15-462 Computer Graphics I Lecture 17

Spatial Data Structures

Hierarchical Bounding Volumes Regular Grids Octrees

[Angel 8.9]

BSP Trees Constructive Solid Geometry (CSG)

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http://www.cs.cmu.edu/~fp/courses/graphics/

Ray Tracing Acceleration

- · Faster intersections
 - Faster ray-object intersections
 - · Object bounding volume
 - · Efficient intersectors
 - Fewer ray-object intersections
 - Hierarchical bounding volumes (boxes, spheres)
 - · Spatial data structures
 - · Directional techniques
- Fewer ravs
 - Adaptive tree-depth control
 - Stochastic sampling
- · Generalized rays (beams, cones)

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Spatial Data Structures

- · Data structures to store geometric information
- · Sample applications
 - Collision detection
 - Location queries
 - Chemical simulations
 - Rendering
- · Spatial data structures for ray tracing
 - Object-centric data structures (bounding volumes)
 - Space subdivision (grids, octrees, BSP trees)
 - Speed-up of 10x, 100x, or more

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Bounding Volumes

- · Wrap complex objects in simple ones
- · Does ray intersect bounding box?
 - No: does not intersect enclosed objects
 - Yes: calculate intersection with enclosed objects
- · Common types
 - Boxes, axis-aligned
 - Boxes, oriented
 - Spheres
 - Finite intersections or unions of above

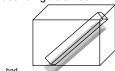


Selection of Bounding Volumes

- · Effectiveness depends on:
 - Probability that ray hits bounding volume, but not enclosed objects (tight fit is better)
 - Expense to calculate intersections with bounding volume and enclosed objects
- · Amortize calculation of bounding volumes

Use heuristics





Hierarchical Bounding Volumes

- · With simple bounding volumes, ray casting still has requires O(n) intersection tests
- · Idea use tree data structure
 - Larger bounding volumes contain smaller ones etc.
 - Sometimes naturally available (e.g. human figure)
 - Sometimes difficult to compute
- Often reduces complexity to O(log(n))

Ray Intersection Algorithm

- · Recursively descend tree
- · If ray misses bounding volume, no intersection
- If ray intersects bounding volume, recurse with enclosed volumes and objects
- · Maintain near and far bounds to prune further
- Overall effectiveness depends on model and constructed hierarchy

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Spatial Subdivision

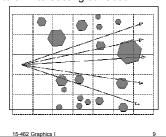
- · Bounding volumes enclose objects, recursively
- · Alternatively, divide space
- For each segment of space keep list of intersecting surfaces or objects
- · Basic techniques
 - Regular grids
 - Octrees (axis-aligned, non-uniform partition)
 - BSP trees (recursive Binary Space Partition, planes)

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Grids

- · 3D array of cells (voxels) that tile space
- · Each cell points to all intersecting surfaces
- Intersection alg steps from cell to cell



Caching Intersection points

- · Objects can span multiple cells
- · For A need to test intersection only once
- For B need to cache intersection and check next cell for closer one

 If not, C could be missed (yellow ray)

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Assessment of Grids

- Poor choice when world is non-homogeneous
- · Size of grid
 - Too small: too many surfaces per cell
 - Too large: too many empty cells to traverse
 - Can use alg like Bresenham's for efficient traversal
- · Non-uniform spatial subdivision more flexible
 - Can adjust to objects that are present

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Outline

- · Hierarchical Bounding Volumes
- Regular Grids
- · Octrees
- · BSP Trees
- Constructive Solid Geometry (CSG)

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Quadtrees

- · Generalization of binary trees in 2D
 - Node (cell) is a square
 - Recursively split into 4 equal sub-squares
 - Stop subdivision based on number of objects
- · Ray intersection has to traverse quadtree
- · More difficult to step to next cell



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Octrees

- · Generalization of quadtree in 3D
- · Each cell may be split into 8 equal sub-cells
- · Internal nodes store pointers to children
- · Leaf nodes store list of surfaces
- · Adapts well to non-homogeneous scenes

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Assessment for Ray Tracing

- · Grids
 - Easy to implement
 - Require a lot of memory
 - Poor results for non-homogeneous scense
- Octrees
 - Better on most scenes (more adaptive)
- · Alternative: nested grids
- · Spatial subdivision expensive for animations
- · Hierarchical bounding volumes
 - Natural for hierarchical objects
 - Better for dynamic scenes

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Other Spatial Subdivision Techniques

