## Data Representation

15-110 - Monday $1 / 22$

## Announcements

- Check1 was due at noon today. If you forgot to turn it in, you can still submit up until the revision deadline!
- We'll try to get feedback released by the next lecture
- Going forward, most assignments will be due on Mondays
- Note that Hw1 (due next Monday!) has a programming component. This will be completed in a separate Python file.
- Tutorial: how to use and submit the programming starter file


## Learning Objectives

- Understand how different number systems can represent the same information
- Translate binary numbers to decimal, and vice versa
- Interpret binary numbers as abstracted types, including colors and text

Number Systems

## Computers Run on Os and 1s

Computers represent everything by using 0 s and 1 s . You've likely seen references to this before.

How can we represent text, or images, or sound with 0 s and 1 s ? This brings us back to abstraction.


## Abstraction is About Representation

Recall our definition of abstraction from the first lecture:

Abstraction is a technique used to make complex systems manageable by changing the amount of detail used to represent or interact with the system.

We'll use abstraction to translate $0 s$ and $1 s$ to decimal numbers, then translate those numbers to other types.

## Number Systems - Coins

A number system is a way of representing numbers using symbols.

One example of a number system is currency. In the US currency system, how much is each of the following symbols worth?


Penny
1 cent
Nickel
5 cents
Dime
10 cents

Quarter 25 cents

## Number Systems - Dollars

Alternatively, we can represent money using dollars and cents, in decimal form.

For example, a medium coffee at La Prima Cafe is $\mathbf{\$ 2 . 4 5}$.


## Converting Coins to Dollars

We can convert between number systems by translating a value from one system to the other.

For example, the coins on the left represent the same value as $\$ 0.87$

Using pictures is clunky. Let's make a new representation system for coins.


## Coin Number Representation

To represent coins, we'll make a number with four digits.

The first represents quarters, the second dimes, the third nickels, and the fourth pennies.

c.3.1.0.2 =

3*\$0.25 + 1*\$0.10 + 0*\$0.05 + 2*\$0.01 =

## Q D N P

## c 3102

\$0.87

## Converting Dollars to Coins

Think about an algorithm to convert from a dollar amount to coins, using as few coins as possible.

You do: How would you begin such an algorithm?

## Conversion Example

What is $\$ 0.59$ in coin representation?
$\$ 0.59=2 * \$ 0.25+0 * \$ 0.10+1 * \$ 0.05+4 * \$ 0.01=c .2 \cdot 0.1 .4$

## Activity: Coin Conversion

You do: Now try the following calculations:

What is c.1.1.1.2 in dollars?

What is $\$ 0.61$ in coin representation?

## Number Systems - Decimal

When we work with ordinary numbers outside of any specific context, we usually use the decimal number system, which uses digits $0,1,2,3,4,5,6,7,8$, and 9 .

Moving from the right, the first digit is the number of 1 s , the second is 10 s , the third is 100 s , etc. Each digit represents a power of 10. For example, 1980 in decimal is 1 * $1000+9 * 100+8 * 10+0 * 1$

But this isn't the only abstract number system we can use!


## Number Systems - Binary

We can represent numbers using only the digits $0 s$ and $1 s$ with the binary number system.

Instead of counting the number of $1 \mathrm{~s}, 5 \mathrm{~s}, 10 \mathrm{~s}$, and 25 s in coins, or $1 \mathrm{~s}, 10 \mathrm{~s}, 100 \mathrm{~s}$, and 1000s in abstract amounts, count the number of $1 \mathrm{~s}, 2 \mathrm{~s}, 4 \mathrm{~s}, 8 \mathrm{~s}$, etc. For example, 1101 in binary is $1 * 8+1 * 4+0 * 2+1 * 1=13$ in decimal.

Why these numbers? They're powers of 2. This is a number in base $\mathbf{2}$, which only needs the digits 0 and 1 .

$$
\begin{array}{rrrr}
{ }^{23} \boldsymbol{8} & { }^{2} \mathbf{4} & { }^{2}{ }^{2} & { }^{20} \mathbf{1} \\
1 & 1 & 0 & 1
\end{array}
$$

## Bits and Bytes

When working with binary and computers, we often refer to a set of binary values used together to represent a number.

