Bug Catching: Automated Program Verification 15414/15614 Spring 2024 Lecture 1: Introduction

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Cayden Codel



Pratap Singh



Tony Yu



Ying Sun

For this lecture

- What is this course about?
- What are the learning objectives for the course?
- ► How does it fit into the curriculum?
- ► How does the course work?

Disastrous Software and Hardware Bugs







1962 - Mariner 1 probe

- Destroyed 293 seconds after launch
- Overbar missing in the mathematical specification
- Cost: \$18.5 million dollars

1996 - Ariane 5 fight 501

- Destroyed 37 seconds after launch
- Arithmetic overflow from 64-bit floating point to 16-bit signed integer
- Cost: \$370 million dollars

1994 - Pentium FDIV bug

- Flaw in the division algorithm:
- 4195835.0/3145727.0 = 1.333 820 449 136 241 000 (Correct)
- 4195835.0/3145727.0 = 1.333 739 068 902 037 589 (FDIV)
- Cost: \$475 million dollars

► April, 2014 OpenSSL announced critical vulnerability in their implementation of the Heartbeat Extension.

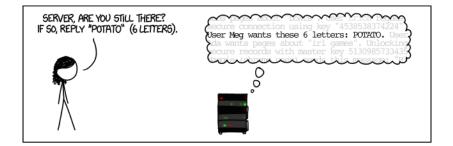


- ► April, 2014 OpenSSL announced critical vulnerability in their implementation of the Heartbeat Extension.
- "The Heartbleed bug allows anyone on the Internet to read the memory of the systems protected by the vulnerable versions of the OpenSSL software."

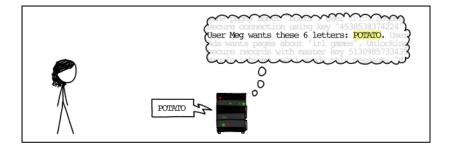


- ► April, 2014 OpenSSL announced critical vulnerability in their implementation of the Heartbeat Extension.
- "The Heartbleed bug allows anyone on the Internet to read the memory of the systems protected by the vulnerable versions of the OpenSSL software."
- "...this allows attackers to eavesdrop on communications, steal data directly from the services and users and to impersonate services and users."



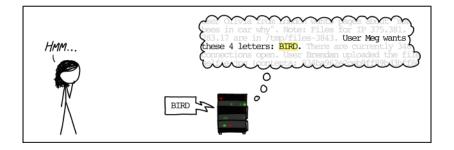


Heartbleed, explained



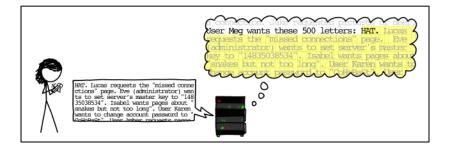


Heartbleed, explained





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• Hard to say, but estimates are \sim \$500 million

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- Stolen data
- Certificate revocation
- Bandwidth
- Engineering effort
- ▶

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Tech giants spend millions to stop another Heartbleed

() 25 April 2014

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XPLOITS AND VULNERABILITIES | NEWS

Five years later, Heartbleed vulnerability still unpatched

Posted: September 12, 2019 by Gilad Maayan

```
int binarySearch(int key, int[] a, int n) {
     int low = 0;
     int high = n;
3
4
     while (low < high) {</pre>
5
          int mid = (low + high) / 2;
6
          if(a[mid] == key) return mid; // key found
8
          else if(a[mid] < key) {</pre>
9
              low = mid + 1;
10
          } else {
              high = mid;
          }
     }
14
     return -1; // key not found.
15
16 }
```

But what if low + high > $2^{31} - 1$?

This is a correct binary search algorithm But what if low + high > $2^{31} - 1$?

Then mid = (low + high) / 2 becomes negative

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- Worst case: undefined (that is, arbitrary) behavior

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- Best case: ArrayIndexOutOfBoundsException
- ► Worst case: undefined (that is, arbitrary) behavior

Algorithm may be correct—but we run code, not algorithms.

