Warm Up: Represent this Blocks World

A robot arm (yellow) can pick up and put down blocks to form stacks.

It cannot pick up a block that has another block on top of it.

It cannot pick up more than one block at a time.

Any number of blocks can sit on the table.

Only one block fits on top of another.

How would you represent this block world to be able to run BFS? How would you represent this block world to use logic to find a plan? Hint: How would you represent the states, actions, goals, transitions?

Announcements

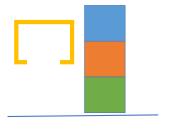
Midterm 1 Exam Graded

Assignments:

- HW5
 - Due Tue 2/25, 10pm
- P3: Logic and Classical Planning
 - Out 2/22, Due Thu 3/5 10 pm before spring break!
- HW6
 - Out Tue 2/25, 10pm
 - Due Tue 3/3, 10pm

Al: Representation and Problem Solving

Classical Planning or Symbolic Planning



Instructors: Pat Virtue & Stephanie Rosenthal

Slide credits: CMU AI, http://ai.berkeley.edu

Represent this Blocks World

A robot arm (yellow) can pick up and put down blocks to form stacks.

It cannot pick up a block that has another block on top of it.

It cannot pick up more than one block at a time.

Any number of blocks can sit on the table.



How would you represent this block world to be able to run BFS?

Zon: [(blue,ora), (ora., green)], hand: None table: [green] }, orange

States

Actions

Goals

Transitions

Represent this Blocks World

A robot arm (yellow) can pick up and put down blocks to form stacks.

It cannot pick up a block that has another block on top of it.

It cannot pick up more than one block at a time.

Any number of blocks can sit on the table.



Actions

Goals

Transitions

Pros and Cons of the Approaches

BFS

- + concise representation of objects
- more challenging to write a definition of the actions for each possible state Logical Planning
- + successor-state axioms are relatively concise to write but there are many
- states and fluents are cumbersome to write and debug

Classical Planning:

- + concise object representation and clearer action definitions
- still only works for deterministic fully observable worlds

Symbolic Representation

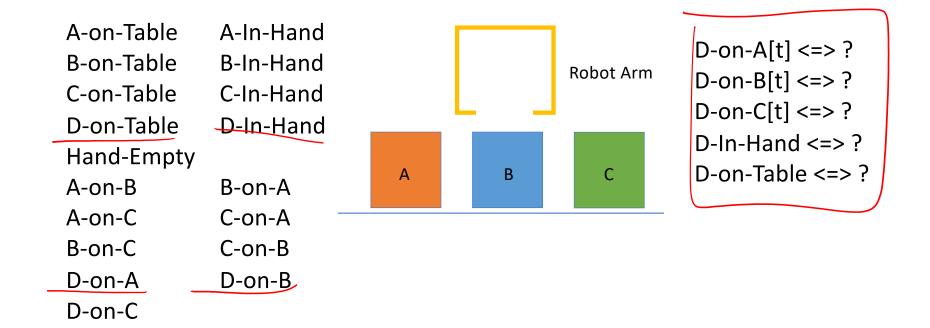
In Logic, we represent each object in location as a Boolean proposition

A-on-Table	A-In-Hand			
B-on-Table	B-In-Hand			Robot Arm
C-on-Table	C-In-Hand			
Hand-Empty				
A-on-B	B-on-A	•		C
A-on-C	C-on-A	Α	В	
B-on-C	C-on-B			
Clear-A	Clear-B			
Clear-C				

Symbolic Representation

In Logic, we represent each object in location as a Boolean proposition

The issue is that every time you add an object into this world, your number of propositions expands exponentially as do your successor-state axioms



Idea of Classical Planning

Notes: We can give them any names we want! And we can change representation too!

Represent objects/values separately from the state (instances)

A, B, C, Table

Define predicates as true/false functions over the objects

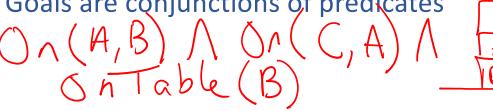
On (A, Table) = True On (A,B) = False

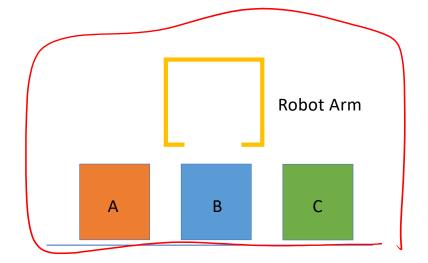
Ontable (

States are conjunctions of predicates

On Table (A) \(On table (5) \\
On table (C) \(\) Hand \(\) \(\)

Goals are conjunctions of predicates





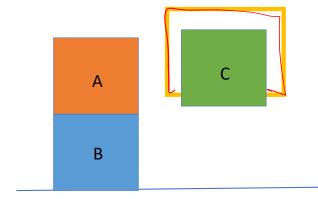
Piazza Poll 1

Which predicates apply to this state? (Select all that apply)

Instances: A, B, C

Predicates:

- 1) In-Hand(A)
- 2) In-Hand(B)
- 3) In-Hand(C)
- 4) On-Table(A)
- 5) On-Table(B)
- 6) On-Table(C)
- 7) On-Block(B,C)
- 8) On-Block(A,B)
- 9) HandEmpty()



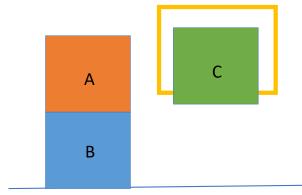
Piazza Poll 1

Which predicates apply to this state? (Select all that apply)

Instances: A, B, C

Predicates:

- 1) In-Hand(A)
- 2) In-Hand(B)
- (3) In-Hand(C)
- 4) On-Table(A)
- 5) On-Table(B)
- 6) On-Table(C)
- 7) On-Block(B,C)
- 8) On-Block(A,B)
- 9) HandEmpty()



Full State Description

Instances: A, B, C

Predicates:

In-Hand(C)
On-Table(B)
On-Block(A,B)
Clear(A)
Clear(C)

Optional: ~HandEmpty(), ~On-Table(C), ~On-Table(A), ~On-Block(B,A), ~On-Block(C,A), ~On-Block(B,C), ~On-Block(C,B), ~On-Block(A,C), ~Clear(B), ~In-Hand(A), ~In-Hand(B)

Operators

Operators change the state by adding/deleting predicates

Preconditions:

Actions can be applied only if all precondition predicates are true in the current state

Effects:

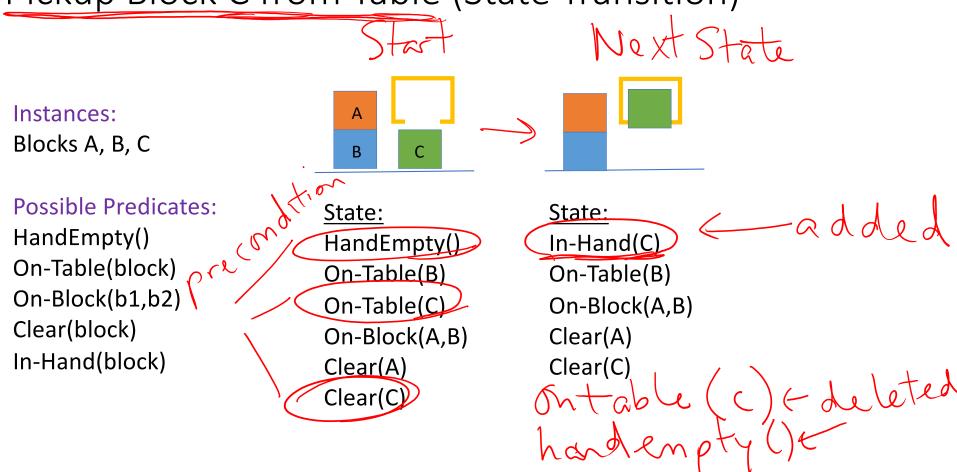
New state is a copy of the current predicates with the addition or deletion of specified predicates

Unlike the successor-state axioms, we do not explicitly represent time and we can use our objects and predicates to more easily scale to new more complex problems (e.g., new objects, predicates, and operators).

Rules of Block World

Blocks are picked up and put down by the hand
Blocks can be picked up only if they are clear
Hand can pick up a block only if the hand is empty
Hand can pick up and put down blocks on blocks or on the table

Pickup Block C from Table (State Transition)



Pickup Block C from Table (Preconditions, Effects)

Instances:

Blocks A, B, C

Possible Predicates:

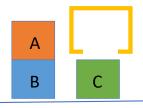
HandEmpty()

On-Table(block)

On-Block(b1,b2)

Clear(block)

In-Hand(block)



State:

HandEmpty()

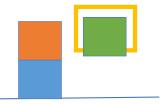
On-Table(B)

On-Table(C)

On-Block(A,B)

Clear(A)

Clear(C)



State:

In-Hand(C)

On-Table(B)

On-Block(A,B)

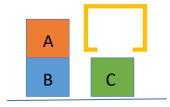
Clear(A)

Clear(C)

Delete HandEmpty()

Delete On-Table(C)

Operator: Pickup-Block-C from Table



Preconditions

HandEmpty()

Clear(C)

On-Table(C)

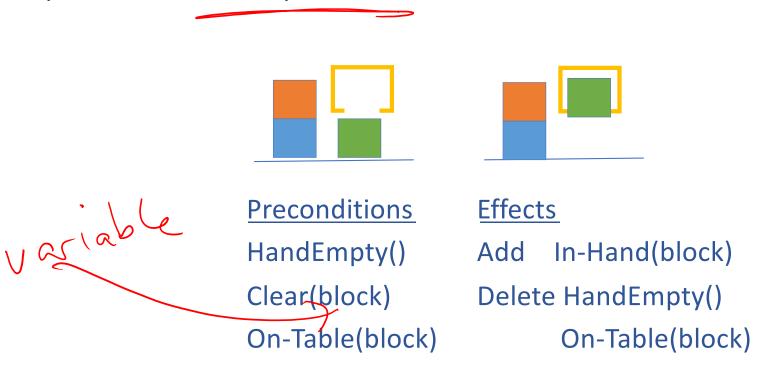
Effects

Add In-Hand(C)

Delete HandEmpty()

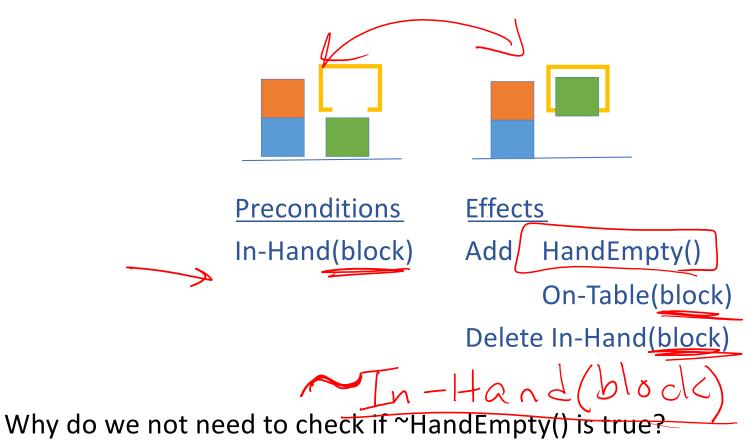
On-Table(C)

Operator: Pickup-Block from Table



Create a variable that takes on the value of a particular instance for all times it appears in an operator.

Operator: PutDown-Block on Table



Full State Description

```
Instances: A, B, C

Predicates:

In-Hand(C)
On-Table(B)
On-Block(A,B)
Clear(A)
Clear(C)

Optional: ~HandEmpty(), ~On-Table(C), ~On-Table(A), ~On-Block(B,A), ~On-Block(C,A), ~On-Block(B,C), ~On-Block(C,B), ~On-Block(A,C), ~Clear(B), ~In-Hand(A), ~In-Hand(B)
```

RULE OF THUMB: If you must match that Predicate is explicitly not true, you must include ~Predicate in the state description.

