

Decoupling indexing from  
correctness for improved  
concurrency  
(and other good things)

15-712 Fall 2007

## Efficient Locking for Concurrent Operations on B-Trees.

**Lehman81:** Philip Lehman, S. Bing Yao.  
ACM Trans. on Database Systems  
(TODS), vol 6, no 4, December 1981.

## Guest Appearance

- The Chord Distributed Hash Table (DHT)

- Ion Stoica, Robert Morris, David Karger, M. Frans Kaashoek, and Hari Balakrishnan, *Chord: A Scalable Peer-to-peer Lookup Service for Internet Applications*, ACM SIGCOMM 2001, San Deigo, CA, August 2001, pp. 149-160.

## B-tree Index Access

- B-Trees common concurrent data structure
  - Indices for databases of all kinds
  - Good at fixed, short depth of tree for fast lookup
    - Based on all nodes having a min and max number of keys, and splitting or redistributing keys to nodes (rebalancing)
  - Insertion & deletion can change many nodes
    - if the tree becomes unbalanced, parent nodes must be updated, which can split or merge them, continuing up to the root

## Eg. Splitting a B-Tree

- Add item with key 47
  - Node for 47 is full
  - Split node into two
  - Add entry in parent
- If parent is full
  - Propagate split up
- Delete is messier still
  - To preserve constant depth, may need to rotate keys from a sibling or compress a whole level

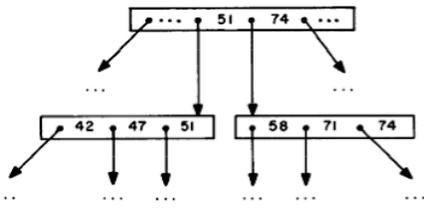
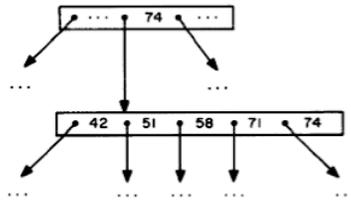


Fig. 4. Splitting a node after adding "47" ( $k = 2$ ).

## Concurrent Access Problems

- Indices are shared data structures with high concurrency
  - specialize concurrency control

```

search(15)
1. C ← read(x)
2.
3. examine C; get ptr to y
4.
5.
6.
7.
8.
9.
10. C ← read(y)
11. error: 15 not found!

insert(9)
A ← read(x)
examine A; get ptr to y
A ← read(y)
insert 9 into A; must split into A, B
put(B, y)
put(A, y)
Add to node x a pointer to node y.
    
```

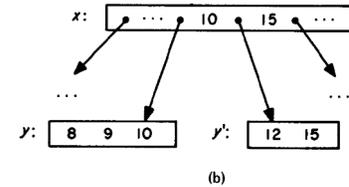
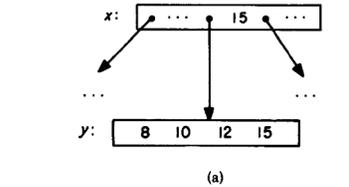


Fig. 5. Counterexample to naive approach.

## Lock-based Concurrency Control

- Used by most databases today for all applic code
  - Inside any transaction, all accessed data is protected by read/write locks & stored in shadow pages or undo logs (later lecture) until changes are committed & written
  - All locks acquired are held until transaction is done (!)
  - So concurrent transactions sharing any page are serialized by page locks, that is, with respect to shared pages, execute one at a time
  - Beware deadlocks -- if locks cannot be hierarchicalized, then detect lock cycles and break with abort & rollback

## Concurrent B-tree Access

- Simple: lock all nodes that might change as you look for point of insertion
  - But this locks top of tree, blocking everything else
- Bayer77: don't write lock top of tree on first try; hope splitting will not need to change top of tree
  - If wrong, abort and retry holding all write locks

## B-Link-Tree Example

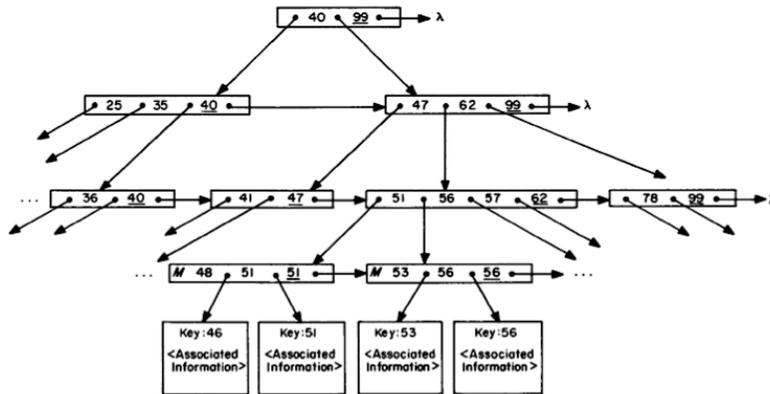


Fig. 7. A B<sup>+</sup>-tree.

## Lehman81: more concurrency

- Small maximum number of locks held (3)
- Readers are never blocked; tree is always valid
  - Reader may “miss” concurrent insertion
- B-link-tree adds same-level next-node link
  - New pointer points to node at same level with next key
  - Reader searching a node being split may see new “highest value” smaller than search key, & go on to next node
  - Effectively hides splitting from concurrent readers until the atomic update of the parent pointer
  - Writers only lock an individual node wrt other writers
  - Careful coding of split/rebalance needed
  - Useful for fast range scans too
- “Disk” ops get(), put() are indivisible (atomic)

## Readers never lock!

- What atomic ops make not locking work?

