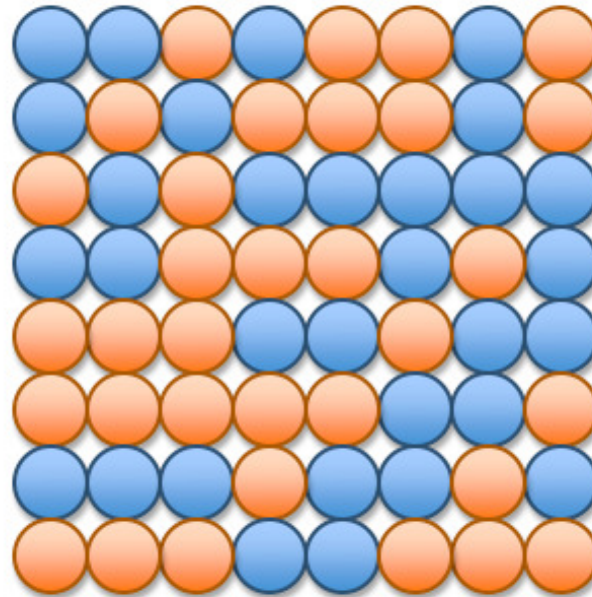




UNIT 4B

Iteration: Sorting

Announcements

- lab1, lab2, pa1,pa2, ps1 grades should be available now
 - Contact your TA/instructor if they are missing
- Ps3 is due Friday Feb 8th in class
- New FAQ section on the web page
 - Please visit before sending email
 - Will continue to add things
