

15-462 Computer Graphics I
Lecture 20

Visualization

Height Fields and Contours
Scalar Fields
Volume Rendering
Vector Fields

[Angel Ch. 12]

April 15, 2003
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<http://www.cs.cmu.edu/~fp/courses/graphics/>

Scientific Visualization

- Generally do not start with a 3D model
- Must deal with very large data sets
 - MRI, e.g. $512 \times 512 \times 200 \approx 50\text{MB}$ points
 - Visible Human $512 \times 512 \times 1734 \approx 433\text{ MB}$ points
- Visualize both real-world and simulation data
- User interaction
- Automatic search

Types of Data

- Scalar fields (3D volume of scalars)
 - E.g., x-ray densities (MRI, CT scan)
- Vector fields (3D volume of vectors)
 - E.g., velocities in a wind tunnel
- Tensor fields (3D volume of tensors [matrices])
 - E.g., stresses in a mechanical part [Angel 12.7]
- Static or through time

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Height Field

- Visualizing an explicit function

$$z = f(x,y)$$



- Adding contour curves

$$g(x,y) = c$$



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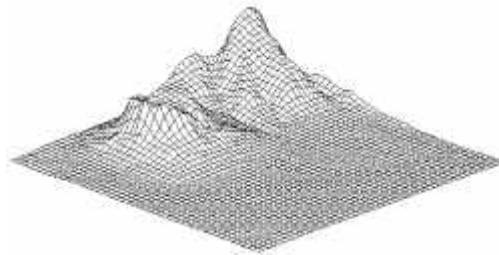
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Meshes

- Function is sampled (given) at $x_i, y_j, 0 \leq i, j \leq n$
- Assume equally spaced

$$\begin{aligned}x_i &= x_0 + i\Delta x & z_{ij} &= f(x_i, y_j) \\y_j &= y_0 + j\Delta y\end{aligned}$$

- Generate quadrilateral or triangular mesh
- [Asst 1]



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Contour Curves

- Recall: implicit curve $f(x,y) = 0$
- $f(x,y) < 0$ inside, $f(x,y) > 0$ outside
- Here: contour curve at $f(x,y) = c$
- Sample at regular intervals for x, y

$$\begin{aligned}x_i &= x_0 + i\Delta x \\y_j &= y_0 + j\Delta y\end{aligned}$$

- How can we draw the curve?

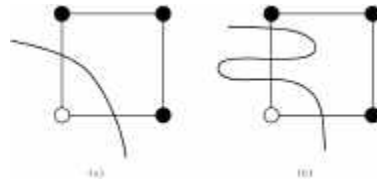
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Marching Squares

- Sample function f at every grid point x_i, y_j
- For every point $f_{ij} = f(x_i, y_j)$ either $f_{ij} \leq c$ or $f_{ij} > c$
- Distinguish those cases for each corner x
 - White: $f_{ij} \leq c$
 - Black: $f_{ij} > c$
- Now consider cases for curve
- Assume “smooth”
- Ignore $f_{ij} = 0$



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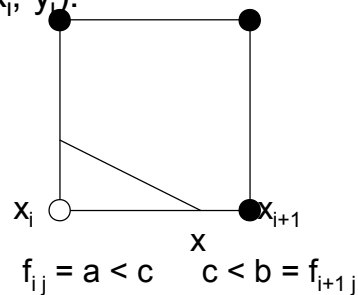
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Interpolating Intersections

- Approximate intersection
 - Midpoint between x_i, x_{i+1} and y_j, y_{j+1}
 - Better: interpolate
- If $f_{ij} = a$ is closer to c than $b = f_{i+1,j}$ then intersection is closer to (x_i, y_j) :

$$\frac{x - x_i}{x_{i+1} - x} = \frac{c - a}{b - c}$$

- Analogous calculation for y direction



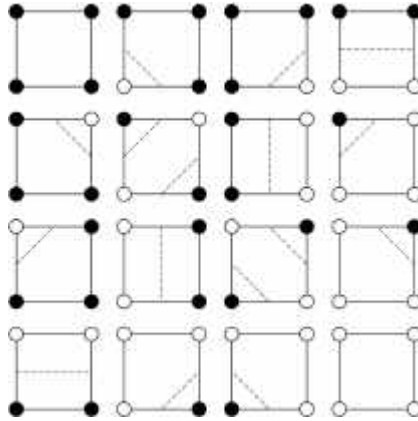
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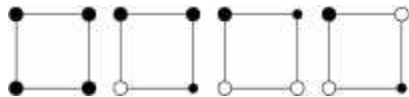
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Cases for Vertex Labels

