



Large Graph Mining: Power Tools and a Practitioner's guide

Task 6: Virus/Influence Propagation

Faloutsos, Miller, Tsourakakis

CMU



Outline

- Introduction – Motivation
- Task 1: Node importance
- Task 2: Community detection
- Task 3: Recommendations
- Task 4: Connection sub-graphs
- Task 5: Mining graphs over time
- ➔ • **Task 6: Virus/influence propagation**
- Task 7: Spectral graph theory
- Task 8: Tera/peta graph mining: hadoop
- Observations – patterns of real graphs
- Conclusions



Detailed outline

- Epidemic threshold
 - Problem definition
 - Analysis
 - Experiments
- Fraud detection in e-bay



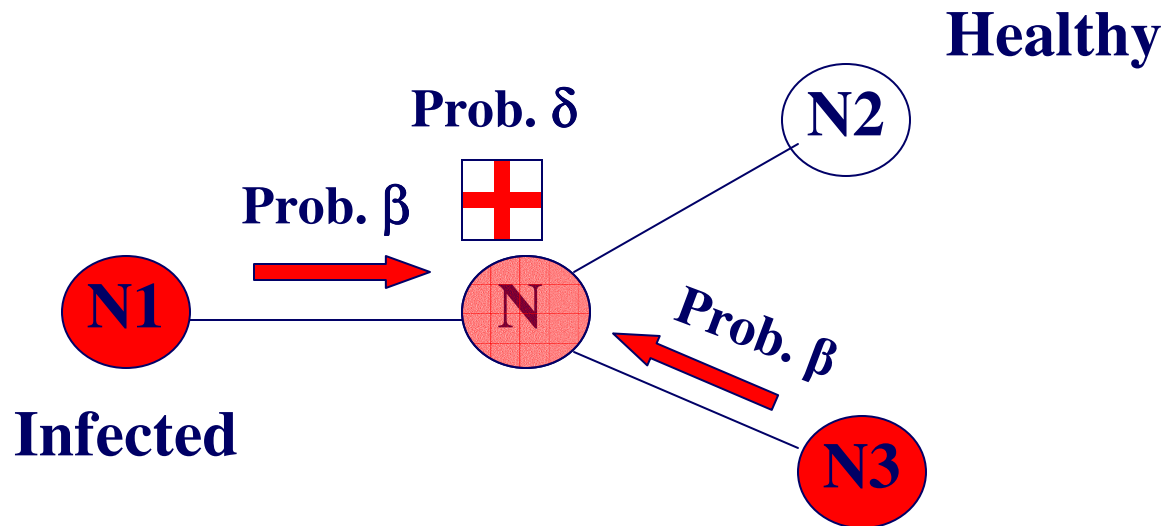
Virus propagation

- How do viruses/rumors propagate?
- Blog influence?
- Will a flu-like virus linger, or will it become extinct soon?



The model: SIS

- ‘Flu’ like: Susceptible-Infected-Susceptible
- Virus ‘strength’ $s = \beta / \delta$





Epidemic threshold τ

of a graph: the value of τ , such that

$$\text{if strength } s = \beta / \delta < \tau$$

an epidemic can not happen

Thus,

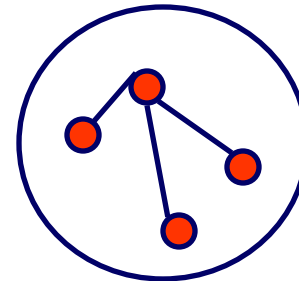
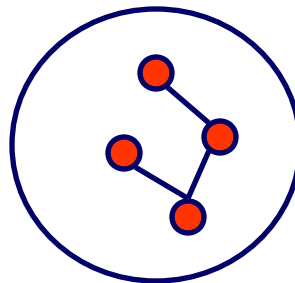
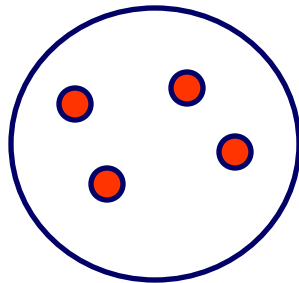
- given a graph
- compute its epidemic threshold



Epidemic threshold τ

What should τ depend on?

- avg. degree? and/or highest degree?
- and/or variance of degree?
- and/or third moment of degree?
- and/or diameter?





