

**ME 24-354: General Robotics
Final Exam**

Date Handed Out: May 5, 2002

Time Allotted: 1 hour and 30 minutes

- Please show all work.
- You may use one crib sheet.
- You must attempt all problems.
- GOOD LUCK!!!

P1. [D-H Notation, 20pts] Consider the following four degree-of-freedom manipulator with one prismatic (linear translation) joint, followed by a prismatic (linear translation) joint that is perpendicular to the previous one, and then two revolute joints (Figure 1).

- (a) [5pts] Baring joint limits, can this robot arbitrarily position and orient an object in the plane? Why.
- (b) [15pts] Write out the Denavit-Hartenburg parameters and variables for this robot. Circle the variables.

P2. [Two-link Manipulator Path Planning, 25pts] Consider the follow two-link manipulator in its work space along side its configuration space. The range of motion for each joint is 0° to 259.99° , i.e., the robot has joint limits.

- (a) [5pts] How many degrees of freedom does the robot have?
- (b) [5pts] Write out the definition of L^1 and L^2 metric and state a reason as to why one is better than the other.
- (c) [10pts] Using the wave front planner based on the better metric chosen in the previous sub-problem, find the shortest path from the start to goal configuration
- (d) [5pts] Draw five intermediate configurations between the start and goal configurations, not including the start and goal

P3. [5pts] A mobile robot has a planar two-link manipulator, where link 1 is 3 units and link 2 is 2 units in length. List and define the variables that describe the configuration space for this robot.

P4. [Inverse Kinematics, 30pts] Consider the two-link manipulator in Figure 4 whose base can slide in a track of length L .

- (a) [2pts] Write out the variable specifying this robot.

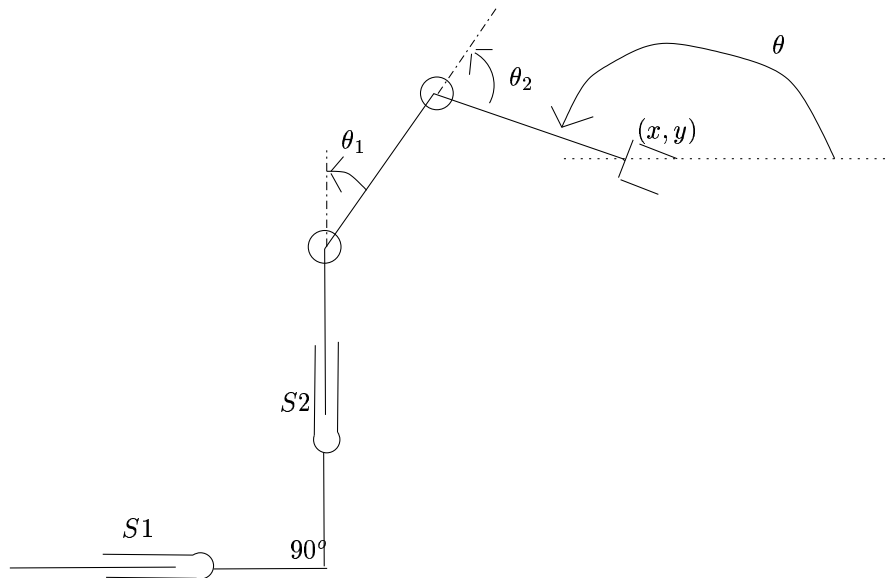


Figure 1. D-H Notation Question

- (b) [8pts] Assume that $l_2 < l_1$, draw in your blue book the workspace of this robot.
- (c) [20pts] Determine the joint variables that reach a given x, y in the workspace of the robot.
- P5. [Non-holonomic Planning, 20pts] Consider the differentially driven cart in Figure 5 that has two independently driven wheels.
- (a) [5pts] How many degrees of freedom does the cart have in the plane?
- (b) [5pts] What is the non-holonomic constraint for the cart (i.e., determine the w) and what does it mean.
- (c) [5pts] What are the initial allowable motions (i.e., determine the g 's from the w) and what do they mean
- (d) [5pts] Can the cart arbitrarily position and orient itself in the plane? Use Lie Brackets to show this.
- P6. [Overview, 5pts] Robotics can be broken down into various classes of sub-categories. Pick three sub-categories that together encompass the robotics field and then define them.

