

# **The Middle-End**

**15-411/15-611 Compiler Design**

Seth Copen Goldstein

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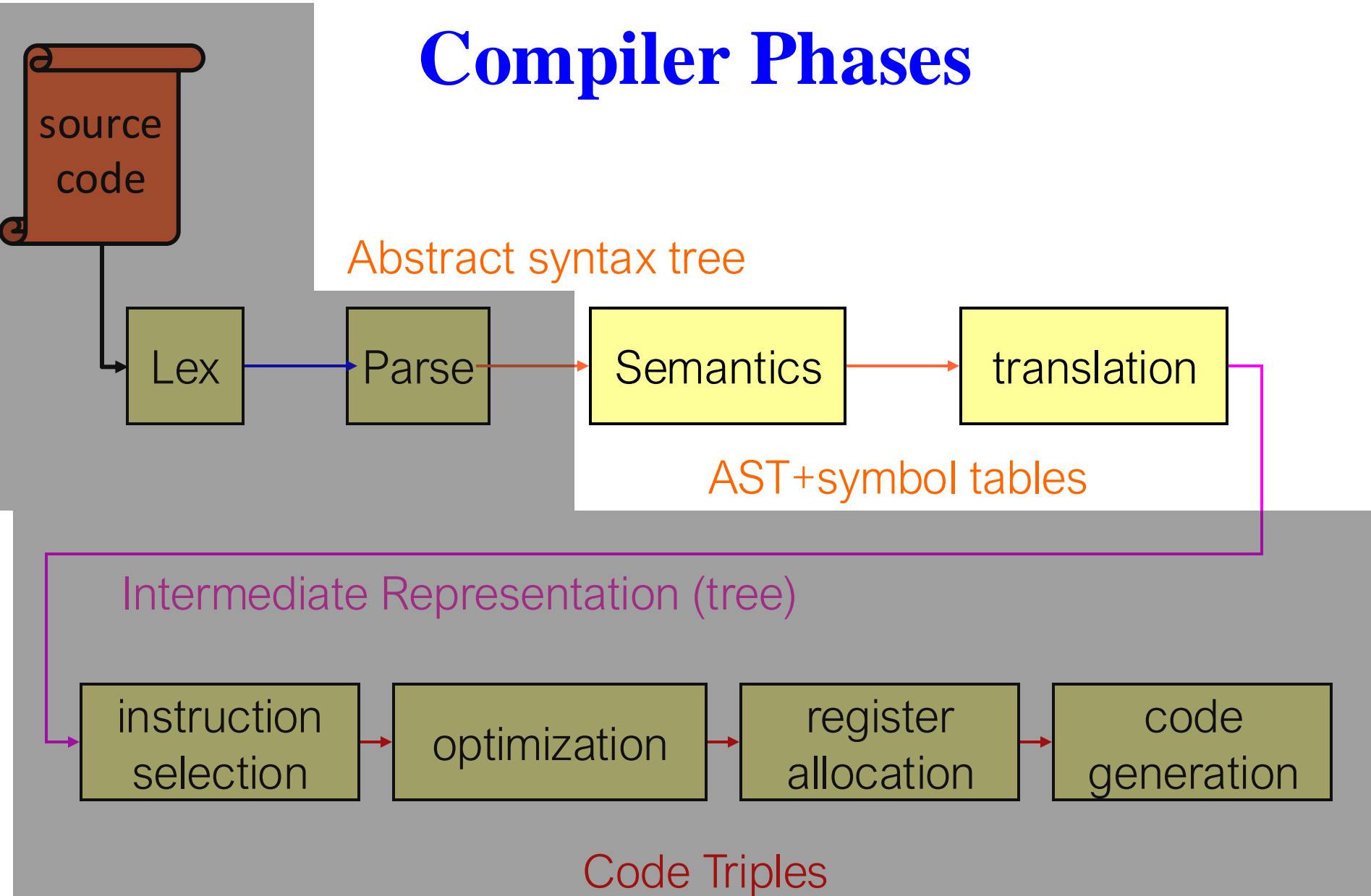
# Today

