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15110 Principles of Computing,
Carnegie Mellon University

## Announcement

- Lab Exam 2 Today
- Final Exam Part 1 : Friday 9am
- Final Exam Part 2 : Friday 4:30pm


## Overview

- Security issues
- Encryption and cryptanalysis
- Encryption in the digital age
- Symmetric encryption
- Asymmetric encryption
- Applications of encryption
- Encryption is not security!


## Security issues

## Data Privacy

- Suppose you send an email to a friend.
- Who has access to that email?
- What if you encrypt the message so it is private?
- Can someone who intercepts the email decrypt it?
- On the Internet and any computer network, any transmitted data can be intercepted and copied.


## Networking is a security issue

- Why?
- If you want a really secure machine, lock it in an electromagnetically shielded room and don't connect it to any networks or other sources of data beyond your control.
- Not much fun, is it?


## The Problem

- The Internet is public
- Messages sent pass through many machines and media
- Anyone intercepting a message might
- read it and/or
- replace it with a different message
- The Internet is anonymous
- IP addresses don't establish identity
- Anyone may send messages under a false identity


## A Shady Example

- I want to make a purchase online and click a link that takes me to http://www.sketchystore.com/checkout.jsp
- What I see in my browser:

Enter your credit card number: 2837283726495601
Enter your expiration date: 0109

## Submit

## A Shady Example (cont' d)

- When I press SUBMIT, my browser sends this:

POST /purchase.jsp HTTP/1.1
Host: www.sketchystore.com
User-Agent: Mozilla/4.0
Content-Length: 48
Content-Type: application/x-www-form-urlencoded userid=rbd\&creditcard=2837283726495601\&exp=01/09

## A Shady Example (cont' d)

- If this information is sent unencrypted, who has access to my credit card number?
- Other people who can connect to my wireless ethernet
- Other people physically connected to my wired ethernet ○ ...
- Packets are passed from router to router.
- All those routers have access to my data.


## A caveat

## cryptography is not security



WHAT WOULD ACTUALLY HAPPEN:
HIS LAPTOP'S ENCRYPTED. DRUG HIM AND HIT HIM WITH THIS $\$ 5$ WRENCH UNTLL HE TEUS US THE PASSWORD.


## Encryption and cryptanalysis

basic concepts

## Encryption

- We encrypt (encode) our data so others can't understand it (easily) except for the person who is supposed to receive it.
- We call the data to encode plaintext and the encoded data the ciphertext.
- Encoding and decoding are inverse functions of each other.


## Encryption/Decryption



## secret key



## ATTACKATDAWN

plaintext


## Cryptanalysis



# Encryption techniques 

substitution and transposition

## Two basic ways of altering text to encrypt/decrypt

- Substitute one letter for another using some kind of rule


## Substitution cipher

- Scramble the order of the letters using some kind of rule


## Transposition cipher

## Substitution Ciphers

- Simple encryption scheme using a substitution cipher:

Shift every letter forward by 1 :

$$
\begin{aligned}
& \mathrm{A} \rightarrow \mathrm{~B}, \mathrm{~B} \rightarrow \mathrm{C}, \ldots, \quad \mathrm{Z} \rightarrow \mathrm{~A} \\
& \text { MESSAGE } \rightarrow \text { NFTTBHF }
\end{aligned}
$$

- Can you decrypt TFDSFU?

ABCDEFGHIJKLMNOPQRSTUVWXYZ

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Shift every letter forward by 1 :

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\end{aligned}
$$

- Can you decrypt TFDSFU? SECRET ABCDEFGHIJKLMNOPQRSTUVWXYZ


## Caesar Cipher

- Shift forward $n$ letters; $\boldsymbol{n}$ is the secret key.

For example, shift forward 3 letters
(This is a Caesar cipher using a key of 3):

$$
\begin{aligned}
& \mathrm{A} \rightarrow \mathrm{D}, \quad \mathrm{~B} \rightarrow \mathrm{E}, \ldots, \mathrm{Z} \rightarrow \mathrm{C} \\
& \text { MESSAGE } \rightarrow \text { PHVVDJH } \\
& \text { ABCDEFGHIJKLMNOPQRSTUVWXYZ }
\end{aligned}
$$

- How can we crack this encrypted message if we don't know the key?