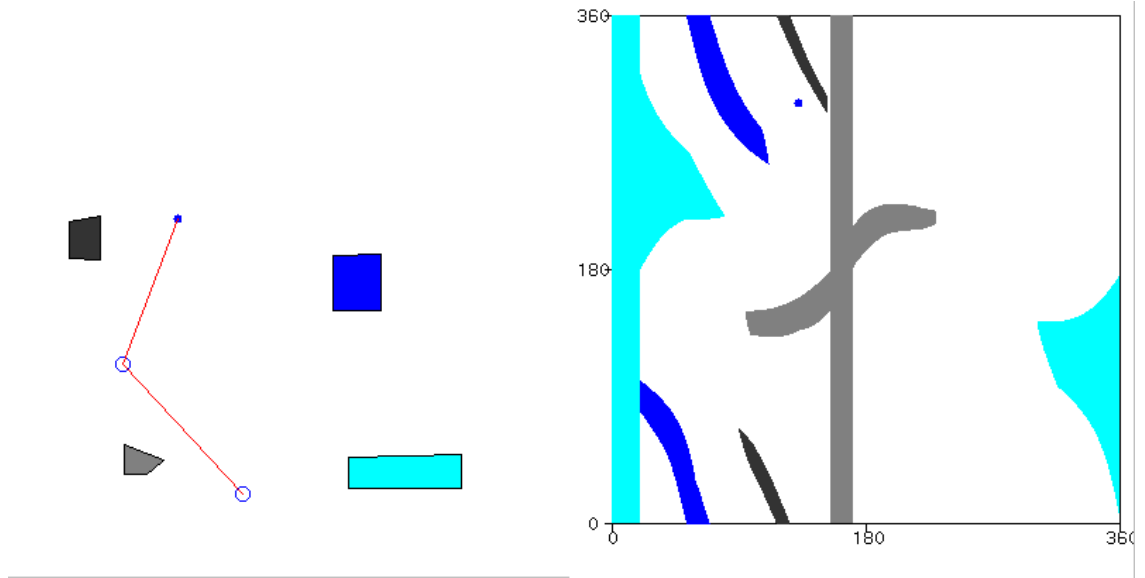


Figure 2. Start Configuration.

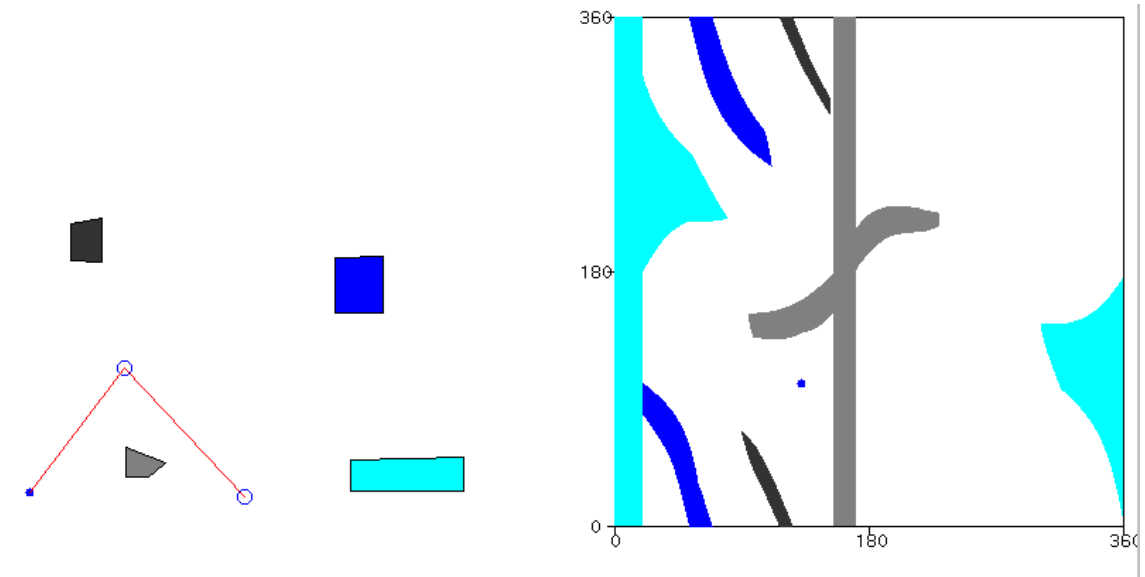


Figure 3. Goal Configuration.

