Warm-up as you walk in

Write the pseudo code for breadth first search and depth first search

Iterative version, not recursive

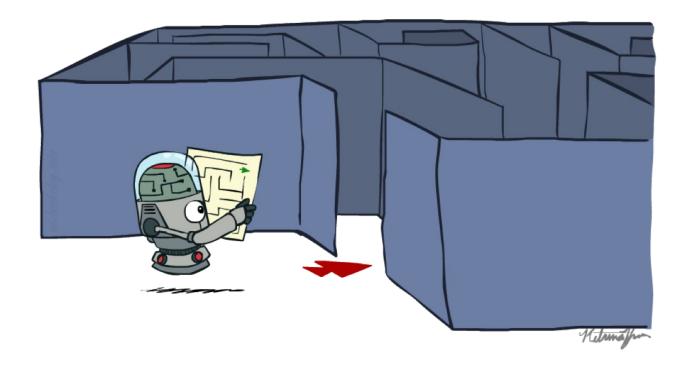
```
class TreeNode
    TreeNode[] children()
    boolean isGoal()

BFS(TreeNode start)...

DFS(TreeNode start)...
```

AI: Representation and Problem Solving

Agents and Search Techniques



Instructor: Pat Virtue

Slide credits: CMU AI, http://ai.berkeley.edu

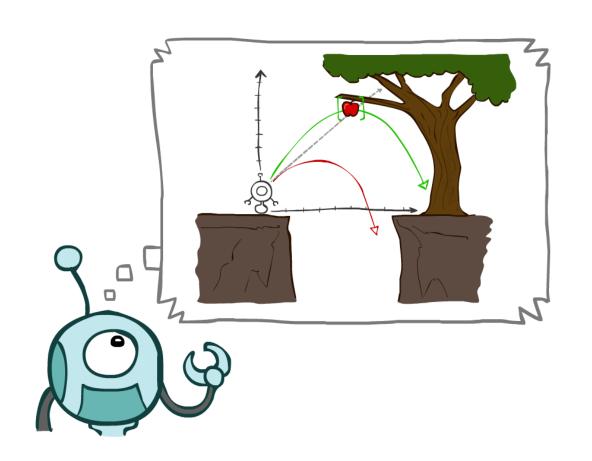
Outline

Agents and Environments

Search Problems

Uninformed Search Techniques

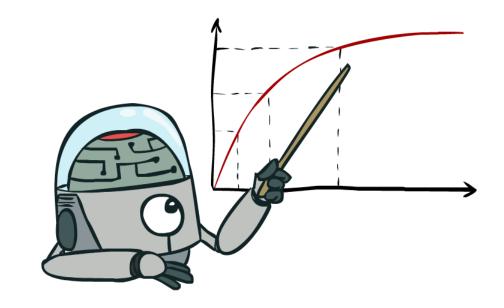
- Depth-First Search
- Breadth-First Search
- Uniform-Cost Search



Rationality, contd.

What is rational depends on:

- Performance measure
- Agent's prior knowledge of environment
- Actions available to agent
- Percept sequence to date



Being rational means maximizing your expected utility

Rational Agents

Are rational agents *omniscient*?

■ No — they are limited by the available percepts

Are rational agents *clairvoyant*?

■ No — they may lack knowledge of the environment dynamics

Do rational agents *explore* and *learn*?

■ Yes — in unknown environments these are essential

So rational agents are not necessarily successful, but they are *autonomous* (i.e., transcend initial program)

Task Environment - PEAS

Performance measure

-1 per step; +10 food; +500 win; -500 die;
 +200 hit scared ghost

Environment

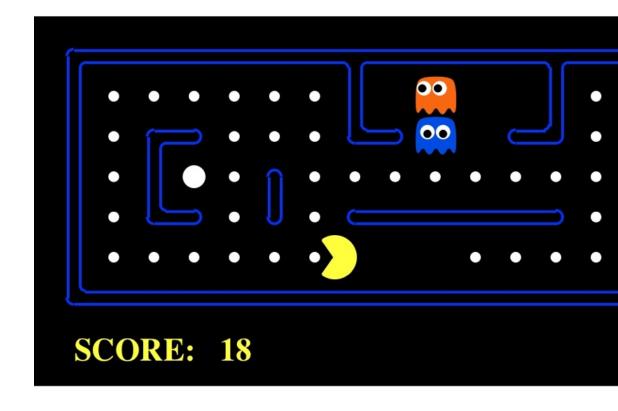
Pacman dynamics (incl ghost behavior)

Actuators

North, South, East, West, (Stop)

Sensors

Entire state is visible



PEAS: Automated Taxi

Performance measure

 Income, happy customer, vehicle costs, fines, insurance premiums

Environment

US streets, other drivers, customers

Actuators

Steering, brake, gas, display/speaker

Sensors

 Camera, radar, accelerometer, engine sensors, microphone



Environment Types





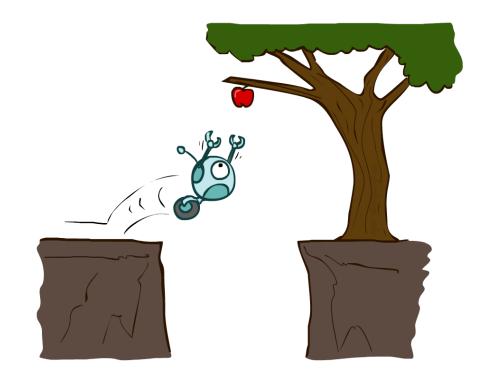
	Pacman	Taxi
Fully or partially observable	$F_{4}//\sqrt{2}$	Partially
Single agent or multi-agen	t Mul+:	Mn/+;
Deterministic or stochastic	STOLT (.	Stoch.
Static or dynamic	(in 281) Static - turn-taking	Dynamic
Discrete or continuous	Discrete	Cont.

Reflex Agents

Reflex agents:

- Choose action based on current percept (and maybe memory)
- May have memory or a model of the world's current state
- Do not consider the future consequences of their actions
- Consider how the world IS

Can a reflex agent be rational?



[Demo: reflex optimal (L2D1)]

[Demo: reflex optimal (L2D2)]

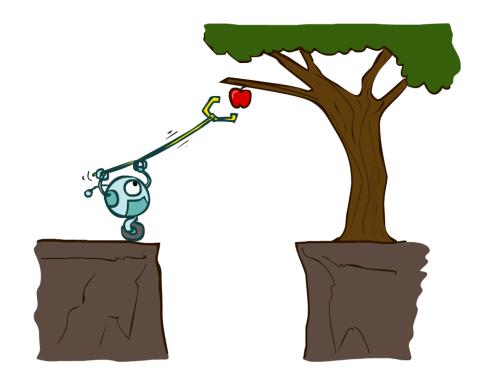
Agents that Plan Ahead

Planning agents:

- Decisions based on *predicted consequences* of actions
- Must have a transition model: how the world evolves in response to actions
- Must formulate a goal
- Consider how the world WOULD BE

Spectrum of deliberativeness:

- Generate complete, optimal plan offline, then execute
- Generate a simple, greedy plan, start executing, replan when something goes wrong





Search Problems

Search Problems

A search problem consists of:

A state space





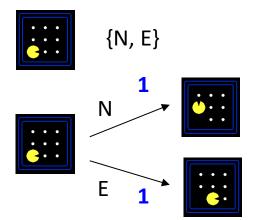








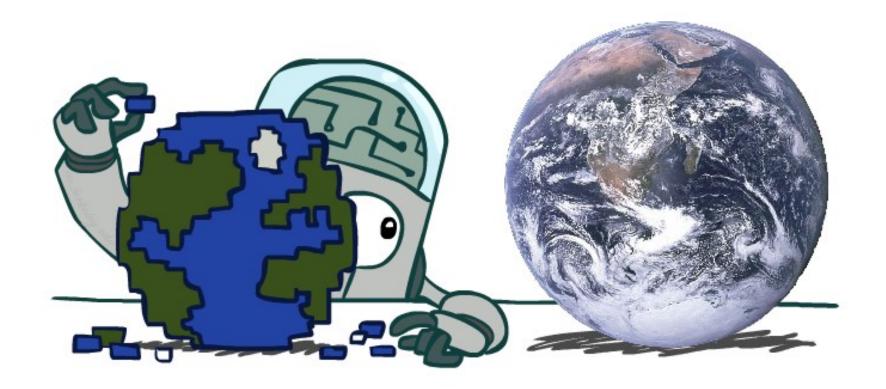
- For each state, a setActions(s) of allowable actions
- A transition model Result(s,a)
- A step cost function c(s,a,s')
- A start state and a goal test



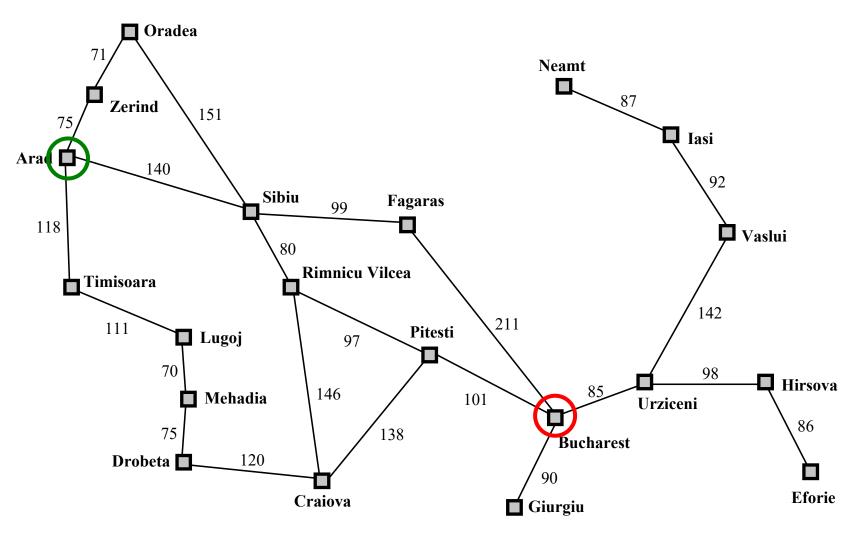
A solution is a sequence of actions (a plan) which transforms the start state to a goal state

Search Problems Are Models

They are a simplification/approximation of the real world



Example: Travelling in Romania



State space:

Cities

Actions:

Go to adjacent city

Transition model

■ Result(A, Go(B)) = B

Step cost

Distance along road link

Start state:

Arad

Goal test:

Is state == Bucharest?

Solution?

State Space Representation and Size?

World state:

Agent positions: 120

■ Food count: 30

Ghost positions: 12

Agent facing: NSEW

State representation

World states?

$$(p, f_1, ..., f_{30}, g_1, g_2, d)$$

Eat top left dot?

(p)

States for eat-all-dots?