Operators for Block Stacking

```
Pickup_Table(b): Pickup_Block(b,c):
```

Pre: HandEmpty(), Clear(b), On-Table(b)

Pre: HandEmpty(), On-Block(b,c), b!=c

Add: In-Hand(b), Clear(c)

Delete: HandEmpty(), On-Table(b)

Delete: HandEmpty(), On-Block(b,c)

Putdown_Table(b): Putdown_Block(b,c):

Pre: In-Hand(b), Clear(c)

Add: HandEmpty(), On-Table(b)

Add: HandEmpty(), On-Block(b,c)

Delete: In-Hand(b)

Delete: Clear(c), In-Hand(b)

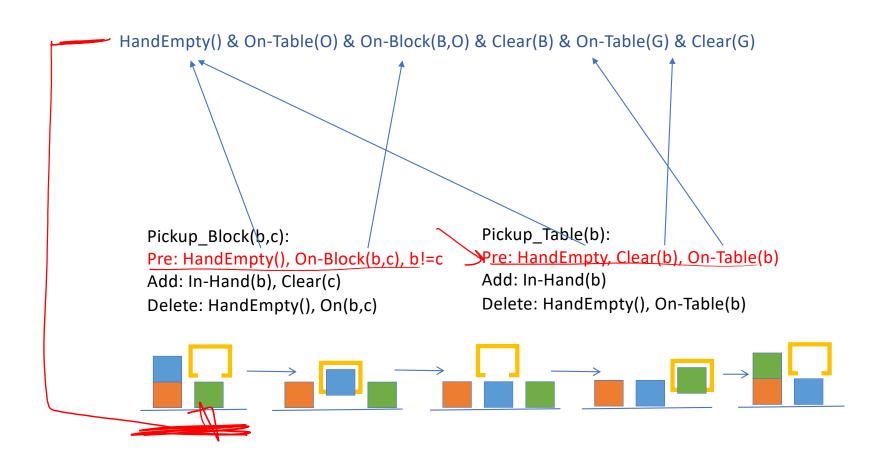
Why do we need separate operators for table vs on a block?

Example Matching Operators

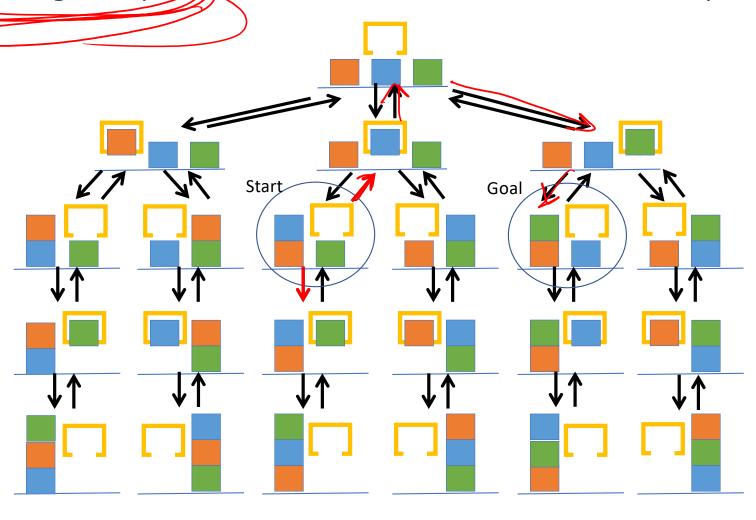
HandEmpty() & On-Table(O) & On-Block(B,O) & Clear(B) & On-Table(G) & Clear(G)



Example Matching Operators



Planning Graph (sometimes called Reachability Graph)



Example Matching Operators

```
HandEmpty() & On-Table(O) & On-Block(B,O) & Clear(B) & On-Table(G) & Clear(G)

**Pickup_Block(B,O)**

On-Table(O) & Clear(B) & On-Table(G) & Clear(G) & In-Hand(B) & Clear(O)

**Putdown_Table(B)**

On-Table(O) & Clear(O) & On-Table(G) & Clear(G) & Clear(B) & On-Table(B) & HandEmpty()

**Pickup_Table(G)**

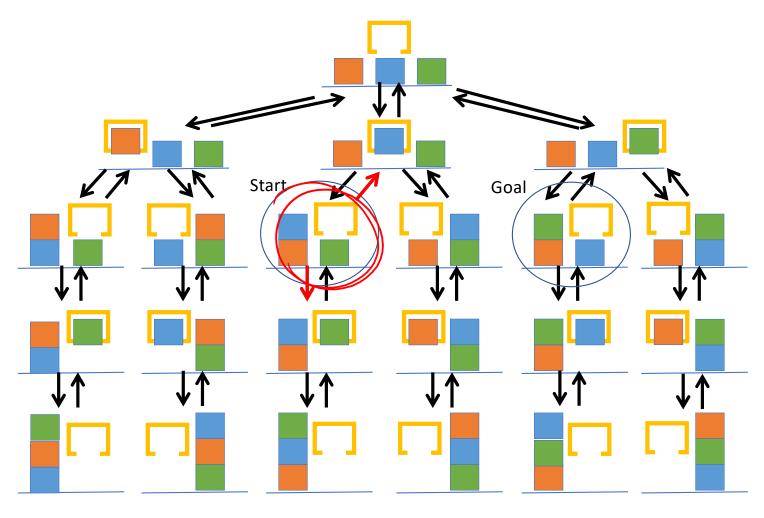
On-Table(O) & Clear(B) & Clear(G) & Clear(O) & On-Table(B) & In-Hand(G)

**Putdown_Block(G,O)**

On-Table(O) & Clear(B) & Clear(G) & On-Table(B) & On-Block(G,O) & HandEmpty()
```



What kind of search can we do with a Planning Graph?



Finding Plans with Symbolic Representations

Breadth-First Search

Sound? Yes

Complete? Yes

Optimal? Yes

Soundness - all solutions found are legal plans

Completeness - a solution can be found whenever one actually exists

Optimality - the order in which solutions are found is consistent with some measure of plan quality

Linear Planning

Since we have a conjunction of goal predicates, let's try to solve one at a time

- Maintain a stack of achievable goals
- Use BFS (or anything else) to find a plan to achieve that single goal
- Add a goal back on the stack if a later change makes it violated

```
Goal Stack:
On-Table(B)
On-Table(O)
On-Block(G,O)
Clear(G)
Clear(B)
```

```
Action Plan:
On-Table(B)

Pickup-Block(B,O)

Put-Table(B)
```

