

Administrivia

- Start Homework earlier

Lists

Lists: Type of problems

- **Cat 1:** given a list L, process L and compute some value out of its elements. Example: `alternatingSum`, `hasDuplicates`
- **Cat 2:** Given some input, return a **NEW** list with some properties. Example: return the *first n Zish* numbers, `findDuplicates`

Example: alternating sum

- Given a list of positive integers, calculate the alternating sum
- `alternatingSum([1, 2, 3, 4]) == -2`
 - because $1 - 2 + 3 - 4 = -2$
- `alternatingSum([15, 5, 10, 1]) == -2`
 - because $15 - 5 + 10 - 1 = 19$

Example: find duplicates

- Write the function `findDuplicates(L)` that takes a list `L` of arbitrary values, and returns the list of duplicate values.
- The order is not important, but there shouldn't be duplicate values in the result
- `assert(findDuplicates([1,1,1,2]) == [1])`
- `assert(findDuplicates([1,4,2,1,3,4,5,2]) == [1,4,2])`

What's really happening here?

```
L = [15112, 42, 15122, 2023]  
L.append(2024)
```

```
L = [15112, 42, 15122, 2023]
```

```
def ....(theList):  
    ...
```

```
theList == [15112, 42, 15122, 2023]
```

Aliasing

- Using lists as function arguments
- [Python tutor: example](#)

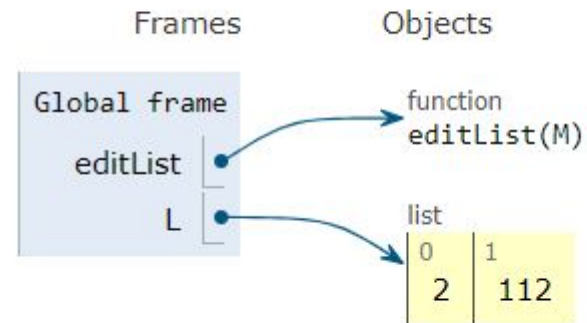
Python 3.6
[known limitations](#)

```
1 def editList(M):
2     M[0] = 2
3
4
5 L = [15, 112]
6
7 editList(L)
8
9 → print(L)
```

[Edit this code](#)

Print output (drag lower right corner to resize)

[2, 112]



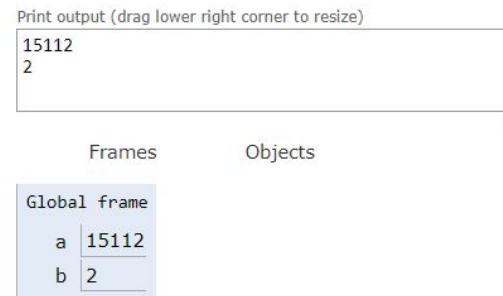
Aliasing

- Python tutor: example 1

Python 3.6
[known limitations](#)

```
1 a = 15112
2 b = 2
3
4
5 print(a)
→ 6 print(b)
```

[Edit this code](#)

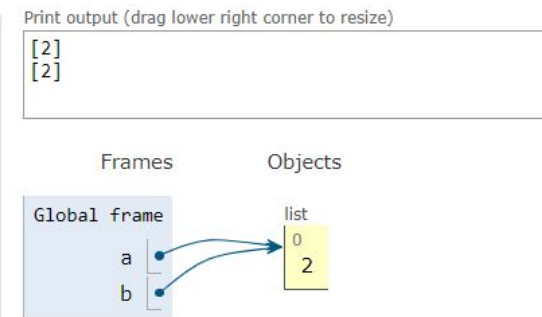


- Python tutor: example 2

Python 3.6
[known limitations](#)

```
1 a = [15112]
2 b = a
3
4 b[0] = 2
5
6 print(a)
→ 7 print(b)
```

[Edit this code](#)



Lists: Taxonomy of problems

- **Cat 1:** given a list L, process L and compute some value out of its elements. Example: `alternatingSum`, `hasDuplicates`
- **Cat 2:** Given some input, return a **NEW** list with some properties. Example: return the *first n 7ish* numbers, `findDuplicates`
- **Cat 3:** Given a list L, write a ***non-destructive function*** to solve some task using L **without modifying** the original L.
Example: `nondestructiveRemoveNonInts`
- **Cat 4:** Given a list L, write a ***destructive function*** to solve some task that **mutates** L.
Example: `destructiveRemoveNonInts`



Example: nondestructiveRemoveNonInts

- Write the function `nondestructiveRemoveNonInts(L)` that returns a new list that is equivalent to `L` without the non-integer values. It should not modify the original `L`.

```
L = [112, 'hi', '3', 1, 5]
```

```
nondestructiveRemoveNonInts(L) returns [112, 1, 5]
```

```
assert(L == [112, 'hi', '3', 1, 5])
```

Example: destructiveRemoveNonInts

- Write the function `destructiveRemoveNonInts(L)` that removes the non-integer values from `L`.

```
L = [112, 'hi', '3', 1, 5]
```

```
destructiveRemoveNonInts(L) # assumed to return None
```

```
assert(L == [112, 1, 5])
```