16 cases for vertex labels



4 unique mod. symmetries

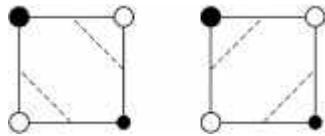


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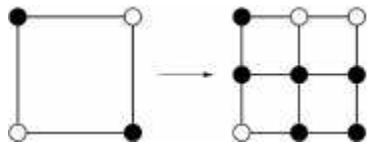
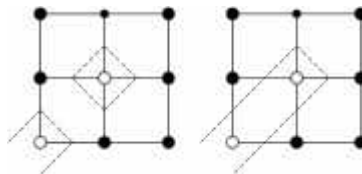
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Ambiguities of Labelings



Ambiguous labels

Different resulting contours



Resolution by subdivision
(where possible)

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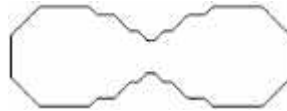
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Marching Squares Examples

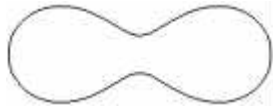
- Ovals of Cassini, 50×50 grid

$$f(x, y) = (x^2 + y^2 + a^2)^2 - 4a^2x^2 - b^4$$

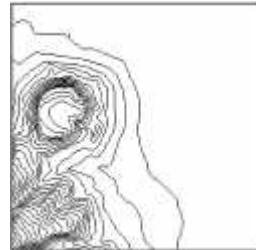
$$a = 0.49, b = 0.5$$



Midpoint



Interpolation



Contour plot of Honolulu data

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Outline

- Height Fields and Contours
- Scalar Fields
- Volume Rendering
- Vector Fields

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Scalar Fields

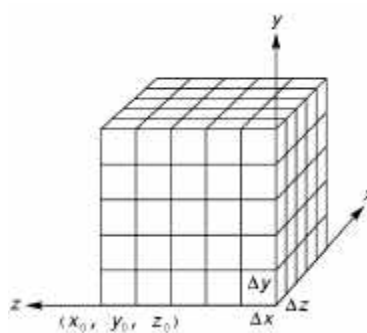
- Volumetric data sets
- Example: tissue density
- Assume again regularly sampled

$$x_i = x_0 + i\Delta x$$

$$y_j = y_0 + j\Delta y$$

$$z_k = z_0 + k\Delta z$$

- Represent as voxels



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Isosurfaces

- $f(x,y,z)$ represents volumetric data set
- Two rendering methods
 - Isosurface rendering
 - Direct volume rendering (use all values [next])
- Isosurface given by $f(x,y,z) = c$
- Recall implicit surface $g(x, y, z)$:
 - $g(x, y, z) < 0$ inside
 - $g(x, y, z) = 0$ surface
 - $g(x, y, z) > 0$ outside
- Generalize right-hand side from 0 to c

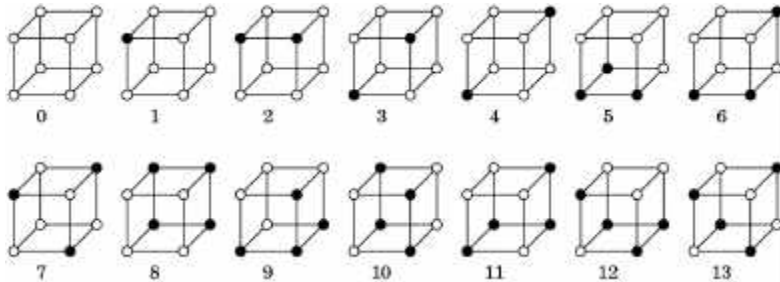
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Marching Cubes

- Display technique for isosurfaces
- 3D version of marching squares
- 14 cube labelings (after elimination symmetries)



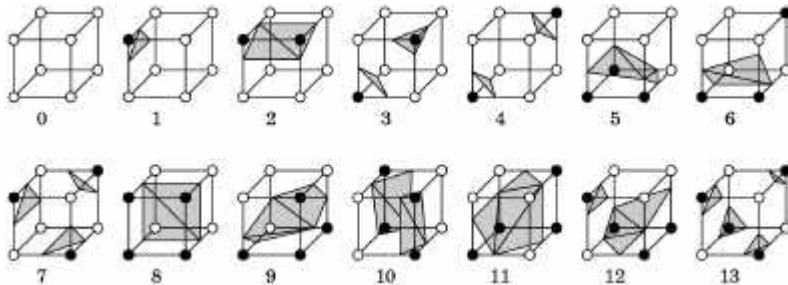
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Marching Cube Tessellations