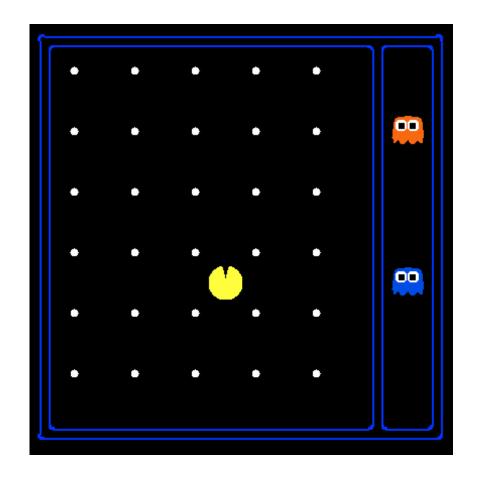
$$(p, f_1, ..., f_{30})$$

State space size

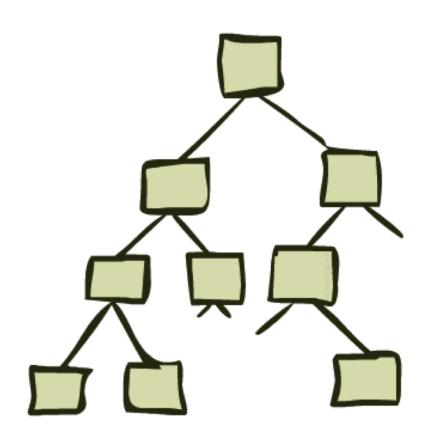
 $120x(2^{30})x(12^2)x4$

120

 $120x(2^{30})$



State Space Graphs and Search Trees



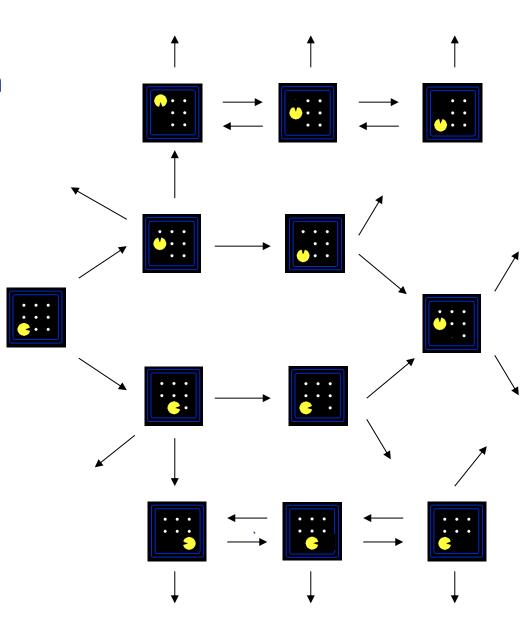
State Space Graphs

State space graph: A mathematical representation of a search problem

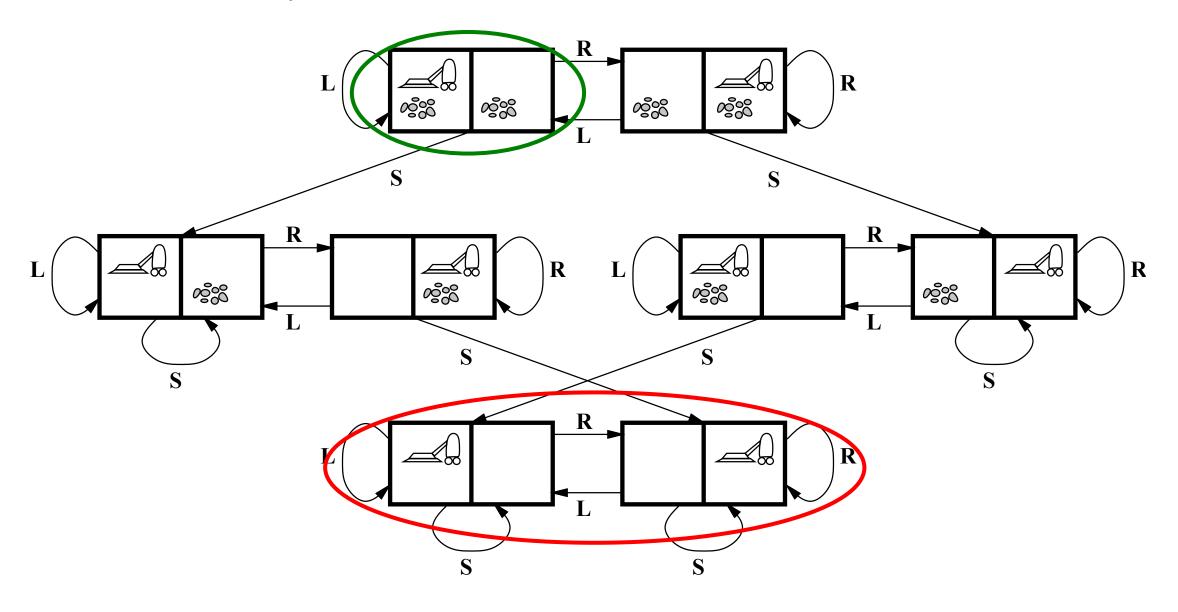
- Vertices are (abstracted) world configurations
- Edges represent transitions resulting from actions
- The goal test is a set of goal nodes (maybe only one)

In a state space graph, each state occurs only once!

We can rarely build this full graph in memory (it's too big), but it's a useful idea



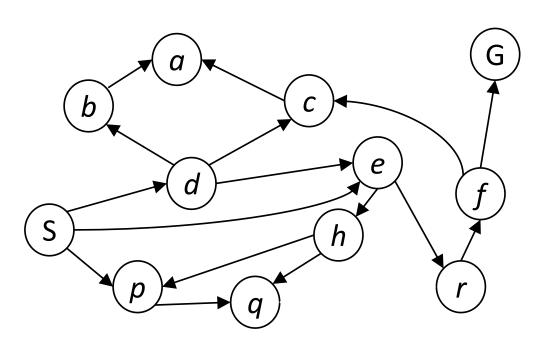
More Examples



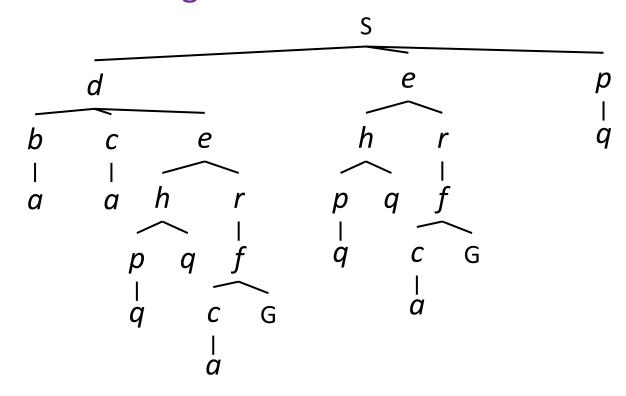
State Space Graphs vs. Search Trees

We build a search tree by traversing various paths in a state space graph, beginning from a specific start state.

State space graph



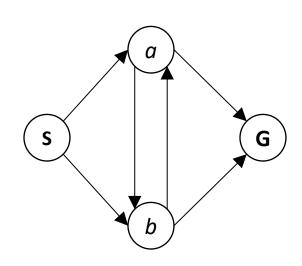
Resulting search tree



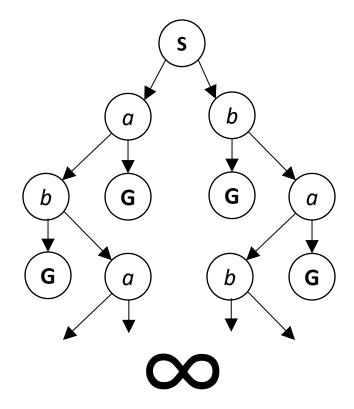
Important: Lots of repeated structure in the search tree!

State Space Graphs vs. Search Trees

Consider this 4-state graph:

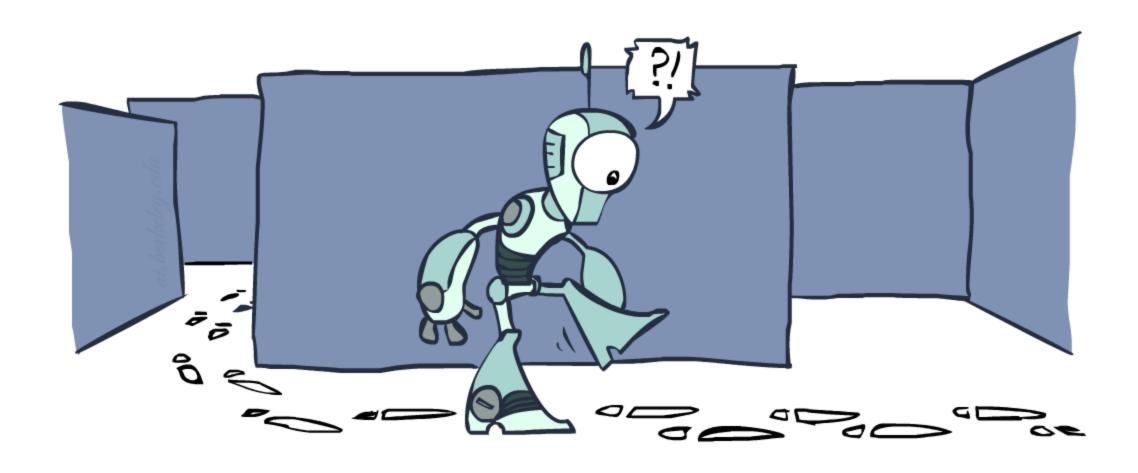


How big is its search tree (from S)?



Important: With loops in the graph, the search tree can go on forever

Tree Search vs Graph Search



```
function TREE_SEARCH(problem) returns a solution, or failure
```

```
initialize the frontier as a specific work list (stack, queue, priority queue)
add initial state of problem to frontier
loop do
    if the frontier is empty then
         return failure
    choose a node and remove it from the frontier
    if the node contains a goal state then
         return the corresponding solution
```

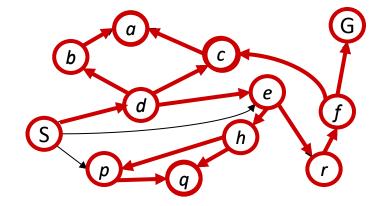
for each resulting child from node add child to the frontier

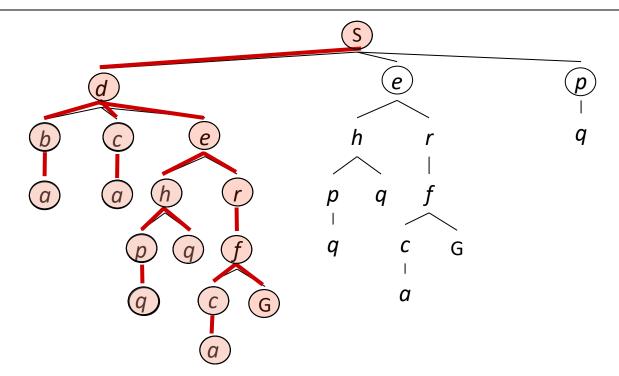
Depth-First (Tree) Search

Strategy: expand a deepest node first

Implementation:

Frontier is a LIFO stack





function GRAPH SEARCH(problem) returns a solution, or failure

initialize the explored set to be empty

initialize the frontier as a specific work list (stack, queue, priority queue)

add initial state of problem to frontier

loop do

if the frontier is empty then return failure

choose a node and remove it from the frontier

if the node contains a goal state then

return the corresponding solution

add the node state to the explored set

for each resulting child from node

if the child state is not already in the frontier or explored set then

add child to the frontier

Data structure note:

"Nodes" go on frontier

States go on explored set

5-A-B

13

A Note on Implementation

```
Nodes have
```

state, parent, action, path-cost

A child of parent_node by action *a* has:

```
state = result(parent_node.state,a)
```

parent = parent_node

action = a

```
path-cost = parent_node.path_cost +
    step_cost(parent_node.state, a, self.state)
```

PARENT Node Action = RightPATH-COST = 6**S**TATE

Extract solution by tracing back parent pointers, collecting actions

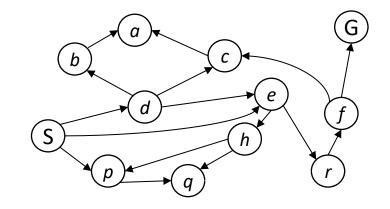
Depth-First (Graph) Search

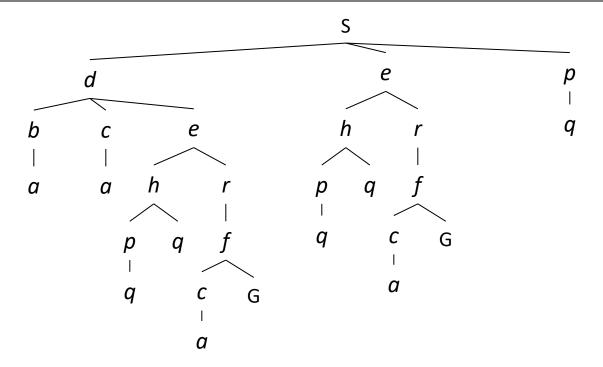
Strategy: expand a deepest node first

Implementation:

Frontier is a LIFO stack

Explored set prevents loops and repeated work





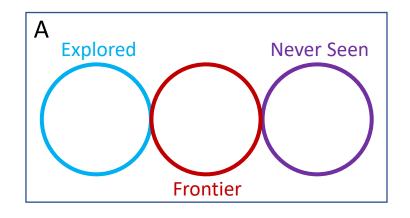
Poll 1

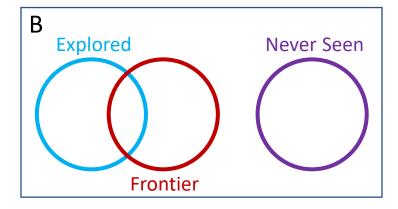
```
function GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the explored set to be empty
   initialize the frontier as a specific work list (stack, queue, priority queue)
  add initial state of problem to frontier
   loop do
       if the frontier is empty then
            return failure
       choose a node and remove it from the frontier
       if the node contains a goal state then
           return the corresponding solution
       add the node state to the explored set
       for each resulting child from node
           if the child state is not already in the frontier or explored set then
                add child to the frontier
```

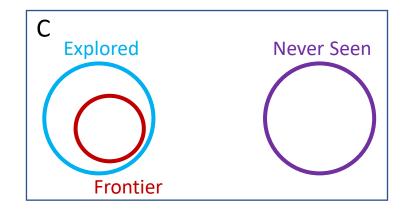
Poll 1

What is the relationship between these sets of states after each loop iteration in GRAPH_SEARCH?

(Loop invariants!!!)