- lab2
- Elaboration
- Static Semantics
  - scope
  - symbol tables
- Type Checking (in brief)
- Inference Rules
  - Control Flow Checks
  - Initialization checks
- Basic Blocks

# L2

```
⟨program⟩ ::= int main () ⟨block⟩
⟨block⟩   ::= { ⟨stmts⟩ }
⟨type⟩    ::= int | bool
⟨decl⟩    ::= ⟨type⟩ ident | ⟨type⟩ ident = ⟨exp⟩
⟨stmts⟩   ::= ε | ⟨stmt⟩ ⟨stmts⟩
⟨stmt⟩    ::= ⟨simp⟩ ; | ⟨control⟩ | ⟨block⟩
⟨simp⟩    ::= ⟨lvalue⟩ ⟨asop⟩ ⟨exp⟩ | ⟨lvalue⟩ ⟨postop⟩ | ⟨decl⟩ | ⟨exp⟩
⟨simpopt⟩ ::= ε | ⟨simp⟩
⟨lvalue⟩  ::= ident | ( ⟨lvalue⟩ )
⟨elseopt⟩ ::= ε | else ⟨stmt⟩
⟨control⟩ ::= if ( ⟨exp⟩ ) ⟨stmt⟩ ⟨elseopt⟩
           | while ( ⟨exp⟩ ) ⟨stmt⟩
           | for ( ⟨simpopt⟩ ; ⟨exp⟩ ; ⟨simpopt⟩ ) ⟨stmt⟩
           | return ⟨exp⟩ ;
⟨exp⟩     ::= ( ⟨exp⟩ ) | ⟨intconst⟩ | true | false | ident
           | ⟨unop⟩ ⟨exp⟩ | ⟨exp⟩ ⟨binop⟩ ⟨exp⟩ | ⟨exp⟩ ? ⟨exp⟩ : ⟨exp⟩
⟨intconst⟩ ::= num
⟨asop⟩     ::= = | += | -= | *= | /= | %= | &= | ^= | |= | <<= | >>=
⟨binop⟩    ::= + | - | * | / | % | < | <= | > | >= | == | !=
           | && | || | & | ^ | | | << | >>
⟨unop⟩     ::= ! | ~ | -
⟨postop⟩   ::= ++ | --
```

# Compiler Phases



# Elaboration

- Eliminate syntactic sugar
- Simplify future analysis
- For example:
  - `for (init; test; incr) stmt`
  - `while (test) stmt`
  - `expr && expr`
  - `expr || expr`
  - others?

# for loop

`for (init; test; incr) stmt`

$\Rightarrow$  `{`  
    `init;`  
    `while (test) { stmt; incr; }`  
    `}`

# **X && Y**

**exp1 && exp2**

**$\Rightarrow$**

**exp1 || exp2**

**$\Rightarrow$**

# X && Y

`exp1 && exp2`

$\Rightarrow \text{exp1} ? \text{exp2} : \text{false}$

`exp1 || exp2`

$\Rightarrow \text{exp1} ? \text{true} : \text{exp2}$



# When?

- When to do elaboration?
  - While parsing?

```
stmt := for ( simpstmt ; expr; simpstmt ) stmt
        {
            $$ = new Block( );
            $$->append($3);
            Block body = new Block();
            body->append($9);
            body->append($7);
            $$->append(new While($5, body));
        }
```

- As a separate pass, after parsing?

# What?

- Absolutely: **for**, **&&**, **||**
- What about: **int x = e;**
  - What would we elaborate it to?
  - Why would this be good? Bad?
- Other things to keep in mind:
  - line numbers
  - errors

# Now ready to goto IR?

- Many choices of IR (discussed in lecture 2)
  - I chose tree-IR and Triples
- Before converting to IR: Semantic Analysis

# Semantic Analysis

- Semantic analysis is a **static analysis** of the program to make sure it has a meaning
- It is a context **sensitive** analysis!
- At this point in the compilation we have an AST of the input program  
i.e., we know it is syntactically correct
- What kinds of checks are needed to ensure a semantically correct program?