The culprit: mid = (low + high) / 2

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Solution: mid = low + (high - low)/2

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The fix

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The fix

```
int binarySearch(int key, int[] a, int n)
2 //@requires 0 <= n && n <= \length(a);
3 // @requires is_sorted(a, 0, n);
4 / * Qensures ( | result == -1 & U ! is_in(key, A, O, n))
       // (0 <= \result && \result < n
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- Humans are fallible, bugs are subtle
- What's the specification?

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 $Specification \iff Implementation$

How do we know if it's correct?

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- Correctness definitely important, but not the only thing
- Humans are fallible, bugs are subtle
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Specification \iff Implementation

- Specification must be precise
- Meaning of code must be comprehensive
- Reasoning must be sound

Course objectives

Identify and formalize program correctness

- Understand language semantics
- Apply mathematical reasoning to program correctness
- Learn how to write correct software, from beginning to end
- Use automated tools that assist verifying your code
- Understand how verification tools work

Identify and formalize program correctness

- Understand language semantics
- Apply mathematical reasoning to program correctness
- Learn how to write correct software, from beginning to end
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- Make you better programmers

Course outline

Part I: Reasoning about programs: from 122 and 150 to 414

• Gain intuitive understanding of language and methodology

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Part II: From inform to formal reasoning

- Specifying meaning of programs
- Specifying meaning of propositions
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Part III: Mechanized reasoning

Techniques for automated proving

Algorithmic approaches

Formal proofs are tedious

Automatic methods can:

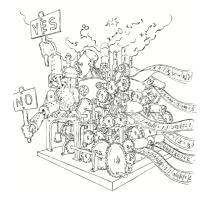


Image source: Daniel Kroening & Ofer Strichman, *Decision Procedures*

Automatic methods can:

- Check our work
- ► Fill in low-level details
- ► Give diagnostic info

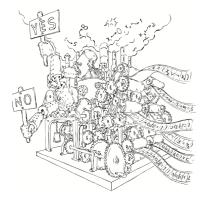


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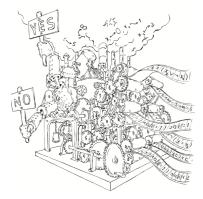


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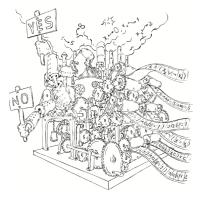


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This is what you will learn!

- Make use of these methods
- ► How (and when) they work

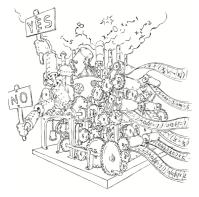


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Why3 (this course) supports both!

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Functional and imperative code in WhyML

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We focus on automated proving

- ► Specification
- ► Proof

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Specify behavior with logic

- Declarative
- Precise

- Specification
- ► Proof

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Systematic proof techniques

- Derived from semantics
- Exhaustive proof rules
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```
int[] array_copy(int[] A, int n)
_2 //@requires 0 <= n && n <= \length(A);
3 //@ensures \length(\result) == n;
4 {
    int[] B = alloc_array(int, n);
5
6
    for (int i = 0: i < n: i++)</pre>
7
   //@loop_invariant 0 <= i;</pre>
8
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     B[i] = A[i];
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- Verification toolchain

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When it works! (It's not quite like a type-checker ...)

Systems that prove that programs match their specifications

Basic idea:

- 1. Translate programs into *proof* obligations
- 2. Encode proof obligations as satisfiability
- 3. Solve using a decision procedure

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Problem is undecidable!

- 1. Prover needs "hints" from programmer
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Verifiers are complex systems

- We'll deep-dive into selected components
- Understand "big picture" for the rest

Basic idea:

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- 2. Encode proof obligations as satisfiability
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\$0penAI

Implement a 'sat' function in Why3 that matches this signature:

sat (cnf : cnf) : option valuation

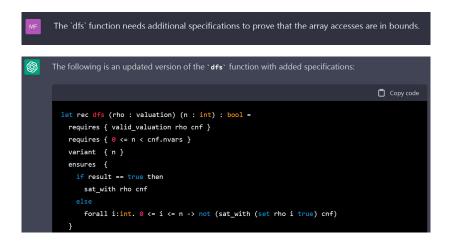
If 'cnf' is satisfiable, then 'sat' should return 'Some rho', where 'rho' is a satisfying assignment for 'cnf'. Otherwise, it should return 'None'.

Recent developments

