

# 1 First Order Logic

1. Vocab check: are you familiar with the following terms?

- |                    |                     |
|--------------------|---------------------|
| (a) Objects        | (g) Connectives     |
| (b) Relations      | (h) Equality        |
| (c) Functions      | (i) Quantifiers     |
| (d) Constants      | (j) Atomic Sentence |
| (e) Variables      | (k) Unification     |
| (f) Interpretation |                     |

2. Which of the following FOL sentences correctly expresses its corresponding English sentence?

(a) There was a student at CMU who never did 281 homework but passed the class.  
 $\exists x, \text{IsStudent}(x, \text{CMU}) \wedge \neg \text{DoesHW}(x, 281) \implies \text{Pass}(x, 281)$

(b) If a student likes Pat, they'll pass the class.  
 $\forall x, \text{Student}(x) \wedge \text{Likes}(x, \text{Pat}) \implies \text{Pass}(x, 281)$

(c) All students at CMU who never did 281 homework passed the class.  
 $\forall x, \text{IsStudent}(x, \text{CMU}) \wedge \neg \text{DoesHW}(x, 281) \wedge \text{Pass}(x, 281)$

3. Which of the following is true with respect to the English sentences (a) and (c) above?

(a)  $\models$  (c)    (c)  $\models$  (a)    Both    Neither

4. Forward Chaining

(a) What are the requirements for Knowledge Base in Forward Chaining?

(b) What does FOL Forward Chaining return?

5. DPLL: determine whether the following are satisfiable or unsatisfiable using DPLL.

(a)  $(P \vee Q \vee \neg R) \wedge (P \vee \neg Q) \wedge \neg P \wedge R \wedge U$

$$(b) (P \vee Q) \wedge \neg Q \wedge (\neg P \vee Q \vee \neg R)$$

## 2 Planning

1. Vocab check: are you familiar with the following terms?
  - (a) Predicates
  - (b) Operators
  - (c) Linear Planning
  - (d) Non-linear Planning
  - (e) Inconsistency
  - (f) Interference
  - (g) Competing Needs
  - (h) Complete
  - (i) Sound
  - (j) Optimal
2. What are in the knowledge base of logic agents and classical planning problem, respectively?
3. What are the 3 components when defining an operator?
4. Is linear planning complete? Optimal? What about non-linear planning?
5. The monkey-and-bananas problem is faced by a monkey in a laboratory with some bananas hanging out of reach from the ceiling. A box is available that will enable the monkey to reach the bananas if he climbs on it. Initially, the monkey is at *A*, the bananas at *B*, and the box at *C*. The monkey and box have height *Low*, but if the monkey climbs onto the box he will have height *High*, the same as the bananas. The actions available to the monkey include *Go* from one place to another, *Push* an object from one place to another, *ClimbUp* onto or *ClimbDown* from an object, and *Grasp* or *Ungrasp* an object. The result of a *Grasp* is that the monkey holds the object if the monkey and object are in the same place at the same height. We want to formulate this problem using GraphPlan.
  - (a) Define the initial and goal states.
  - (b) Write the six action schemas, i.e., define the preconditions and effects for each possible action the monkey can take.