- Generalize marching squares, just more cases
- Interpolate as in 2D
- Ambiguities similar to 2D



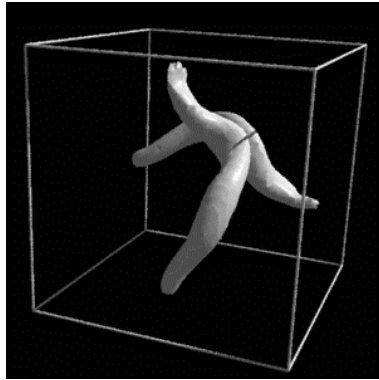
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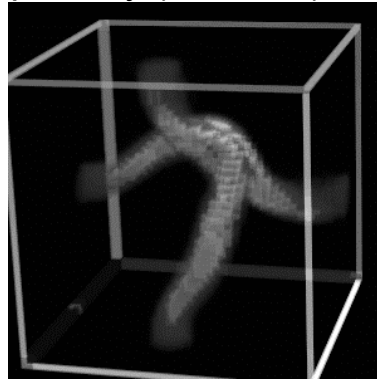
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Volume Rendering

- Sometimes isosurfaces are unnatural
- Use all voxels and transparency (α -values)



Ray-traced isosurface



Volume rendering

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Surface vs. Volume Rendering

- | | |
|---------------------------|----------------------------|
| • 3D model of surfaces | • Scalar field in 3D |
| • Convert to triangles | • Convert to RGBA values |
| • Draw primitives | • Render volume “directly” |
| • Lose or disguise data | • See data as given |
| • Good for opaque objects | • Good for complex objects |

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Sample Applications

- Medical
 - Computed Tomography (CT)
 - Magnetic Resonance Imaging (MRI)
 - Ultrasound
- Engineering and Science
 - Computational Fluid Dynamic (CFD)
 - Aerodynamic simulations
 - Meteorology
 - Astrophysics

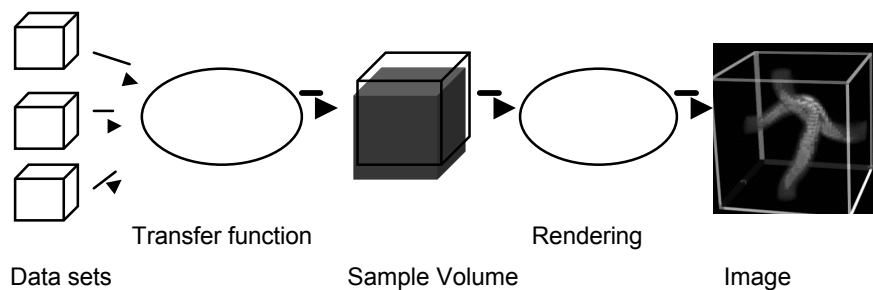
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Volume Rendering Pipeline

- Transfer function: from data set to colors and opacities
 - Example: $256 \times 256 \times 64 \times 2 = 4$ MB
 - Example: use colormap (8 bit color, 8 bit opacity)



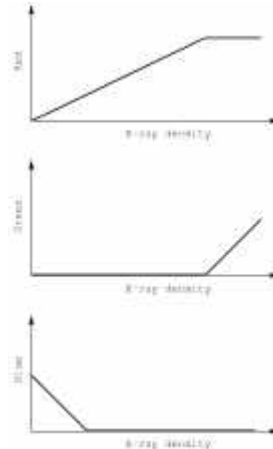
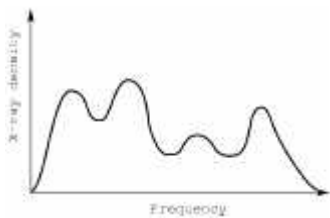
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Transfer Functions

- Transform scalar data values to RGBA values
- Apply to every voxel in volume
- Highly application dependent
- Start from data histogram
- Opacity for emphasis



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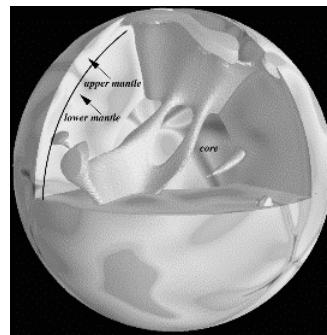
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Transfer Function Example