A single binary value is called a bit.

A set of 8 bits is called a byte.

We commonly use some number of bytes to represent data values.

## Counting in Binary

$$
\begin{aligned}
& \mathbf{O}=\begin{array}{c|c|c|c|c|c|c|c|}
2^{2} \mathbf{1 2 8} \\
{ }^{26} \mathbf{6 4} & { }^{25} \mathbf{3 2} & 2^{4} \mathbf{1 6} & { }^{2^{3}} \mathbf{8} & 2^{2} \mathbf{4} & { }^{2^{1}} \mathbf{2} & { }^{20} \mathbf{1} \\
\hline 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
\hline
\end{array} \\
& \mathbf{2}=\begin{array}{c|c|c|c|c|c|c|c|}
2^{1} \mathbf{1 2 8} \\
{ }^{2^{6}} \mathbf{6 4} & 2^{5} \mathbf{3 2} & 2^{4} \mathbf{1 6} & { }^{2^{3}} \mathbf{8} & 2^{2} \mathbf{4} & 2^{1} \mathbf{2} & { }^{20} \mathbf{1} \\
\hline 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\
\hline
\end{array} \\
& \mathbf{4}=\begin{array}{c|c|c|c|c|c|c|c|}
\hline 2^{2} \mathbf{1 2 8} & { }^{26} \mathbf{6 4} & { }^{2^{5}} \mathbf{3 2} & 2^{2^{4} \mathbf{1 6}} & { }^{23} \mathbf{8} & { }^{2 \boldsymbol{4}} \mathbf{4} & { }^{21} \mathbf{2} & { }^{20} \mathbf{1} \\
\hline 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\
\hline
\end{array} \\
& \mathbf{6}=\begin{array}{c|c|c|c|c|c|c|c|}
\hline{ }^{2} \mathbf{1 2 8} & 2^{2^{6}} \mathbf{6 4} & { }^{2^{5}} \mathbf{3 2} & { }^{24} \mathbf{1 6} & { }^{2^{3}} \mathbf{8} & { }^{2} \mathbf{4} & { }^{21} \mathbf{2} & { }^{20} \mathbf{1} \\
\hline 0 & 0 & 0 & 0 & 0 & 1 & 1 & 0 \\
\hline
\end{array}
\end{aligned}
$$

## Converting Binary to Decimal

To convert a binary number to decimal, just add each power of 2 that is represented by a 1.


Another example: $10010001=128+16+1=145$


## Converting Decimal to Binary

Converting decimal to binary uses the same process as converting dollars to coins.

Look for the largest power of 2 that can fit in the number and subtract it from the number. Repeat with the next power of 2 , etc., until you reach 0 .

For example, $36=32+4$-> 00100100

| $128$ | ${ }^{26} 64$ | $2^{5} 32$ | ${ }^{24} 16$ | ${ }^{23} 8$ |  | $2^{1}$ | $2_{1}^{20}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 0 | 0 | 1 | 0 |  |

Another example:

| $103=64+39$ |  |  |  |  |  |  |  |  |  |  | 2 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| + $32+4+3=64+32+4+2+1$-> |  |  |  |  | - |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  | 01100111

## Activity: Converting Binary

You do: Now try converting numbers on your own.

First: what is 01011011 in decimal?

Second: what is 75 in binary?

Abstracted Types

## Binary and Abstraction

Now that we can represent numbers using binary, we can represent everything computers store using binary.

We just need to use abstraction to interpret bits or numbers in particular ways.

Let's consider dates, images, and text.

## Discussion: Representing Dates

It can be helpful to think logically about how to represent a value before learning how it's done in practice. Let's do that now.

Discuss: We can convert binary directly into numbers, but how could we use binary and number to represent a date (i.e., 10/15/2023)?

## Answer: Representing Dates

Simple Approach: reserve 4 bits to represent the month (1-12), 5 bits to represent the date (1-31) and 12 bits to represent the year (1-4095). Convert the month, day, year normally from decimal to binary.

Actual Approach: in the commonly used Unix Timestamp approach, you count the seconds from a certain date (00:00:00 of 01/01/1970) and convert the number of seconds to binary. Any dates that occur before this time would be negative numbers, and any dates after would be positive numbers!