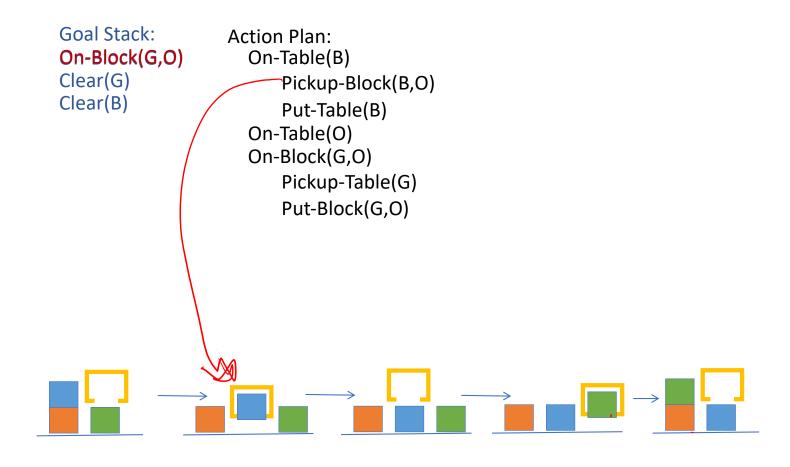




Goal Stack: Action Plan:
On-Table(O) On-Block(G,O) Pickup-Block(B,O)
Clear(G) Put-Table(B)
Clear(B) On-Table(O)







```
Goal Stack:
Clear(G)
Clear(B)

Action Plan:
On-Table(B)

Pickup-Block(B,O)

Put-Table(B)

On-Table(O)

On-Block(G,O)

Pickup-Table(G)

Put-Block(G,O)

Clear(G)

Clear(B)
```



Goal Stack:
On-Block(O,G)
On-Table(B)
On-Block(G,B)
Clear(O)

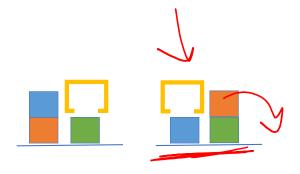
Action Plan:
On-Block(O,G)

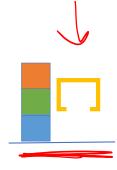
Pickup-Block(B,O)

Put-Table(B)

Pickup-Table(O)

Put-Block(O,G)





```
Goal Stack:
On-Table(B)
On-Block(G,B)
Clear(O)
```

```
Action Plan:
On-Block(O,G)
Pickup-Block(B,O)
Put-Table(B)
Pickup-Table(O)
Put-Block(O,G)
On-Table(B)
```



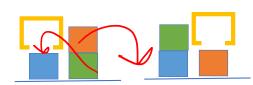




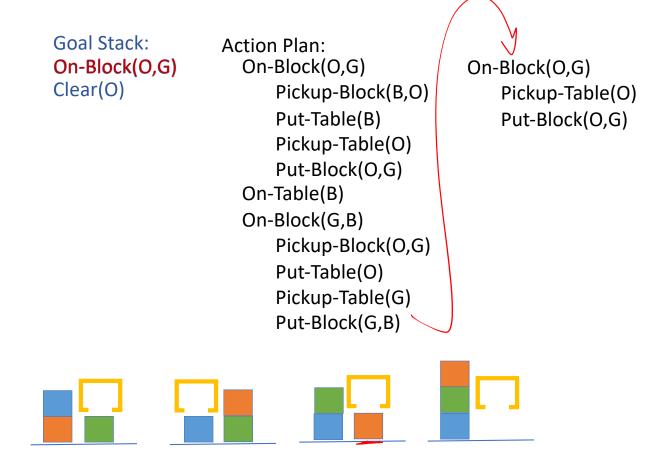
```
Goal Stack:
On-Block(G,B)
Clear(O)

Action Plan:
On-Block(O,G)
Pickup-Block(B,O)
Put-Table(B)
Pickup-Table(O)
Put-Block(O,G)
On-Table(B)
On-Block(G,B)
Pickup-Block(O,G)
Put-Table(O)
Put-Table(O)
Put-Table(O)
Pickup-Table(G)
Put-Block(G,B)
```









Linear Planning Example 2

```
Goal Stack:
                  Action Plan:
Clear(O)
                     On-Block(O,G)
                                              On-Block(O,G)
                        Pickup-Block(B,O)
                                                  Pickup-Table(O)
                                                  Put-Block(O,G)
                        Put-Table(B)
                        Pickup-Table(O)
                                              Clear(O)
                        Put-Block(O,G)
                     On-Table(B)
                     On-Block(G,B)
                        Pickup-Block(O,G)
                        Put-Table(O)
                        Pickup-Table(G)
                        Put-Block(G,B)
```

Linear Planning Example 2

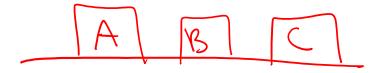
Goal Stack: Action Plan: On-Block(O,G) On-Block(O,G) Pickup-Block(B,O) Pickup-Table(O) Put-Table(B) Put-Block(O,G) Pickup-Table(O) Clear(O) Put-Block(O,G) On-Table(B) What happened? On-Block(G,B) Pickup-Block(O,G) <u>Is linear planning sound?</u> Put-Table(O) Is linear planning complete? Pickup-Table(G) Is linear planning optimal? Put-Block(G,B)

Sussman's Anomaly

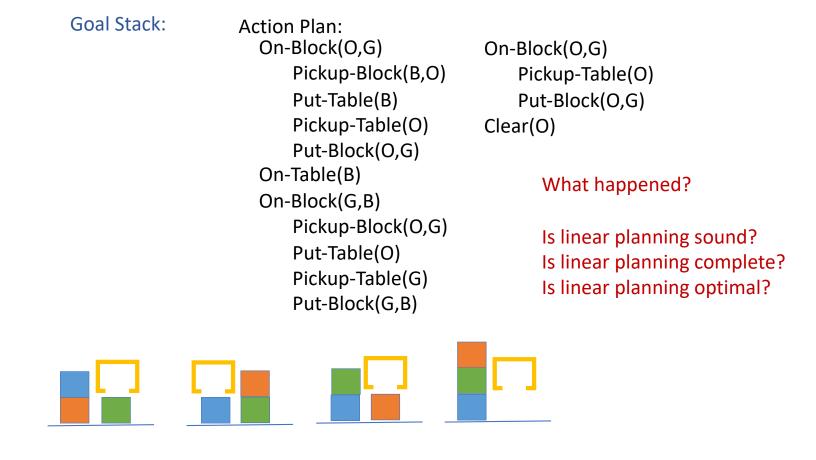
A weakness of linear planning is that sometimes you get long plans
One goal can be achieved
The second goal immediately undoes it

In fact, there are some problems for which solving goals one at a time will never result in a feasible plan.