Epidemic threshold

- [Theorem 1] We have no epidemic, if

$$\beta/\delta < \tau = 1/\lambda_{1,A}$$



Epidemic threshold

- [Theorem 1] We have no epidemic (*), if

recovery prob. $\beta/\delta < \tau = 1/\lambda_{1,A}$ epidemic threshold

attack prob. β/δ

largest eigenvalue of adj. matrix A

Proof: [Wang+03]

(*) under mild, conditional-independence assumptions



Beginning of proof

Healthy @ t+1:

- (healthy or healed)
- and not attacked @ t

Let: $p(i, t) = \text{Prob node } i \text{ is sick @ } t+1$

$$1 - p(i, t+1) = (1 - p(i, t) + p(i, t) * \delta) * \prod_j (1 - \beta a_{ji} * p(j, t))$$

Below threshold, if the above *non-linear dynamical system* above is 'stable' (eigenvalue of Hessian < 1)



Epidemic threshold for various networks

Formula includes older results as special cases:

- Homogeneous networks [Kephart+White]
 - $\lambda_{I,A} = \langle k \rangle$; $\tau = 1/\langle k \rangle$ ($\langle k \rangle$: avg degree)
- Star networks (d = degree of center)
 - $\lambda_{I,A} = \text{sqrt}(d)$; $\tau = 1/\text{sqrt}(d)$
- Infinite power-law networks
 - $\lambda_{I,A} = \infty$; $\tau = 0$; [Barabasi]



Epidemic threshold

- [Theorem 2] Below the epidemic threshold, the epidemic dies out exponentially

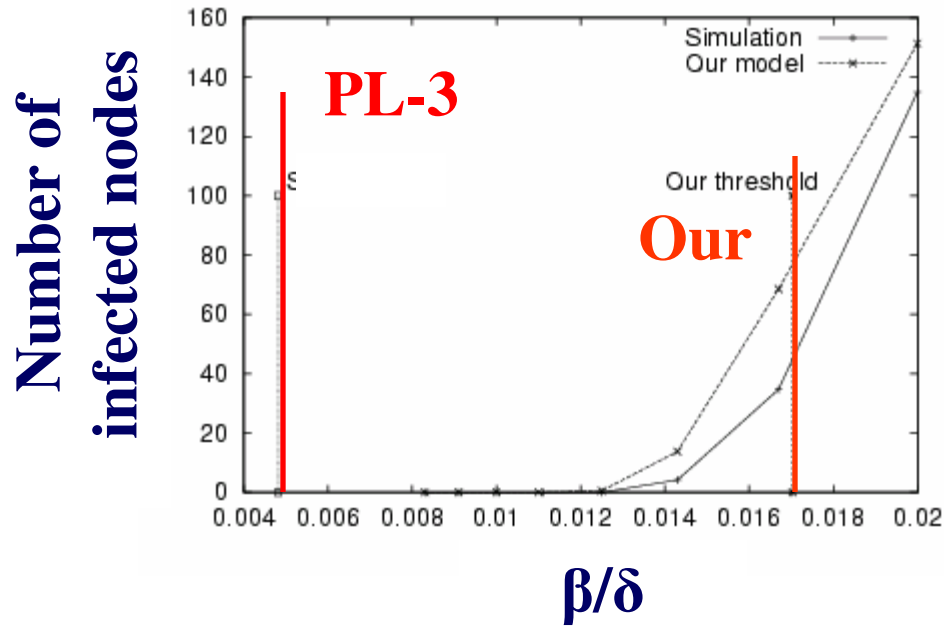


Detailed outline

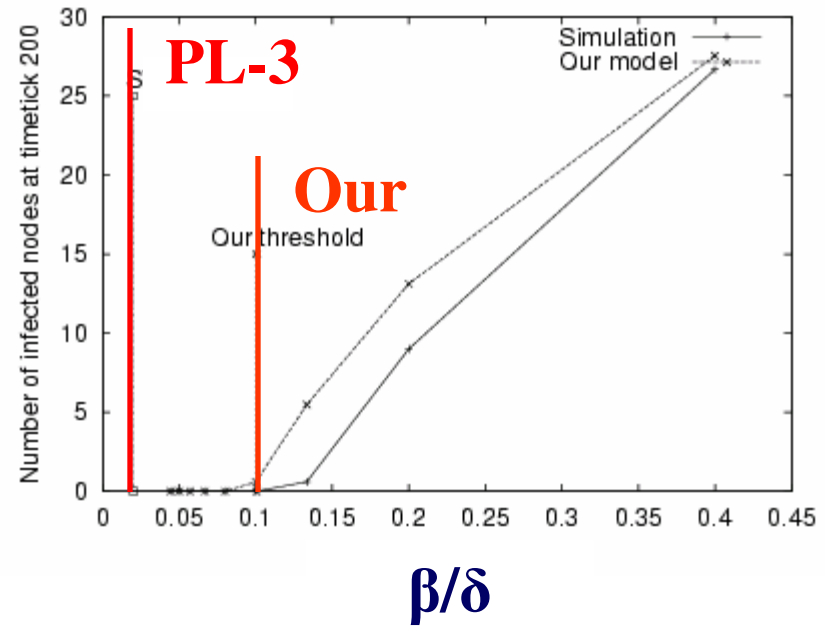
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Current prediction vs. previous