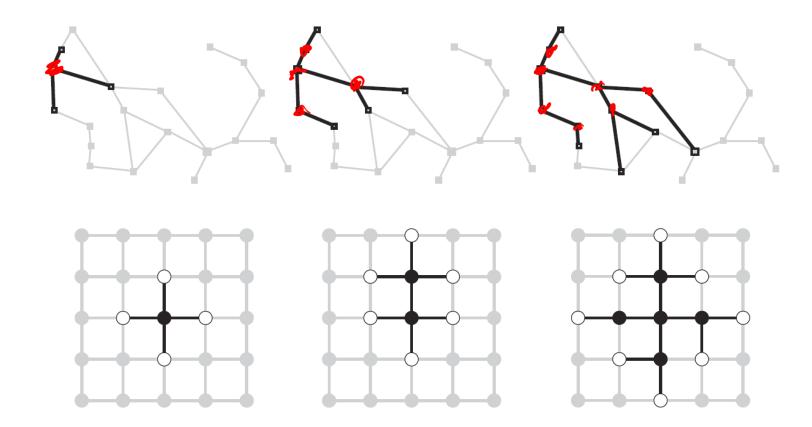




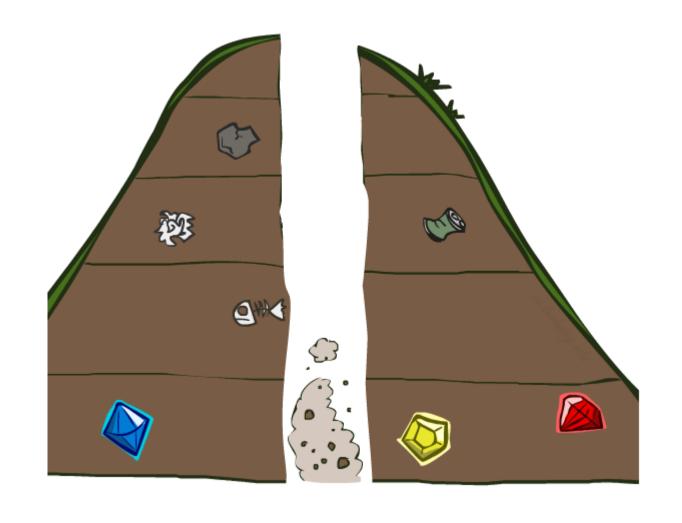
Graph Search

This graph search algorithm overlays a tree on a graph

The frontier states separate the explored states from never seen states

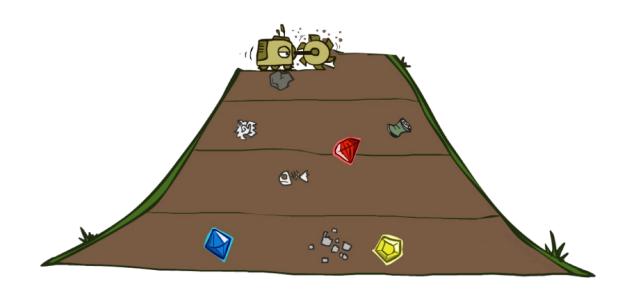


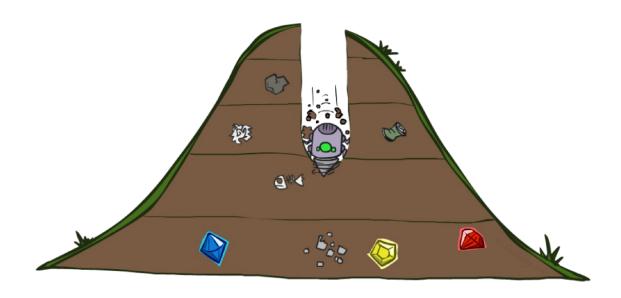
Images: AIMA, Figure 3.8, 3.9



Search Algorithm Properties

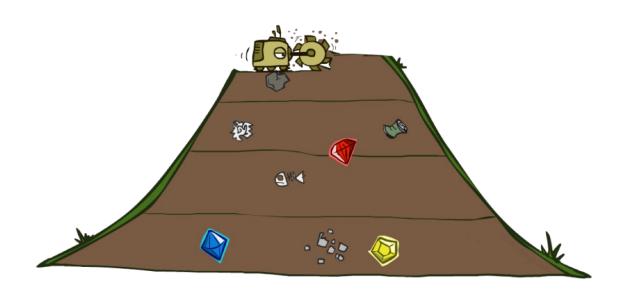
BFS vs DFS





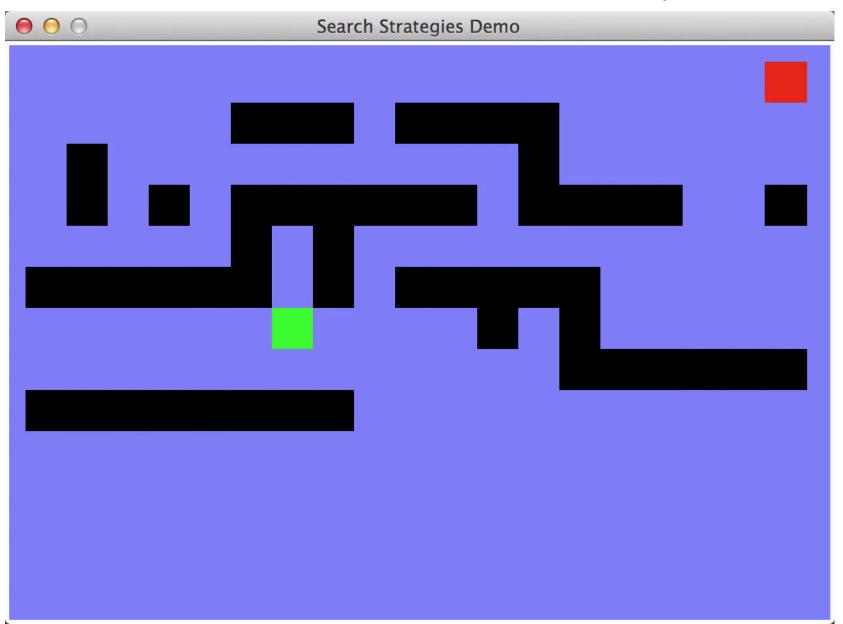
BFS vs DFS

Is the following demo using BFS or DFS

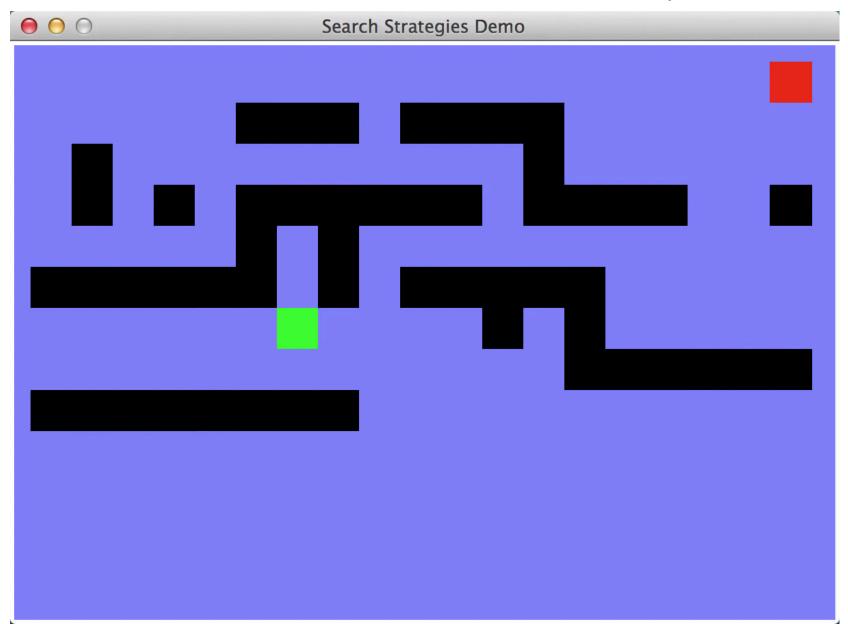




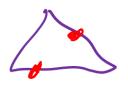
Video of Demo Maze Water DFS/BFS (part 1)



Video of Demo Maze Water DFS/BFS (part 2)

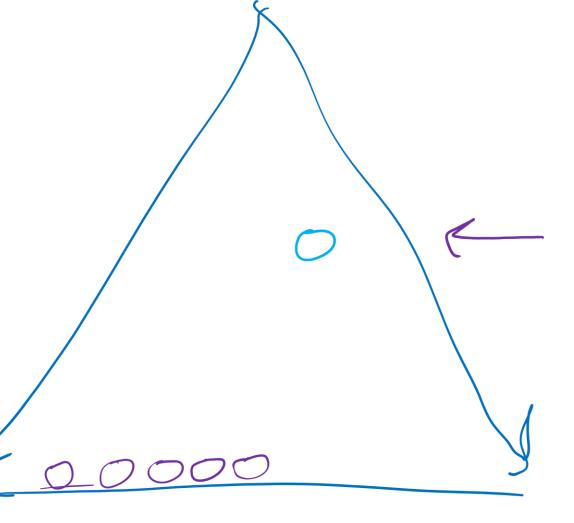


BFS vs DFS



When will BFS outperform DFS?
Optimal goal is shallow

When will DFS outperform BFS?
Optimal goal (3) are at
max depth



Search Algorithm Properties

Complete: Guaranteed to find a solution if one exists?

Optimal: Guaranteed to find the least cost path?

Time complexity?

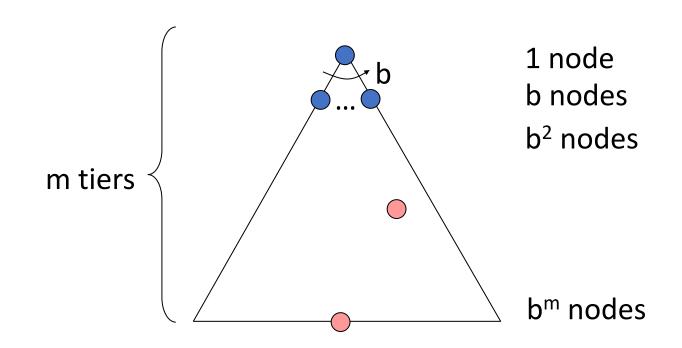
Space complexity?

Cartoon of search tree:

- b is the branching factor
- m is the maximum depth
- solutions at various depths

Number of nodes in entire tree?

■
$$1 + b + b^2 + b^m = O(b^m)$$



Search Algorithm Properties

Complete: Guaranteed to find a solution if one exists?

Optimal: Guaranteed to find the least cost path?

Time complexity?

Space complexity?

Cartoon of search tree:

b is the branching factor

b 1 node b nodes b² nodes

Poll 2

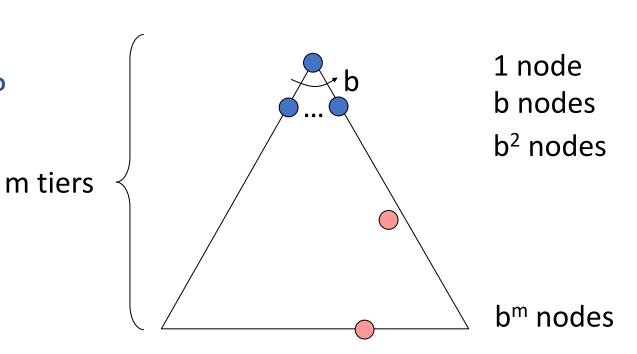
Are these the properties for BFS or DFS?