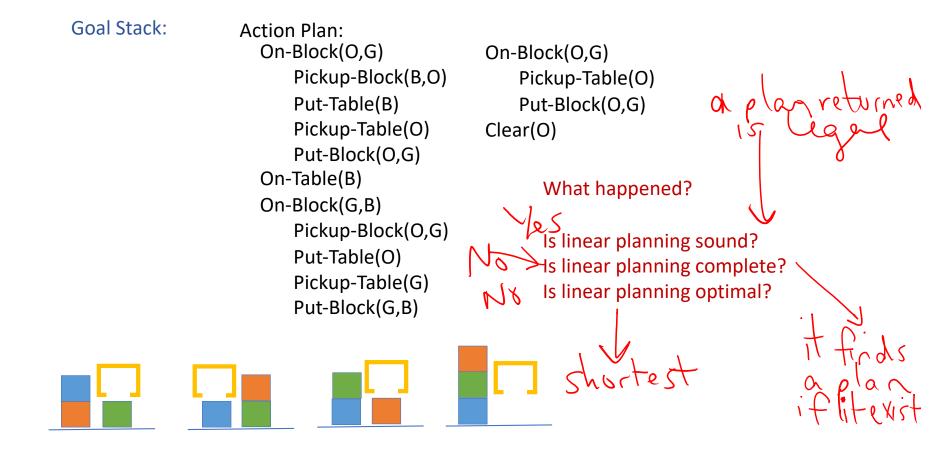
Note: This isn't just a choice of goals. The anomaly happens no matter which goal is first



Linear Planning Soundness, Completeness, Optimality



Piazza Poll 2



Non-Linear Planning

Interleave goals to achieve plans

- Maintain a set of unachieved goals
- Search all interleavings of goals
- Add a goal back to the set if a later change makes it violated

Non-Linear Planning Example (same as Lin Plan 2)

Goal Set:
On-Block(O,G)
On-Table(B)
On-Block(G,B)
Clear(O)

Action Plan:
On-Block(O,G)
Pickup-Block(B,O)
Put-Table(B)
Stop and Switch Goals!

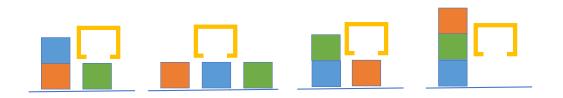




Linear Planning Example 2

```
Goal Set:
On-Block(O,G)
On-Table(B)
On-Block(G,B)
Clear(O)
```

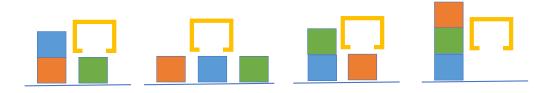
```
Action Plan:
On-Block(O,G)
Pickup-Block(B,O)
Put-Table(B)
Stop and Switch Goals!
On-Block(G,B)
Pickup-Table(G)
Put-Block(G,B)
```



Non-Linear Planning Example

Goal Set:
On-Block(O,G)
On-Table(B)
On-Block(G,B)
Clear(O)

Action Plan:
On-Block(O,G)
Pickup-Block(B,O)
Put-Table(B)
Stop and Switch Goals!
On-Block(G,B)
Pickup-Table(G)
Put-Block(G,B)
On-Block(O,G)
Pickup-Table(O)
Put-Block(O,G)



Non-Linear Planning

Interleave goals to achieve plans

- Maintain a <u>set of unachieved</u> goals
- Search all meterleavings of goals
- Add a goal back to the set if a later change makes it violated

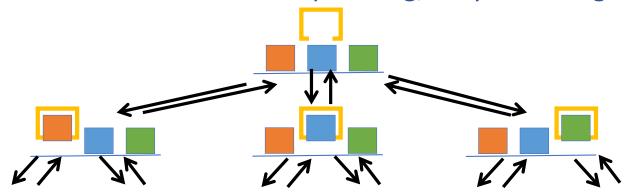
It is complete, but takes longer to search
It can produce shorter plans

Optimal plans if all interleavings are searched

Size of the Search Tree



A planning tree's size is exponential in the number of predicates Even if we use linear or non-linear planning, they use this graph



Can we reduce the size of the planning graph?

GraphPlan and GraphPlan Graph Representation

Construct an approximation of the planning graph in polynomial space

■ The GraphPlan graph computes the **possibly reachable** states although they aren't necessarily feasible multiple actions Sfirst time I have a plan w/o mutex alctions

Planning graphs contain two types of layers

- Proposition layers all reachable predicates
- Action layers actions that could be taken
- Both layers represent one time step

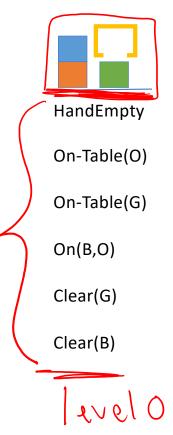
GraphPlan algorithm includes two subtasks

Textend: One time step (two layers) in the planning graph

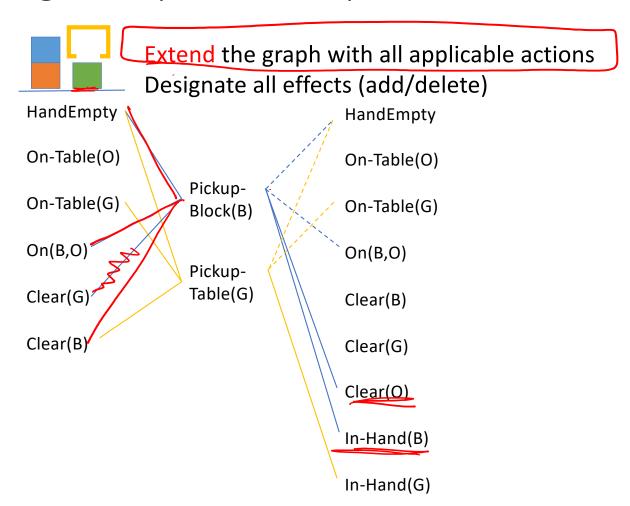
Search: Find a valid plan in the planning graph