Oregon

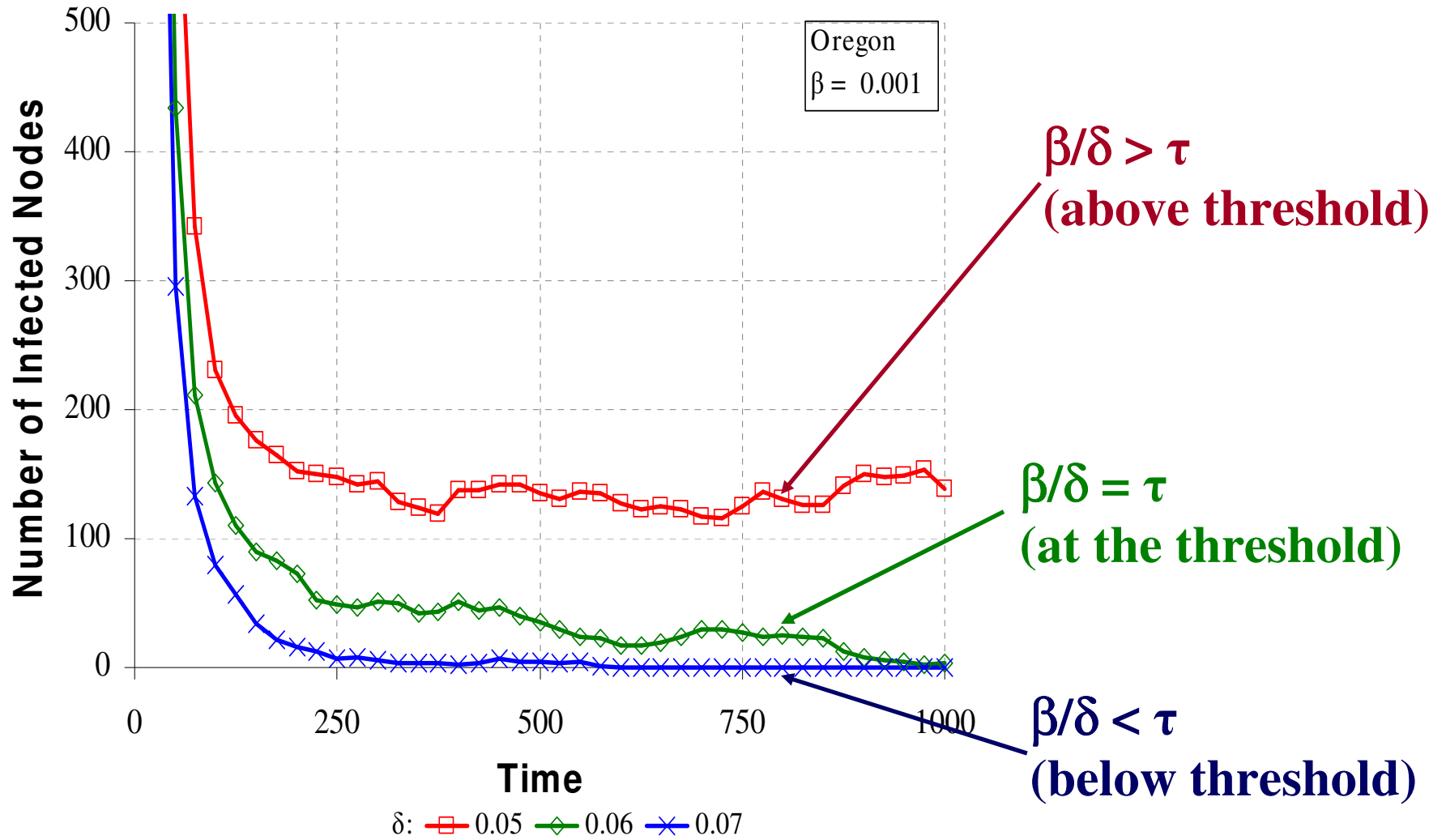


Star

The formula's predictions are more accurate



Experiments (Oregon)