Mantle Convection



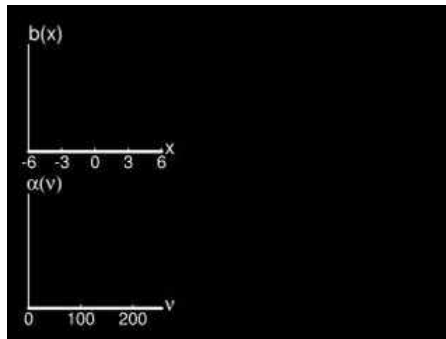
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Transfer Function Example



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Volume Ray Casting

- Three volume rendering techniques
 - Volume ray casting
 - Splatting
 - 3D texture mapping
- Ray Casting
 - Integrate color through volume
 - Consider lighting (surfaces?)
 - Use regular x,y,z data grid when possible
 - Finite elements when necessary (e.g., ultrasound)
 - 3D-rasterize geometrical primitives

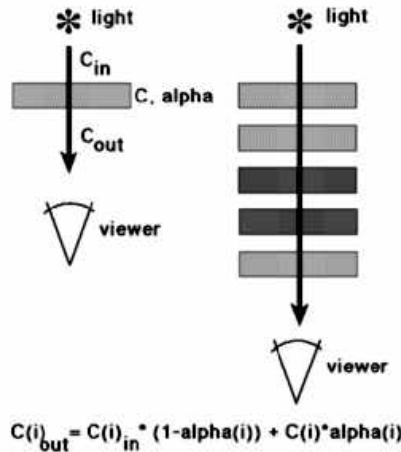
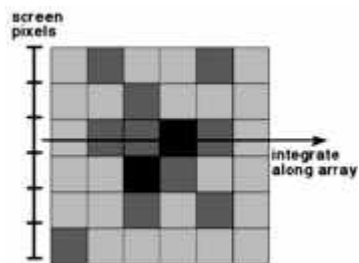
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Accumulating Opacity

- $\alpha = 1.0$ is opaque
- Composit multiple layers according to opacity
- Use local gradient of opacity to detect surfaces for lighting



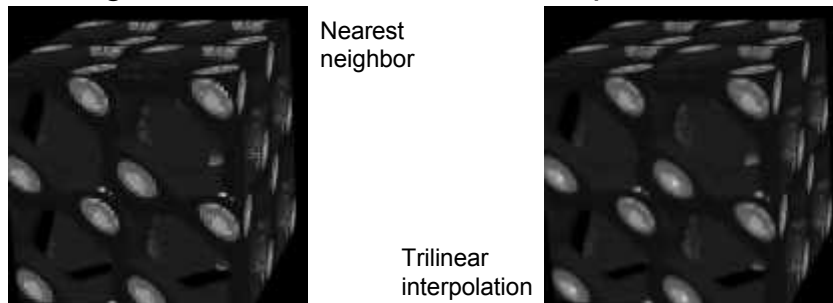
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Trilinear Interpolation

- Interpolate to compute RGBA away from grid
- Nearest neighbor yields blocky images
- Use trilinear interpolation
- 3D generalization of bilinear interpolation



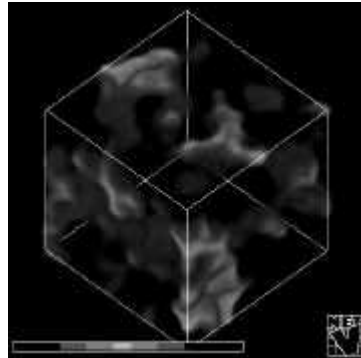
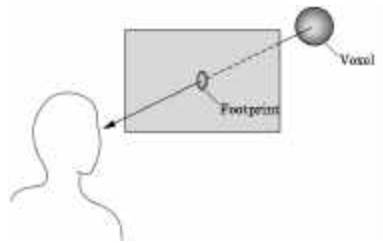
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Splatting

- Alternative to ray tracing
- Assign shape to each voxel (e.g., Gaussian)
- Project onto image plane (splat)
- Draw voxels back-to-front
- Composite (α -blend)



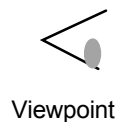
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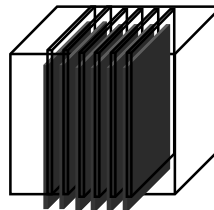
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3D Textures

- Alternative to ray tracing, splatting
- Build a 3D texture (including opacity)
- Draw a stack of polygons, back-to-front
- Efficient if supported in graphics hardware
- Few polygons, much texture memory