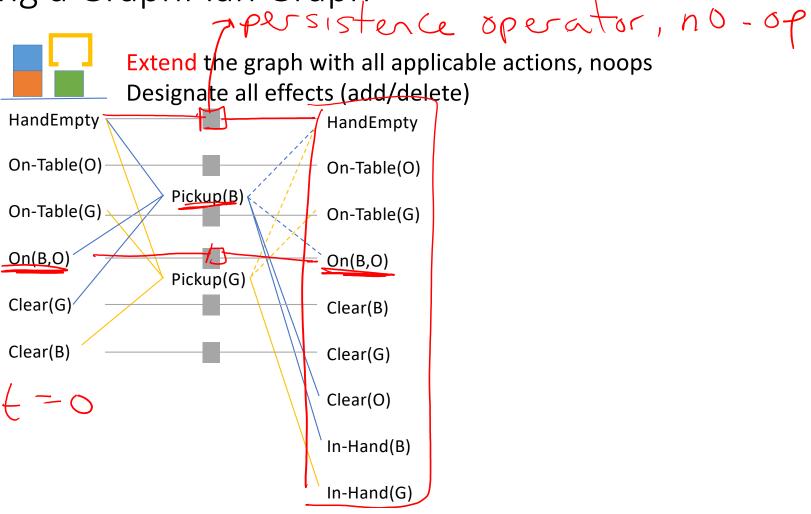
GraphPlan finds a plan or proves that no plan has fewer time steps

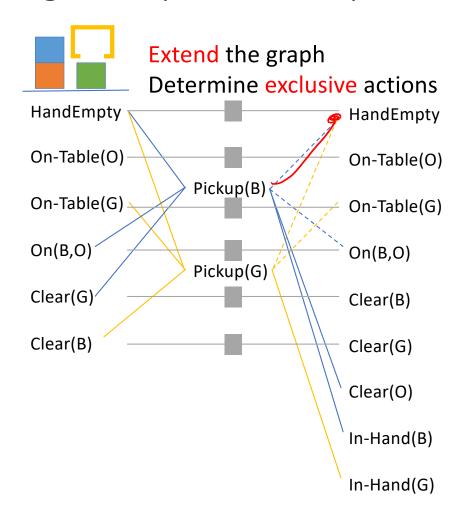
■ Each time step can contain multiple actions



Start the planning graph with all starting predicates





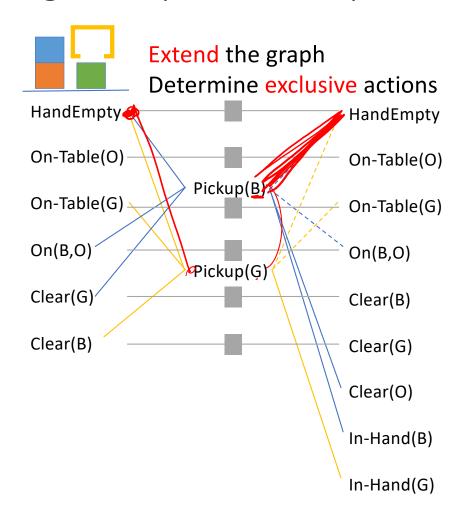


Actions A and B are exclusive (mutex) at action-level i, if:

Interference: one action effect deletes or negates a precondition of the other

Inconsistency: one action effect deletes or negates the effect of the other

Competing Needs: the actions have preconditions that are mutex in proposition-level *i* – 1

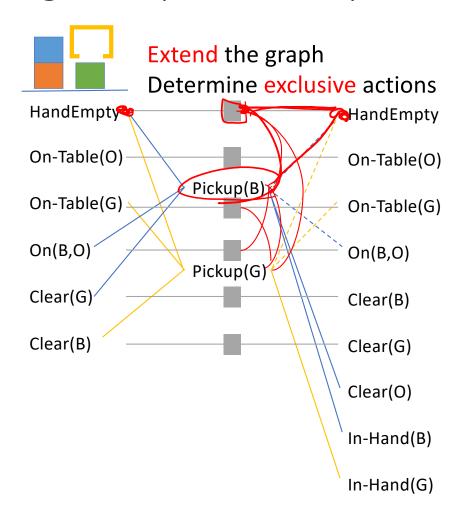


Actions A and B are **exclusive** (mutex) at action-level i, if:

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Competing Needs: the actions have preconditions that are mutex in proposition-level i-1

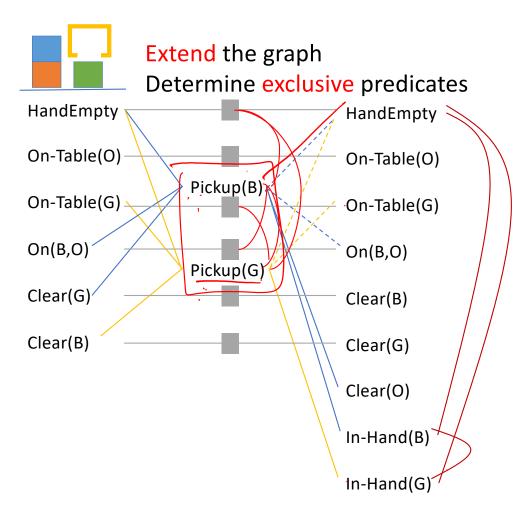


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Actions A and B are **exclusive** (mutex) at action-level i, if:

Interference: one action effect deletes or negates a precondition of the other

Inconsistency: one action effect deletes or negates the effect of the other

Competing Needs: the actions have preconditions that are mutex in proposition-level i-1

Propositions P and Q are *exclusive* (*mutex*) at action-level *i*, if:

Negation: They are the negation of each other

Inconsistent Support: all actions that produce those propositions at i-1 are mutex

Searching the GraphPlan Graph

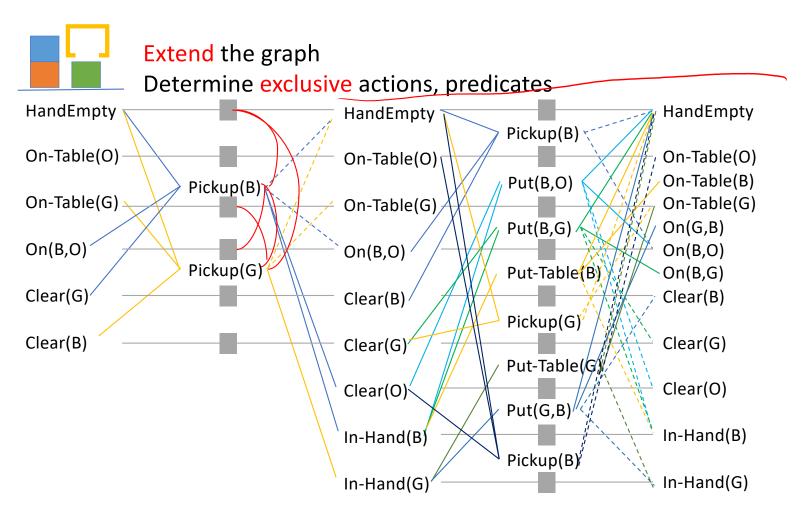
Extend until first time all goals are present at a proposition level