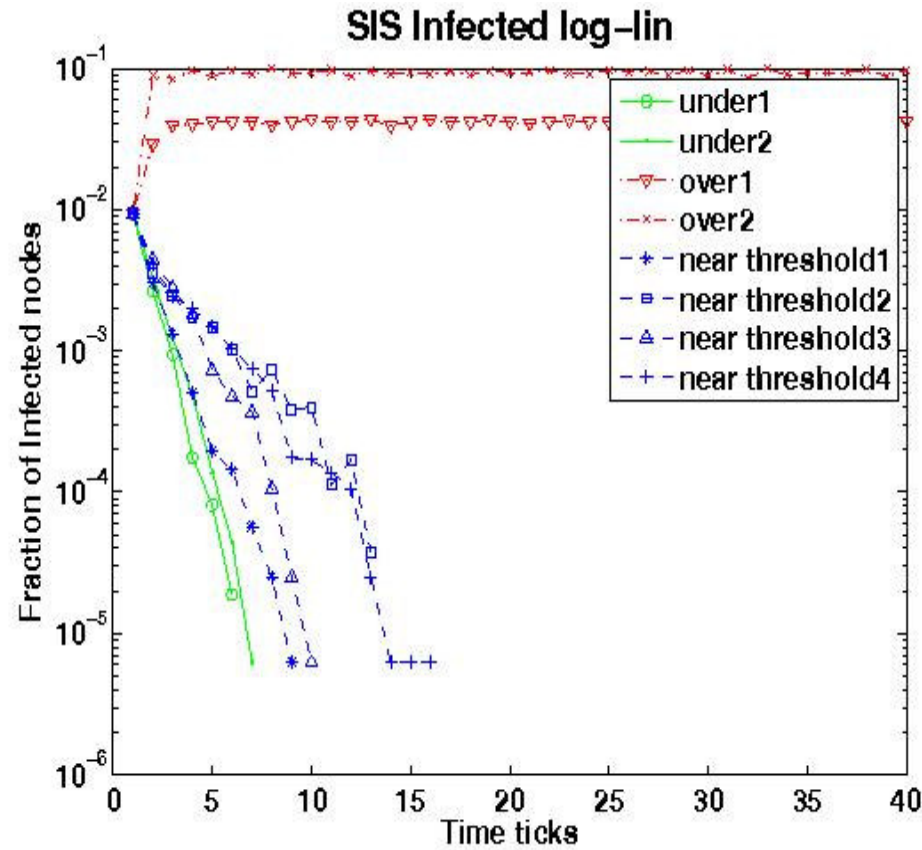




SIS simulation - # infected nodes vs time

Log - Lin

#inf.
(log scale)



— above
— at
— below

Time (linear scale)