$x \leftarrow \text{scannode}(v, A)$  denotes the operation of examining the tree node in memory block  $A$  for value  $v$  and returning the appropriate pointer from  $A$  (into  $x$ ).

```

procedure search(v)
  current ← root;                               /* Get ptr to root node */
  A ← get(current);                             /* Read node into memory */
  while current is not a leaf do
  begin
    current ← scannode(v, A);                   /* Scan through tree */
    A ← get(current);                           /* Find correct (maybe link) ptr */
  end;                                          /* Read node into memory */

  while t ← scannode(v, A) = link ptr of A do  /* Now we have reached leaves. */
  begin
    current ← t;                               /* Keep moving right if necessary */
    A ← get(current);                           /* Get node */
  end;

  if v is in A then done "success" else done "failure"
  /* Now we have the leaf node in which v should exist. */
  
```

## Reading re-written

```

node n = root
while (n.type != TYPE_LEAF) {
  n = n.scan_for(key)
} /* log(n) */

while ((c = n.scan_for(key)) == n.link) {
  n = c
} /* linked list traversal */

if (n.contains(key)) return n.lookup(key)
return NULL
  
```

# Insertion

- Inserted value appears at step c, although f still not updated
- Is tree always balanced?
  - no? so why is approach used?
  - trade weakening of maximal comparisons for more concurrency

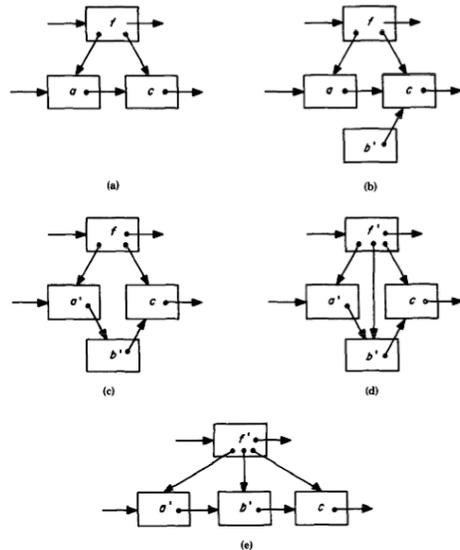


Fig. 8. Splitting node a into nodes a' and b'. (Note that (d) and (e) show identical structures.)

# Insertion

- Nasty code!
- Livelock possible
- Eraser would ....

```

procedure insert(v)
  initialize stack;
  current ← root;
  A ← get(current);
  while current is not a leaf do
    t ← current;
    current ← scanode(t, A);
    if new current was not link pointer in A then
      push(t);
      A ← get(current);
  endwhile;
  A ← get(current);
  A ← node.insert(A, u, v);
  put(A, current);
  unlock(current);
end else begin
  u ← allocate(1 new page for B);
  A, B ← rearrange old A, adding v and u, to make 2 nodes,
  where link ptr of A, link ptr of B) ← (u, link ptr of old A);
  y ← max value stored in new A;
  put(B, u);
  put(A, current);
  oldnode ← current;
  u ← u;
  w ← u;
  current ← pop(stack);
  lock(current);
  A ← get(current);
  move.right;
  unlock(oldnode);
  goto Doinserter;
end

procedure move.right
  while t ← scanode(t, A) is a link pointer of A do
    lock(t);
    unlock(current);
    current ← t;
    A ← get(current);
  endwhile;
end
    
```

# Deletion

- “allow fewer than k entries in a leaf node”
  - far simpler than one that requires underflows and concatenations
  - uses a “little” extra storage (and comparisons)
  - if needed defragment with batch reorganization locking whole tree
    - Possibly a cop-out: Slower worst-case
    - But may avoid unnecessary merges w/ later insert
- it would be better if there was a GFS-like background process renormalizing the B-link tree

# Eval

- Proof-based, part of theoretical DB work
  - Makes assumptions about primitives, OS functions and invariants (so proof must be tested :-)
- Some subsequent use of these methods
  - Boxwood at MSR
- Fragile code!
  - Not a database transaction ....
- Gives up balance properties for unknown duration
  - Worst case analysis gets worse, normal case better

## Context & Comparison

- Not transaction locking
  - May still need to ensure consistency btwn multiple read/writes (Kung does this; Lehman does not!)
- Thoughts?

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## Technique

- Correctness depends on link pointers
  - Some operations could (very rarely!) degrade to a linked-list traversal
- Similar in “feel” to some DHT techniques, like Chord
  - Consistent Hashing
  - Node IDs = hash(node IP), mapped in circular 128-bit (or whatever) key space
  - Items “belong” to successor node

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## Operation

- Node insertion:
  - Search for yourself in the ring
    - succ = ring\_search(me)
  - Update your predecessor
    - me.next = succ
    - pred.next = succ.prev
  - Quick insertion == *correctness*, but

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## Optimizing searches

- Finger table
  - Points 1/2, 1/4, 1/8th of way around the ring
    - How to find? Search for items in those spaces!
- Finger table (“index!”) correctness not critical for integrity
  - Can always fall back to linear search
  - But provides eventual efficiency

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## Points

- Decoupled optimization and correctness  
good for distributed implementation
  - Sagiv's B\*-link tree variant
  - Chord's "finger table"
  - Skip-list based approaches