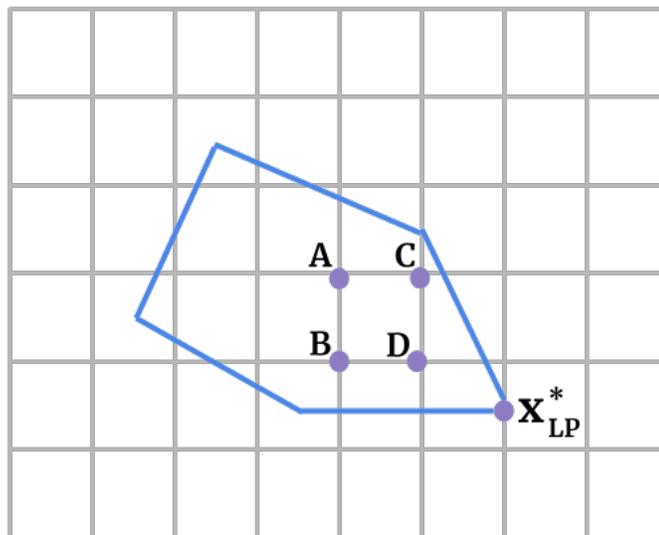


### 3 IP

1. What is the relationship between branch and bound and pruning?

2. Consider the integer programming problem illustrated by the figure below.

- The blue lines represent the boundaries of the feasible region and the gray vertical and horizontal lines represent the integer values for each axis.
- Let  $x_{LP}^*$  be the unique point that minimizes the relaxed linear program. It happens to lie on a vertical gray line and a horizontal blue line.
- Let  $x_{IP}^*$  (unlabeled) be the unique point that minimizes the integer program.
- When running branch and bound, we will explore the  $x_i$  less than constraint subtree before the  $x_i$  greater than constraint subtree (“less” being to the left and down).



(a) Which of the points (A, B, C, or D) can possibly be  $x_{IP}^*$ ?

(b) Which of the points from your answer to part (a) needs to be  $x_{IP}^*$  in order for branch and bound to find the IP solution at the minimum possible depth?

## 4 MDPs

### 1. Concepts:

- (a) What does the Markov Property state?
- (b) What are the Bellman Equations, and when are they used?
- (c) What is a policy? What is an optimal policy?
- (d) How does the discount factor  $\gamma$  affect the agent's policy search? Why is it important?
- (e) What are the two steps to Policy Iteration?
- (f) What is the relationship between  $V^*(s)$  and  $Q^*(s, a)$ ?

2. In a certain country there are  $N$  cities, all connected by roads in a circular fashion. A wandering poet is travelling around the country and staging shows in its different cities. She can choose to move from a city to each of the neighboring ones or she can stay in her current city  $i$  and perform, getting a reward  $r_i$ . If she chooses to travel, she will have a success probability of  $p_i$ . There is a  $1 - p_i$  chance she will encounter a dragon along the way, which means she will have to turn back and wait the next day. If she is successful in travelling, she gains a reward of 0 for the day. And if she is unsuccessful at travelling, she can still perform a little bit when she gets back, giving her a reward of  $r_i/2$ .

Let  $r_i = 1$  and  $p_i = 0.5$  for all  $i$  and let  $\gamma = 0.5$ . For  $1 \leq i \leq N$ , answer the following questions with concrete numbers:

- i) What is the value  $V^{\text{stay}}(i)$  under the policy the wandering poet always chooses to stay?
- ii) What is the value  $V^{\text{next}}(i)$  under the policy the wandering poet always chooses to go to the next city? You may assume that the values of each state converge to the same value.

## 5 Reinforcement Learning: Just Add Water

Rikki the mermaid is trying to learn a general policy for swimming to Mako Island while avoiding Charlotte<sup>1</sup>, the inferior and annoying mermaid. Rikki always starts in grid A shown below.

Rikki's possible environment states are of the form  $(x, y)$ , where  $x \in \{A, B, C\}$ , representing her grid position, and  $y$  is 1 if Charlotte is present in grid C, 0 if she is nowhere on the map. Rikki's possible actions are swim (S) or heat (H). She observes the episodes shown to the right:

<table border="1" style="border-collapse: collapse; width: 60px; height: 100px; margin: auto;"> <tr><td style="text-align: center; padding: 5px;">A</td></tr> <tr><td style="text-align: center; padding: 5px;">B</td></tr> <tr><td style="text-align: center; padding: 5px;">C</td></tr> </table>	A	B	C	$s$	$a$	$s'$	$r$
	A						
	B						
	C						
		(A, 1)	S	(C, 1)	-4		
		(A, 1)	S	(B, 1)	0		
		(B, 1)	S	(C, 1)	-4		
		(A, 0)	S	(C, 0)	2		
		(A, 0)	S	(B, 0)	0		
		(B, 0)	S	(C, 0)	2		
		(A, 1)	S	(B, 1)	0		
		(B, 1)	H	(B, 0)	0		
	(B, 0)	S	(C, 0)	2			