# Semantic Analysis

- Type checks
  - Is variable **x** declared?
  - What is its type?
  - Can an operator operate on a particular type?
  - What is the result type of an operation?
- Control flow checks
  - Is the placement of a **break** or **continue** legal?
  - Is the placement of a **return** legal?

# Semantic Analysis

- Uniqueness checks
  - Is a variable declared more than once?
  - Are the labels in a switch unique?
  - Are the labels in a procedure legal?
  - Are the field names in a record unique?
- Matching Name checks
  - E.g., in ada loops can have names at start and end and they must be the same

# Semantic Analysis

- Static analysis:
  - Type checks
  - Control flow checks
  - Uniqueness checks
  - Matching Name checks
- As opposed to dynamic analysis:
  - dereferencing a null pointer
  - array bounds checks
  - infinite loops
- Why do we defer the static checks til now?

# The easy cases

- Control flow checks
- Matching names
- Uniqueness?



# The easy cases

- Control flow checks
  - recursively walk AST keeping track of loop depth.
  - If break or continue encountered, then  $\text{depth} == 0 \Rightarrow \text{error}$ .
- Matching names
- Uniqueness?

# The easy cases

- Control flow checks
  - recursively walk AST keeping track of loop depth.
  - If break or continue encountered, then  $\text{depth} == 0 \Rightarrow \text{error}$ .
- Matching names
  - recursive walk of tree keep track of “opening” name and then match to “closing” name.
- Uniqueness?

# Uniqueness

- These questions are harder:
  - Is a variable declared more than once?
  - Are the labels in a switch unique?
  - Are the labels in a procedure legal?
  - Are the field names in a record unique?
- When is a variable declared more than once?

```
int foo(int a) {  
    int a;  
    for (i=0; i<100; i++) {  
        int a = i*i;  
        ...  
    }  
}
```

- In checking types and declarations we must take scope into account.

# Scope

- Declarations associate information with names
  - a variable name to its type, storage, etc.
  - a type name to a particular type
  - a function name to its parameter list, body, etc.
- The scope rules of a language determine the extent that the declaration is valid
- or
- They determine which declaration applies to a name at a given place in the program

# Different Kinds of Scope Rules

- C like
  - static/lexical scoping
  - global, static, local, block (most closely nested)
- Pascal
  - local, block
  - nested procedures
- Java
  - global, package, file, class, method, block
- Lisp
  - dynamic scope

# Example of nesting

```
int f(int b) {  
    b = 0;  
    { int b = 1; int c = 1;  
        {int b = 2; int c = 2;  
            ...  
        }  
        {int b = 3; ... c ...  
        }  
        ...  
    }  
    ...  
}
```

Not legal c0!

# Dynamic V. Static Scope

```
void weird() {  
    int N = 1;  
    void show() {  
        print(N); print(" ")  
    }  
    void two() {  
        int N = 2;  
        show();  
    }  
    show(); two(); show(); two();  
}
```

Static scope: "1 1 1 1"

Dynamic scope: "1 2 1 2"

# Symbol Tables

- Symbol tables are key data structure for semantic analysis
- A symbol table maps identifiers to attributes
  - its type
  - its location on stack
  - its register name if any
  - storage class
  - offset from base of record
  - etc.
- Structure of symbol table(s) must reflect scope of program
- It must be efficient
- Support multiple name spaces



# Symbol Tables

- Two main choices:
  - A Stack of tables:
    - entering a scope: create new table, link to parent
    - leaving a scope: remove table
  - Table of stacks
    - one symbol table
    - A stack for variables pointing to entry in table
    - On leaving scope, remove all variables declared in current scope
- Where do we store information, e.g., type, ...