- Written exam – Wed Feb 20th
 - There will be help sessions (stay tuned)

Sorting

Comparison sorting

- Keys can be compared
 - keys are comparable as a whole
 - ints, strings, characters
 - Ascii table

"aaa" < "baB"
 ↑ ↑
 97 98

5, 2, 1, 12, 23

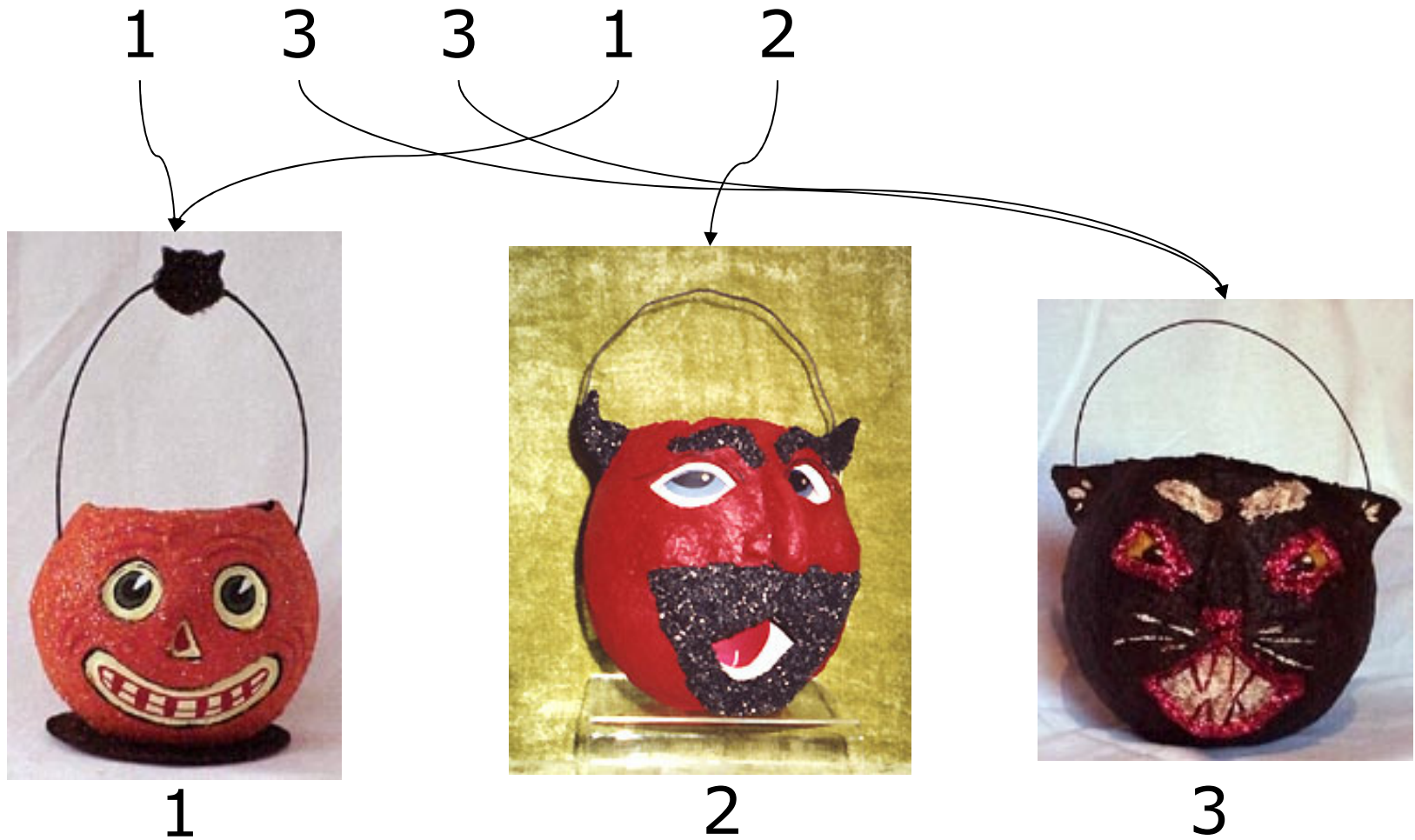
"a" < "b" < "c"