DEEDUSEKBTFEIIYRBOTUSETUJXYI

## Caesar Cipher (cont'd)

DEEDUSEKBTFEIIYRBOTUSETUJXYI
EFFEVTFLCUGFJJZSCPUVTFUVKYZJ FGGFWUGMDVHGKKATDQVWUGVWLZAK GHHGXVHNEWIHLLBUERWXVHWXMABL HIIHYWIOFXJIMMCVFSXYWIXYNBCM IJJIZXJPGYKJNNDWGTYZXJYZOCDN JKKJAYKQHZLKOOEXHUZAYKZAPDEO KLLKBZLRIAMLPPFYIVABZLABQEFP LMMLCAMSJBNMQQGZJWBCAMBCRFGQ MNNMDBNTKCONRRHAKXCDBNCDSGHR NOONECOULDPOSSIBLYDECODETHIS OPPOFDPVMEQPTTJCMZEFDPEFUIJT PQQPGEQWNFRQUUKDNAFGEQFGVJKU

QRRQHFRXOGSRVVLEOBGHFRGHWKLV RSSRIGSYPHTSWWMFPCHIGSHIXLMW STTSJHTZQIUTXXNGQDIJHTIJYMNX TUUTKIUARJVUYYOHREJKIUJKZNOY UVVULJVBSKWVZZPISFKLJVKLAOPZ VWWVMKWCTLXWAAQJTGLMKWLMBPQA WXXWNLXDUMYXBBRKUHMNLXMNCQRB XYYXOMYEVNZYCCSLVINOMYNODRSC YZZYPNZFWOAZDDTMWJOPNZOPESTD ZAAZQOAGXPBAEEUNXKPQOAPQFTUE ABBARPBHYQCBFFVOYLQRPBQRGUVF BCCBSQCIZRDCGGWPZMRSQCRSHVWG CDDCTRDJASEDHHXQANSTRDSTIWXH

- How long would it take a computer to try all 25 shifts?


## Vigenère Cipher

- Shift different amount for each letter. Use a key word; each letter in the key determines how many shifts we do for the corresponding letter in the message.
- Example: key word "cmu": shift by $2,12,20$
- Message "pittsburgh"
cmucmucmuc
encrypted: runvevwdaj
- Try it yourself at
http://www.simonsingh.net/The Black_Chamber/v square.html


## ABCDEFGHIJKLMNOPQRSTUVWXYZ

A ABCDEFGHIJKLMNOPQRSTUVWXYZ no shift B BCDEFGHIJKLMNOPQRSTUVWXYZA shift by 1
C CDEFGHIJKLMNOPQRSTUVWXYZAB shift by 2
D DEFGHIJKLMNOPQRSTUVWXYZABC shift by 3
E EFGHIJKLMNOPQRSTUVWXYZABCD etc.
F
FGHIJKLMNOPQRSTUVWXYZABCDE

- Message:
- Pick a secret key
- Encrypted:


## ATTACKATDAWN <br> DECAFDECAFDE

 D1 st letter in the message is shifted by $3,2^{\text {nd }}$ letter is shifted by $4, \ldots$

## ABCDEFGHIJKLMNOPQRSTUVWXYZ

A ABCDEFGHIJKLMNOPQRSTUVWXYZ
B BCDEFGHIJKLMNOPQRSTUVWXYZA
C CDEFGHIJKLMNOPQRSTUVWXYZAB
D DEFGHIJKLMNOPQRSTUVWXYZABC
E EFGHIJKLMNOPQRSTUVWXYZABCD
F FGHIJKLMNOPQRSTUVWXYZABCDE

- Message:
- Pick a secret key
- Encrypted:


## ATTACKATDAWN DECAFDECAFDE

 DX1 st letter in the message is shifted by $3,2^{\text {nd }}$ letter is shifted by $4, \ldots$