Destructive vs Non-Destructive Operations

How do we add a value to a list **destructively**? Use `append`, `insert`, or `+=`.

```
lst = [1, 2, 3]
lst.append(5)
lst.insert(1, "foo")
lst += [10, 20] # Annoyingly different from lst = lst + [10, 20]
```

How do we add a value to a list **non-destructively**? Use variable assignment with list concatenation.

```
lst = [1, 2, 3]
lst = lst + [5, 10, 20]
```

Destructive vs Non-Destructive Operations

How do we remove a value from a list **destructively**? Use remove or pop.

```
lst = [1, 2, 3]
lst.remove(2)    # remove the value 2
lst.pop(1)       # remove the value at index 1
```

How do we remove a value from a list **non-destructively**? Use variable assignment with list slicing.

```
lst = [1, 2, 3]
lst = lst[:1]
```

Exercise

- At the end of this set of operations, which pairs of lists will still be aliased?

```
1 a = [ 1, 2, "x", "y" ]
2 b = a
3 c = [ 1, 2, "x", "y" ]
4 d = c
5 a.pop(2)
6 b = b + [ "wow" ]
7 c[0] = 42
8 d.insert(3, "yey")
```

- a** and **b**
- c** and **d**
- All** lists are aliases of the **same** list
- None** of them are aliased

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return the *first n 7ish* numbers, `findDuplicates`
- **Cat 3:** Given a list L, write a ***non-destructive function*** to solve some task using L **without modifying** the original L.
 - Example: `nondestructiveRemoveNonInts`
- **Cat 4:** Given a list L, write a ***destructive function*** to solve some task that **mutates** L.
 - Example: `destructiveRemoveNonInts`
- **Cat 5:** Solve a task involving **2d lists**.
 - Example: `isMagicSquare`



isMagicSquare

- Write the function `isMagicSquare(L)` that takes an arbitrary list `L` and returns `True` if it is a magic square and `False` otherwise, where a magic square has these properties:
 - The list is 2d, non-empty, **square**, and contains **only integers**, where no integer occurs more than once in the square.
 - Each row, each column, and each of the 2 diagonals each sum to the same total. Note that we do not require that the integers are strictly in the range from 1 to n for some n . We only require that the integers are unique and that the sums are identical.

| | | | |
|-----|-----|-----|-----|
| 2 | 7 | 6 | →15 |
| 9 | 5 | 1 | →15 |
| 4 | 3 | 8 | →15 |
| ↙15 | ↓15 | ↓15 | ↓15 |



isMagicSquare(L)

- Check that L is a list
- Check that L is a non-empty *square* 2d list
 - Check that all elements are lists
 - Check that all elements have `len(L)` elements
- Check that all elements in every row of L are integers
- Check that all elements in every row are unique
- Check that the sum of rows, the sum of columns, and the sum of diagonals are equal

| | | | | |
|-----|-----|-----|-----|-----|
| 2 | 7 | 6 | →15 | |
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| ↙15 | ↓15 | ↓15 | ↓15 | ↘15 |

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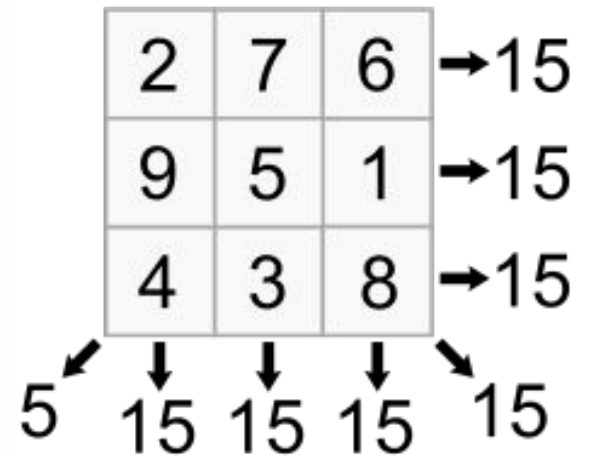
| | | | | |
|-----|-----|-----|-----|-----|
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| 4 | 3 | 8 | →15 | |
| ↙15 | ↓15 | ↓15 | ↓15 | ↘15 |

isValidSquare(L)

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 - Check that all elements are lists
 - Check that all elements have len(L) elements
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- Check that all elements in every row are unique

```
1 def isValidSquare(L):
2     if not isinstance(L, list):
3         return False
4     if len(L) == 0:
5         return False
6     for row in L:
7         if not isinstance(row, list):
8             return False
9     nrows = len(L)
10    for row in L:
11        if len(row) != nrows:
12            return False
13    for row in L:
14        for val in row:
15            if not isinstance(val, int):
16                return False
17    valuesSeen = []
18    for row in L:
19        for val in row:
20            if val in valuesSeen:
21                return False
22            valuesSeen.append(val)
23    return True
```



isMagicSquare(L)

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| | | | | |
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| 4 | 3 | 8 | →15 | |
| ↙15 | ↓15 | ↓15 | ↓15 | ↘15 |