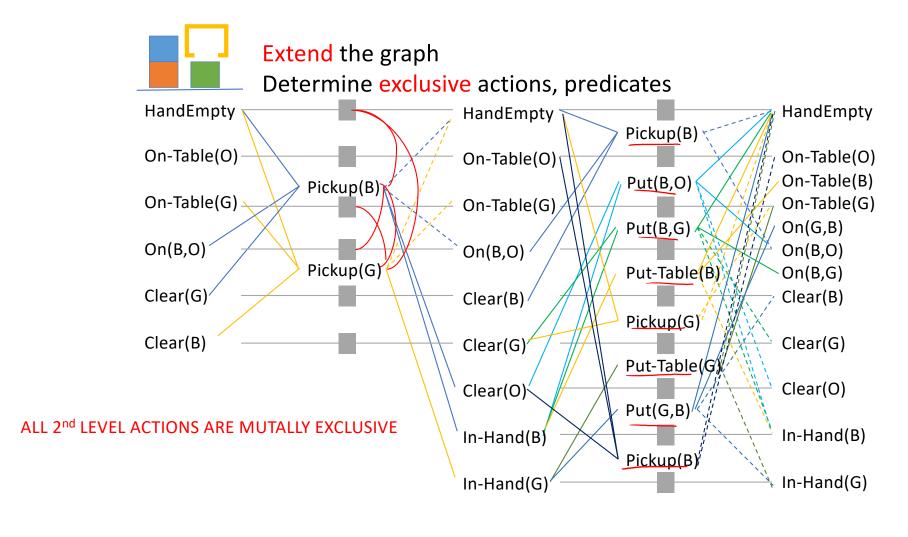
May not be a solution, at that level

For each goal (predicate) present (in some arbitrary order)

- Select an action at level *i*=1 that achieves that goal and is not exclusive with any other action already selected at that level
- Add all its preconditions to the set of goals at level i-2
- Do this for all the goals at level i
 - Use already selected actions, when possible
- Backtrack if no non-exclusive action exists

If search is exhausted, extend planning graph one more proposition level





Piazza Poll 3

What kind of mutex are actions to each other? (select all that apply)

1) Pickup-pickup are interference mutex preconditions

2) Pickup-pickup are inconsistency

3) Pickup-pickup are competing needs

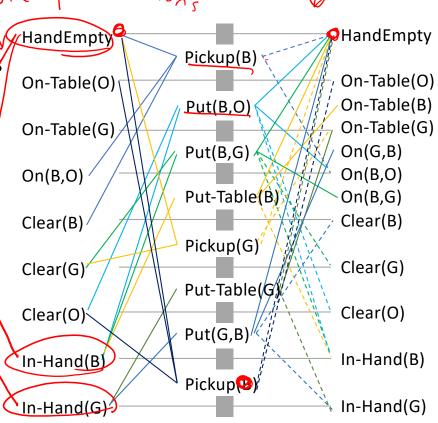
- 4) Pickup-put are interference
- 5) Pickup-put are inconsistency
- 6) Pickup-put are competing needs

Actions A and B are **exclusive** (mutex) at action-level *i*, if:

Interference: one action effect deletes or negates a precondition of the other

Inconsistency: one action effect deletes or negates the effect of the other

Competing Needs: the actions have preconditions that are mutex in proposition-level i-1



GraphPlan Takeaways

GraphPlan is a relaxation of other classical planning search techniques like BFS

It creates a different kind of graph that allows you to decide that **no plan is reachable at a given depth**.

If it finds a **reachable** solution, it may not be a feasible solution because it **allows you to perform multiple actions at the same time**.

The search graph is linear space in the number of predicates Know the differences between the mutex conditions!!

Literals: Each thing/object in our model

i = Instance("name",TYPE)

Inky Pink Oyde

Variables: Can take on any TYPE thing

 $v = Variable("v_name", TYPE)$

Block World Example:

Pickup_from_Table(b):

Pre: HandEmpty(), Clear(1), On-Table(1)

Add: In-Hand(b)

Delete: HandEmpty(), On-Table(b)

Instances: "A", "B", "C" of type BLOCK

Variable: "b" of type BLOCK

In this operator, b can take on the

value of any block instance

Literals: Each thing/object in our model

```
i_a = Instance("A",BLOCK), i_b = Instance("B",BLOCK")
```

Variables: Can take on any TYPE thing

b = Variable("b",BLOCK)

ALERT: no two literals nor variables can have the same string name!!

Block World Example:

Pickup_from_Table(b):

Pre: HandEmpty(), Clear(b), On-Table(b)

Add: In-Hand(b)

Delete: HandEmpty(), On-Table(b)

Literals: Each thing/object in our model

Variables: Can take on any TYPE thing

Propositions: Predicate Relationships

Proposition(<u>"relation</u>", v_a, <u>i,</u> ...)

integer 1 i 1 = I ("1", IM)

ALERT: variables and instances do not have to start with i_ and v_

Block World Example:

HandEmpty(), Clear(b), On-Table(b), On-Block(b1,b2)

Proposition("handempty"), Proposition("clear",v_block),
Proposition("on-table",v_block), Proposition("on-block",v_block, i_a)

Initial State and Goal State

Create lists of Propositions as the initial state and goal state

```
initial = Proposition("handempty"), Proposition("on-table", i_c), Proposition("on-table", i_b), Proposition("on-block", i_a, i_b), Proposition("clear", i_a), Proposition("clear", i_c)]
```

```
Goal = [Proposition("on-table",i_b), Proposition("on-table",i_c), Proposition("on-block",i_a, i_c), Proposition("clear",i_a), Proposition("clear","c")]
```

Operators: the actions we take change state

pickup_table = Operator("pick_table", #name

Lists are conjunctions!

All propositions with a variable must take on the same instance!