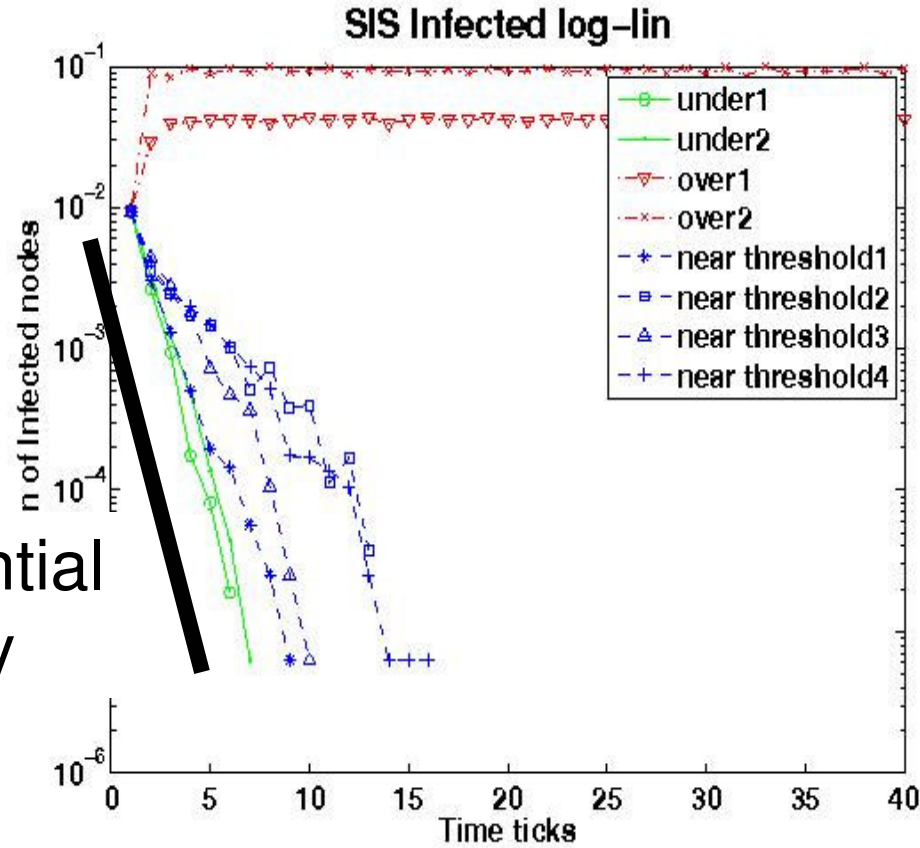


SIS simulation - # infected nodes vs time

Log - Lin

#inf.
(log scale)

Exponential
decay



— above
 — at
 — below

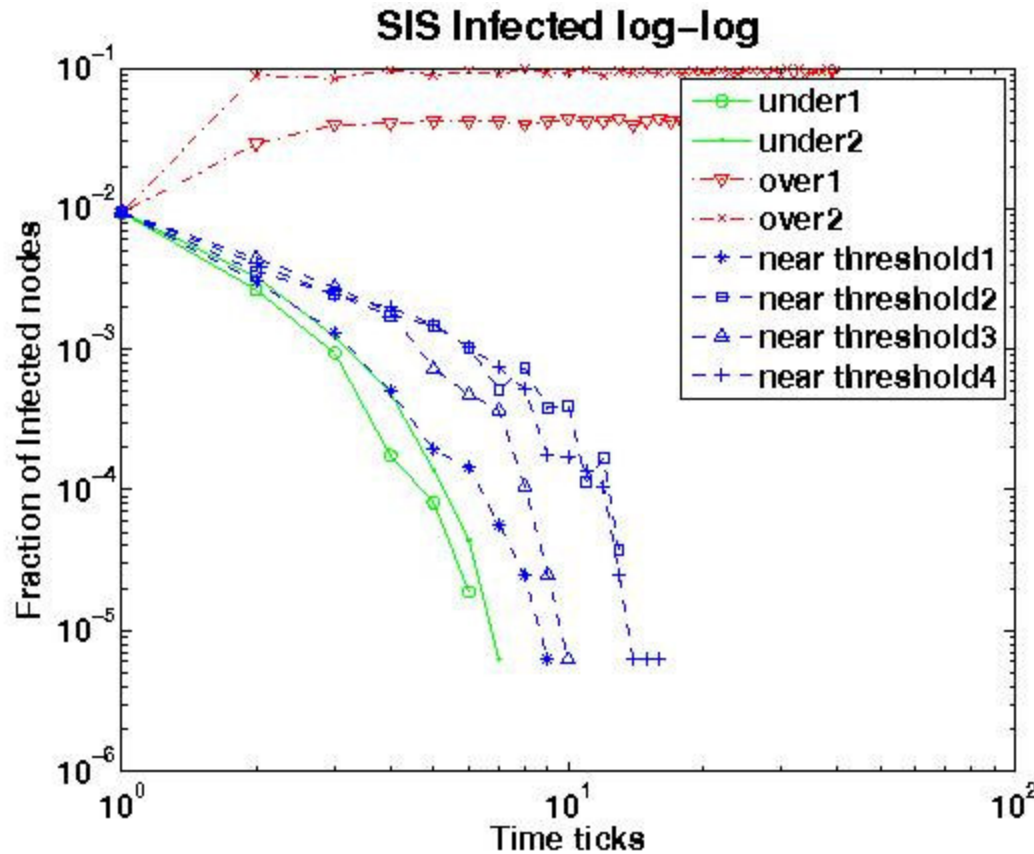
Time (linear scale)



SIS simulation - # infected nodes vs time

Log - Log

#inf.
(log scale)



— above
— at
— below

Time (log scale)

