15-462 Computer Graphics I Lecture 7

Lighting and Shading

Light Sources
Phong Illumination Model
Normal Vectors
[Angel, Ch. 6.1-6.4]

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http://www.cs.cmu.edu/~fp/courses/graphics/

Remarks About Assignment 2

- Remember that object transformations are applied in the reverse order in which they appear in the code!
- Remember that transformation matrices are multiplied on the right and executed from right to left: (R S T)v = R (S (T v))!
- Look at the model solution (when it is out) and make sure you understand it before the midterm

Outline

- Light Sources
- Phong Illumination Model
- Normal Vectors

Lighting and Shading

- Approximate physical reality
- Ray tracing:
 - Follow light rays through a scene
 - Accurate, but expensive (off-line)
- Radiosity:
 - Calculate surface inter-reflection approximately
 - Accurate, especially interiors, but expensive (off-line)
- Phong Illumination model (this lecture):
 - Approximate only interaction light, surface, viewer
 - Relatively fast (on-line), supported in OpenGL

Radiosity Example



Restaurant Interior. Guillermo Leal, Evolucion Visual

Raytracing Example



Martin Moeck, Siemens Lighting

Light Sources and Material Properties

- Appearance depends on
 - Light sources, their locations and properties
 - Material (surface) properties
 - Viewer position
- Ray tracing: from viewer into scene
- Radiosity: between surface patches
- Phong Model: at material, from light to viewer

Types of Light Sources

- Ambient light: no identifiable source or direction
- Point source: given only by point
- Distant light: given only by direction
- Spotlight: from source in direction
 - Cut-off angle defines a cone of light
 - Attenuation function (brighter in center)
- Light source described by a luminance
 - Each color is described separately
 - $-I = [I_r \ I_g \ I_b]^T$ (I for intensity)
 - Sometimes calculate generically (applies to r, g, b)

Ambient Light

- Global ambient light
 - Independent of light source
 - Lights entire scene
- Local ambient light
 - Contributed by additional light sources
 - Can be different for each light and primary color
- Computationally inexpensive

$$\mathbf{I}_a = \left[egin{array}{c} I_{ar} \ I_{ag} \ I_{ab} \end{array}
ight]$$

Point Source

- Given by a point p₀
- Light emitted equally in all directions

$$\mathbf{I}(\mathbf{p}_0) = \left[egin{array}{l} I_r(\mathbf{p}_0) \ I_g(\mathbf{p}_0) \ I_b(\mathbf{p}_0) \end{array}
ight]$$

Intensity decreases with square of distance

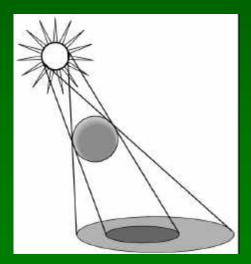
$$I(p, p_0) = \frac{1}{|p - p_0|^2} I(p_0)$$

Limitations of Point Sources

- Shading and shadows inaccurate
- Example: penumbra (partial "soft" shadow)
- Similar problems with highlights
- Compensate with attenuation

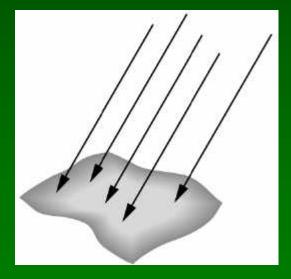
$$\frac{1}{(a+bd+cd^2)} \quad \text{d = distance } |\mathbf{p}-\mathbf{p}_0|$$
a, b, c constants

- Softens lighting
- Better with ray tracing
- Better with radiosity



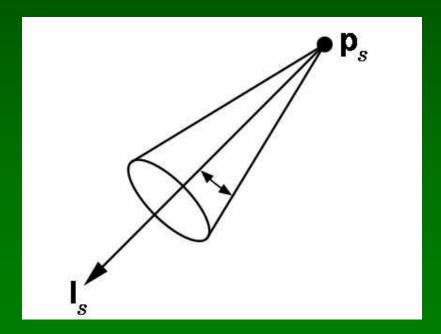
Distant Light Source

- Given by a vector v
- Simplifies some calculations
- In OpenGL:
 - Point source $[x \ y \ z \ 1]^T$
 - Distant source [x y z 0]^T