We use 32 bits to represent each date; the first bit is used to indicate if the number was positive (0) or negative (1), and the remaining 31 bits are used to represent the number of seconds elapsed. Thus, we restrict the number of bits to represent the date to 31 bits.

## Represent Images as Grids of Colors

What if we want to represent an image? How can we convert that to numbers?

First, break the image down into a grid of colors, where each square of color has a distinct hue. A square of color in this context is called a pixel.

If we can represent a pixel in binary, we can interpret a series of pixels as an image.


## Representing Colors in Binary

We need to represent a single color (a pixel) as a number.
There are a few ways to do this, but we'll focus on RGB. Any color can be represented as a combination of Red, Green, and Blue.

Red, green, and blue intensity can be represented using one byte each, where 00000000 (0) is none and 11111111 (255) is very intense. Each pixel will therefore require 3 bytes to encode.

Try it out here:
https://www.w3schools.com/colors/colors rgb.asp

## Example: Representing Beige

To make the campus-building beige, we'd need:
Red $=\mathbf{2 4 9} \mathbf{= 1 1 1 1 1 0 0 1}$

Green $=228 \mathbf{= 1 1 1 0 0 1 0 0}$
Blue = 183 = 10110111


Which makes beige!


## Represent Text as Individual Characters

Finally, how do we represent text?

First, we break it down into smaller parts, like with images. In this case, we can break text down into individual characters.

For example, the text "Hello World" becomes
H, e, I, I, o, space, W, o, r, I, d

## Use a Lookup Table to Convert Characters

Unlike colors, characters don't have a natural connection to numbers.

Instead, we can use a lookup table that maps each possible character to an integer.

As long as every computer uses the same lookup table, computers can always translate a set of numbers into the same set of characters.

