

15-462 Computer Graphics I
Lecture 20

Image Processing

Display Color Models
Filters
Dithering
Image Compression

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<http://www.cs.cmu.edu/~fp/courses/graphics/>

Displays and Framebuffers

- Image stored in memory as 2D pixel array, called framebuffer
- Value of each pixel controls color
- Video hardware scans the framebuffer at 60Hz
- Depth of framebuffer is information per pixel
 - 1 bit: black and white display (cf. Smithsonian)
 - 8 bit: 256 colors at any given time via colormap
 - 16 bit: 5, 6, 5 bits (R,G,B), $2^{16} = 65,536$ colors
 - 24 bit: 8, 8, 8 bits (R,G,B), $2^{24} = 16,777,216$ colors

Fewer Bits: Colormaps

- Colormaps typical for 8 bit framebuffer depth
- With screen $1024 * 768 = 786432 = 0.75$ MB
- Each pixel value is index into colormap
- Colormap is array of RGB values, 8 bits each
- All 2^{24} colors can be represented
- Only $2^8 = 256$ at a time
- Poor approximation of full color
- Who owns the colormap?
- Colormap hacks: affect image w/o changing framebuffer (only colormap)

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More Bits: Graphics Hardware

- 24 bits: RGB
- + 8 bits: A (α -channel for opacity)
- + 16 bits: Z (for hidden-surface removal)
- * 2: double buffering for smooth animation
- = 96 bits
- For $1024 * 768$ screen: 9 MB

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Image Processing

- 2D generalization of signal processing
- Image as a two-dimensional signal
- Point processing: modify pixels independently
- Filtering: modify based on neighborhood
- Compositing: combine several images
- Image compression: space-efficient formats
- Other topics (not in this course)
 - Image enhancement and restoration
 - Special effects (cf. Tuesday's lecture)
 - Computer vision

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Outline

- Display Color Models
- Filters
- Dithering
- Image Compression

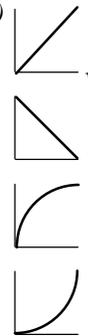
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Point Processing

- Input: $a(x,y)$; Output: $b(x,y) = f(a(x,y))$
- Useful for contrast adjustment, false colors
- Examples for grayscale, $0 \leq v \leq 1$
 - $f(v) = v$ (identity)
 - $f(v) = 1-v$ (negate image)
 - $f(v) = v^p$, $p < 1$ (brighten)
 - $f(v) = v^p$, $p > 1$ (darken)
- Gamma correction compensates monitor brightness loss



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Gamma Correction Example

$$\Gamma = 1.0; f(v) = v$$

$$\Gamma = 0.5; f(v) = v^{1/0.5} = v^2$$

$$\Gamma = 2.5; f(v) = v^{1/2.5} = v^{0.4}$$

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Signals and Filtering

- Audio recording is 1D signal: amplitude(t)
- Image is a 2D signal: color(x,y)
- Signals can be continuous or discrete
- Raster images are discrete
 - In space: sampled in x, y
 - In color: quantized in value
- Filtering: a mapping from signal to signal

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Linear and Shift-Invariant Filters

- Linear with respect to input signal
- Shift-invariant with respect to parameter
- Convolution in 1D
 - a(t) is input signal
 - b(s) is output signal
 - h(u) is filter
 - Shorthand: $b = a * h$ (= $h * a$, as an aside)
- Convolution in 2D

$$b(x, y) = \sum_{u=-\infty}^{+\infty} \sum_{v=-\infty}^{+\infty} a(u, v)h(x - u, y - v)$$

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Filters with Finite Support

- Filter $h(u,v)$ is 0 except in given region
- Represent h in form of a matrix
- Example: 3×3 blurring filter

$$b(x,y) = \frac{1}{9} \begin{pmatrix} a(x-1,y-1) & +a(x,y-1) & +a(x+1,y-1) \\ +a(x-1,y) & +a(x,y) & +a(x+1,y) \\ +a(x-1,y+1) & +a(x,y+1) & +a(x+1,y+1) \end{pmatrix}$$

- As function
$$h(u,v) = \begin{cases} \frac{1}{9} & \text{if } -1 \leq u, v \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

- In matrix form

$$\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

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Blurring Filters

- Average values of surrounding pixels
- Can be used for anti-aliasing
- Size of blurring filter should be odd
- What do we do at the edges and corners?
- For noise reduction, use median, not average
 - Eliminates intensity spikes
 - Non-linear filter

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Examples of Blurring Filter

Original Image

Blur 3x3 mask

Blur 7x7 mask

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Example Noise Reduction

Original image

Image with noise

Median filter (5x5?)