# Rewrite AST

- When we insert a new entry, attach attribute information to decl node
- When we lookup a name, point to the decl node to which it maps.
- When we are done with this pass the symbol table is no longer needed!

# Semantic Analysis

- Type checks
  - Is variable **x** declared?
  - What is its type?
  - Can an operator operate on a particular type?
  - What is the result type of an operation?
- Control flow checks
- Uniqueness checks
  - Is a variable declared more than once?
  - Are the labels in a switch unique?
  - Are the labels in a procedure legal?
  - Are the field names in a record unique?
- Matching Name checks

# Type Checking

- Ensures that type of an expression is valid in the context in which it appears.
- For example:
  - arguments to + are integers
  - index operation is applied to arrays
  - that '.' is applied to records
  - function call has proper number of args (and they are of proper type)
  - casts are legal

# What is a Type?

- A type describes a class of values.
- So far in C0
  - int: class of integers
  - bool: true or false
  - More coming soon
- Two kinds of declarations:
  - Type declarations create new types from other types.
  - Variable declarations specify that a variable will always have a particular type.

# What does decl of x tell us

- From the type:
  - Know what kinds of values are stored in x
  - Know what kinds of operations are legal
    - $+$ ,  $-$ ,  $*$ , ...
    - Function call: # of args, return type
  - How big x is
- From the scope:
  - Where it is stored
  - How it is allocated, init'd
  - How long it should be kept around

# Type Checking

- Build up an environment which maps
  - variables to type
  - values to types
  - expressions to types
- Given an environment and an expression
  - check that it is correct
  - update the environment
- Do this on entire program
- This is a syntax directed analysis, i.e., recursively walk ast checking types as we go.

# Approaches to Semantic Analysis

- Ad hoc, e.g., tree-walk to make sure all control-flow paths end in a return
- Attribute grammars: Use a grammar to automatically generate an analysis pass
- Inference rules, judgements and solvers



# Using Inference Rules

- Our language:

$e := n \mid x \mid e1 + e2 \mid e1 \ \&\& \ e2$

$s := x \leftarrow e$

$\mid \text{if}(e, s1, s2)$

$\mid \text{while}(e, s)$

$\mid \text{return}(e)$

$\mid \text{seq}(s1, s2)$

$\mid \text{decl}(x, \tau, s)$

# Check for Proper Returns

$$\frac{}{\text{hasret}(\mathbf{return}(e))}$$
$$\frac{\text{hasret}(s1)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$
$$\frac{\text{hasret}(s2)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$

decl?

if?

while?

nop?

assign?

# Check for Proper Returns

$$\frac{}{\text{hasret}(\mathbf{return}(e))}$$
$$\frac{\text{hasret}(s1)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$
$$\frac{\text{hasret}(s2)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$
$$\frac{\text{hasret}(s)}{\text{hasret}(\mathbf{decl}(x, \tau, s))}$$
$$\frac{\text{hasret}(s1) \text{ hasret}(s2)}{\text{hasret}(\mathbf{if}(e, s1, s2))}$$

# Implementation

$$\frac{}{\text{hasret}(\mathbf{return}(e))}$$
$$\frac{\text{hasret}(s1)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$
$$\frac{\text{hasret}(s2)}{\text{hasret}(\mathbf{seq}(s1, s2))}$$
$$\frac{\text{hasret}(s)}{\text{hasret}(\mathbf{decl}(x, \tau, s))}$$
$$\frac{\text{hasret}(s1) \text{ hasret}(s2)}{\text{hasret}(\mathbf{if}(e, s1, s2))}$$

A recursive treewalk using judgements as cases.

$\text{hasret}(\mathbf{return}(e)) = \text{true}$

$\text{hasret}(\mathbf{seq}(s1, s2)) = \text{hasret}(s1) \mid \mid \text{hasret}(s2)$

$\text{hasret}(\mathbf{decl}(x, \tau, s)) = \text{hasret}(s)$

$\text{hasret}(\mathbf{if}(e, s1, s2)) = \text{hasret}(s1) \& \& \text{hasret}(s2)$

$\text{hasret}(\mathbf{while}(e, s)) = \text{false}$

....

