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Hint: This is an old school handwritten exam. There is no authenticated login. If we can't read your AndrewID, we won't easily know who should get credit for this exam. If we can't read either your AndrewID or Full Name, we're in real bind. Please write neatly :-)

## 18-213/18-613, Fall 2021 Final Exam

Makeup-Backup

Instructions:

- Make sure that your exam is not missing any sheets (check page numbers at bottom)
- Write your Andrew ID and full name on this page (and we suggest on each and every page)
- This exam is closed book and closed notes (except for 2 double-sided note sheets).
- You may not use any electronic devices or anything other than what we provide, your notes sheets, and writing implements, such as pens and pencils.
- Write your answers in the space provided for the problem.
- If you make a mess, clearly indicate your final answer.
- The exam has a maximum score of 100 points.
- The point value of each problem is indicated.
- Good luck!

| Problem \# | Scope | Max Points | Score |
| :---: | :--- | :---: | :---: |
| 1 | Data Representation: "Simple" Scalars: Ints and Floats | 10 |  |
| 2 | Data Representation: Arrays, Structs, Unions, and Alignment | 10 |  |
| 3 | Assembly, Stack Discipline, Calling Convention, and x86-64 ISA | 15 |  |
| 4 | Caching, Locality, Memory Hierarchy, Effective Access Time | 15 |  |
| 5 | Malloc(), Free(), and User-Level Memory Allocation | 10 |  |
| 6 | Virtual Memory, Paging, and the TLB | 15 |  |
| 7 | Process Representation and Lifecycle + Signals and Files | 10 |  |
| 8 | Concurrency Control: Maladies, Semaphores, Mutexes, BB, RW | 15 |  |
| TOTAL | Total points across all problems | $\mathbf{1 0 0}$ |  |

## Question 1: Representation: "Simple" Scalars (10 points)

## Part A: Integers (5 points, 1 point per blank)

Assume we are running code on two machines using two's complement arithmetic for signed integers.

- Machine 1 has 4-bit integers
- Machine 2 has 8 -bit integers.

Fill in the five empty boxes in the table below when possible and indicate "UNABLE" when impossible.

|  | Machine 1: 4-bit <br> w/2s complement signed | Machine 2: 8-bit <br> w/2s complement signed |
| :--- | :--- | :--- |
| Binary representation of 11 <br> decimal |  |  |
| Binary representation of -6 <br> decimal |  |  |
| Binary representation of - <br> Tmin |  |  |
| Binary representation of -1 <br> decimal |  |  |

## Continued on next page.

## Part B: Floats (5 points, $1 / 2$ point per blank)

For this problem, please consider a floating point number representation based upon an IEEE-like floating point format as described below.

- Format A :
- There are 6 bits
- There is 1 sign bit $s$.
- There are $k=3$ exponent bits.
- You need to determine the number of fraction bits.
- Format B:
- There are 6 bits
- There is 1 sign bit s .
- There are $\mathrm{n}=3$ fraction bits.

Fill in the empty (non grayed-out) boxes on the net page as instructed

|  | Format A | Format B |
| :---: | :---: | :---: |
| Total Number of Bits (Decimal) | 6 | 6 |
| Number of Sign Bits (Decimal) | 1 | 1 |
| Number of Fraction Bits (Decimal) |  |  |
| Number of Exponent Bits (Decimal) | 3 |  |
| Bias <br> (Decimal) |  |  |
| -Infinity <br> (Binary bit pattern) |  |  |
| $101010$ <br> (Decimal value, unrounded) |  |  |
| 000010 <br> (Decimal value, unrounded) |  |  |
| $\begin{aligned} & 0 \\ & \text { (Binary bit pattern) } \end{aligned}$ |  |  |
| $\begin{aligned} & / / x, y, \text { and } z \text { are floats } \\ & \left(x^{*} y / z\right)==\left(x / z^{*} y\right) \end{aligned}$ | Circle one: <br> Always equal <br> Always unequal <br> It depends |  |

## Question 2: Representation: Arrays, Structs, Unions, Alignment, etc. (10 points)

## Part A: Arrays (5 points)

Consider the following code running in an x86-64 system with 8-byte pointers and 4-byte ints. Assume it successfully prints each and every element of the numbers array.

```
void fn(int **numbers) {
    for (int row=0; row < 3; row++)
        for (int col=0; col < 2; col++)
            printf ("numbers[%d][%d]=%d", row, col, numbers[row][col]);
}
```

2(A)(1) (1 point): How many bytes are allocated to numbers? (Write "UNKNOWN" if not knowable).
Hint: Think sizeof()

2(A)(2) (1 point): What is the minimum size of the memory allocation directly referenced by numbers?