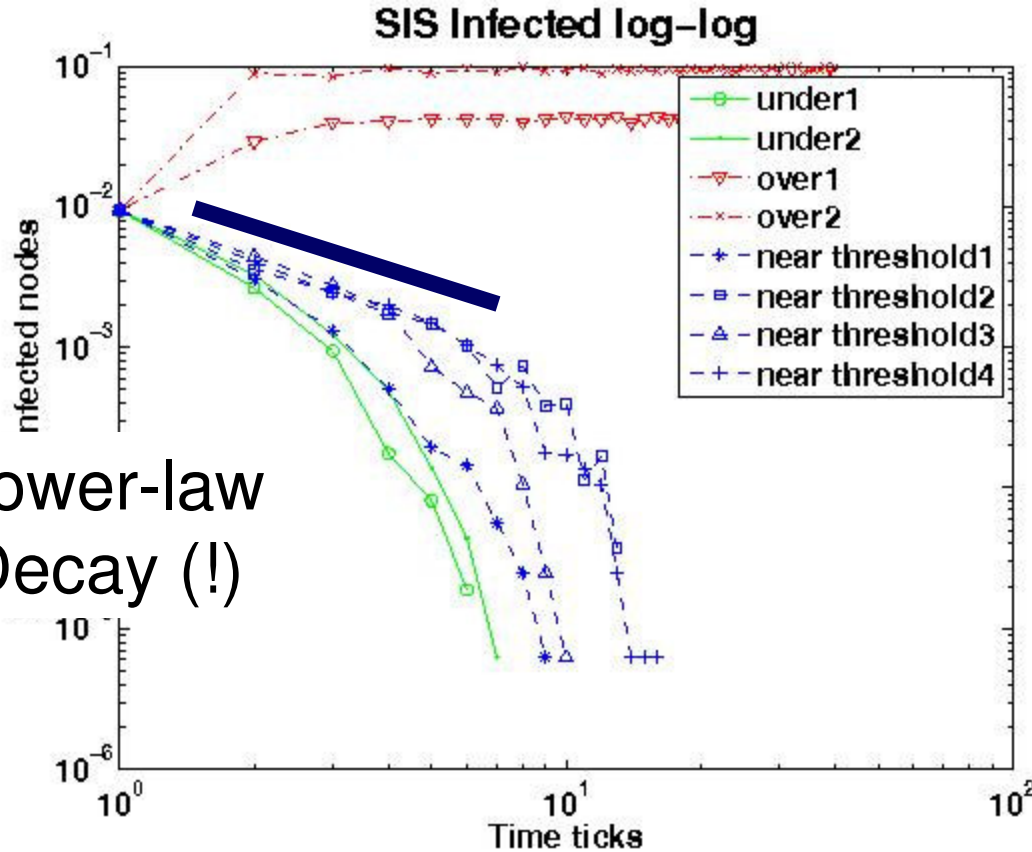


SIS simulation - # infected nodes vs time

Log - Log

#inf.
(log scale)

Power-law
Decay (!)



