Name:	Andrew Id:
ranc	Allulew lu

$15\text{-}112~\mathrm{Spring}~2024~\mathrm{Quiz}~9$

Up to 25 minutes. No calculators, no notes, no books, no computers. Show your work! Do not use try/except on this quiz.

1. **Code Tracing**: Indicate what the following programs print. Place your answers (and nothing else) in the boxes below the code.

```
(a) (6 points) CT1
    def ct1(s):
        if len(s) == 0:
            return ""
        elif len(s) == 1:
            print(s)
            return s
        else:
            print(s)
            return s[0] + ct1(s[1:][::-1])

print(ct1("chats"))
```

```
(b) (6 points) CT2
    def ct2(s):
        if len(s) == 0:
            return ""
        print(s)
        if len(s) == 1:
            return s
        x = len(s) // 2
        return s[x] + ct2(s[:x]) + ct2(s[x + 1 :])

print(ct2("dance"))
```

2. Free Response: Digit Count Map

This two-part problem is very similar to the homework, and the concept of a digit count map is the same.

Your solutions to this problem must be entirely recursive. No loops or iterative functions are allowed; their use will result in a zero score for this problem. Using str() to convert a multidigit integer to a string is iterative and therefore not allowed.

(a) (4 points) Write the recursive function addDigitsToMap(countMap, n) which, given a dictionary countMap and a non-negative integer n, adds the count of all of the digits in n to countMap. The function does not return anything. Consider the following examples:

```
d = dict()
addDigitsToMap(d, 155)
assert d == {1: 1, 5: 2}

d = dict()
addDigitsToMap(d, 155)
addDigitsToMap(d, 2045)
assert d == {0: 1, 1: 1, 2: 1, 4: 1, 5: 3}
```

(b) (4 points) Write the recursive function digitCountMapFromList(L) that takes a list of non-negative integers, L, and returns a map of the counts of all the digits that occur in the numbers in the list. For example, consider digitCountMapFromList([12, 10, 9, 11]). These numbers include one 0, four 1's, one 2, and one 9, so the call would return a dictionary containing: { 0:1, 1:4, 2:1, 9:1 }. Consider the following additional examples:

```
assert digitCountMapFromList([6, 2, 7, 1, 5, 6]) == {1: 1, 2: 1, 5: 1, 6: 2, 7: 1}
assert digitCountMapFromList([12, 10, 9, 11]) == {0: 1, 1: 4, 2: 1, 9: 1}
assert(digitCountMapFromList([4, 686, 64, 89, 710]) == {0:1, 1:1, 4:2, 6:3, 7:1, 8:2, 9:1})
assert digitCountMapFromList([]) == {}
```

You may assume that you have a working implementation of addDigitsToMap(countMap, n), even if yours does not work.