2(A)(3) (3 points) Write C Language code to free all dynamic memory associated with numbers. It is not necessary to set the numbers pointer to NULL once done.

```
void fn(int **numbers) {
```

\}

## Continued on next page.

## Question 2: Representation: Arrays, Structs, Unions, Alignment, etc. (10 points)

## Part B: Structs, Unions, and Alignment (5 points)

For this question please assume "Natural alignment", in other words, please assume that each type must be aligned to a multiple of its data type size.

Please consider the following struct:

```
struct {
    char c1; // 1-byte type
    int i; // 4-byte type
    char c2;
} partB;
```

2(B)(1) (1 point): What would you expect to be the value of the expression below?

```
sizeof(struct partB)
```

2(B)(2) (1 points): Rewrite the struct above to minimize its size after alignment-mandated padding:

Soln: Answers may vary but should all be the same size as this:
struct \{
\} partB;

2(B)(3) (1 points): How many bytes are required for the struct you designed for 2(B)(2) above?

## Continued on next page.

2(B)(3) (1 points): How many bytes are required for the following union? Hint: Think sizeof()

```
union {
    int i; // 4-byte type
    short s; // 2-byte type
    long l; // 8-byte type
} u;
```

2(B)(4) (1 points): Given the definition above and the code below, and assuming an x86-64 host, is the code below guaranteed to print the same value twice? Why or why not?

```
union u;
scanf("%d", &u.i);
printf ("%d\n", u.i);
printf ("%ld\n", u.l);
```


## Question 3: Assembly, Stack Discipline, Calling Convention, and x86-64 ISA

## Part A: Loops and Calling Convention (7 points)

Consider the following code:

```
function:
. LFB0:
    pushq }\quad\mathrm{ %rbp 
    subq $32, %rsp
    movl %edi, -20(%rbp)
    movl %esi, -24(%rbp)
    movl -20(%rbp), %eax
    movl %eax, -4 (%rbp)
    jmp .L2
.L5:
    movl $0, -8(%rbp)
    jmp .L3
.L4:
    addl $1, -8(%rbp)
.L3:
    movl -8(%rbp), %eax
    cmpl -4(%rbp), %eax
    jl .L4
    movl $88, %edi # 88 is ASCII for 'X'
    call putchar
    movl $10, %edi # 10 is ASCII for '\n'
    call putchar
    addl $1, -4(%rbp)
.L2 :
    movl -4(%rbp), %eax
    cmpl -24(%rbp), %eax
    jl .L5
    nop
    leave
    ret
```

3(A)(1) (2 points): How many loops does this function have? How do you know?

3(A)(2) (1 points): How many arguments does this function receive (and use)?

Continued on next page.

3(A)(3) (2 points): For each argument you listed, please indicate either (a) which specific register was used to pass it in, or (b) that it was sourced from the stack (you don't need to give the address). Please leave any extra blanks empty (Hint: You won't need all of them).

| Argument | Specific register or "Stack" |
| :--- | :--- |
| 1st |  |
| 2nd |  |
| 3rd |  |
| 4th |  |
| 5th |  |

Consider the following function activation. Consistent with your answer to the question above, it includes more arguments that the function actually requires. Please ignore any extra arguments.
function(10, 9, 8, 7, 6);
3(A)(2) (2 points): How many times does the inner-most loop run?
Hint: If the inner-most loop is nested, you may need to consider the loops in which it is nested.

## Continued on next page.

## Part B: Conditionals (8 points)

Consider the following code:

```
(gdb) disassemble function
Dump of assembler code for function function:
    0x0000000000400533 <+0>: cmp %esi,%edi
    0x0000000000400535 <+2>: jg 0x400561 <function+46>
    0x0000000000400537 <+4>: cmp $0x5,%edi
    0x000000000040053a <+7>: ja 0x400557 <function+36>
    0x000000000040053c <+9>: mov %edi,%eax
    0x000000000040053e <+11>: jmpq *0x400630(,%rax,8)
    0x0000000000400545 <+18>: mov $0x1,%edi
    0x000000000040054a <+23>: mov %edi,%eax
    0x000000000040054c <+25>: imul %edi,%eax
    0x000000000040054f <+28>: add %edi,%eax
    0x00000000000400551 <+30>: retq
    0x0000000000400552 <+31>: mov $0xffffffec,%edi
    0x0000000000400557 <+36>: mov %edi,%eax
    0x0000000000400559 <+38>: shr $0x1f,%eax
    0x000000000040055c <+41>: add %edi,%eax
    0x000000000040055e <+43>: sar %eax
    0x0000000000400560<+45>: retq $0xffffffffe%eax
    0x0000000000400566<+51>: retq <
    0x00000000000400567<+52>: mov $0x8,%eax
    0x000000000040056c <+57>: retq
End of assembler dump.
```