Takes O(b^m) time

Uses O(bm) space on frontier

Complete with graph search

 Not optimal unless all goals are in the same level (and the same step cost everywhere)



Depth-First Search (DFS) Properties

What nodes does DFS expand?

- Some left prefix of the tree.
- Could process the whole tree!
- If m is finite, takes time O(b^m)

How much space does the frontier take?

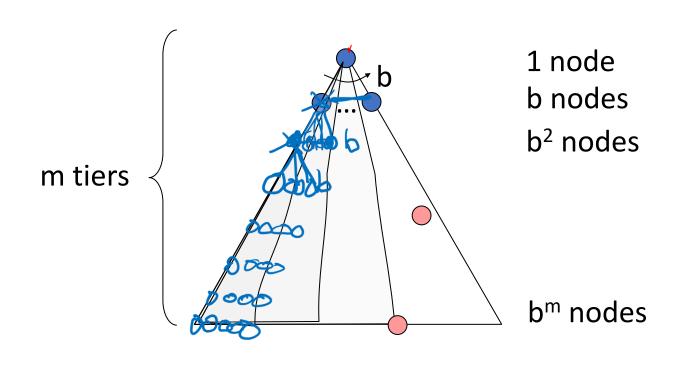
Only has siblings on path to root, so O(bm)

Is it complete?

 m could be infinite, so only if we prevent cycles (graph search)

Is it optimal?

No, it finds the "leftmost" solution, regardless of depth or cost



Breadth-First Search (BFS) Properties

What nodes does BFS expand?

- Processes all nodes above shallowest solution
- Let depth of shallowest solution be s
- Search takes time O(b^s)

How much space does the frontier take?

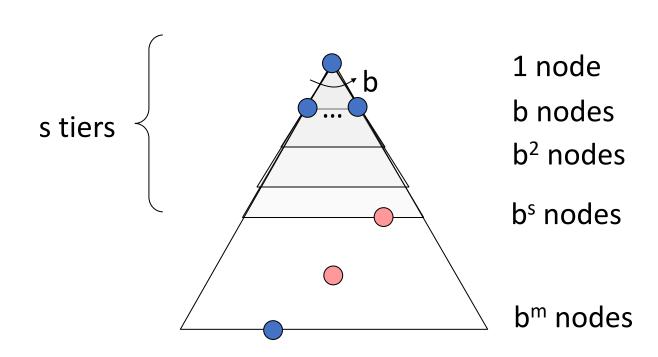
Has roughly the last tier, so O(b^s)

Is it complete?

s must be finite if a solution exists, so yes!

Is it optimal?

Only if costs are all the same (more on costs later)



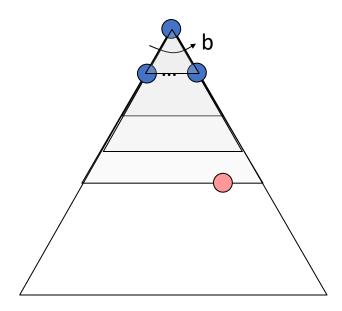
Iterative Deepening

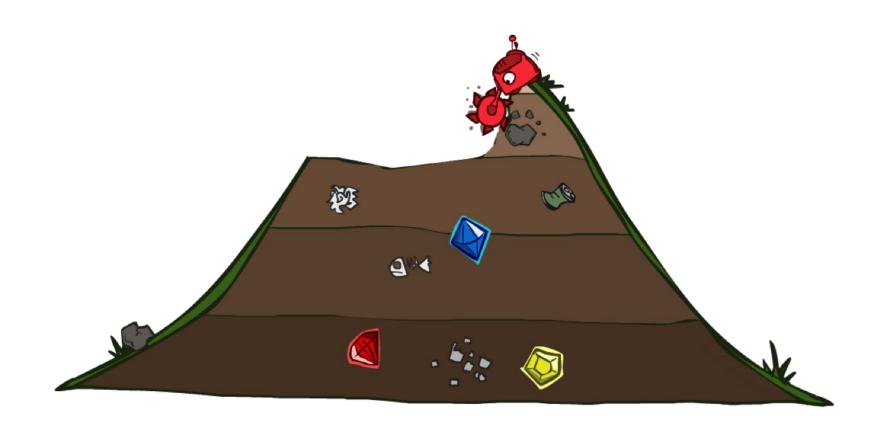
Idea: get DFS's space advantage with BFS's time / shallow-solution advantages

- Run a DFS with depth limit 1. If no solution...
- Run a DFS with depth limit 2. If no solution...
- Run a DFS with depth limit 3.

Isn't that wastefully redundant?

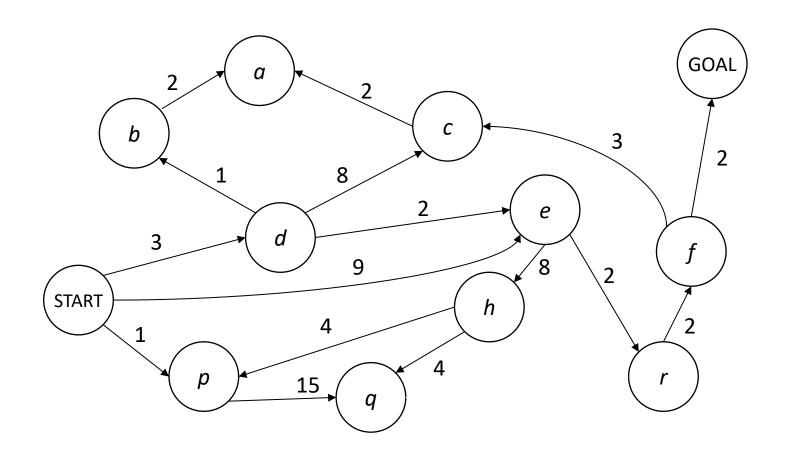
Generally most work happens in the lowest level searched, so not so bad!





Uniform Cost Search

Finding a Least-Cost Path

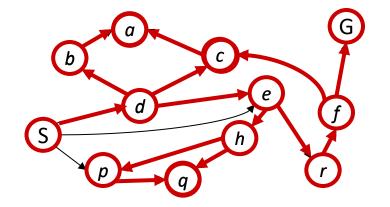


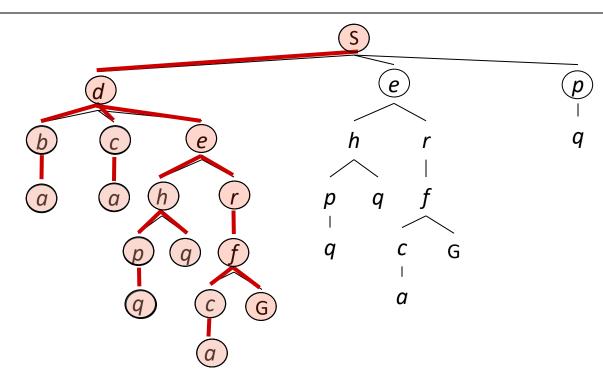
Depth-First (Tree) Search

Strategy: expand a deepest node first

Implementation:

Frontier is a LIFO stack



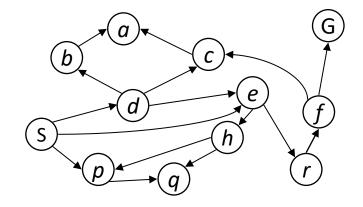


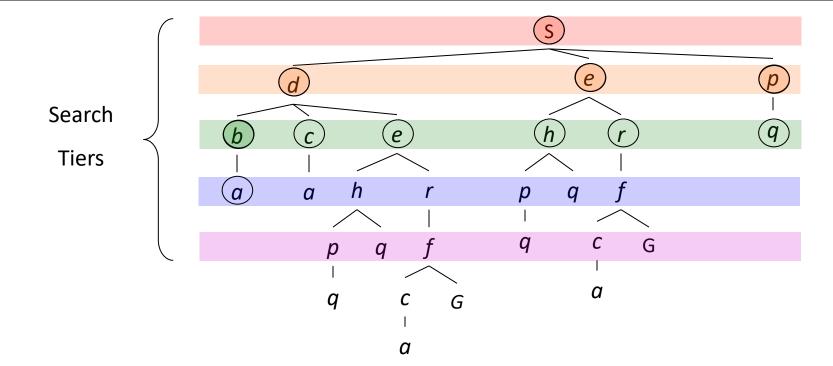
Breadth-First (Tree) Search

Strategy: expand a shallowest node first

Implementation:

Frontier is a FIFO queue



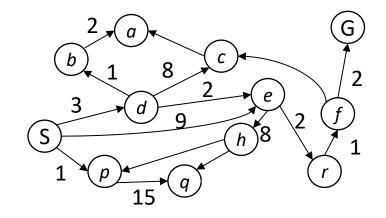


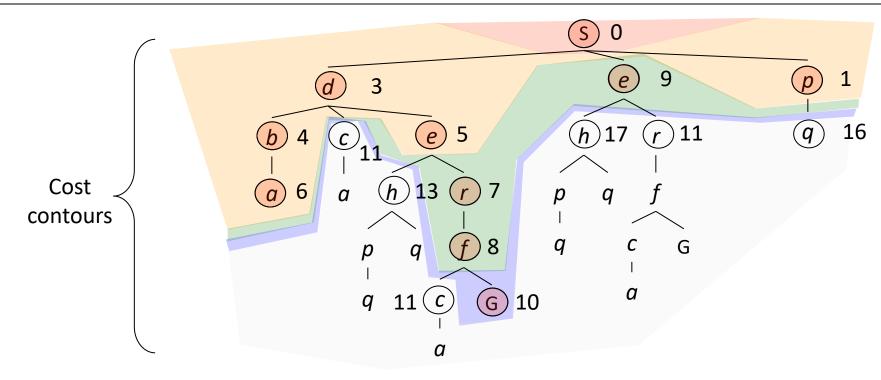
Uniform Cost (Tree) Search

Strategy: expand a cheapest

node first:

Frontier is a priority queue (priority: cumulative cost)





```
function GRAPH SEARCH(problem) returns a solution, or failure
  initialize the explored set to be empty
  initialize the frontier as a specific work list (stack, queue, priority queue)
  add initial state of problem to frontier
  loop do
       if the frontier is empty then
            return failure
       choose a node and remove it from the frontier
       if the node contains a goal state then
            return the corresponding solution
       add the node state to the explored set
       for each resulting child from node
            if the child state is not already in the frontier or explored set then
                add child to the frontier
```

function UNIFORM-COST-SEARCH(problem) returns a solution, or failure initialize the explored set to be empty initialize the frontier as a priority queue using node path_cost as the priority

add initial state of problem to frontier with path_cost = 0

loop do

if the frontier is empty then return failure

choose a node and remove it from the frontier

if the node contains a goal state then

return the corresponding solution

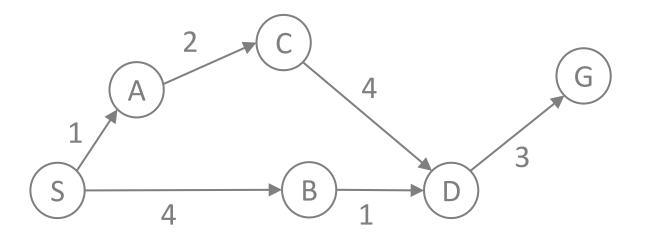
add the node state to the explored set

for each resulting child from node

if the child state is not already in the frontier or explored set then add child to the frontier

else if the child is already in the frontier with higher path_cost then replace that frontier node with child

Walk-through UCS



Walk-through UCS

Frontier

Sto

S-A: 1

S-B. 4

S-A-C. 3

S-A-C-D: 7

S-B-D: 5 ??

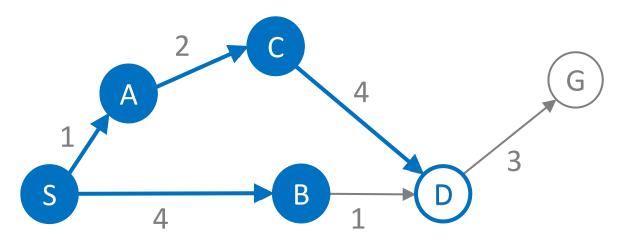
Explored

S

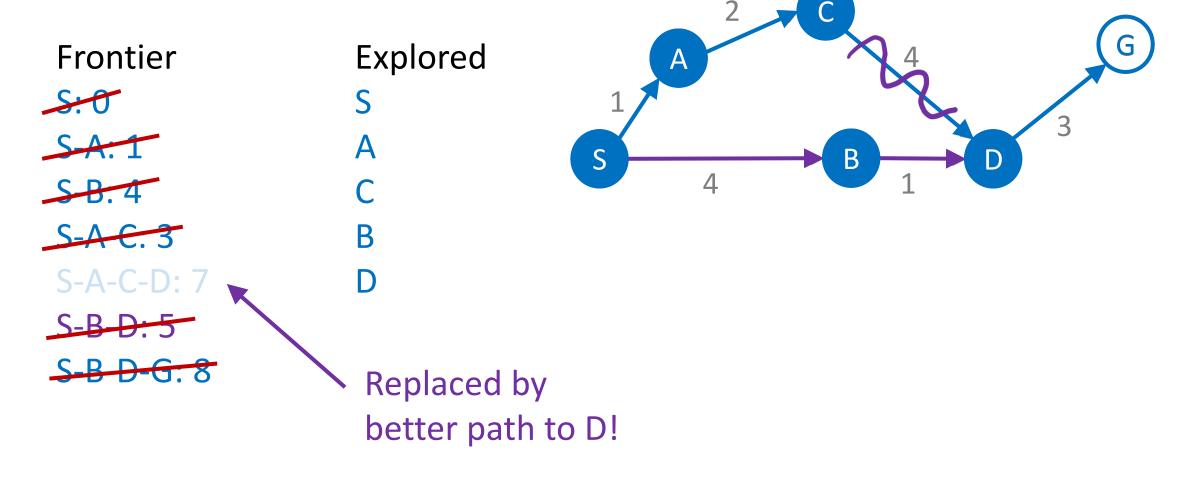
A

C

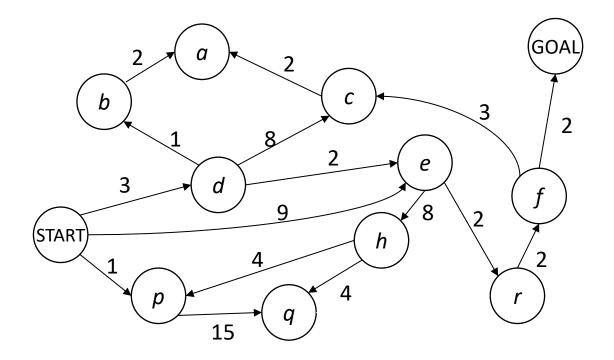
B



Walk-through UCS



Result: S-B-D-G (path cost 8)