Spotlight

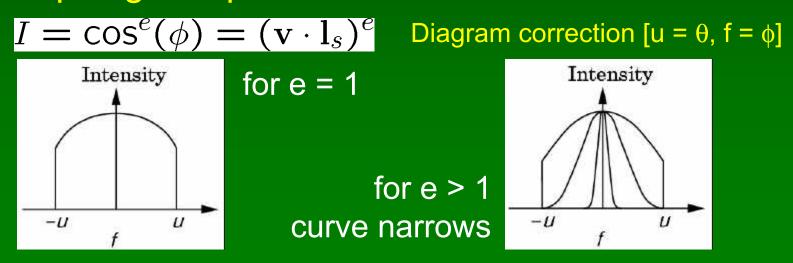
- Most complex light source in OpenGL
- Light still emanates from point
- Cut-off by cone determined by angle θ



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Spotlight Attenuation

- Spotlight is brightest along I_s
- Intensity determined by cos φ
- Corresponds to projection of v onto I_s
- Spotlight exponent e determines rate



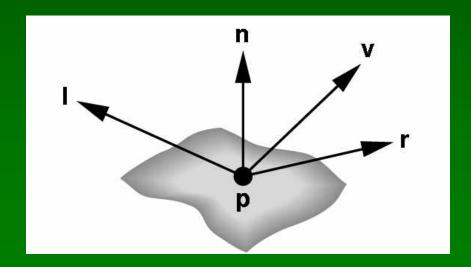
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Phong Illumination Model

- Calculate color for arbitrary point on surface
- Compromise between realism and efficiency
- Local computation (no visibility calculations)
- Basic inputs are material properties and I, n, v:

I = vector to light source
n = surface normal
v = vector to viewer
r = reflection of I at p
 (determined by I and n)



Basic Calculation

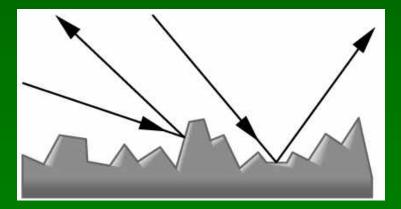
- Calculate each primary color separately
- Start with global ambient light
- Add reflections from each light source
- Clamp to [0, 1]
- Reflection decomposed into
 - Ambient reflection
 - Diffuse reflection
 - Specular reflection
- Based on ambient, diffuse, and specular lighting and material properties

Ambient Reflection

- Intensity of ambient light uniform at every point
- Ambient reflection coefficient k_a , $0 \le k_a \le 1$
- May be different for every surface and r,g,b
- Determines reflected fraction of ambient light
- L_a = ambient component of light source
- Ambient intensity I_a = k_a L_a
- Note: L_a is not a physically meaningful quantity

Diffuse Reflection

- Diffuse reflector scatters light
- Assume equally all direction
- Called Lambertian surface
- Diffuse reflection coefficient k_d, 0 ≤ k_d ≤ 1
- Angle of incoming light still critical



Lambert's Law

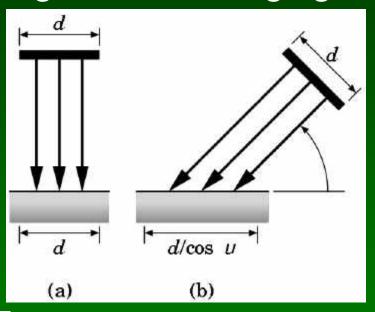
- Intensity depends on angle of incoming light
- Recall

I = unit vector from light n = unit surface normal θ = angle to normal



•
$$I_d = k_n (I \cdot n) L_d$$

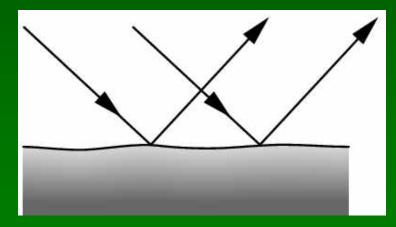
$$I_d = \frac{k_d}{a + bq + cq^2} (\mathbf{l} \cdot \mathbf{n}) L_d$$



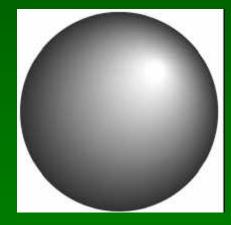
q = distance to light source, L_d = diffuse component of light

Specular Reflection

- Specular reflection coefficient k_s, 0 ≤ k_s ≤ 1
- Shiny surfaces have high specular coefficient
- Used to model specular highlights
- Do not get mirror effect (need other techniques)