Consider also the following memory dump:

| (gdb) $\mathrm{x} / 10 \mathrm{gx}$ | 0620 |  |
| :---: | :---: | :---: |
| 0x400620: | 0x0000000000020001 | 0x0000000000000000 |
| 0x400630: | 0x0000000000400545 | 0x000000000040054a |
| 0x400640: | 0x0000000000400557 | 0x000000000040054a |
| 0x400650: | 0x0000000000400567 | 0x0000000000400552 |
| 0x400660: | 0x000000443b031.b01 | 0xfffffda000000007 |

## Continued on next page.

(3)(B)(1) (1 points): How many "if statements" are likely present in the C Language code from which this assembly was compiled? At what address of the assembly code shown above does each occur?

This code was compiled from C Language code containing a switch statement. Please do not include any "if statement" present in the assembly that is likely part of the switch statement in the original C code, i.e. do not count any "if statement" that is used to manage one or more "cases" of a "switch statement".
(3)(B)(2) (2 points): What integer input values are managed by non-default cases of the switch statement? How do you know?
(3)(B)(3) (1 point): Is there a default case? If so, at what address does it begin? How do you know?
(3)(B)(4) (2 points): Which case(s), if any, share exactly the same code? How do you know?
(3)(B)(5) (2 points): Which case(s), if any, fall through to the next case after executing some of their own code? How do you know?

## Question 4: Caching, Locality, Memory Hierarchy, Effective Access Time (15 points)

## Part A: Caching (8 points)

Given a model described as follows:

- Number of sets: 2
- Total size: 48 bytes (not counting meta data)
- Block size: 8 bytes/block
- Replacement policy: Set-wise LRU
- 8-bit addresses

4(A)(1) (1 point) How many bits for the block offset?

4(A)(2) (1 point) How many blocks per set?

4(A)(3) (1 point) How many bits for the tag?

4(A)(4) (5 points, $1 / 2$ point each): For each of the following addresses, please indicate if it hits, or misses, and if it misses, if it suffers from a capacity miss, a conflict miss, or a cold miss:

| Address | Circle one <br> (per row): | Circle one <br> (per row): |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0xF1 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0xA2 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0xAB | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0XF7 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0X5C | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0XF9 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0X00 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0X87 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0XA1 | Hit | Miss | Capacity | Cold | Conflict | N/A |
| 0XA2 | Hit | Miss | Capacity | Cold | Conflict | N/A |

## Part B: Locality (4 points)

4(B)(1) (2 points): Consider the following code:

```
int array[SIZE1][SIZE2];
int sum=0;
for (int outer=0; outer<SIZE1; outer+=STEP)
    for (int inner=0; inner<(SIZE2-1); inner++)
    sum += array[inner][outer] + 2*array[inner][outer+1];
```

Considering only access to "array", as "step" increases (significantly), please mark how each type of locality would be impacted. Please also explain why in the space provided.

| Spatial | Decrease | Increase | Unaffected |
| :--- | :--- | :--- | :--- |
| Temporal | Decrease | Increase | Unaffected |

4(B)(2) (2 points): Consider the following code:

```
int array[ROWS][COLS];
int array2[ROWS][COLS];
int sum=0;
for (int row=0; index<ROWS; row ++)
    for (int col=0; col<(COLS-1); col ++)
        sum += array[col][row] + array2[row][col+1];
```

Imagine arrays extremely large in all dimensions, an int size of 4 bytes, and a cache block size of 16 bytes. To the nearest whole percent or simple fraction, what would you expect the combined miss rate for accesses to "array" and "array2" within the inner loop to be? Why?

## Continued on next page.

## Part C: Memory Hierarchy and Effective Access Time (3 points)

Imagine a system with a main memory layered beneath a cache:

- The cache has a 10 nS access time.
- The overall effective access time is 11 nS .
- The cache miss rate is $1 \%$.
- In the event of a miss, memory access time and cache access time do not overlap: They occur $100 \%$ sequentially, one after the other.


## FOR SIMPLICITY, AVOID COMPLEX CALCULATION AND LEAVE YOUR ANSWER AS A SIMPLE FRACTION

What is the main memory access time?