"B" < "a"

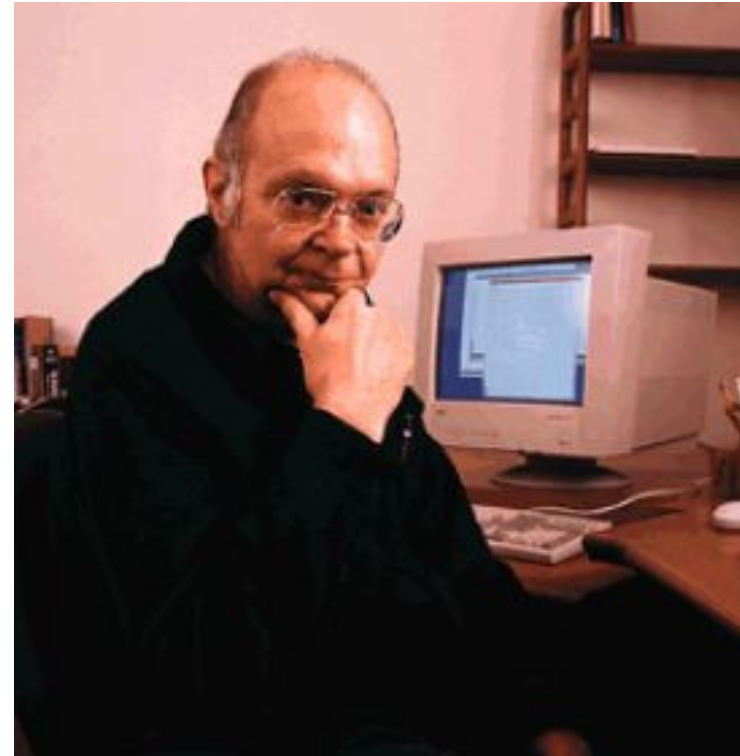
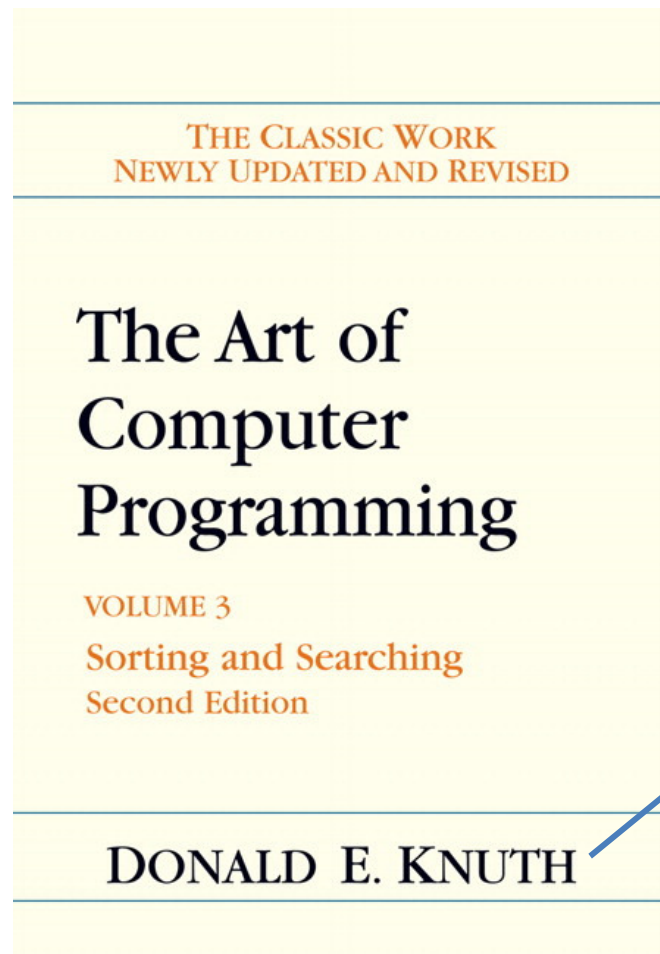
Dec	Hx	Oct	Char	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr
0	0	000	NUL (null)	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	SOH (start of heading)	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	STX (start of text)	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	ETX (end of text)	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	EOT (end of transmission)	36	24	044	$	\$	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ (enquiry)	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	ACK (acknowledge)	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	BEL (bell)	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	BS (backspace)	40	28	050	(	(	72	48	110	H	H	104	68	150	h	h
9	9	011	TAB (horizontal tab)	41	29	051	)	)	73	49	111	I	I	105	69	151	i	i
10	A	012	LF (NL line feed, new line)	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	VT (vertical tab)	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	FF (NP form feed, new page)	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	CR (carriage return)	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	SO (shift out)	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	SI (shift in)	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	DLE (data link escape)	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	DC1 (device control 1)	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2 (device control 2)	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	DC3 (device control 3)	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	DC4 (device control 4)	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	NAK (negative acknowledge)	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	SYN (synchronous idle)	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	ETB (end of trans. block)	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	CAN (cancel)	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	EM (end of medium)	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	SUB (substitute)	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	ESC (escape)	59	3B	073	;	:	91	5B	133	[	[	123	7B	173	{	{
28	1C	034	FS (file separator)	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	
29	1D	035	GS (group separator)	61	3D	075	=	=	93	5D	135	]	]	125	7D	175	}	}
30	1E	036	RS (record separator)	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	US (unit separator)	63	3F	077	?	?	95	5F	137	_	_	127	7F	177		DEL