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Edge Filters

- Discover edges in image
- Characterized by large gradient

$$\nabla a = \begin{bmatrix} \frac{\partial a}{\partial x} & \frac{\partial a}{\partial y} \end{bmatrix}, \quad |\nabla a| = \sqrt{\left(\frac{\partial a}{\partial x}\right)^2 + \left(\frac{\partial a}{\partial y}\right)^2}$$

- Approximate square root

$$|\nabla a| \approx \left| \frac{\partial a}{\partial x} \right| + \left| \frac{\partial a}{\partial y} \right|$$

- Approximate partial derivatives, e.g.

$$\frac{\partial a}{\partial x} \approx a(x+1) - a(x-1)$$

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Sobel Filter

- Edge detection filter, with some smoothing
- Approximate

$$\frac{\partial}{\partial x} \approx \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, \quad \frac{\partial}{\partial y} \approx \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- Sobel filter is non-linear
 - Square and square root (more exact computation)
 - Absolute value (faster computation)

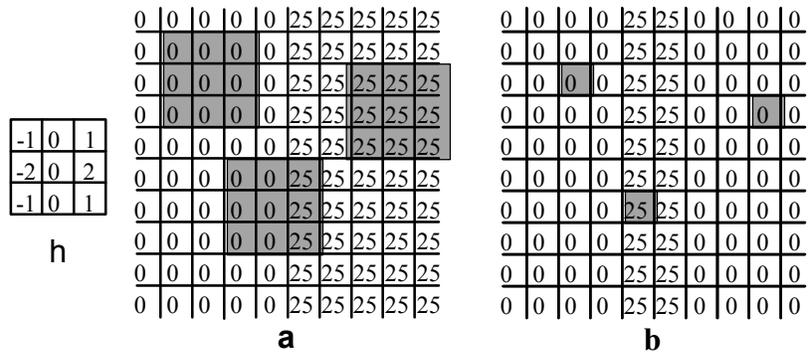
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Sample Filter Computation

- Part of Sobel filter, detects vertical edges



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Example of Edge Filter

Original image

Edge filter, then brightened

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Image Compositing

- Use α -channel (RGBA)
- Already discussed in this course
- Used for retouching and special effects
- Other image compositing techniques
 - Morphing
 - See Steve Sullivan's talk

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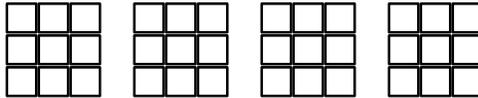
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Dithering

- Compensates for lack of color resolution
- Give up spatial resolution for color resolution
- Eye does spatial averaging
- Black/white dithering to achieve gray scale
 - Each pixel is black or white
 - From far away, color determined by fraction of white
 - For 3x3 block, 10 levels of gray scale



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Halftone Screens

- Regular patterns create some artefacts
 - Avoid stripes
 - Avoid isolated pixels (e.g. on laser printer)
 - Monotonicity: keep pixels on at higher intensities
- Example of good 3×3 dithering matrix
 - For intensity n , turn on pixels $0..n-1$

$$\begin{bmatrix} 6 & 8 & 4 \\ 1 & 0 & 3 \\ 5 & 2 & 7 \end{bmatrix}$$

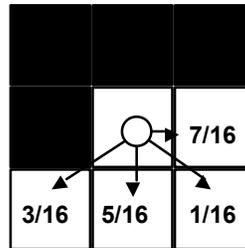
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Floyd-Steinberg Error Diffusion

- Approximation without fixed resolution loss
- Scan in raster order
- At each pixel, draw least error output value
- Divide error into 4 different fractions
- Add the error fractions into adjacent, unwritten pixels