- above
- at
- below



Detailed outline

extra

- Epidemic threshold
- ➔ • Fraud detection in e-bay

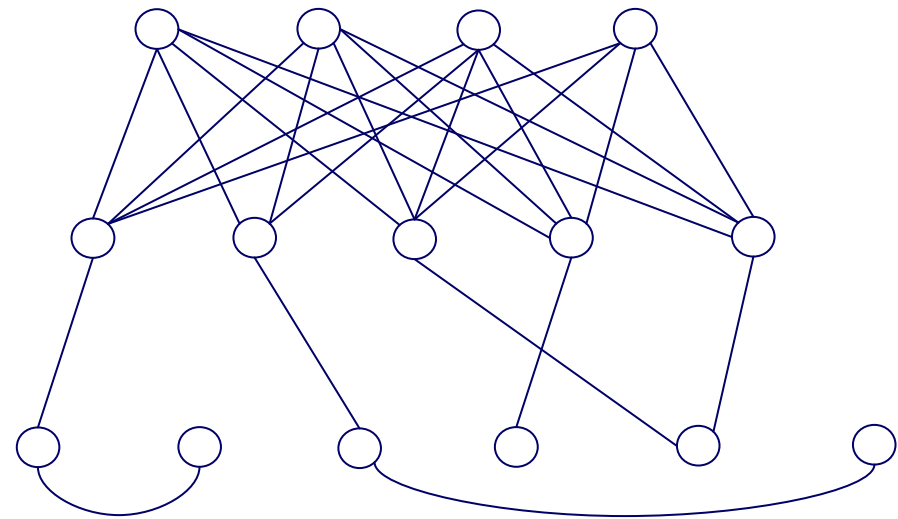


E-bay Fraud detection

extra



w/ Polo Chau &
Shashank Pandit, CMU



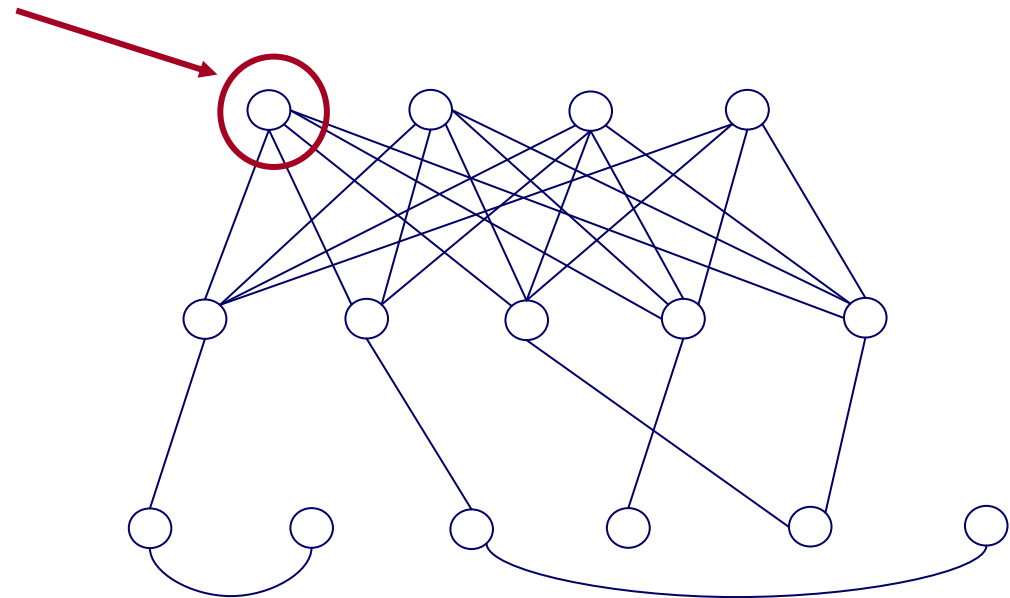
NetProbe: A Fast and Scalable System for Fraud Detection in Online Auction Networks, S. Pandit, D. H. Chau, S. Wang, and C. Faloutsos (*WWW'07*), pp. 201-210



E-bay Fraud detection

extra

- lines: positive feedbacks
- would you buy from him/her?