Source: www.LookupTables.com

Category Sorting



The Art of Computer Programming Volume 3: Sorting and Searching

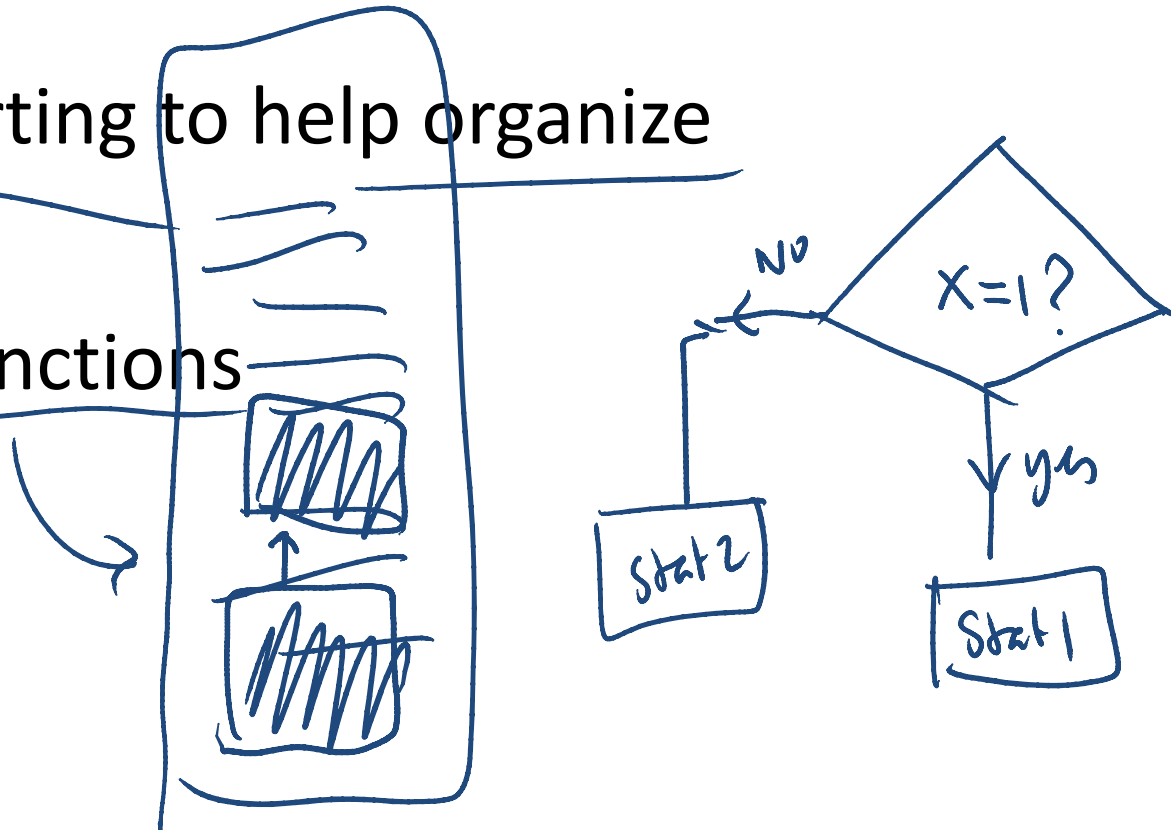


Insertion Sort

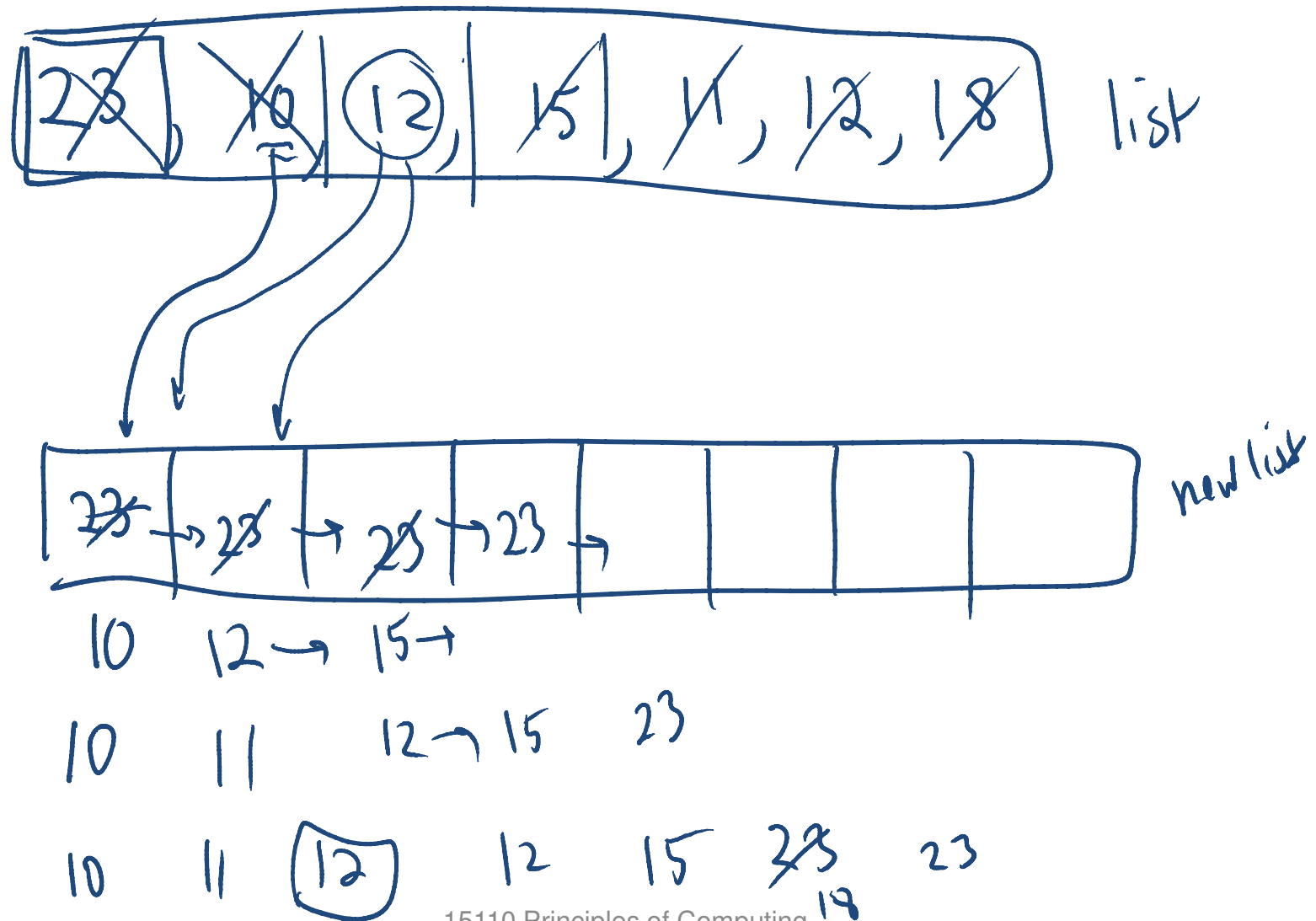


Good Practices of writing code

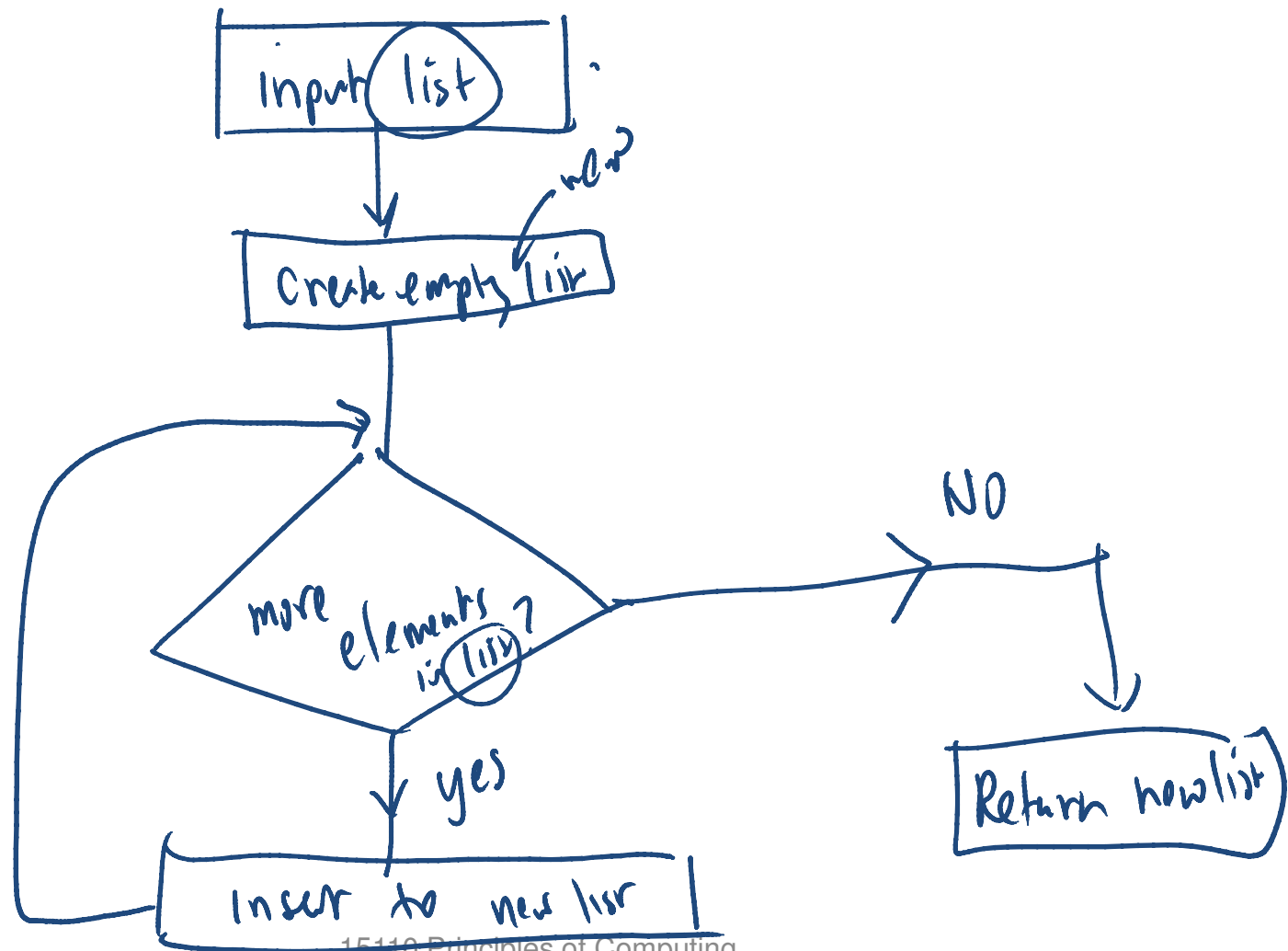
- From high level to detail
- Flow charting to help organize
- Helper functions
- testing



Insertion sort demo



To a flow chart



Flow chart to pseudo code

```
def isort(list)  
  -- create an empty newlist  
  - for value in list  
    - insert value in-order to newlist  
  - end  
end
```

From pseudo code to partial code

```
def isort (list)
    result = [ ]
    for val in list do
        # insert val in its proper place in result
    end
    return result
end
```

create an empty list

sorted

Need a way to insert something into an array

Array Insert method

- list.insert(position, value)

```
>> a = [10, 20, 30]
```

```
=> [10, 20, 30]
```

```
>> a.insert(0, "foo")
```

```
=> ["foo", 10, 20, 30]
```

```
>> a.insert(2, "bar")
```

```
=> ["foo", 10, "bar", 20, 30]
```

```
>> a.insert(5, "baz")
```

```
=> ["foo", 10, "bar", 20, 30, "baz"]
```

Insertion Sort, Refined

```
def isort (list)
```

```
  result = [ ]
```

```
  for val in list do
```

```
    place = /* compute this */ ✓  
    result.insert(place, val)
```

```
  end
```

```
  return result
```

```
end
```

Computing the place to insert

index of first element greater than item

```
def gindex (list, item)
```

```
    index = 0
```