```
let rho = Array.make cnf.nvars False in
let rec dfs (n : int) : bool =
    requires { valid_valuation rho cnf }
    requires { 0 <= n <= cnf.nvars }
    variant { cnf.nvars - n }
    ensures {
        if result == true then
            sat_with rho cnf
        else
            forall rho':valuation. array_eq_sub rho' rho 0 n -> not (sat_with rho' cnf)
    }
```



The 'dfs' function needs additional specifications to prove that the array accesses are in bounds.



Recent developments

MF

The 'ensures' specification on 'dfs' is not correct. Specifying 'sat_with (set rho i true) cnf' for all 'i' in the range from '0' to 'n' is not relevant; what is relevant is that if 'result <> true', then 'unsat cnf'.

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\$	The following is an updated version of the `dfs` function with a corrected `ensures` specification:	
	Copy code	
	<pre>let rec dfs (rho : valuation) (n : int) : bool = requires { valid_valuation rho cnf } requires { 0 <= n < cnf.nvars } variant { n } ensures { if result == true then sat_with rho cnf else unsat cnf } </pre>	

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- Describe the relevant parts in your solution

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If you use a code model/assistant in this course:

- Document your approach thoroughly
- Describe the relevant parts in your solution
- Come talk to me about it

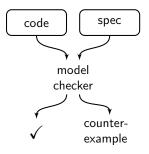
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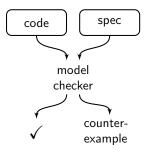
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If you are interested in research related to this, let me know!

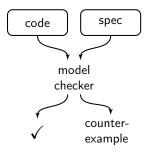
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- Verification by exhaustive state space search
- Diagnostic counterexamples



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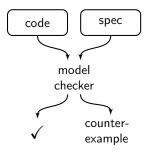
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- ► No proofs!
- ► **Downside**: "State explosion" 10⁷⁰ atoms 10⁵⁰⁰⁰⁰⁰ states







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- Bounded model checking
- Symbolic representations
- Abstraction & refinement

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Ed Clarke, 1945–2020 Turing Award, 2007

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Ed Clarke, 1945–2020 Turing Award, 2007 First developed this course!

. . .

Breakdown:

- 50% assignments (written + programming)
- ▶ 15% mini-project 1
- ▶ 15% mini-project 2
- ▶ 20% final exam

8 assignments done individually

2 mini-projects pick from small menu can work with a partner

Participation:

- Come to lecture
- Answer questions (in class and on Piazza!)
- Contribute to discussion

Written homeworks focus on theory and fundamental skills

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Grades are based on:

- Correctness of your answer
- How you present your reasoning

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Strive for clarity & conciseness

- Show each step of your reasoning
- State your assumptions
- Answers without these \longrightarrow no points

Programming parts of assignments

For the programming, you will:

- Implement some functionality (data structure or algorithm)
- Specify correctness for that functionality
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- Correct implementation
- Correct specification
- Correct contracts
- Sufficient contracts for verification

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- ► Correct implementation
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Partial credit depending on how many of these you achieve

Clarity & conciseness is necessary for partial credit!

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- Writing good specifications
- Applying course principles to practice
- Making effective use of automated tools
- ► Writing useful & correct code

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Gradual progression to sophistication:

- 1. Familiarize yourself with Why3
- 2. Implement and prove something
- 3. Work with more complex data structures
- 4. Implement and prove something really interesting
- 5. Optimize your implementation, still verified

Late days

- ▶ 5 late days to use throughout the semester
- No more than 2 late days on any assignment
- Late days do not apply to mini-projects!

Website: http://www.cs.cmu.edu/~15414

Course staff contact: Piazza https://piazza.com/cmu/spring2024/15414

Lecture: Tuesdays & Thursdays, 12:30pm-1:50pm, HH B131

Office Hours: TBD, schedule on website and course calendar soon

Assignments: Gradescope https://www.gradescope.com/courses/709329 (entry code: RK3262)