## ASCII is a Simple Lookup Table

|  | Dec | Oct | Dec Hex | Oc HTML | Chr | Dec | Oct | Chr | Dec Hex | Oct | Chr |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 00 | 000 NULL | 3220 | 040 \&\#032; | Space | 6440 | 100 \&\#064; | @ | 9660 | 140 \&\#096; |  |
| Smal set of characters | 11 | 001 Start of Header | 3321 | 041 \&\#033; | ! | 6541 | 101 \&\#065; | A | 9761 | 141 \&\#097; | a |
| SMAdisetof characters, | 22 | 002 Start of Text | 3422 | 042 \&\#034; | " | 6642 | 102 \&\#066; | B | 9862 | 142 \&\#098; | b |
|  | 33 | 003 End of Text | 3523 | 043 \&\#035; | \# | 6743 | 103 \&\#067; | C | 9963 | 143 \&\#099; | c |
| We can use the encoalne | 44 | 004 End of Transmission | 3624 | 044 \&\#036; | \$ | 6844 | 104 \&\#068; | D | 10064 | 144 \&\#100; | d |
|  | 55 | 005 Enquiry | 3725 | 045 \&\#037; | \% | 6945 | 105 \&\#069; | E | 10165 | 145 \&\#101; | e |
| SVStem called ASC\\|. This | 66 7 7 | 006 Acknowledgment | 3826 | 046 \&\#038; | \& | 7046 | 106 \&\#070; | F | 10266 | 146 \&\#102; | $f$ |
|  | 77 | 007 Bell | 3927 | 047 \&\#039; |  | 7147 | 107 \&\#071; | G | 10367 | 147 \&\#103; | g |
|  | 88 | 010 Backspace | 4028 | 050 \& \#040; | ( | 7248 | 110 \&\#072; | H | 10468 | 150 \&\#104; | h |
| mapsthenumbers oto 25 | 99 | 011 Horizontal Tab | 4129 | 051 \&\#041; | ) | 7349 | 111 \&\#073; | I | 10569 | 151 \&\#105; | i |
|  | 10 A | 012 Line feed | 42 2A | 052 \&\#042; |  | 74 4A | 112 \&\#074; | J | 106 6A | 152 \&\#106; | j |
|  | 11 B | 013 Vertical Tab | 43 2B | 053 \&\#043; | + | 75 4B | 113 \&\#075; | K | 107 6B | 153 \&\#107; | k |
| Characters. nerefore, one | 12 C | 014 Form feed | 44 2C | 054 \&\#044; |  | 76 4C | 114 \&\#076; | L | 108 6C | 154 \&\#108; | 1 |
|  | 13 D | 015 Carriage return | 45 2D | 055 \&\#045; | - | 77 4D | 115 \&\#077; | M | 109 6D | 155 \&\#109; | m |
| cter is represented by | 14 E | 016 Shift Out | 46 2E | 056 \&\#046; |  | 78 4E | 116 \&\#078; | N | 110 6E | 156 \&\#110; | n |
| inaracer is represented by | 15 F | 017 Shift In | 47 2F | 057 \&\#047; | / | 79 4F | 117 \&\#079; | O | 111 6F | 157 \&\#111; | - |
|  | 1610 | 020 Data Link Escape | 4830 | 060 \&\#048; | 0 | 8050 | 120 \&\#080; | P | 11270 | 160 \&\#112; | p |
| ne ovte | 1711 | 021 Device Control 1 | 4931 | 061 \&\#049; | 1 | 8151 | 121 \&\#081; | Q | 11371 | 161 \&\#113; | q |
|  | 1812 | 022 Device Control 2 | 5032 | 062 \&\#050; | 2 | 8252 | 122 \&\#082; | R | 11472 | 162 \&\#114; | r |
|  | 1913 | 023 Device Control 3 | 5133 | 063 \&\#051; | 3 | 8353 | 123 \&\#083; | S | 11573 | 163 \&\#115; | s |
|  | 2014 | 024 Device Control 4 | 5234 | 064 \&\#052; | 4 | 8454 | 124 \&\#084; | T | 11674 | 164 \&\#116; | t |
|  | 2115 | 025 Negative Ack. | 5335 | 065 \&\#053; | 5 | 8555 | 125 \&\#085; | U | 11775 | 165 \&\#117; | u |
|  | 2216 | 026 Synchronous idle | 5436 | 066 \&\#054; | 6 | 8656 | 126 \&\#086; | V | 11876 | 166 \&\#118; | v |
|  | 2317 | 027 End of Trans. Block | 5537 | 067 \&\#055; | 7 | 8757 | 127 \&\#087; | W | 11977 | 167 \&\#119; | w |
| neck It out nere: | $2418$ | 030 Cancel | 5638 | 070 \&\#056; | 8 | 8858 | 130 \&\#088; | X | 12078 | 170 \&\#120; | x |
|  | 2519 | 031 End of Medium | 5739 | 071 \&\#057; | 9 | 8959 | 131 \&\#089; | Y | 12179 | 171 \&\#121; | y |
| ttos:/ / WWW.asciitable.con/ | 26 1A | 032 Substitute | 58 3A | 072 \&\#058; | : | 90 5A | 132 \&\#090; | Z | 122 7A | 172 \&\#122; | z |
| LuNS. WW.aSCilcanle.com | 27 1B | 033 Escape | 59 3B | 073 \&\#059; | ; | 91 5B | 133 \&\#091; | [ | 123 7B | 173 \&\#123; | \{ |
|  | 281 C | 034 File Separator | 60 3C | 074 \&\#060; | < | 92 5C | 134 \&\#092; | 1 | 1247 C | 174 \&\#124; | I |
|  | 29 1D | 035 Group Separator | 61 3D | 075 \&\#061; | = | 93 5D | 135 \&\#093; | ] | 125 7D | 175 \&\#125; | \} |
|  | 301 E | 036 Record Separator | 623 E | 076 \&\#062; 077 \&\#063; | ? | 945 E 95 | 136 \&\#094; 137 \&\#095; | $\wedge$ | 1267 E 127 FF | $\begin{aligned} & 176 \text { \&\#126; } \\ & 177 \text { \&\#127; } \end{aligned}$ | Del |