# Initialization Checking

- How do we make sure all variables are initialized before they are used?

$e := n \mid x \mid e1 + e2 \mid e1 \ \&\& \ e2$

$s := x \leftarrow e$

$\mid \text{nop}$

$\mid \text{if}(e, s1, s2)$

$\mid \text{while}(e, s)$

$\mid \text{return}(e)$

$\mid \text{seq}(s1, s2)$

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$\mid \text{return}(e)$

$\mid \text{seq}(s1, s2)$

$\mid \text{decl}(x, \tau, s)$

If variable is live at point of declaration, then we have an error.

# Plan for Verifying Proper Init

- If variable is live at point of declaration, then we have an error.
  - Determine if a variable is **live** at a statement
  - Will depend on whether there is a **use** of a variable in an expression
  - Determine if a statement will **define** a variable
  - Put it all together in a predicate to check for proper **initialization**.

# the init predicate

$$\frac{}{\text{init}(\text{nop})} \qquad \frac{\text{init}(s_1) \quad \text{init}(s_2)}{\text{init}(\text{seq}(s_1, s_2))}$$
$$\frac{\text{init}(s) \quad \neg \text{live}(s, x)}{\text{init}(\text{decl}(x, \tau, s))}$$

If variable is live at point of declaration, then we have an error.



# Plan for Verifying Proper Init

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# live predicate (take 1)

$$\frac{\text{use}(e, x)}{\text{live}(\text{assign}(y, e), x)}$$

# Plan for Verifying Proper Init

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# the use predicate

no rule for  
 $\text{use}(n, x)$

$\frac{}{\text{use}(x, x)}$

no rule for  
 $\text{use}(y, x), y \neq x$

$\frac{\text{use}(e_1, x)}{\text{use}(e_1 \oplus e_2, x)}$

$\frac{\text{use}(e_2, x)}{\text{use}(e_1 \oplus e_2, x)}$

$\frac{\text{use}(e_1, x)}{\text{use}(e_1 \&\& e_2, x)}$

$\frac{\text{use}(e_2, x)}{\text{use}(e_1 \&\& e_2, x)}$

$\text{use}(e, x)$  is a may-property: no guarantee  $x$  will be used, but it may be used.

# live predicate (take 2)

$$\begin{array}{c}
 \frac{\text{use}(e, x)}{\text{live}(\text{assign}(y, e), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \quad \frac{\text{live}(s_1, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \quad \frac{\text{live}(s_2, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{while}(e, s), x)} \quad \frac{\text{live}(s, x)}{\text{live}(\text{while}(e, s), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{return}(e), x)} \quad \text{no rule for } \text{live}(\text{nop}, x) \quad \frac{\text{live}(x, s) \quad y \neq x}{\text{live}(\text{decl}(y, \tau, s), x)} \\
 \\
 \frac{\text{live}(s_1, x)}{\text{live}(\text{seq}(s_1, s_2), x)} \quad \frac{\neg \text{def}(s_1, x) \quad \text{live}(s_2, x)}{\text{live}(\text{seq}(s_1, s_2), x)}
 \end{array}$$

# live predicate (take 2)

$$\begin{array}{c}
 \frac{\text{use}(e, x)}{\text{live}(\text{assign}(y, e), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \quad \frac{\text{live}(s_1, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \quad \frac{\text{live}(s_2, x)}{\text{live}(\text{if}(e, s_1, s_2), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{while}(e, s), x)} \quad \frac{\text{live}(s, x)}{\text{live}(\text{while}(e, s), x)} \\
 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{return}(e), x)} \quad \text{no rule for } \text{live}(\text{nop}, x) \quad \boxed{\frac{\text{live}(x, s) \quad y \neq x}{\text{live}(\text{decl}(y, \tau, s), x)}} \\
 \\
 \frac{\text{live}(s_1, x)}{\text{live}(\text{seq}(s_1, s_2), x)} \quad \frac{\neg \text{def}(s_1, x) \quad \text{live}(s_2, x)}{\text{live}(\text{seq}(s_1, s_2), x)}
 \end{array}$$

