

Image Processing

Display Color Models
Filters
Dithering
Image Compression

April 18, 2002
Frank Pfenning
Carnegie Mellon University
<http://www.cs.cmu.edu/~fp/courses/graphics/>

Displays and Framebuffers

- Image stored in memory as 2D pixel array, called framebuffer
- Value of each pixel controls color
- Video hardware scans the framebuffer at 60Hz
- Depth of framebuffer is information per pixel
 - 1 bit: black and white display (cf. Smithsonian)
 - 8 bit: 256 colors at any given time via colormap
 - 16 bit: 5, 6, 5 bits (R,G,B), $2^{16} = 65,536$ colors
 - 24 bit: 8, 8, 8 bits (R,G,B), $2^{24} = 16,777,216$ colors

04/18/2002

15-462 Graphics I

2

Fewer Bits: Colormaps

- Colormaps typical for 8 bit framebuffer depth
- With screen $1024 * 768 = 786432 = 0.75$ MB
- Each pixel value is index into colormap
- Colormap is array of RGB values, 8 bits each
- All 2^{24} colors can be represented
- Only $2^8 = 256$ at a time
- Poor approximation of full color
- Who owns the colormap?
- Colormap hacks: affect image w/o changing framebuffer (only colormap)

04/18/2002

15-462 Graphics I

3

More Bits: Graphics Hardware

- 24 bits: RGB
- + 8 bits: A (α -channel for opacity)
- + 16 bits: Z (for hidden-surface removal)
- * 2: double buffering for smooth animation
- = 96 bits
- For $1024 * 768$ screen: 9 MB

04/18/2002

15-462 Graphics I

4

Image Processing

- 2D generalization of signal processing
- Image as a two-dimensional signal
- Point processing: modify pixels independently
- Filtering: modify based on neighborhood
- Compositing: combine several images
- Image compression: space-efficient formats
- Other topics (not in this course)
 - Image enhancement and restoration
 - Special effects (cf. Tuesday's lecture)
 - Computer vision

04/18/2002

15-462 Graphics I

5

Outline

- Display Color Models
- Filters
- Dithering
- Image Compression

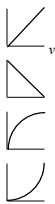
04/18/2002

15-462 Graphics I

6

Point Processing

- Input: $a(x,y)$; Output: $b(x,y) = f(a(x,y))$
- Useful for contrast adjustment, false colors
- Examples for grayscale, $0 \leq v \leq 1$
 - $f(v) = v$ (identity)
 - $f(v) = 1-v$ (negate image)
 - $f(v) = v^p$, $p < 1$ (brighten)
 - $f(v) = v^p$, $p > 1$ (darken)
- Gamma correction compensates monitor brightness loss



04/18/2002

15-462 Graphics I

7

Gamma Correction Example

$$\Gamma = 1.0; f(v) = v$$

$$\Gamma = 0.5; f(v) = v^{1/0.5} = v^2 \quad \Gamma = 2.5; f(v) = v^{1/2.5} = v^{0.4}$$

04/18/2002

15-462 Graphics I

8

Signals and Filtering

- Audio recording is 1D signal: amplitude(t)
- Image is a 2D signal: color(x,y)
- Signals can be continuous or discrete
- Raster images are discrete
 - In space: sampled in x, y
 - In color: quantized in value
- Filtering: a mapping from signal to signal

04/18/2002

15-462 Graphics I

9

Linear and Shift-Invariant Filters

- Linear with respect to input signal
- Shift-invariant with respect to parameter
- Convolution in 1D
 - $a(t)$ is input signal
 - $b(s)$ is output signal
 - $h(u)$ is filter
 - Shorthand: $b = a * h$ (= $h * a$, as an aside)
- Convolution in 2D

$$b(x, y) = \sum_{u=-\infty}^{+\infty} \sum_{v=-\infty}^{+\infty} a(u, v) h(x - u, y - v)$$

04/18/2002

15-462 Graphics I

10

Filters with Finite Support

- Filter $h(u,v)$ is 0 except in given region
- Represent h in form of a matrix
- Example: 3×3 blurring filter

$$b(x, y) = \frac{1}{9} (a(x-1, y-1) + a(x, y-1) + a(x+1, y-1) + a(x-1, y) + a(x, y) + a(x+1, y) + a(x-1, y+1) + a(x, y+1) + a(x+1, y+1))$$
- As function

$$h(u, v) = \begin{cases} \frac{1}{9} & \text{if } -1 \leq u, v \leq 1 \\ 0 & \text{otherwise} \end{cases}$$
- In matrix form

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

04/18/2002

15-462 Graphics I

11

Blurring Filters

- Average values of surrounding pixels
- Can be used for anti-aliasing
- Size of blurring filter should be odd
- What do we do at the edges and corners?
- For noise reduction, use median, not average
 - Eliminates intensity spikes
 - Non-linear filter

04/18/2002

15-462 Graphics I

12

Examples of Blurring Filter

Original Image Blur 3x3 mask Blur 7x7 mask

04/18/2002 15-462 Graphics I 13

Blur 7x7 mask

13

Example Noise Reduction

Original image Image with noise Median filter (5x5?)