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Floyd-Steinberg Example

Gray Scale Ramp

- Some worms
- Some checkerboards
- Enhance edges

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Color Dithering

- Example: 8 bit framebuffer
 - Set color map by dividing 8 bits into 3,3,2 for RGB
 - Blue is deemphasized since we see it less well
- Dither RGB separately
 - Works well with Floyd-Steinberg
- Assemble results into 8 bit index into colormap
- Generally looks good

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Image Compression

- Exploit redundancy
 - Coding: some pixel values more common
 - Interpixel: adjacent pixels often similar
 - Psychovisual: some color differences imperceptible
- Distinguish lossy and lossless methods

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Some Image File Formats

	Depth	File Size	Comments
JPEG	24	Small	Lossy compression
TIFF	8, 24	Medium	Good general purpose
GIF	1, 4, 8	Medium	Popular, but 8 bit
PPM	24	Big	Easy to read/write
EPS	1,2,4,8,24	Huge	Good for printing

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Image Sizes

- 1024*1024 at 24 bits uses 3 MB
- Encyclopedia Britannica at 300 pixels/inch and 1 bit/pixes requires 25 gigabytes (25K pages)
- 90 minute movie at 640x480, 24 bits per pixels, 24 frames per second requires 120 gigabytes
- Applications: HDTV, DVD, satellite image transmission, medial image processing, fax, ...

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Exploiting Coding Redundancy

- Not limited to images (text, other digital info)
- Exploit nonuniform probabilities of symbols
- Entropy as measure of information content
 - $H = -\sum_i \text{Prob}(s_i) \log_2 (\text{Prob}(s_i))$
 - If source is independent random variable need H bits
- Idea:
 - More frequent symbols get shorter code strings
 - Best with high redundancy (= low entropy)
- Common algorithms
 - Huffman coding
 - LZW coding (gzip)

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Huffman Coding

- Codebook is precomputed and static
 - Use probability of each symbol to assign code
 - Map symbol to code
 - Store codebook and code sequence
- Precomputation is expensive
- What is “symbol” for image compression?

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Lempel-Ziv-Welch (LZW) Coding

- Compute codebook on the fly
- Fast compression and decompression
- Can tune various parameters
- Both Huffman and LZW are lossless

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Exploiting Interpixel Redundancy

- Neighboring pixels are correlated
- Spatial methods for low-noise image
 - Run-length coding:
 - Alternate values and run-length
 - Good if horizontal neighbors are same
 - Can be 1D or 2D (e.g. used in fax standard)
 - Quadtrees:
 - Recursively subdivide until cells are constant color
 - Region encoding:
 - Represent boundary curves of color-constant regions
- Combine methods
- Not good on natural images directly

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Improving Noise Tolerance

- Predictive coding:
 - Predict next pixel based on prior ones
 - Output difference to actual
- Fractal image compression
 - Describe image via recursive affine transformation
- Transform coding
 - Exploit frequency domain
 - Example: discrete cosine transform (DCT)
 - Used in JPEG
- Transform coding for lossy compression

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Discrete Cosine Transform

- Used for lossy compression (as in JPEG)

$$F(u, v) = c(u)c(v) \sum_{x=0}^{n-1} \sum_{y=0}^{n-1} f(x, y) \cos \frac{(2x+1)u\pi}{2n} \cos \frac{(2y+1)v\pi}{2n}$$

where $c(u) = 1/\sqrt{n}$ if $u = 0$, $c(u) = \sqrt{2/n}$ otherwise

- JPEG (Joint Photographic Expert Group)
 - Subdivide image into $n \times n$ blocks ($n = 8$)
 - Apply discrete cosine transform for each block
 - Quantize, zig-zag order, run-length code coefficients
 - Use variable length coding (e.g. Huffman)
- Many natural images can be compressed to 4 bits/pixels with little visible error

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Summary

- Display Color Models
 - 8 bit (colormap), 24 bit, 96 bit
- Filters
 - Blur, edge detect, sharpen, despeckle
- Dithering
 - Floyd-Steinberg error diffusion
- Image Compression
 - Coding, interpixel, psychovisual redundancy
 - Lossless vs. lossy compression

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Preview

- Assignment 6 graded
- Tuesday: Scientific Visualization
- Assignment 7 due Tuesday
- Assignment 8 (written) out Tuesday