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 \\
 \frac{\text{use}(e, x)}{\text{live}(\text{while}(e, s), x)} \quad \frac{\text{live}(s, x)}{\text{live}(\text{while}(e, s), x)} \\
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 \\
 \frac{\text{live}(s_1, x)}{\text{live}(\text{seq}(s_1, s_2), x)} \quad \boxed{\frac{\neg \text{def}(s_1, x) \quad \text{live}(s_2, x)}{\text{live}(\text{seq}(s_1, s_2), x)}}
 \end{array}$$

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- If variable is live at point of declaration, then we have an error.
  - Determine if a variable is **live** at a statement
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# the def predicate

$\frac{}{\text{def}(\text{assign}(x, e), x)}$	no rule for $\text{def}(\text{assign}(y, e), x), y \neq x$
-----------------------------------------------	---------------------------------------------------------------

$\frac{\text{def}(s_1, x) \quad \text{def}(s_2, x)}{\text{def}(\text{if}(e, s_1, s_2), x)}$	no rule for $\text{def}(\text{while}(e, s), x)$
---------------------------------------------------------------------------------------------	----------------------------------------------------

no rule for $\text{def}(\text{nop}, x)$	$\frac{\text{def}(s_1, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$	$\frac{\text{def}(s_2, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$
--------------------------------------------	------------------------------------------------------------------	------------------------------------------------------------------

$\frac{\text{def}(s, x) \quad y \neq x}{\text{def}(\text{decl}(y, \tau, s), x)}$
----------------------------------------------------------------------------------

$\frac{}{\text{def}(\text{return}(e), x)}$
--------------------------------------------

# the def predicate

$\frac{}{\text{def}(\text{assign}(x, e), x)}$       no rule for  $\text{def}(\text{assign}(y, e), x), y \neq x$

$\frac{\text{def}(s_1, x) \quad \text{def}(s_2, x)}{\text{def}(\text{if}(e, s_1, s_2), x)}$       no rule for  $\text{def}(\text{while}(e, s), x)$

no rule for  $\text{def}(\text{nop}, x)$        $\frac{\text{def}(s_1, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$        $\frac{\text{def}(s_2, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$

$\frac{\text{def}(s, x) \quad y \neq x}{\text{def}(\text{decl}(y, \tau, s), x)}$

$\frac{}{\text{def}(\text{return}(e), x)}$

s is in scope of y

# the def predicate

$\frac{}{\text{def}(\text{assign}(x, e), x)}$       no rule for  $\text{def}(\text{assign}(y, e), x), y \neq x$

$\frac{\text{def}(s_1, x) \quad \text{def}(s_2, x)}{\text{def}(\text{if}(e, s_1, s_2), x)}$       no rule for  $\text{def}(\text{while}(e, s), x)$

no rule for  $\text{def}(\text{nop}, x)$        $\frac{\text{def}(s_1, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$        $\frac{\text{def}(s_2, x)}{\text{def}(\text{seq}(s_1, s_2), x)}$

$\frac{\text{def}(s, x) \quad y \neq x}{\text{def}(\text{decl}(y, \tau, s), x)}$

$\frac{}{\text{def}(\text{return}(e), x)}$

# the init predicate

$$\frac{}{\text{init}(\text{nop})} \qquad \frac{\text{init}(s_1) \quad \text{init}(s_2)}{\text{init}(\text{seq}(s_1, s_2))}$$

$$\frac{\text{init}(s) \quad \neg \text{live}(s, x)}{\text{init}(\text{decl}(x, \tau, s))}$$

# After Static Semantics ...

- Translate AST to IR
- Then (or simultaneously) create Basic Blocks and CFG