## Translating Text to Numbers

Y a y ->

8997121 ->

0101100101100001 01111001

| Dec Hex | Oct Chr | Dec Hex | Oct HTML | Chr | Dec Hex | Oct | HTML | Chr | Dec Hex | Oct | HTML | Chr |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 00 | 000 NULL | 3220 | 040 \&\#032; | Space | 6440 | 100 | \&\#064; | @ | 9660 |  | \&\#096; |  |
| 11 | 001 Start of Header | 3321 | 041 \&\#033; | ! | 6541 |  | \&\#065; | A | 9761 |  | \&\#097; | a |
| 22 | 002 Start of Text | 3422 | 042 \&\#034; |  | 6642 |  | \&\#066; | B | 9862 |  | \&\#098; | b |
| 33 | 003 End of Text | 3523 | 043 \&\#035; | \# | 6743 | 103 | \&\#067; | C | 9963 |  | \&\#099; | C |
| 44 | 004 End of Transmission | 3624 | 044 \&\#036; | \$ | 6844 | 104 | \&\#068; | D | 10064 |  | \&\#100; | d |
| 55 | 005 Enquiry | 3725 | 045 \&\#037; | \% | 6945 | 105 | \&\#069; | E | 10165 |  | \&\#101; | e |
| 66 | 006 Acknowledgment | 3826 | 046 \&\#038; | \& | 7046 | 106 | \&\#070; | F | 10266 |  | \&\#102; | f |
| 77 | 007 Bell | 3927 | 047 \&\#039; |  | 7147 | 107 | \&\#071; | G | 10367 |  | \&\#103; | g |
| 88 | 010 Backspace | 4028 | 050 \&\#040; | ( | 7248 | 110 | \&\#072; | H | 10468 |  | \&\#104; | h |
| 99 | 011 Horizontal Tab | 4129 | 051 \&\#041; | ) | 7349 | 111 | \&\#073; | I | 10569 |  | \&\#105; | i |
| 10 A | 012 Line feed | 42 2A | 052 \&\#042; | * | 74 4A | 112 | \&\#074; | J | 106 6A | 152 | \&\#106; | j |
| 11 B | 013 Vertical Tab | 43 2B | 053 \&\#043; | + | 75 4B | 113 | \&\#075; | K | 107 6B |  | \&\#107; | k |
| 12 C | 014 Form feed | 44 2C | 054 \&\#044; |  | 76 4C | 114 | \&\#076; | L | 108 6C |  | \&\#108; | 1 |
| 13 D | 015 Carriage return | 45 2D | 055 \&\#045; | - | 77 4D | 115 | \&\#077; | M | 109 6D |  | \&\#109; | m |
| 14 E | 016 Shift Out | 46 2E | 056 \&\#046; |  | 78 4E | 116 | \&\#078; | N | 110 6E |  | \&\#110; | n |
| 15 F | 017 Shift In | 47 2F | 057 \&\#047; | / | 79 4F | 117 | \&\#079; | O | 111 6F |  | \&\#111; | - |
| 1610 | 020 Data Link Escape | 4830 | 060 \&\#048; | 0 | 8050 | 120 | \&\#080; | P | 11270 |  | \&\#112; | P |
| 1711 | 021 Device Control 1 | 4931 | 061 \&\#049; | 1 | 8151 | 121 | \&\#081; | Q | 11371 |  | \&\#113; | q |
| 1812 | 022 Device Control 2 | 5032 | 062 \&\#050; | 2 | 8252 | 122 | \&\#082; | R | 11472 |  | \&\#114; | r |
| 1913 | 023 Device Control 3 | 5133 | 063 \&\#051; | 3 | 8353 | 123 | \&\#083; | S | 11573 |  | \&\#115; | 5 |
| 2014 | 024 Device Control 4 | 5234 | 064 \&\#052; | 4 | 8454 | 124 | \&\#084; | T | 11674 |  | \&\#116; | t |
| 2115 | 025 Negative Ack. | 5335 | 065 \&\#053; | 5 | 8555 | 125 | \&\#085; | U | 11775 |  | \&\#117; | u |
| 2216 | 026 Synchronous idle | 5436 | 066 \&\#054; | 6 | 8656 | 126 | \&\#086; | V | 11876 |  | \&\#118; | $v$ |
| 2317 | 027 End of Trans. Block | 5537 | 067 \&\#055; | 7 | 8757 | 127 | \&\#087; | W | 11977 | 167 | \&\#119; | W |
| 2418 | 030 Cancel | 5638 | 070 \&\#056; | 8 | 8858 | 130 | \&\#088; | X | 12078 |  | \&\#120; | x |
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| 26 1A | 032 Substitute | 583 A | 072 \&\#058; | : | 905 A | 132 | \&\#090; | Z | 122 7A |  | \&\#122; | z |
| 27 1B | 033 Escape | 59 3B | 073 \&\#059; | ; | 91 5B | 133 | \&\#091; | [ | 123 7B |  | \&\#123; | 1 |
| 28 1C | 034 File Separator | 603 C | 074 \&\#060; | < | 92 5C | 134 | \&\#092; | \} | 124 7C |  | \&\#124; |  |
| 29 1D | 035 Group Separator | 61 3D | 075 \&\#061; | $=$ | 93 5D | 135 | \&\#093; | ] | 125 7D |  | \&\#125; | \} |
| 301 E | 036 Record Separator | 62 3E | 076 \&\#062; | > | 94 5E | 136 | \&\#094; | $\wedge$ | 126 7E | 176 | \&\#126; | ~ |
| 31 1F | 037 Unit Separator | 63 3F | 077 \&\#063; | ? | 95 5F | 137 | \&\#095; | - | 127 7F | 177 | \&\#127; | Del |