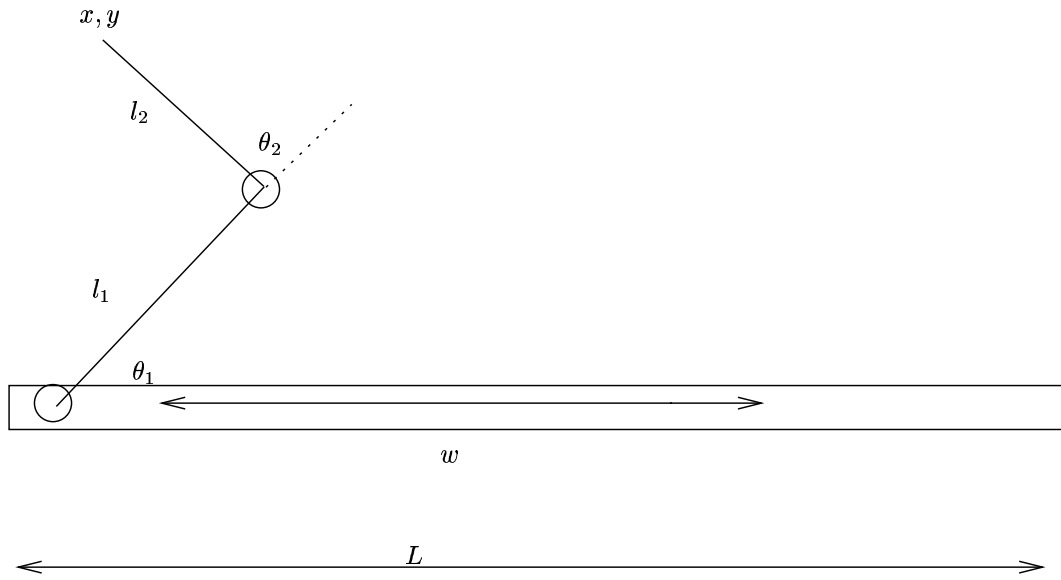


Figure 4. Two-link manipulator in a track.

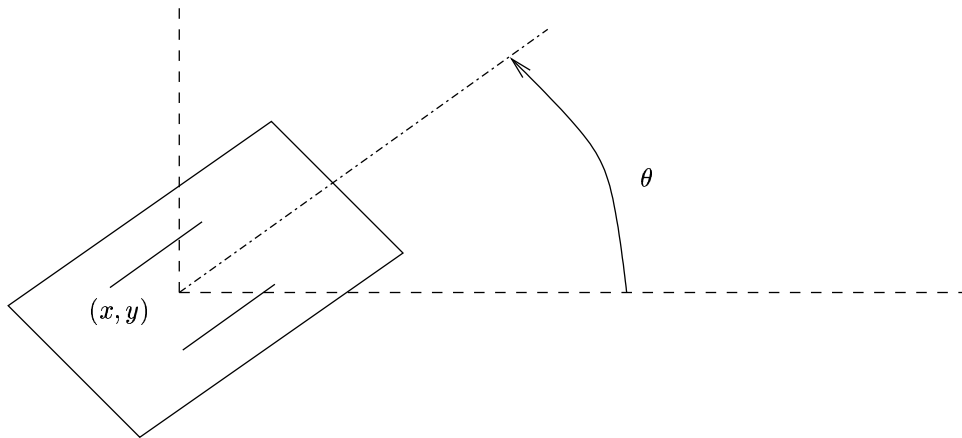


Figure 5. Cart.