- Which of the following are techniques Rikki can use to try finding an optimal policy (without having to use any other process in addition to the technique)?
  - Policy iteration
  - TD learning
  - Estimate  $T$  and  $R$ , then policy iteration
  - Q-learning
  - Value iteration, then policy extraction
  - Approximate Q-learning
- Let  $Q(s, a) = 0$  initially for all Q-states  $(s, a)$ , and that  $(C, 0)$  and  $(C, 1)$  are terminal states. Let  $\gamma = \alpha = 0.5$ . Now calculate  $Q(s, a)$  for the entries in the following table after Q-learning.

$s$	(A, 1)	(A, 0)	(B, 1)	(B, 0)	(A, 1)	(B, 1)
$a$	S	S	S	S	H	H
$Q(s, a)$						

- According to the observed episodes, what is Rikki's optimal policy?
- Suppose Rikki uses  $\epsilon$ -greedy search, and that her environment is deterministic. She starts with  $\epsilon = 0$  and doesn't change it. Is she guaranteed to learn the optimal policy? Why or why not?

<sup>1</sup>who sucks

5. Now suppose Rikki sets  $\epsilon = 1$  and doesn't change it. Is she guaranteed to learn the optimal policy? Why/why not?

6. Rikki's no ordinary girl, so she decides to use approximate Q-learning, with  $\alpha = \gamma = 0.5$ . Suppose she has three features  $f_1, f_2, f_3$ , and corresponding weights  $w_1, w_2, w_3$ . Her approximate function is

$$Q_w(s, a) = w_1^2 f_1(s, a) + e^{w_2 f_2(s, a)} + w_3^3 f_3(s, a).$$

Initially,  $w_1 = 2, w_2 = 0, w_3 = 3$ . Suppose  $f_1((A, 1), S) = f_2((A, 1), S) = f_3((A, 1), S) = 1$ .

- (a) What is the approximate Q-value for  $((A, 1), S)$ ?
- (b) What is the value of  $((A, 1), S)$  according to Rikki's first observation  $((A, 1), S, (C, 1), -4)$ ? Suppose  $\max_{a'} Q_w((C, 1), a') = 4$ .
- (c) What are the new weights after the first observation?

## 6 Probability

Recall the example of *marginalization*, which means summing out variables from a joint distribution. Consider three random variables  $A$ ,  $B$ , and  $C$  with domains  $\{a_1, a_2\}$ ,  $\{b_1\}$ , and  $\{c_1, c_2, c_3\}$ , respectively. Remember that  $P(C)$  refers to the table of probabilities of all the elements of the domain  $C$ .

1. Express  $P(C)$  in terms of the joint distribution  $P(A, B, C)$ . Your answers should contain summations.
2. Express  $P(C)$  in terms of  $P(B)$ ,  $P(A | B)$  and  $P(C | A, B)$ . Reorder any summations in your solution to minimize the number of arithmetic operations.
3. Expand the sums from part (b) to show the two elements of  $P(C)$  ( $P(c_1)$ ,  $P(c_2)$ , and  $P(c_3)$ ) in terms of the individual probabilities (e.g.  $P(a_2)$ ,  $P(b_1)$  instead of  $P(A)$  or  $P(B)$ ).
4. Each of the following terms represents a conditional probability table. What do the entries for each table sum to? (For example, the entries of the table  $P(A)$  sum to 1.)
  - (a)  $P(A | B)$
  - (b)  $P(A | C)$
  - (c)  $P(C | a_1, b_1)$
  - (d)  $P(C | a_1, B)$
  - (e)  $P(C | A, b_1)$