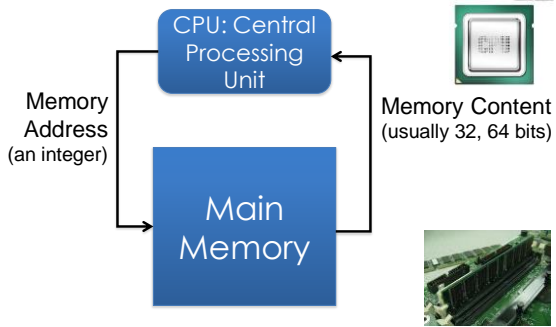


Organizing Data: Arrays, Linked Lists

Computer Memory



Recall Lists

- Ordered *collection* of data
- Our mental model is based on indexed data slots



- But how are lists actually stored in computer's memory?

Arrays in Memory

- An **array** is a very simple data structure for holding a **sequence of data**. They have a direct correspondence with memory system in most computers.
- Typically, array elements are **stored in adjacent memory cells**. The subscript (or index) is used to calculate an offset to find the desired element.

Address	Content	Example:
100:	50	data = [50, 42, 85, 71, 99] Assume we have a byte-addressable computer, * integers are stored using 4 bytes (32 bits) * the first element is stored at address 100 (Nothing special about 100, just an example). The array could start at any address.
104:	42	
108:	85	
112:	71	
116:	99	

Arrays in Memory

- Example: data = [50, 42, 85, 71, 99]
Assume we have a byte-addressable computer, integers are stored using 4 bytes (32 bits) and our array starts at address 100.
- If we want data[3], the computer takes the address of the start of the array (100 in our example) and adds **the index * the size** of an array element (4 bytes in our example) to find the element we want.

Location of data[3] is $100 + 3 * 4 = 112$

- **Do you see why it makes sense for the first index of an array to be 0?**

Content
100: 50
104: 42
108: 85
112: 71
116: 99

Arrays: Pros and Cons

- Pros:
 - **Access** to an array element is **fast** since we can compute its location quickly (constant time).
- Cons:
 - If we want to **insert or delete** an element, we have to **shift** subsequent elements **which slows** our computation down.
 - We need a **large enough block of memory** to hold our array.

Arrays in Python

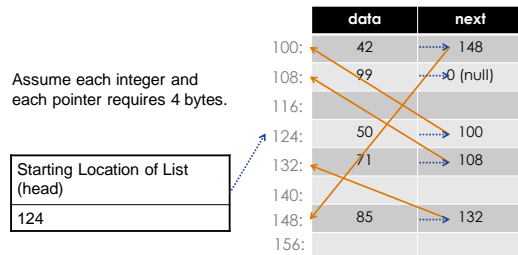
- Array module
- Arrays are sequence types and behave very much like lists, except that the **type of objects** stored in them is constrained.
- We only use Python lists in 15110. Python lists are akin to structures called **dynamic arrays**.

Linked Lists

- ▣ Another data structure that stores a sequence of data values is the **linked list**.
- ▣ Data values in a linked list do **not have to be** stored in **adjacent** memory cells.
- ▣ To accommodate this feature, each data value has an additional "**pointer**" that indicates where the *next data value* is in computer memory.
- ▣ In order to use the linked list, we only need to know where the *first data value* is stored.

Linked List Example

- ▣ Linked list to store the sequence: data = [50, 42, 85, 71, 99]



Linked List Example

To insert a new element, we only need to change a few pointers.

Example:

Insert 20 between 42 and 85

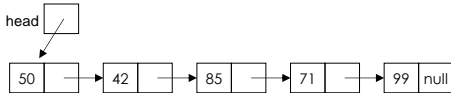
Starting Location of List (head)
124

Assume each integer and pointer requires 4 bytes.

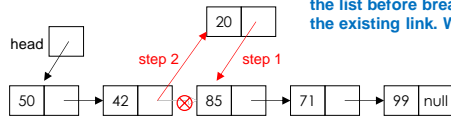
	data	next
100:	42	156
108:	99	0 (null)
116:		
124:	50	100
132:	71	108
140:		
148:	85	132
156:	20	148

Drawing Linked Lists Abstractly

[50, 42, 85, 71, 99]



Inserting 20 after 42:



We link the new node to the list before breaking the existing link. Why?