04/18/2002 15-462 Graphics I 14

Median filter (5x5?)

14

Edge Filters

- Discover edges in image
- Characterized by large gradient
$$\nabla a = \begin{bmatrix} \frac{\partial a}{\partial x} & \frac{\partial a}{\partial y} \end{bmatrix}, \quad |\nabla a| = \sqrt{\left(\frac{\partial a}{\partial x}\right)^2 + \left(\frac{\partial a}{\partial y}\right)^2}$$
- Approximate square root
$$|\nabla a| \approx \left| \frac{\partial a}{\partial x} \right| + \left| \frac{\partial a}{\partial y} \right|$$
- Approximate partial derivatives, e.g.
$$\frac{\partial a}{\partial x} \approx a(x+1) - a(x-1)$$

04/18/2002 15-462 Graphics I 15

- $$\nabla a = \left[\frac{\partial a}{\partial x} \quad \frac{\partial a}{\partial y} \right], \quad |\nabla a| = \sqrt{\left(\frac{\partial a}{\partial x} \right)^2 + \left(\frac{\partial a}{\partial y} \right)^2}$$

- $$|\nabla a| \approx \left| \frac{\partial a}{\partial x} \right| + \left| \frac{\partial a}{\partial y} \right|$$

- $$\frac{\partial a}{\partial x} \approx a(x+1) - a(x-1)$$

15

Sobel Filter

- Edge detection filter, with some smoothing
- Approximate
$$\frac{\partial}{\partial x} \approx \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, \quad \frac{\partial}{\partial y} \approx \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$
- Sobel filter is non-linear
 - Square and square root (more exact computation)
 - Absolute value (faster computation)

04/18/2002 15-462 Graphics I 16

- $$\frac{\partial}{\partial x} \approx \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, \quad \frac{\partial}{\partial y} \approx \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- 16

[illegible]

-
- Figure 1 displays two 10x10 matrices, (a) and (b), representing the 10x10 grid world. Matrix (a) shows the transition matrix, and matrix (b) shows the reward matrix. The matrices are labeled 'a' and 'b' respectively. A 3x3 grid is shown to the left of matrix (a), with values -1, 0, 1 in the top row and -2, 0, 2 in the bottom row, and the label 'h' below it.

17

Example of Edge Filter

Edge filter, then brightened

10

Image Compositing

- Use α -channel (RGBA)
- Already discussed in this course
- Used for retouching and special effects
- Other image compositing techniques
 - Morphing
 - See Steve Sullivan's talk

04/18/2002

15-462 Graphics I

19

Outline

- Display Color Models
- Filters
- Dithering
- Image Compression

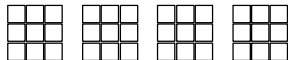
04/18/2002

15-462 Graphics I

20

Dithering

- Compensates for lack of color resolution
- Give up spatial resolution for color resolution
- Eye does spatial averaging
- Black/white dithering to achieve gray scale
 - Each pixel is black or white
 - From far away, color determined by fraction of white
 - For 3x3 block, 10 levels of gray scale



04/18/2002

15-462 Graphics I

21

Halftone Screens

- Regular patterns create some artefacts
 - Avoid stripes
 - Avoid isolated pixels (e.g. on laser printer)
 - Monotonicity: keep pixels on at higher intensities
- Example of good 3x3 dithering matrix
 - For intensity n , turn on pixels $0..n-1$

$$\begin{bmatrix} 6 & 8 & 4 \\ 1 & 0 & 3 \\ 5 & 2 & 7 \end{bmatrix}$$

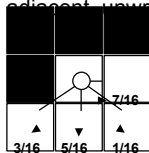
04/18/2002

15-462 Graphics I

22

Floyd-Steinberg Error Diffusion

- Approximation without fixed resolution loss
- Scan in raster order
- At each pixel, draw least error output value
- Divide error into 4 different fractions
- Add the error fractions into adjacent, unwritten pixels



04/18/2002

15-462 Graphics I

23

Floyd-Steinberg Example

Gray Scale Ramp

- Some worms
- Some checkerboards
- Enhance edges

Peter Anderson

04/18/2002

15-462 Graphics I

24

Color Dithering

- Example: 8 bit framebuffer
 - Set color map by dividing 8 bits into 3,3,2 for RGB
 - Blue is deemphasized since we see it less well
- Dither RGB separately
 - Works well with Floyd-Steinberg
- Assemble results into 8 bit index into colormap
- Generally looks good

