

**Assignment 6: Branching-Time Properties**  
**15-414/15-424 Bug Catching: Automated Program Verification**

Due: **11:59pm**, Friday 12/1/17

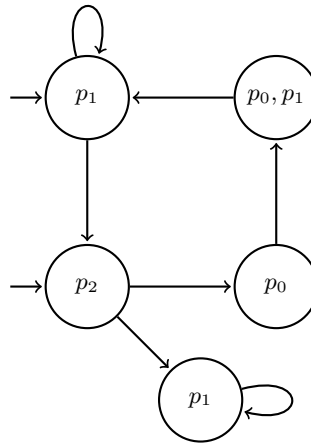
Total Points: 50

1. **Unfinished business (5 points).** Complete the proof of Theorem 3 from Lecture 22 by proving that  $\llbracket \mathbf{EFP} \rrbracket$  is the least fixpoint of  $\llbracket P \rrbracket \cup \tau_{\mathbf{EX}}(\llbracket \mathbf{EFP} \rrbracket)$ .

2. **Computation tree semantics (5 points).** Consider the computation structure  $K$  below, and the CTL formula:

$$\mathbf{A}(p_0 \mathbf{U} p_1) \vee \mathbf{EX}(\mathbf{AG} p_1)$$

For each state in the computation structure, write down the subformulas of the above CTL satisfied by the state. Then, say whether the structure satisfies the formula, i.e.  $K \models \mathbf{A}(p_0 \mathbf{U} p_1) \vee \mathbf{EX}(\mathbf{AG} p_1)$ . To make sure that you understand the CTL model checking algorithm from Lecture 22, you are encouraged to apply the Tarski-Knaster fixpoint theorem to arrive at your answers.



3. **Both  $P$  and  $\neg P$  (5 points).** Recall that a computation structure  $K = (W, \leadsto, v)$  with initial states  $W_0 \subseteq W$  satisfies a CTL formula  $P$  if and only if each initial state  $s \in W_0$  satisfies  $P$ :

$$K \models P \text{ if and only if } \forall s_0 \in W. s_0 \models P$$

This definition has a strange property, where it is possible that a given structure  $K$  there exists a formula  $P$  where  $K \not\models P$  and  $K \not\models \neg P$ . Find a CTL formula and (simple) transition system for which this is the case.