- · Relax rules for quadtrees and octrees
- k-dimensional tree (k-d tree)
 - Split at arbitrary interior point
 - Split one dimension at a time
- Binary space partitioning tree (BSP tree)
 - In 2 dimensions, split with any line
 - In k dims. split with k-1 dimensional hyperplane
 - Particularly useful for painter's algorithm
 - Can also be used for ray tracing [see handout]

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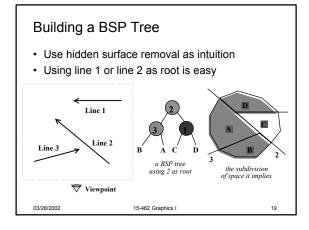
BSP Trees

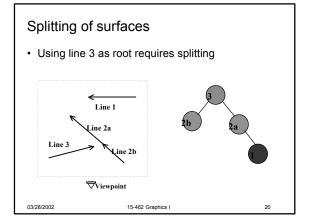
- Split space with any line (2D) or plane (3D)
- Applications
 - Painters algorithm for hidden surface removal
 - Ray casting
- Inherent spatial ordering given viewpoint
 - Left subtree: in front, right subtree: behind
- · Problem: finding good space partitions
 - Proper ordering for
 - Balance tree
- For details, see http://reality.sgi.com/bspfaq/

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Building a Good Tree

- Naive partitioning of n polygons yields O(n³) polygons (in 3D)
- · Algorithms with O(n2) increase exist
 - Try all, use polygon with fewest splits
 - Do not need to split exactly along polygon planes
- Should balance tree
 - More splits allow easier balancing
 - Rebalancing?

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Painter's Algorithm with BSP Trees

- · Building the tree
 - May need to split some polygons
 - Slow, but done only once
- Traverse back-to-front or front-to-back
 - Order is viewer-direction dependent
 - What is front and what is back of each line changes
 - Determine order on the fly

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Details of Painter's Algorithm

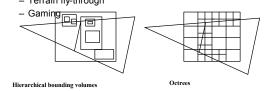
- Each face has form Ax + By + Cz + D
- · Plug in coordinates and determine
 - Positive: front side
 - Zero: on plane
 - Negative: back side
- · Back-to-front: inorder traversal, farther child first
- Front-to-back: inorder traversal, near child first
- · Do backface culling with same sign test
- Clip against visible portion of space (portals)

[Guest Lecture: John Ketchpaw]

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Clipping With Spatial Data Structures

- · Accelerate clipping
 - Goal: accept or rejects whole sets of objects
 - Can use an spatial data structures
- · Scene should be mostly fixed
 - Terrain fly-through



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Data Structure Demos

- · BSP Tree construction
- KD Tree construction http://www.rolemaker.dk/nonRoleMaker/uni/algogem/kdtree.htm

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Real-Time and Interactive Ray Tracing

- Interactive ray tracing via space subdivision
- Interactive ray tracing with good hardware

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Outline

- · Hierarchical Bounding Volumes
- · Regular Grids
- · Octrees
- · BSP Trees
- · Constructive Solid Geometry (CSG)

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Constructive Solid Geometry (CSG)

- · Generate complex shapes with simple building blocks (boxes, spheres, cylinders, cones, ...)
- · Particularly applicable for machined objects
- · Efficient with ray tracing



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Example: A CSG Train



Boolean Operations

- · Intersection and union
- Subtraction
 - Example: drilling a hote Subtract

CSG Trees

• Set operations yield tree-based representation



- Use these trees for ray/objects intersections
- · Think about how!

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Implicit Functions for Booleans

- Solid as implicit function, F(x,y,z)
 - F(x, y, z) < 0 interior
 - F(x, y, z) = 0 surface
 - F(x, y, z) > 0 exterior
- For CSG, use $F(x,\,y,\,z)\in\{\text{-}1,\,0,\,1\}$
- $F_{A \cap B}(\mathbf{p}) = \max(F_A(\mathbf{p}), F_B(\mathbf{p}))$
- $F_{A \cup B}(\mathbf{p}) = \min(F_A(\mathbf{p}), F_B(\mathbf{p}))$
- $F_{A-B}(\mathbf{p}) = \max (F_A(\mathbf{p}), -F_B(\mathbf{p}))$

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Summary

- · Hierarchical Bounding Volumes
- · Regular Grids
- Octrees
- BSP Trees
- Constructive Solid Geometry (CSG)

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Preview

- Radiosity
- · Image Processing
- · Assignment 6 due today
- · Assignment 7 (ray tracing) out late today

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