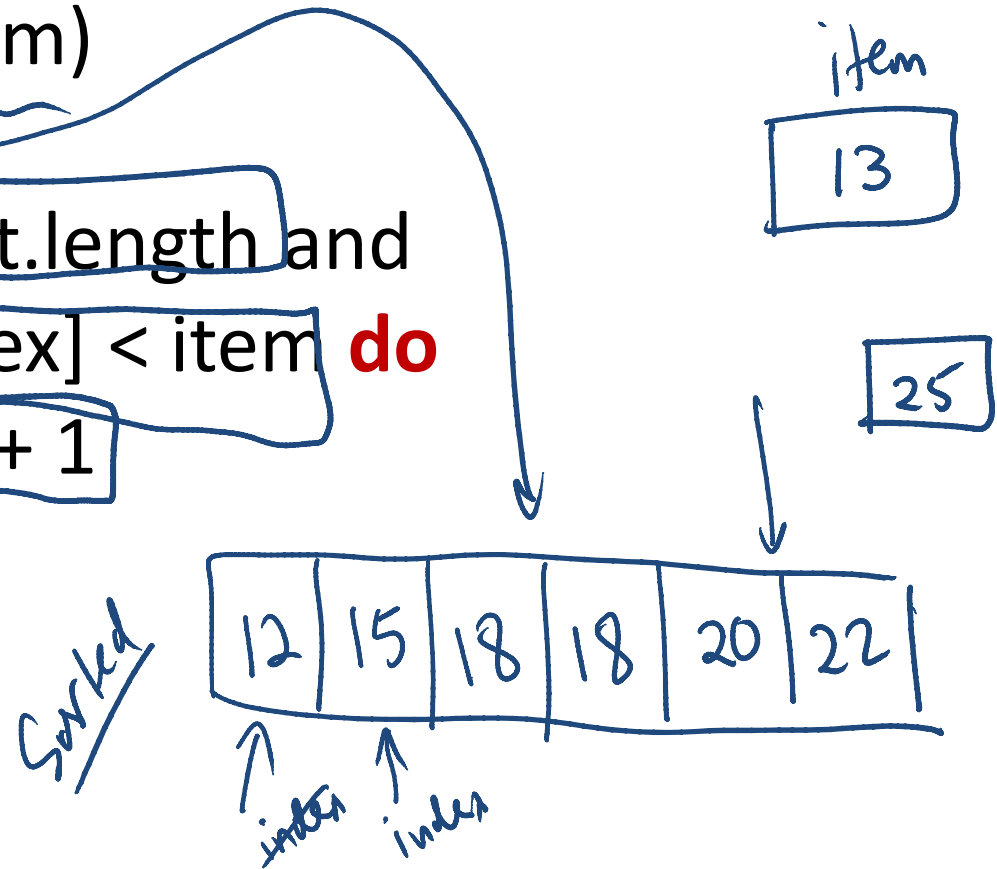
```
    while index < list.length and  
          list[index] < item do
```

```
        index = index + 1
```

```
    end
```

```
    return index
```

```
end
```



Testing gindex

```
>> a = [10, 20, 30, 40, 50]
=> [10, 20, 30, 40, 50]
>> gindex(a, 3)
=> 0
>> gindex(a, 14)
=> 1
>> gindex(a, 37)
=> 3
>> gindex(a, 99)
=> 5
```

Putting it all together

```
def isort (list)
  result = [ ]
  for val in list do
    place = gindex(result, val)
    result.insert(place, val)
  end
  return result
end
```

Tracing the code

```
def isort (list)
    result = [ ]
    for val in list do
        place = gindex(result, val)
        result.insert(place, val)
    end
    return result
end
```

<u>list</u>	<u>result</u>	<u>val</u>	<u>place</u>
[2, <u>1</u> , 3]	[]	2	0
	[2]	1	0
	[1, 2]	3	2
	[1, 2, 3]		

Testing the code

```
def isort (list)
  result = [ ]
  p result    # for debugging
  for val in list do
    result.insert(gindex(result,val), val)
    p result    # for debugging
  end
  return result
end
```

Improving performance

Can We Do Better?

- isort doesn't change its input list.
- Instead it makes a new list, called result.
- This takes twice as much memory.
- Can we write a **destructive version** of the algorithm that doesn't use extra memory?
- That is the version shown in the book (see chapter 4).

Destructive Insertion Sort

Given an array a of length n , $n > 0$.

1. Set $i = 1$.
2. While i is not equal to n , do the following:
 - (i). Insert $a[i]$ into its correct position in $a[0..i]$, shifting the other elements as necessary.
 - (ii). Add 1 to i .
3. Return the array a which will now be sorted.