Frontier

Sto

Sd. 3

S-e: 9

S-p: 1

S-p-q: 16

S-d-b: 4

S-d-c: 11

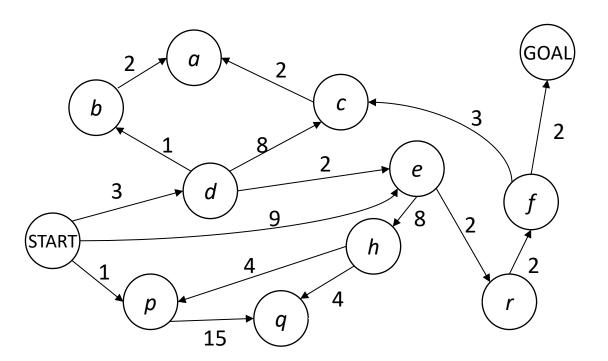
S-d-e: 5 ??

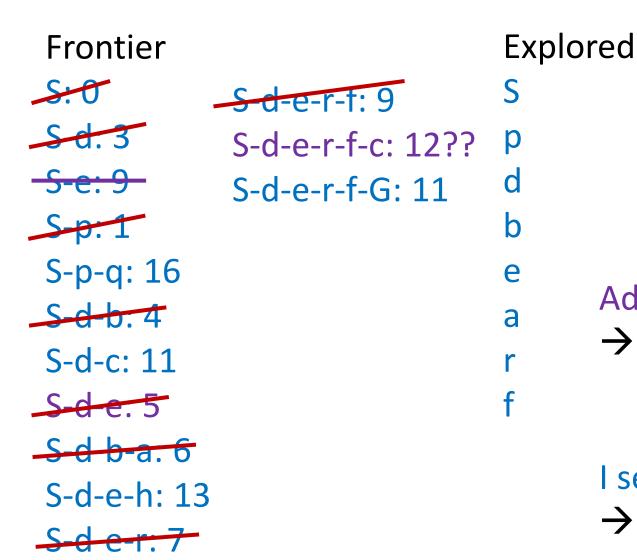
Explored

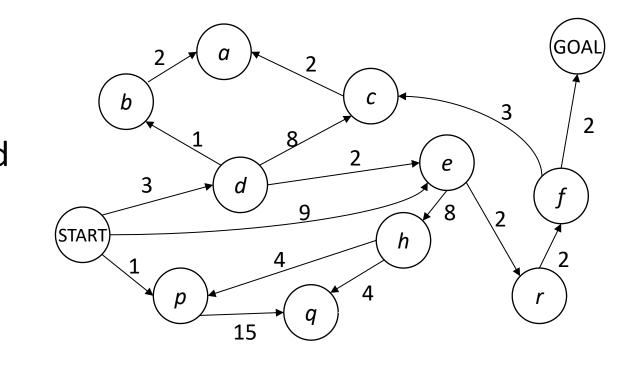
S

p

d







Add S-d-e-r-f-c: 12 to frontier?

→ No, there is a better path to c on the frontier, S-d-c: 11

I see G on the frontier. Are we done?

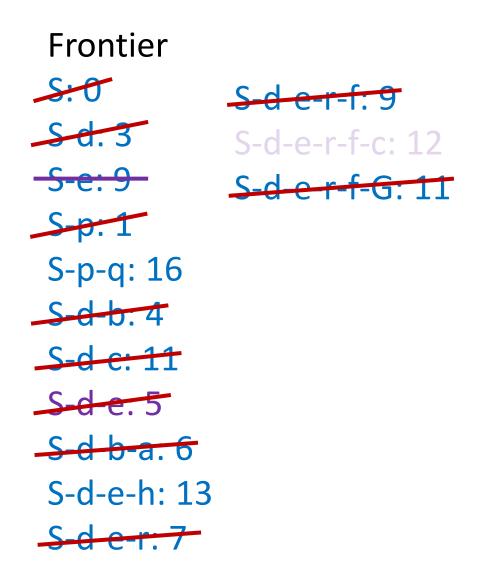
→ No, the goal test doesn't come until after we pop a node from the frontier

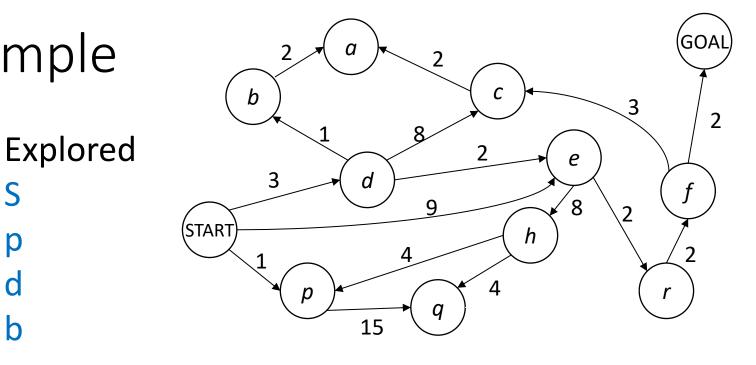
d

b

e

a





FYI: Breaking tie at cost 11 alphabetically

a is already on the explored set, so we don't consider adding S-d-c-a

Result: S-d-e-r-f-G with cost 11

Uniform Cost Search (UCS) Properties

What nodes does UCS expand?

- Processes all nodes with cost less than cheapest solution!
- If that solution costs C^* and arcs cost at least ε , then the "effective depth" is roughly C^*/ε
- Takes time $O(b^{C*/\varepsilon})$ (exponential in effective depth)

How much space does the frontier take?

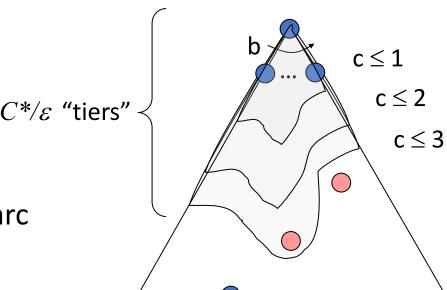
■ Has roughly the last tier, so $O(b^{C^*/\varepsilon})$

Is it complete?

Assuming best solution has a finite cost and minimum arc cost is positive, yes!

Is it optimal?

Yes! (Proof next lecture via A*)



Uniform Cost Issues

Remember:

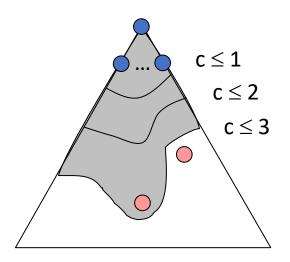
UCS explores increasing cost contours

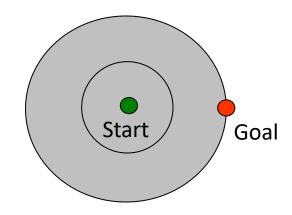
The good:

UCS is complete and optimal!

The bad:

- Explores options in every "direction"
- No information about goal location





We'll fix that!