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## RECAP

FLU VIRUS SIMULATION



## Example: Flu Virus Simulation

- Goal: Develop a simple simulation that shows graphically how disease spreads through a population.

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## Modeling the Spread of Flu Virus

- Every person is either healthy, infected, contagious or immune. We assume that "infected" means infected but not contagious.
- Each day, a healthy person comes in contact with 4 random people. If any of those random people is contagious, then the healthy person becomes infected.
- It takes one day for the infected person to become contagious.
- After a person has been contagious for 4 days, then the person is non-contagious and cannot spread the virus nor can the person get the virus again due to immunity.

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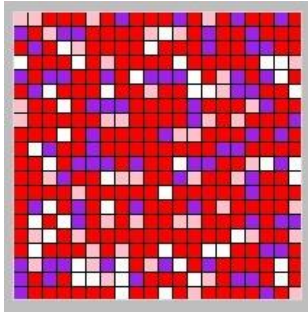
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### Displaying the Population

Color of each cell indicates the health state of the person corresponding to that cell



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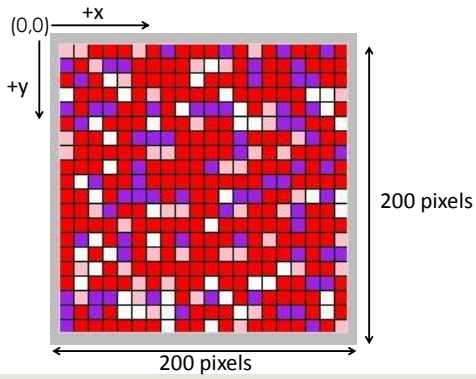
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### Graphics



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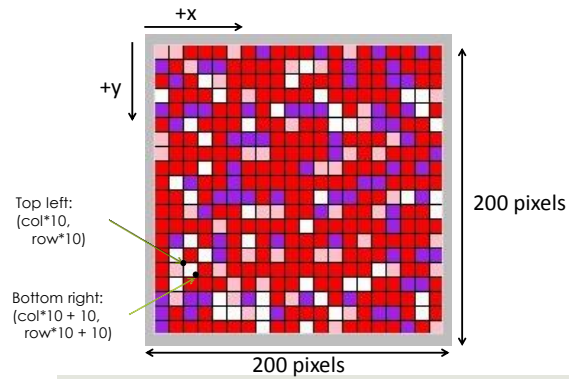
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### Coordinates of each cell



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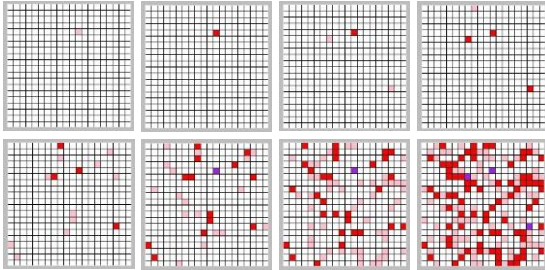
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## Graphical Simulation

Simulation captures the evolution of the health state of the population over time. It evolves in discrete steps: change occurs instantaneously as a new day begins.



## Updating the matrix

```
def simNextDay(data):
    nextDayData = [] # create new matrix and initialize
    for i in range(20):
        nextDayData.append([0] * 20)
    for i in range(20): # create next day
        for j in range(20):
            if immune(data, i, j):
                nextDayData[i][j] = IMMUNE
            elif infected(data, i, j) or contagious(data, i, j):
                nextDayData[i][j] = data[i][j] + 1
            elif healthy(data, i, j):
                nextDayData[i][j] = meetPeople(data, i, j)
    return newMatrix
```

These functions return Boolean value.

```
def meetPeople(currMatrix, row, col):
    for counter in range(4): # repeat 4 times
        if contagious(currMatrix, randrange(20), randrange(20)):
            return INFECTED
    return currMatrix[row][col]
```

## What if Our Model Changes?

- If a healthy person contacts a contagious person, she gets sick 40% of the time.

```
def meetPeople(currMatrix, row, col):
    for counter in range(4): # repeat 4 times
        if contagious(currMatrix, randrange(20), randrange(20))
            and randrange(100) < 40 :
            return INFECTED
    return currMatrix[row][col]
```

## What if Our Model Changes?(cont'd)

- The current model does not capture neighbor relationship. The adjacency of 2 cells does not indicate that they are neighbors.
- What if we used to grid to capture neighbor relationship and assumed that a healthy person gets infected if they have at least one contagious neighbor.