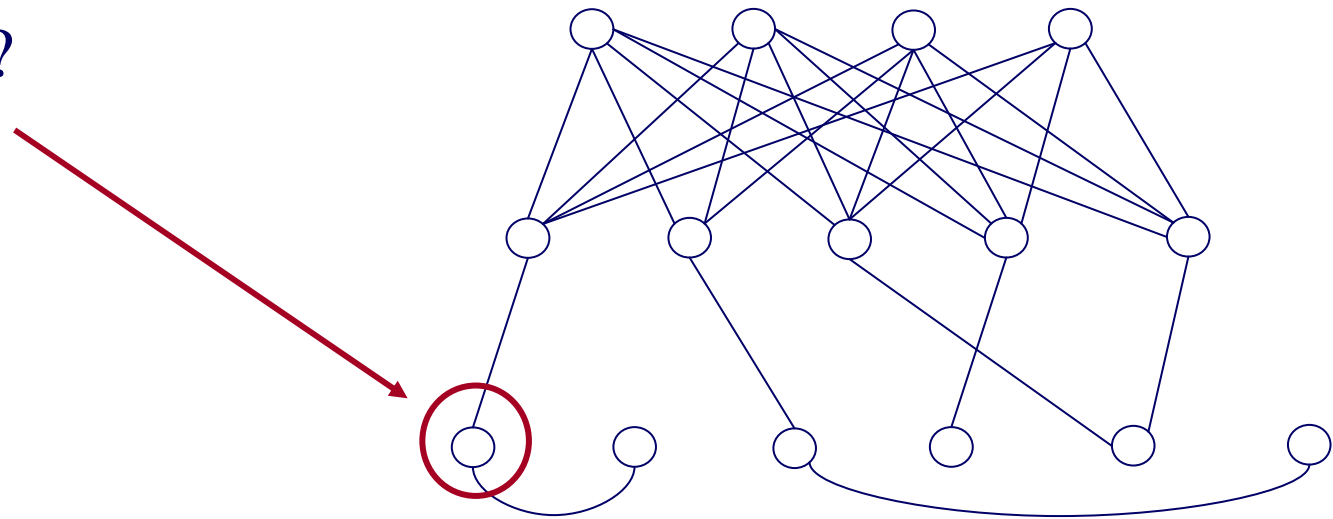




E-bay Fraud detection

extra

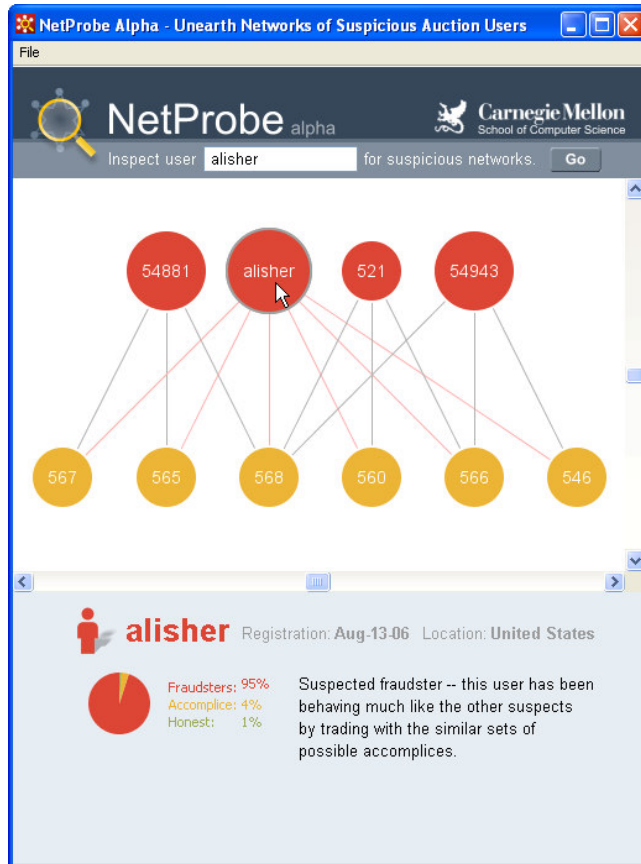
- lines: positive feedbacks
- would you buy from him/her?
- or him/her?



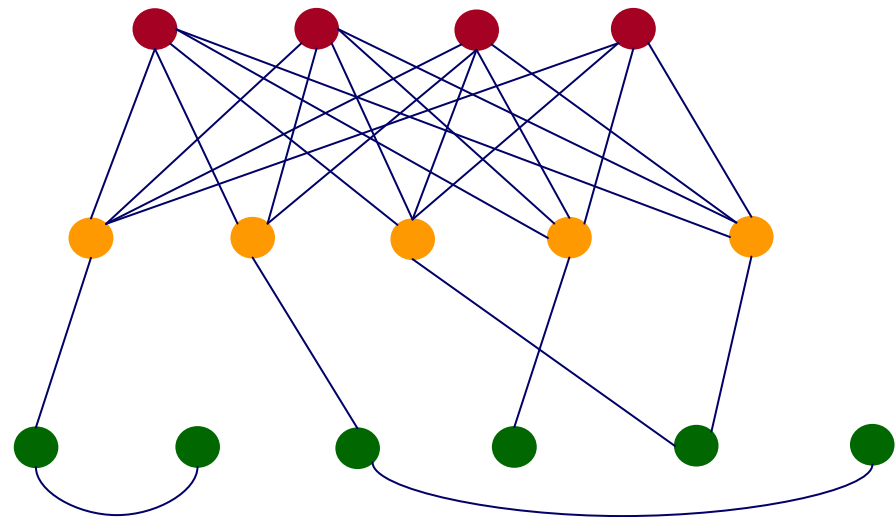


E-bay Fraud detection - NetProbe

extra



Belief Propagation gives:





Conclusions

- $\lambda_{I,A}$: Eigenvalue of adjacency matrix determines the survival of a flu-like virus
 - It gives a measure of how well connected is the graph (\sim # paths – see Task 7, later)
 - May guide immunization policies
- [Belief Propagation: a powerful algo]



References

- D. Chakrabarti, Y. Wang, C. Wang, J. Leskovec, and C. Faloutsos, *Epidemic Thresholds in Real Networks*, in ACM TISSEC, 10(4), 2008
- Ganesh, A., Massoulié, L., and Towsley, D., 2005. The effect of network topology on the spread of epidemics. In *INFOCOM*.



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- Hethcote, H. W. AND Yorke, J. A. 1984. *Gonorrhea Transmission Dynamics and Control*. Vol. 56. Springer. Lecture Notes in Biomathematics.



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- Y. Wang, D. Chakrabarti, C. Wang and C. Faloutsos, *Epidemic Spreading in Real Networks: An Eigenvalue Viewpoint*, in SRDS 2003 (pages 25-34), Florence, Italy