## ABCDEFGHIJKLMNOPQRSTUVWXYZ

A ABCDEFGHIJKLMNOPQRSTUVWXYZ
B BCDEFGHIJKLMNOPQRSTUVWXYZA
C CDEFGHIJKLMNOPQRSTUVWXYZAB
D DEFGHIJKLMNOPQRSTUVWXYZABC EFGHIJKLMNOPQRSTUVWXYZABCD FGHIJKLMNOPQRSTUVWXYZABCDE

- Message:
- Pick a secret key
- Encrypted:

ATTACKATDAWN
DECAFDECAFDE
DXV

1 st letter in the message is shifted by $3,2^{\text {nd }}$ letter is shifted by $4, \ldots$

## ABCDEFGHIJKLMNOPQRSTUVWXYZ

A ABCDEFGHIJKLMNOPQRSTUVWXYZ
B BCDEFGHIJKLMNOPQRSTUVWXYZA
C CDEFGHIJKLMNOPQRSTUVWXYZAB
D DEFGHIJKLMNOPQRSTUVWXYZABC
E EFGHIJKLMNOPQRSTUVWXYZABCD
F
FGHIJKLMNOPQRSTUVWXYZABCDE

- Message:
- Pick a secret key
- Encrypted:

ATTACKATDAWN DECAFDECAFDE

DXVAHNEVDFZR

1 st letter in the message is shifted by $3,2^{\text {nd }}$ letter is shifted by $4, \ldots$

## Vernam Cipher

- Vigenère cipher was broken by Charles Babbage in the mid 1800s by exploiting the repeated key
- The length of the key determines the cycle in which the cipher is repeated.
- Vernam cipher:

Make the key the same length as the message; Babbage's analysis doesn't work.

## One-time Pads

- Vernam cipher is commonly referred to as a one-time pad.


Alice and Bob have identical "pads" (shared keys)

- If random keys are used one-time pads are unbreakabke in theory.


## Transposition ciphers



STSF...EROL...NOUA...DOTN...MPHK...OSEA...RTRN...EOND...

# Encryption in computing 

fast computation makes encryption usable by all of us

## Encryption in computing

- One-time pads impractical on the net (why?)
- Basic assumption:
- the encryption/decryption algorithm is known;
- only the key is secret
- Very complicated encryptions can be computed fast:
- typically, elaborate combinations of substitution and transposition


## リ P D

- Security protocol for the Web, the peoples' encryption
- Purpose:
- confidentiality (prevent eavesdropping)
- message integrity and authentication (prevent "man in the middle" attacks that could alter the messages being sent)
- Techniques:
- asymmetric encryption ("public key" encryption) to exchange secret key
- certificate authority to obtain public keys
- symmetric encryption to exchange actual messages


## Symmetric vs. Asymmetric encryption

- Symmetric (shared-key) encryption: commonly used for long messages
- Often a complicated mix of substitution and transposition encipherment
- Reasonably fast to compute
- Requires a shared secret key usually communicated using (slower) asymmetric encryption
- Asymmetric encryption: different keys are used to encrypt and to decrypt


## Keyspace

- Keyspace is jargon for the number of possible secret keys, for a particular encryption/decryption algorithm
- Number of bits per key determines size of keyspace
- important because we want to make brute force attacks infeasible
- brute force attack: run the (known) decryption algorithm repeatedly with every possible key until a sensible plaintext appears
- Typical key sizes: several hundred bits


## Symmetric (Shared Key) Encryption



## Establishing Shared Keys

- Problem: how can Alice and Bob secretly agree on a key, using a public communication system?
- Solution: asymmetric encryption based on number theory
- Alice has one secret, Bob has a different secret; working together they establish a shared secret
- Examples: Diffie-Hellman key exchange, RSA public key encryption


## One type of asymmetric encryption: RSA

- Common encryption technique for transmitting symmetric keys on the Internet (https, ssl/tls)
- Named after its inventors: Rivest, Shamir and Adleman
- Used in https (you know when you're using it because you see the URL in the address bar begins with https://)


## Asymmetric Public Key Encryption



Enc(plaintext, pubB)

plaintext

Alice uses Bob's public key to encrypt the plaintext to produce the ciphertext
ciphertext
Bob's private key privB

