	gen-
	eralization error									

- O The generalization error would increase as each tree has insufficient training data
- The generalization error would increase as the trees are highly correlated

 \bigcirc False

8.5. In the last semester, someone used AdaBoost on a dataset and recorded all the weights in each iteration but some entries in the table are not recognizable. Clever as you are, you decide to employ your knowledge of Adaboost to determine some of the missing information.

Below, you can see part of table that was used in the problem set. There are columns for the Round # and for the weights of the six training points (A, B, C, D, E, and F) at the start of each round. Some of the entries, marked with "?", are impossible for you to read.

Round	$D_t(A)$	$D_t(B)$	$D_t(C)$	$D_t(D)$	$D_t(E)$	$D_t(F)$			
1	?	?	$\frac{1}{6}$?	?	?			
2	?	?	?	?	?	?			
			•••						
219	?	?	?	?	?	?			
220	$\frac{1}{14}$	$\frac{1}{14}$	$\frac{7}{14}$	$\frac{1}{14}$	$\frac{2}{14}$	$\frac{2}{14}$			
221	$\frac{1}{8}$	$\frac{1}{8}$	$\frac{7}{20}$	$\frac{1}{20}$	$\frac{1}{4}$	$\frac{1}{10}$			
3017	$\frac{1}{2}$	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{16}$	$\frac{1}{16}$	0			
8888	$\frac{1}{8}$	$\frac{3}{8}$	$\frac{1}{8}$	$\frac{2}{8}$	$\frac{3}{8}$	$\frac{1}{8}$			

In the following problems, you may assume that non-consecutive rows are independent of each other, and that a classifier with weighted training error less than $\frac{1}{2}$ was chosen at each step.

Round	$D_2(A)$	$D_2(B)$	$D_2(C)$	$D_2(D)$	$D_2(E)$	$D_2(F)$
2						

(b)	Short answer: During Round 219, which of the training points (A, B, C, D,
	E, F) must have been misclassified, in order to produce the updated weights
	shown at the start of Round 220? List all the points that were misclassified.
	If none were misclassified, write 'None'. If it can't be determined, write 'Not
	Sure' instead.

- (c) **Select one:** You observe that the weights in round 3017 or 8888 (or both) cannot possibly be right. Which one is incorrect? Briefly explain your answer in 1-2 short sentences.
 - O Round 3017 is incorrect.
 - Round 8888 is incorrect.
 - O Both rounds 3017 and 8888 are incorrect.