Insertion sort

Sorted subarray



105	47	13	99	30	222
47	105	13	99	30	222
13	47	105	99	30	222
13	47	99	105	30	222
13	30	47	99	105	222
105	47	13	99	30	222

Insertion Sort in Ruby

```
def isort!(list)
  i = 1
  while i != list.length do
    move_left(list, i)
    i = i + 1
  end
  return list
end
```

← insert a[i] into a[0..i]
in its correct sorted
position

Loop invariants

```
def isort!(list)
  i = 1
  while i != list.length do
    -- what is true about list here?
      move_left(list, i)
      i = i + 1
    end
  end
  return list
end
```

← insert $a[i]$ into $a[0..i]$
in its correct sorted
position

Moving left demo

The `move_left` algorithm

Given an array `a` of length `n`, $n > 0$ and a value at index `i` to be “moved left” in the array.

1. Remove `a[i]` from the array and store in `x`.
2. Set `j = i-1`.
3. While `j >= 0` and `a[j] > x`, do the following:
 - a. Subtract 1 from `j`.
4. Reinsert `x` into position `a[j+1]`.

move_left in Ruby

```
def move_left(a, i)
  x = a.slice!(i)
  j = i-1
  while j >= 0 and a[j] > x do
    j = j - 1
  end
  a.insert(j+1, x)
end
```

← remove the item at position i in array a and store it in x

← logical operator AND: both conditions must be true for the loop to continue

← insert x at position j+1 of array a, shifting all elements from j+1 and beyond over one position

Why is the algorithm correct?

- Reason with loop invariants
 - The loop invariant
 - $A[0..i-1]$ is sorted at i -th iteration
 - The loop invariant is true at the beginning of each iteration
 - Loop invariant is true after the last iteration. After the last iteration, when we go to step 3:
 $a[0..i-1]$ is sorted AND i is equal to n

Review/Bonus slides

iterators

Iterators

- Iterators are another way to operate on the elements of an array.
- The `each` iterator is similar to a for loop:

```
fruits.each { |f| puts "Yummy " + f + "pie!" }
```



This { } thing is called a “block” in Ruby

- Ruby provides lots of other iterators that do cool and useful things.

Compare

Using a for loop:

```
for f in fruits do  
  puts "Yummy " + f  
end
```

Using an iterator:

```
fruits.each { |f|  
  puts "Yummy " + f  
}
```

“Destructive” Iterators

- Some iterators *modify* the array. Beware!

```
items = (1..10).to_a  
=> [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]
```

```
items.delete_if { |i| i.odd? }  
=> [2, 4, 6, 8, 10]
```

```
items => [2, 4, 6, 8, 10]
```

Flow Charts

Flow Charts

```
def nestedcode(n)
  if n<=1 then
    return nil
  end
  for i in 2..n do
    if i%2==0 then
      puts i
    end
  end
end
```

Tracing code

Tracing Code

```
def printtable(n)
  i=n
  while (i>=1) do
    for j in 1..i do
      print j.to_int() + " "
    end
    puts
    i = i-1
  end
end
```

Array Manipulation

Useful Array methods

- `A.length`
- `A.include?(item)`
- `A.index(item)`
- `Array.at(index)`
- `Array.insert(index, item)`
- `Array.delete(index)`

List equivalence

- **Problem:** Given two lists L1 and L2, return true if two lists contains the same elements (in any order)

Best Coding Practices

Grading on Code Formatting

- From now on, you will be graded on the appearance of your code.
- Proper indentation, no gratuitous blank lines. (But in long functions, blank lines can be a good way to group code into sections.)
- Why are we doing this?
 - Because we're mean.
 - Because you cannot find the bugs in your code if you cannot read it properly.

Indenting a FOR Loop

```
for var in values do  
    loop body stuff  
    more loop body stuff  
    even mode loop body stuff  
end
```

Indenting a WHILE Loop

while *test* **do**

loop body stuff

more loop body stuff

even more loop body stuff

end

Indenting an IF

```
if test then
    some then stuff
    more then stuff
else
    some else stuff
    more else stuff
end
```

Nesting

```
x = [3, 13, 5, 25, 4, 64]
```

```
for v in x do
```

```
  if v < 10 then
```

```
    print " ", v
```

```
  else
```

```
    print v
```

```
  end
```

```
    print "\n"
```

```
end
```