## Bob

Decrypt using privB
plaintext
$=\operatorname{Dec}$ (ciphertext, privB
Bob uses his private key to decrypt the ciphertext to recover the plaintext

## How RSA works

- First, we must be able to represent any message as a single number (it may already be a number as is usual for a symmetric key)
- For example:

$$
\begin{gathered}
\text { A T T A C K A T D A W N } \\
012020010311012004012314
\end{gathered}
$$

## Public and Private Keys

- Every receiver has a public key $(e, n)$ and a private key $(d, n)$.
- The transmitter encrypts a (numerical) message $M$ into ciphertext $C$ using the receiver's public key:

$$
M^{e} \text { modulo } n \rightarrow C \text { (ciphertext) }
$$

- The receiver decodes the encrypted message $C$ to get the original message $M$ using the private key (which no one else knows).

$$
C^{d} \text { modulo } n \rightarrow M \quad \text { (plaintext) }
$$

## RSA Example

- Alice' s Public Key: $(3,33)$

$$
\begin{aligned}
& (e=3, n=33) \\
& (d=7, n=33)
\end{aligned}
$$

- Alice' s Private Key: $(7,33)$
- Usually these are really huge numbers with many hundreds of digits!
- Bob wants to send the message 4
- Bob encrypts the message using $e$ and $n$ : $4^{3}$ modulo $33 \rightarrow 31$ ... Bob sends 31
- Alice receives the encoded message 31
- Alice decrypts the message using d and n : $31^{7}$ modulo $33 \rightarrow 4$


## Generating $n, e$ and $d$

- $p$ and $q$ are (big)
$p=3, q=11$ random primes.
- $n=p \times q$
$n=3 \times 11=33$
- $\varphi=(p-1)(q-1)$
- $e$ is small and
$\varphi=2 \times 10=20$
relatively prime to $\varphi$
- $d$, such that:
$e \times d \bmod \varphi=1$
$3 \times d \bmod 20=1$
$d=7$

Usually the primes are huge numbers--hundreds of digits long.

## Cracking RSA

- Everyone knows ( $e, n$ ). Only Alice knows $d$.
- If we know $e$ and $n$, can we figure out $d$ ?
- If so, we can read secret messages to Alice.
- We can determine $d$ from $e$ and $n$.
- Factor $n$ into $p$ and $q$.

$$
\begin{aligned}
& n=p \times q \\
& \varphi=(p-1)(q-1) \\
& e \times d=1(\bmod \varphi)
\end{aligned}
$$

- We know $e$ (which is public), so we can solve for $d$.
- But only if we can factor $n$


## RSA is safe (for now)

- Suppose someone can factor my 5-digit $n$ in 1 ms ,
- At this rate, to factor a 10-digit number would take 2 minutes.
- ... to factor a 15 -digit number
would take 4 months.
- ... 20-digit number ... 30,000 years.
- ... 25-digit number... 3 billion years.
- We're safe with RSA! (at least, from factoring with digital computers)


## Certificate Authorities

- How do we know we have the right public key for someone?
- Certificate Authorities sign digital certificates indicating authenticity of a sender who they have checked out in the real world.
- Senders provide copies of their certificates along with their message or software.
- But can we trust the certificate authorities? (only some)


# Encryption is not security! 

It's just a set of techniques

## How (in)secure is the Internet?

-The NSA has a budget of \$11B
-Corporations and criminals also spy on us
-What can go wrong?

- Insecure pseudo-random number generators
- Untrustworthy certificate authorities
- Malware
- "Social engineering" attacks like phishing
- Deliberately built-in insecurity in crypto products
- Physical tapping of Internet routers


## Security is an unsolved problem

Your cyber systems continue to function and serve you not due to the expertise of your security staff but solely due to the sufferance of your opponents.

- former NSA Information Assurance Director Brian Snow (quoted by Bruce Schneier, https://www.schneier.com/blog/archives/2013/03/phishing_has_go.html )


## Summary

- Cryptography is cool mathematics and protocol design
- But cryptography is not security, only a set of techniques
- Security is a broader issue involving
- Other technology
- Social and legal factors
"Only amateurs attack machines; professionals target people" Bruce Schneier