Viewpoint



Draw back to front

3D RGBA texture

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Example: 3D Textures



Emil Praun'01

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Example: 3D Textures

Emil Praun'01



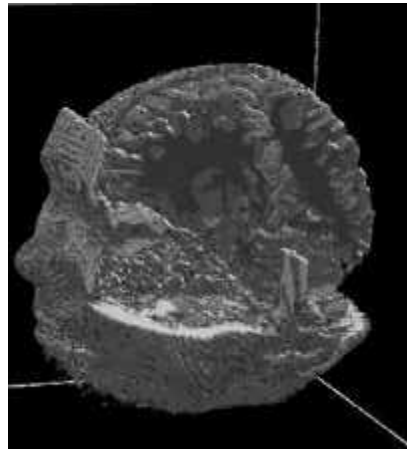
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Other Techniques

- Use CSG for cut-away



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Acceleration of Volume Rendering

- Basic problem: Huge data sets
- Program for locality (cache)
- Divide into multiple blocks if necessary
 - Example: marching cubes
- Use error measures to stop iteration
- Exploit parallelism

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Outline

- Height Fields and Contours
- Scalar Fields
- Volume Rendering
- Vector Fields

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Vector Fields

- Visualize vector at each (x,y,z) point
 - Example: velocity field
 - Example: hair
- Hedgehogs
 - Use 3D directed line segments (sample field)
 - Orientation and magnitude determined by vector
- Animation
 - Use for still image
 - Particle systems

Blood flow in
human carotid artery

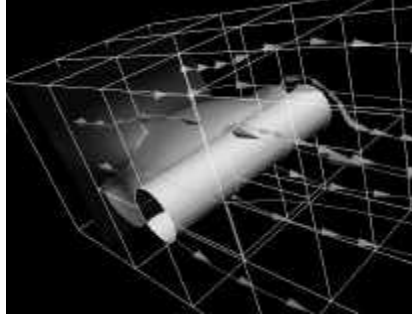


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Using Glyphs and Streaks



Glyphs for air flow



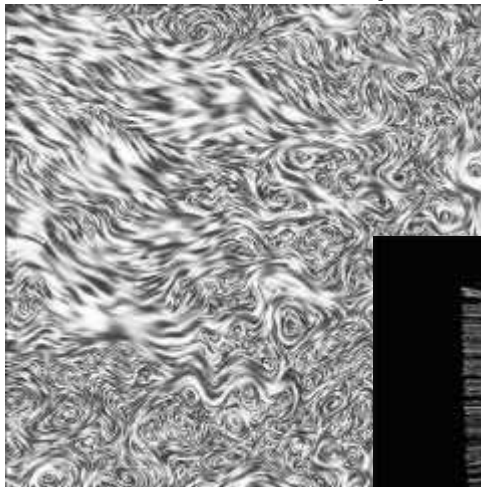
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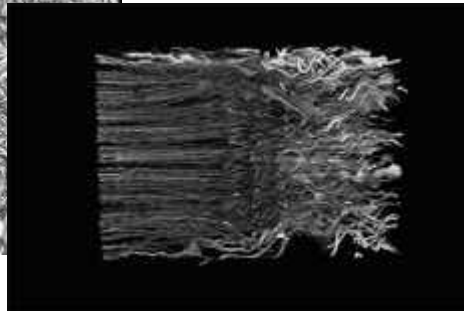
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More Flow Examples



Banks and Interrante

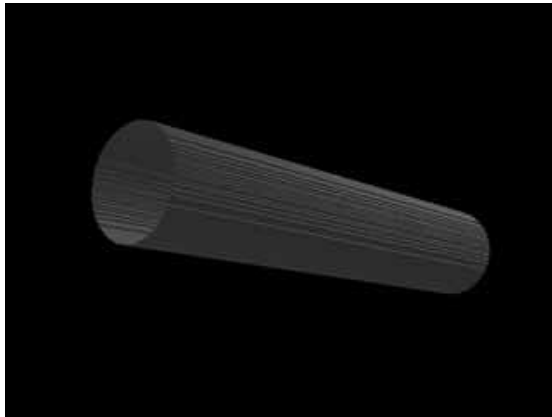


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Example: Jet Shockwave



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<http://www.sci.utah.edu/>

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Summary

- Height Fields and Contours
- Scalar Fields
 - Isosurfaces
 - Marching cubes
- Volume Rendering
 - Volume ray tracing
 - Splatting
 - 3D Textures
- Vector Fields
 - Hedgehogs
 - Animated and interactive visualization

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Preview

- Thursday
 - Non-photo-realistic rendering (NPR)
 - 4:00-5:00 Distinguished Lecture
Ed Catmull, Pixar, WeH 7500
- Assignment 7 (Ray Tracing) due Thu 4/24
- Assignment 8 (written) out Thu (early!)
- Note: no late hand-in on assignment 8!