

Runtime and Big O

1. Put the following runtimes in increasing order - $O(n)$, $O(\log(n))$, $O(n!)$, $O(n^2)$, $O(n\log(n))$, $O(2^n)$

2. What are the big-O complexities of the following functions?

a. **def howManyNumbers(s):**

```
numbers = "1234567890"
count = 0
for char in s:
    for num in numbers:
        if (char == num):
            count = count + 1
return count
```

b. **def containsVowel(s):**

```
for c in s:
    if c in ["a", "e", "i", "o", "u"]:
        return true
return false
```

c. **def f(L):** # L is a list with length n

```
lenList = len(L)
count = 0
for i in range(lenList):
    for j in range(lenList):
        count += L[i]
return count
```

d. **def g(s):** #s is a string of length n

```
result = 0
for char in string.ascii_lowercase:
    if char in s:
        s = s[1:]
        result += 1
return result
```

e. **def h(L):** #L is a list with length n

```
i = 1
```

```
listLength = len(L)
result = []
while i < listLength:
    result += L[i]
    i *= 3
return i
```

3. Given the following function containsVowels that checks if a string contains any vowels, what are the best and worst case runtimes? What are the runtimes of each?

```
def containsVowel(s):
    for c in s:
        if c in ["a", "e", "i", "o", "u"]:
            return true
    return false
```