Linked Lists: Pros and Cons

- Pros:
 - **Inserting** and **deleting** data does not require us to move/shift subsequent data elements.
- Cons:
 - If we want to **access** a specific element, we **need to traverse** the list from the head of the list to find it, which can take longer than an array access.
 - Linked lists require **more memory**. (Why?)

Two-dimensional arrays

- Some data can be organized efficiently in a **table** (also called a **matrix** or **2-dimensional array**)
- Each cell is denoted with two subscripts, a **row** and **column** indicator

B[2][3] = 50

B	0	1	2	3	4
0	3	18	43	49	65
1	14	30	32	53	75
2	9	28	38	50	73
3	10	24	37	58	62
4	7	19	40	46	66

2D Lists in Python

```
data = [ [1, 2, 3, 4],
         [5, 6, 7, 8],
         [9, 10, 11, 12]
       ]
>>> data[0]
[1, 2, 3, 4]
>>> data[1][2]
7
>>> data[2][5]
index error
```

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

2D List Example in Python

- Find the sum of all elements in a 2D array

```
def sum_matrix(table):
    sum = 0
    for row in range(0, len(table)):
        for col in range(0, len(table[row])):
            sum = sum + table[row][col]
    return sum
```

number of rows in the table

number of columns in the given row of the table

In a rectangular matrix, this number will be fixed so we could use a fixed number for row such as len(table[0])

Tracing the Nested Loop

```
def sum_matrix(table):
    sum = 0
    for row in range(0, len(table)):
        for col in range(0, len(table[row])):
            sum = sum + table[row][col]
    return sum
```

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12

```
len(table) = 3
len(table[row]) = 4 for every row
```

row	col	sum
0	0	1
0	1	3
0	2	6
0	3	10
1	0	15
1	1	21
1	2	28
1	3	36
2	0	45
2	1	55
2	2	66
2	3	78

Stacks

- A **stack** is a data structure that works on the principle of **Last In First Out (LIFO)**.
 - LIFO: The last item put on the stack is the first item that can be taken off.
- Common stack operations:
 - Push – put a new element on to the top of the stack
 - Pop – remove the top element from the top of the stack
- Applications: calculators, compilers, programming



RPN

- Some modern calculators use Reverse Polish Notation (RPN)
 - Developed in 1920 by Jan Lukasiewicz
 - Computation of mathematical formulas can be done without using any parentheses

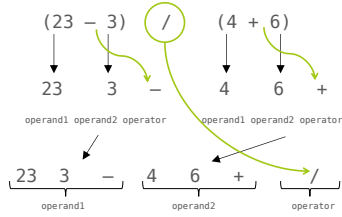
Example:

In RPN $(3 + 4) * 5$
 becomes $3 4 + 5 *$



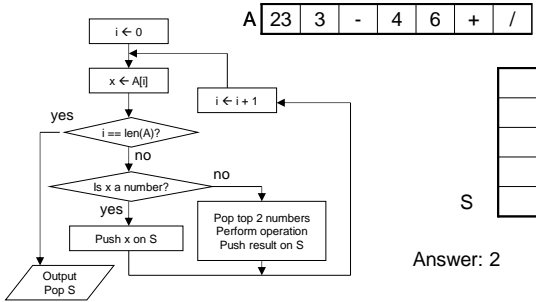
RPN Example

Converting a standard mathematical expression into RPN:



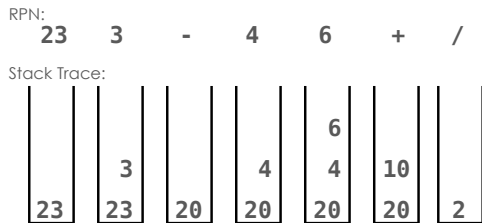
22

Evaluating RPN with a Stack



23

Example Step by Step



24

Stacks in Python

You can treat lists as stacks in Python.

	<u>stack</u>	<u>x</u>
stack = []	[]	
stack.append(1)	[1]	
stack.append(2)	[1,2]	
stack.append(3)	[1,2,3]	
x = stack.pop()	[1,2]	3
x = stack.pop()	[1]	2
x = stack.pop()	[]	1
x = stack.pop()	[]	ERROR

25

Queues



A **queue** is a data structure that works on the principle of **First In First Out (FIFO)**.

- FIFO: The first item stored in the queue is the first item that can be taken out.

Common queue operations:

- Enqueue – put a new element in to the rear of the queue
- Dequeue – remove the first element from the front of the queue



Applications: printers, simulations, networks

26

Next Time

Hash Tables

27