MEMORY_ACCESS_TIME=

## Question 5: Malloc(), Free(), and User-Level Memory Allocation (10 points)

Consider the following code:

```
#define N 4
void *pointers[N];
int i;
for (i = 0; i < N; i++) {
    pointers[i] = malloc(6);
}
for (i = 0; i < N; i++) {
    free(pointers[i]);
}
for (i = 0; i < N; i++) {
    pointers[i] = malloc(42);
}
```

And a malloc implementation as below:

- Implicit list
- Headers of size 8 bytes
- No footers.
- Every block is always constrained to have a size a multiple of 8 (In order to keep payloads aligned to 8 bytes).
- The header of each block stores the size of the block, and since the 3 lowest order bits are guaranteed to be 0 , the lowest order bit is used to store whether the block is allocated or free.
- A first-fit allocation policy is used.
- If no unallocated block of a large enough size to service the request is found, sbrk is called for the smallest multiple of 8 that can service the request.
- The heap is unallocated until it grows in response to the first malloc.
- No coalescing or block splitting is done.

NOTE: You do NOT need to simplify any mathematical expressions. Your final answer may include multiplications, additions, and divisions.

## Continued on next page.

4(A) ( $\mathbf{2}$ points) After the given code sample is run, how many total bytes have been requested via sbrk? In other words, how many bytes are allocated to the heap?

4(B) (2 points) After the given code sample is run, how many of those bytes are used for currently allocated blocks (vs currently free blocks), including internal fragmentation and header information?

4(C) (2 points) After the given code sample is run, how many of those bytes are used to store free blocks (versus currently allocated blocks), including header information?

4(D)(2 points) After the given code sample is run, how much internal fragmentation is there (Answer in bytes)? (Hint: Free blocks have no internal fragmentation).

4(E)(2 points) After the given code sample is run, how many bytes smaller would the heap be if constant-time (immediate) coalescing were employed?

## 6. Virtual Memory, Paging, and the TLB (15 points)

This problem concerns the way virtual addresses are translated into physical addresses. Imagine a system has the following parameters:

- Virtual addresses are 16 bits wide.
- Physical addresses are 12 bits wide.
- The page size is 128 bytes.
- The TLB is 2-way set associative with 16 total entries.
- A single level page table is used


## Part A: Interpreting addresses

6(A)(1)( 1 points): Please label the diagram below showing which bit positions are interpreted as each of the PPO and PPN. Leave any unused entries blank.

| Bit | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| PPN/ <br> PPO |  |  |  |  |  |  |  |  |  |  |  |  |

6(A)(2)( 1 points): Please label the diagram below showing which bit positions are interpreted as each of the VPO and VPN (top line) and each of the TLBI and TLBT (bottom line). Leave any unused entries blank.

| Bit | 15 | 14 | 13 | 12 | 11 | 10 | 9 | 8 | 7 | 6 | 5 | 4 | 3 | 2 | 1 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| VPO/ <br> VPN |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| TLBI/ <br> TLBT |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

6(A)(3) (1 points): How many entries exist within each page table? Hint: This is the same as the total number of pages within each virtual address space.

Continued on next page.

## Part B: Hits and Misses (12 points)

Shown below are a partial TLB and partial page table.
TLB:

| Index | Tag | PPN | Valid | Scratch space for you |
| :--- | :--- | :--- | :--- | :--- |
| 0 | $0 \times 0 \mathrm{~A}$ | 6 | 1 |  |
| 0 | $0 \times 1 \mathrm{~B}$ | 2 | 0 |  |
| 1 | $0 \times 24$ | 11 | 0 |  |
| 1 | $0 \times 31$ | 5 | 0 |  |
| 2 | $0 \times 35$ | 7 | 0 |  |
| 2 | $0 \times 2 \mathrm{~A}$ | 10 | 0 |  |
| 3 | $0 \times 19$ | 12 | 0 |  |
| 3 | $0 \times 02$ | 16 | 0 |  |
| 4 | $0 \times 18$ | 13 | 0 |  |
| 4 | $0 \times 20$ | 15 | 0 |  |

Page Table:

| Index/VPN | PPN | Valid | Scratch space for you |
| :--- | :--- | :--- | :--- |
| 96 | 3 | 1 |  |
| 208 | 12 | 1 |  |
| 289 | 4 | 0 |  |
| 384 | 6 | 1 |  |

For each address shown below, please indicate if it is a TLB Hit or Miss, whether or not it is a page fault, or if either can't be determined from the information provided.
Additionally, if knowable from the information provided, please provide the valid PPN

| Virtual <br> Address | TLB <br> Hit or Miss? | Page Fault? <br> Yes or No | PPN <br> If Knowable |
| :--- | :--- | :--- | :--- |
| $0 \times 6008$ | Hit Miss Not knowable | Yes No Not knowable |  |
| $0 \times D 010$ | Hit Miss Not knowable | Yes No Not knowable |  |
| $0 \times 1800$ | Hit Miss Not knowable | Yes No Not knowable |  |
| $0 \times 9080$ | Hit Miss Not knowable | Yes No Not knowable |  |