04/18/2002

15-462 Graphics I

25

Outline

- Display Color Models
- Filters
- Dithering
- Image Compression

04/18/2002

15-462 Graphics I

26

Image Compression

- Exploit redundancy
 - Coding: some pixel values more common
 - Interpixel: adjacent pixels often similar
 - Psychovisual: some color differences imperceptible
- Distinguish lossy and lossless methods

04/18/2002

15-462 Graphics I

27

Some Image File Formats

	Depth	File Size	Comments
JPEG	24	Small	Lossy compression
TIFF	8, 24	Medium	Good general purpose
GIF	1, 4, 8	Medium	Popular, but 8 bit
PPM	24	Big	Easy to read/write
EPS	1,2,4,8,24	Huge	Good for printing

04/18/2002

15-462 Graphics I

28

Image Sizes

- 1024*1024 at 24 bits uses 3 MB
- Encyclopedia Britannica at 300 pixels/inch and 1 bit/pixes requires 25 gigabytes (25K pages)
- 90 minute movie at 640x480, 24 bits per pixels, 24 frames per second requires 120 gigabytes
- Applications: HDTV, DVD, satellite image transmission, medial image processing, fax, ...

04/18/2002

15-462 Graphics I

29

Exploiting Coding Redundancy

- Not limited to images (text, other digital info)
- Exploit nonuniform probabilities of symbols
- Entropy as measure of information content
 - $H = -\sum_i \text{Prob}(s_i) \log_2 (\text{Prob}(s_i))$
 - If source is independent random variable need H bits
- Idea:
 - More frequent symbols get shorter code strings
 - Best with high redundancy (= low entropy)
- Common algorithms
 - Huffman coding
 - LZW coding (gzip)

04/18/2002

15-462 Graphics I

30

Huffman Coding

- Codebook is precomputed and static
 - Use probability of each symbol to assign code
 - Map symbol to code
 - Store codebook and code sequence
- Precomputation is expensive
- What is “symbol” for image compression?

04/18/2002

15-462 Graphics I

31

Lempel-Ziv-Welch (LZW) Coding

- Compute codebook on the fly
- Fast compression and decompression
- Can tune various parameters
- Both Huffman and LZW are lossless

04/18/2002

15-462 Graphics I

32

Exploiting Interpixel Redundancy

- Neighboring pixels are correlated
- Spatial methods for low-noise image
 - Run-length coding:
 - Alternate values and run-length
 - Good if horizontal neighbors are same
 - Can be 1D or 2D (e.g. used in fax standard)
 - Quadrees:
 - Recursively subdivide until cells are constant color
 - Region encoding:
 - Represent boundary curves of color-constant regions
- Combine methods
- Not good on natural images directly

04/18/2002

15-462 Graphics I

33

Improving Noise Tolerance

- Predictive coding:
 - Predict next pixel based on prior ones
 - Output difference to actual
- Fractal image compression
 - Describe image via recursive affine transformation
- Transform coding
 - Exploit frequency domain
 - Example: discrete cosine transform (DCT)
 - Used in JPEG
- Transform coding for lossy compression

04/18/2002

15-462 Graphics I

34

Discrete Cosine Transform

- Used for lossy compression (as in JPEG)

$$F(u, v) = c(u)c(v) \sum_{x=0}^{n-1} \sum_{y=0}^{n-1} f(x, y) \cos \frac{(2x+1)u\pi}{2n} \cos \frac{(2y+1)v\pi}{2n}$$

where $c(u) = 1/\sqrt{n}$ if $u = 0$, $c(u) = \sqrt{2/n}$ otherwise

- JPEG (Joint Photographic Expert Group)
 - Subdivide image into $n \times n$ blocks ($n = 8$)
 - Apply discrete cosine transform for each block
 - Quantize, zig-zag order, run-length code coefficients
 - Use variable length coding (e.g. Huffman)
- Many natural images can be compressed to 4 bits/pixels with little visible error

04/18/2002

15-462 Graphics I

35

Summary

- Display Color Models
 - 8 bit (colormap), 24 bit, 96 bit
- Filters
 - Blur, edge detect, sharpen, despeckle
- Dithering
 - Floyd-Steinberg error diffusion
- Image Compression
 - Coding, interpixel, psychovisual redundancy
 - Lossless vs. lossy compression

04/18/2002

15-462 Graphics I

36

Preview

- Assignment 6 graded
- Tuesday: Scientific Visualization
- Assignment 7 due Tuesday
- Assignment 8 (written) out Tuesday