## Neighbors

```
cell = matrix[i][j]
north = matrix[i-1][j]    NO!

if i == 0:                YES!
    north = None
else:
    north = matrix[i-1][j]
```

## Continuous Simulation

N-Body Problem

## Continuous-Time Simulations

- Often used to model physical phenomena involving forces acting on objects.
- Is "time" really continuous?
  - Philosophical question. No one knows.
  - Just pretend it is.
- Is simulated time continuous?
  - No. It's divided into discrete time steps.
  - But they can be as small as we like.

## N-Body Problem

- **Newton's theory:** Planets and other bodies move according to the gravitational effects of the objects around them
  - **N-body problem:** Predicting the individual motions of a group of objects interacting with each other gravitationally
    - **With just two bodies**, we can write a **simple formula** to calculate their positions at any future time, given their starting positions.
    - **But with 3 or more bodies**, *no formula exists for this, because the system is highly nonlinear, and potentially chaotic.*
- Our only recourse is **simulation**.

## N-Body Simulation

- Using simulation to predict future locations of bodies  
Astronomers use simulations to predict locations of satellites, plan space travel, track dangerous asteroids etc.

### Main idea of the simulation:

- Start with the current location and heading of each planet. Then repeatedly
  - Determine where the planets would be a short time later if they move according to a straight line
  - Calculate adjustments to headings

## Simulating Gravitational Attraction

Newton's law of universal gravitation:

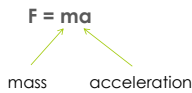
$$F = G \cdot m_1 \cdot m_2 / d^2$$

where G = gravitational constant,  
 m<sub>1</sub> and m<sub>2</sub> are the masses, and  
 d is the distance between them.

## Force and Acceleration

Newton's second law:

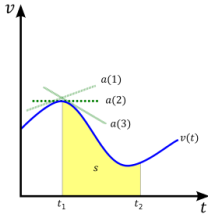
if some external force is applied to a body then  
 the body accelerates (its velocity changes)



## Moving A Single Body

- Calculate the **force** and **acceleration** influencing the body **at a given time**
- Suppose that **acceleration is constant** for a given interval of time and calculate the **velocity** and **distance** moved

## Velocity versus Time graph



$a$  lines represent the values for acceleration at different points along the curve and the yellow area under the curve represents displacement  $s$

Source: Wikipedia

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## Integrating Acceleration

- When an object accelerates, its velocity  $v(t)$  changes. How can we model this?
- Divide time into tiny steps  $\Delta t$ .
- Re-calculate the velocity at each time step.  

$$v(t + \Delta t) = v(t) + a(t) \cdot \Delta t$$
- Smaller  $\Delta t$  brings greater accuracy. Why?

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## Velocity Is Rate of Change of Position

- If an object has non-zero velocity, its position is changing.
- We can use the same integration trick to update the body's position based on velocity.  

$$x(t + \Delta t) = x(t) + v(t) \cdot \Delta t$$

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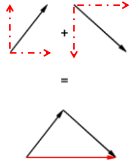
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## Force Vectors

- We can use vectors to keep track of positions, velocities, and accelerations:  $(x, y, z)$  coordinates
- Forces are additive and vector addition performs ordinary addition on each component:  
 $(x_1, y_1, z_1) + (x_2, y_2, z_2) = (x_1+x_2, y_1+y_2, z_1+z_2)$



The vectors in this example has 0 for the z coordinate.  
 The north and south vectors cancel out each other  
 The east vectors add up

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## Force Action on a Single Body

- Calculate all the force vectors influencing the body
- Add the vectors together to determine the cumulative force

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## Moving Multiple Bodies

- At each time step move each body by calculating the force vectors in each direction
- Suppose we are given a method  $\text{interaction}(a,b)$  that calculates the gravitational force between the bodies a and b
- We need to compute all pairwise interactions.
- How many force calculations are there?
  - For the first body interactions with each of the remaining  $N-1$  bodies, for the second one interactions with each of the remaining  $N-2$  bodies because we already took into account its interaction with the first one etc.
  - $N-1 + N-2 + \dots + 1 = N \times (N-1)/2 \Rightarrow O(N^2)$

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