## Question 7: Process Representation and Lifecycle + Signals and Files (10 points)

## Part A (3 points):

Please consider the following code:

```
void main(){
    printf ("A"); fflush(stdout);
        fork();
        printf ("C"); fflush(stdout);
        if (!fork()) {
            printf ("D"); fflush(stdout);
        } else {
            printf ("B"); fflush(stdout);
        }
}
```

7(A)(1) (1 points): Give one possible output string

7(A)(2) (1 points): Give one output string that has the correct output characters (and number of each character), but in an impossible order.

7(A)(3) (1 points): Why can't the output you provided in 7(A)(2) be produced? Specifically, what constraint(s) from the code does it violate?

Continued on next page.

## Part B (3 points):

Please consider the following code and an input file that consists of "ABCDEFGHIJKLMNOP":

```
#include <stdio.h>
#include <unistd.h>
#include <fcntl.h>
void main() {
    int fd1, fd2;
    char c;
    fdl=open("files.txt", O_RDONLY);
    read (fdl, &C, 1); printf ("%c", c); fflush(stdout);
    if (!fork()) {
        read (fdl, &C, 1); printf ("%C", c); fflush(stdout);
        sleep(1);
        read (fdl, &c, 1); printf ("%c", c); fflush(stdout);
        read (fdl, &C, 1); printf ("%c", c); fflush(stdout);
    } else {
        fd2=5;
        dup2(fd1, fd2);
        close (fd1);
        c='X';
        read (fd2, &C, 1); printf ("%c", c); fflush(stdout);
    }
}
```

7(B)(1) (1 points): Give one possible output string:

7(B)(2) (1 points): How many possible output strings are there?

7(B)(3) (1 points): Please explain your answer to $7(B)(2)$ above

## Continued on next page

## Part C (4 points):

Please consider the following code:

```
#include <stdio.h>
#include <signal.h>
#include <unistd.h>
int i = 4;
void handler(int s) {
    i--; // Decrement max call counter
    write (1, "X", 1);
    if (i) {
        kill(getpid(), SIGUSRI); // Note that this is a system call
        // kill(getpid(), SIGUSR1); *** UNCOMMENT FOR PART C(3) ***
    }
}
int main() {
    signal(SIGUSR1, handler);
    kill(getpid(), SIGUSR1); // Note that this is a system call
    printf("%d\n", i);
    return 0;
}
```

7(C)(1) (1 points): What is the fewest number of times " $X$ " might get printed? Why?

7(C)(2) (1 points): What is the greatest number of times " $X$ " might get printed? Why?

7(C)(3) (1 points): If the commented line is uncommented, what is the maximum number of times "C" might get printed? Why?

## Question \#8: Concurrency Control: Maladies, Semaphores, Mutexes, BB, RW (15 points)

Consider a grocery store as follows:

- Four (4) cash registers in the self-checkout area
- An additional three (3) cash registers in the traditional cashier-staffed checkout area
- Each area (not each register) has its own line.
- Because of the usual grocery store confusion, no one can really tell how long the lines are.
- Each customer may choose to wait in the cashier-supported line, or the selfcheckout line, but may not switch lines.

Please model this situation as C-like pseudo-code with proper concurrency control via semaphores. Legal semaphore operations are as follows:

- sem_init (sem_t, count)
- sem_p (sem_t)
- sem_v (sem_t)
- where sem_t is a semaphore variable type.

Specifically, please write the pseudocode for the following methods:

```
// Constants to let us name/identify a check-out lane's
// configuration as self-service or cashier-service and
// compare a lane's configuration to see which it is
// These could just as easily be an enum or #defined.
const int SELF = 0;
const int CASHIER = 1;
// Declare and initialize any needed semaphores
// and/or shared variables here.
// You can assume they are global and shared.
void initialize() {
    // Hint: Think about what the type(s) of resources are and how
    // many instances of each type there are. Find a way to account
    // for each of those pool(s) of resources
```

\}

## Continued on next page.

// Customers call this to wait for a cash register void waitForCashRegister(int selfOrCashier) \{
// Hint: Which pool(s) of resources are used here?
// What needs to happen for this to occur safely?
\}
// Customers call this when done with the cash register void doneWithCashRegister(int selfOrCashier) \{
// Hint: Which pool(s) of resources are being given up here?
// What needs to happen to make them available?