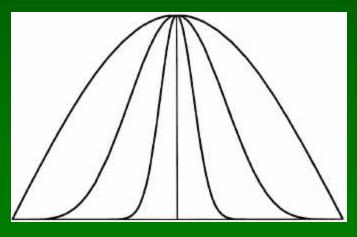
specular reflection



specular highlights

Shininess Coefficient

- L_s is specular component of light
- r is vector of perfect reflection of I about n
- v is vector to viewer
- $I_s = k_s L_s \cos^{\alpha} \phi$
- α is shininess coefficient
- Compute $\cos \phi = r \cdot v$
- Requires |r| = |v| = 1
- Multiply distance term



Higher α is narrower

Summary of Phong Model

- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k a), diffuse (k d), specular (k s)
- Distance q for surface point from light source

$$I = \frac{1}{a + bq + cq^2} (k_d L_d(\mathbf{l} \cdot \mathbf{n}) + k_s L_s(\mathbf{r} \cdot \mathbf{v})^{\alpha}) + k_a L_a$$

I = vector from light r = I reflected about n n = surface normal

v = vector to viewer

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Normal Vectors

Summarize Phong

$$I = \frac{1}{a + bq + cq^2} (k_d L_d(\mathbf{l} \cdot \mathbf{n}) + k_s L_s(\mathbf{r} \cdot \mathbf{v})^{\alpha}) + k_a L_a$$

- Surface normal n is critical
 - Calculate I · n
 - Calculate r and then r · v
- Must calculate and specify the normal vector
 - Even in OpenGL!
- Two examples: plane and sphere

Normals of a Plane, Method I

- Method I: given by ax + by + cz + d = 0
- Let p₀ be a known point on the plane
- Let p be an arbitrary point on the plane
- Recall: u · v = 0 iff u orthogonal v
- $\bullet \ \ \mathbf{n} \cdot (\mathbf{p} \mathbf{p}_0) = \mathbf{n} \cdot \mathbf{p} \mathbf{n} \cdot \mathbf{p}_0 = 0$
- Consequently $n_0 = [a \ b \ c \ 0]^T$
- Normalize to $n = n_0/|n_0|$

Normals of a Plane, Method II

- Method II: plane given by p₀, p₁, p₂
- Points may not be collinear
- Recall: u × v orthogonal to u and v
- $n_0 = (p_1 p_0) \times (p_2 p_0)$
- Order of cross produce determines orientation
- Normalize to $n = n_0/|n_0|$

Normals of Sphere

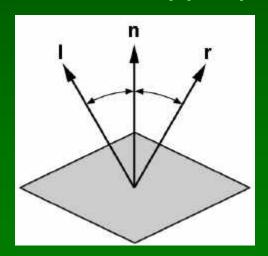
- Implicit Equation $f(x, y, z) = x^2 + y^2 + z^2 1 = 0$
- Vector form: $f(p) = p \cdot p 1 = 0$
- Normal given by gradient vector

$$\mathbf{n}_{0} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \\ \frac{\partial f}{\partial z} \end{bmatrix} = \begin{bmatrix} 2x \\ 2y \\ 2z \end{bmatrix} = 2\mathbf{p}$$

• Normalize $n_0/|n_0| = 2p/2 = p$

Angle of Reflection

- Perfect reflection: angle of incident equals angle of reflection
- Also: I, n, and r lie in the same plane
- Assume |I| = |n| = 1, guarantee |r| = 1



$$\mathbf{l} \cdot \mathbf{n} = \cos \theta = \mathbf{n} \cdot \mathbf{r}$$
 $\mathbf{r} = \alpha \mathbf{l} + \beta \mathbf{n}$ Solution: $\alpha = -1$ and $\beta = 2 (\mathbf{l} \cdot \mathbf{n})$
 $\mathbf{r} = 2(\mathbf{l} \cdot \mathbf{n})\mathbf{n} - \mathbf{l}$

Perhaps easier geometrically

Summary: Normal Vectors

- Critical for Phong model (diffuse and specular)
- Must calculate accurately (even in OpenGL)
- Pitfalls
 - Not unit length
 - How to set at surface boundary?
- Omitted
 - Refraction of transmitted light (Snell's law)
 - Halfway vector (yet another optimization)

Summary

- Light Sources
- Phong Illumination Model
- Normal Vectors

Preview

- Polygonal shading
- Lighting and shading in OpenGL
- [Demo]
- Moving and stationary light sources

Announcements

- Assignment 2 back Thursday
- Check out model solution (before midterm)
- Assignment 3 due a week from Thursday