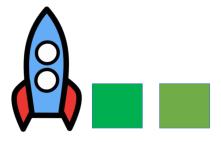
Variables that don't match name don't have to be the same but can be unless otherwise specified!

```
[Proposition("handempty",), #preconditions
Proposition("clear", v_block),
Proposition("on-table", v_block),
[Proposition("in-hand", v_block)], #add effects
[Proposition("handempty"), #delete effects
Proposition("on-table", v_block)
```

We provide the GraphPlan implementation

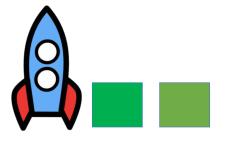
You will create the representation, which will be passed into our GraphPlan implementation

Suppose we have a rocket ship that can only be used once. It has to carry two payloads.



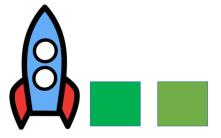
Suppose we have a rocket ship that can only be used once. It has to carry two payloads.

Literals?



Suppose we have a rocket ship that can only be used once. It has to carry two payloads.

Literals: Rocket, G, O, LocA, LocB



Suppose we have a rocket ship that can only be used once. It has to carry two payloads.

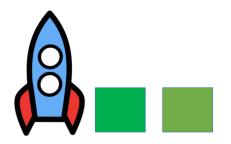
Literals: Rocket, G, O, LocA, LocB

Start state:

At(Rocket, LocA), Has-Fuel(), Unloaded(G,LocA), Unloaded(O,LocA)

Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)



I create literals and variables as I go through the problem. In order to create the start state and the goal state, I need the literals defined.

Literals: Rocket, G, O, LocA, LocB

Start state:

At(Rocket, LocA), Has-Fuel(),

Unloaded(G,LocA), Unloaded(O,LocA)

Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)

As I create my operators, I will add

variables.

Move: Load: Unload:

```
Literals: Rocket, G, O, LocA, LocB

Start state:

At(Rocket, LocA), Has-Fuel(),
Unloaded(G,LocA), Unloaded(O,LocA)

Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)

Variables: L

Move:
P: At(Rocket,L)
A:
D:
```

D:

```
Literals: Rocket, G, O, LocA, LocB

Start state:

At(Rocket, LocA), Has-Fuel(),
Unloaded(G,LocA), Unloaded(O,LocA)

Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)

Variables: L, Dest

Move:
P: At(Rocket,L), Has-Fuel(), L!=Dest
A: At(Rocket,Dest)
```

```
Literals: Rocket, G, O, LocA, LocB

Start state:

At(Rocket, LocA), Has-Fuel(),

Unloaded(G,LocA), Unloaded(O,LocA)

Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)

Variables: L, Dest, Pkg

Load:

P: At(Rocket,L), Unloaded(Pkg,L)

A:

D:
```

```
Literals: Rocket, G, O, LocA, LocB
Start state:

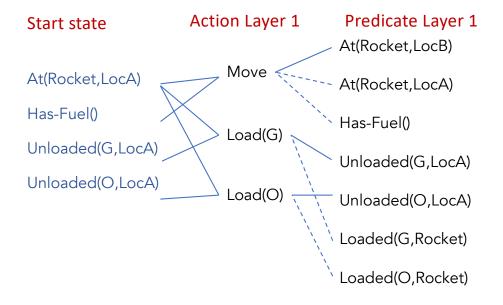
At(Rocket, LocA), Has-Fuel(),
Unloaded(G,LocA), Unloaded(O,LocA)

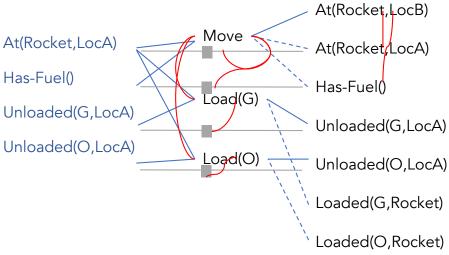
Goal state:

At(Rocket, LocB), Unloaded(G,LocB), Unloaded(O,LocB)

Variables: L, Dest, Pkg

Unload:
P: At(Rocket,Dest), Loaded(Pkg,Rocket)
A: Unloaded(Pkg,Dest)
D: Loaded(Pkg,Rocket)
```





Mutex Actions

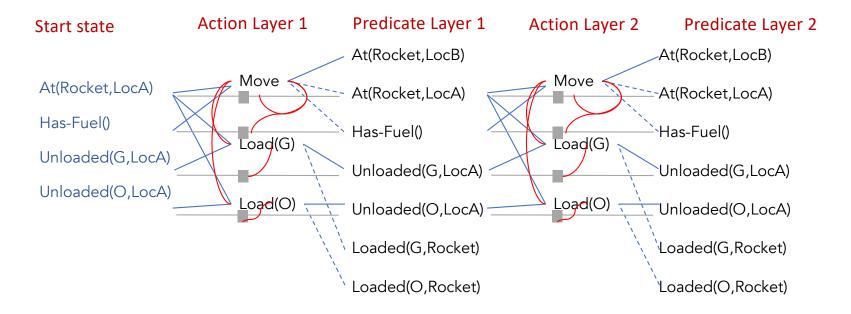
Interference:

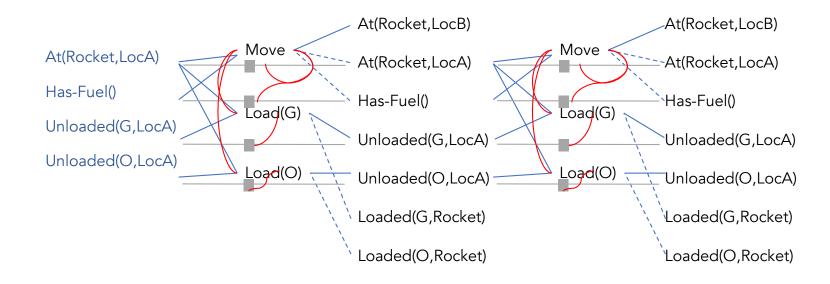
Move deletes At which is a precondition of Load

Inconsistent:

Move deletes At but noop adds it Move deletes Has-Fuel but noop adds it **Mutex Propositions:**

- At(Rocket,LocB) and At(Rocket,LocA) because Move and noop are mutex actions
- What else?





At time 1: Move can be performed OR both Load actions

At time 2: Possible plans include:

Load(G), Load(O), Move(LocB) ← reachable goal in two steps but feasible in three Load(G), Move(LocB)
Load(O), Move(LocB)