## For More Characters, Use Unicode

There are many characters that aren't available in ASCII (characters from nonEnglish languages, advanced symbols, emoji...) due to the limited size.

The Unicode system represents every character that can be typed into a computer. It uses up to 5 bytes, which can represent up to 1 trillion characters! Find all the Unicode characters here: www.unicode-table.com

The Unicode system is also actively under development. The Unicode Consortium regularly updates the standard to add new types of characters and emoji.

Discuss: what are the potential repercussions of using a single standard for all text on computers?

## Learning Objectives

- Understand how different number systems can represent the same information
- Translate binary numbers to decimal, and vice versa
- Interpret binary numbers as abstracted types, including colors and text


## Bonus Slides

In case you want to learn even more about data representation

## Size of Integers

Your machine is either classified as 32 -bit or 64 -bit. This refers to the size of integers used by your computer's operating system.

The largest signed integer that can be represented with $N$ bits is $2^{\mathrm{N}}-1$ (why?). This means that...

Largest int for 32 bits: 4,294,967,295 (or 2,147,483,647 with negative numbers)
Largest int for 64 bits: 18,446,744,073,709,551,615 (18.4 quintillion)

## Integer Overflow

Why does this matter?
By late 2014, the music video Gangnam Style received more than 2 billion views. When it passed the largest positive number that could be represented with 32 bits, YouTube showed the number of views as negative instead!

Now YouTube uses a 64-bit counter instead.


## Computer Memory is Stored as Binary

Your computer keeps track of saved data and all the information it needs to run in its memory, which is represented as binary. You can think about your computer's memory as a really long list of bits, where each bit can be set to 0 or 1 . But usually we think in terms of bytes, groups of 8 bits.

Every byte in your computer has an address, which the computer uses to look up its value.

| 49 | 53 | 49 | 49 | 48 | 75 | 101 | 108 | 198 | 121 | 77 | 97 | 114 | 103 | 97 | 114 | 101 | 116 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\ldots$

## Binary Values Depend on Interpretation

When you open a file on your computer, the application goes to the appropriate address, reads the associated binary, and interprets the binary values based on the file encoding it expects. That interpretation depends on the application you use when opening the file, and the filetype.

You can attempt to open any file using any program, if you convince your computer to let you try. Some programs may crash, and others will show nonsense because the binary isn't being interpreted correctly.

Example: try changing a .docx filetype to .txt, then open it in a plain text editor. .docx files have extra encoding, whereas .txt files use plain ASCII.

## We Use Lots of Bytes!

In modern computing, we use a lot of bytes to represent information.

Smartphone Memory: 64 gigabytes $=64$ billion bytes

Google databases: Over 100 million gigabytes $=100$ quadrillion bytes!

CMU Wifi: 15 million bytes per second

