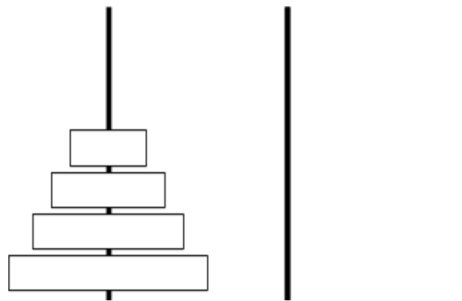


## 1 Tower of Hanoi



The Tower of Hanoi is a canonical puzzle studying problem solving and formulation. The puzzle starts with  $n$  disks of different sizes stacked in order of size (see picture above) on a peg, along with two empty pegs. We can move disks freely between the pegs, but larger disks cannot be stacked on top of smaller ones. The goal is to move all disks to the third peg.

We will attempt to formulate Tower of Hanoi as a search problem.

(a) How could we represent this puzzle as a problem, ie. what would the states be?

For the following questions, assume that you have used your state representation in your answer above.

(b) What is the size of the state space in terms of  $n$ ?

(c) What is the starting state?

(d) From some given state, what legal actions are there?

(e) What is the goal test? Remember that this determines whether a given state is a goal state, `goalTest(state)`.

## 2 Ethics Warmup

Take a look at this description of RedZone, a navigation app that allows you to avoid high crime regions:  
<https://www.androidauthority.com/redzone-navigation-app-avoids-high-crime-areas-686894/>

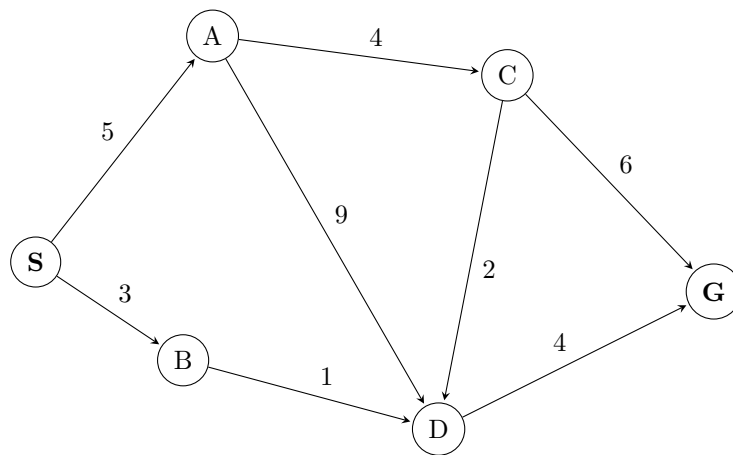
1. If this app became commonly used, what impact could it have on businesses in the “red zone”?
2. Would you want this application to roll out to your hometown? List both positives and negative impacts that the app might have for your community.

### 3 Designing & Understanding Heuristics

Today, we will be taking a closer look at how the performance of  $A^*$  is affected by the heuristics it uses. To do this, we'll be using the graph below. You may have noticed that no heuristic values have been provided (*Recall*: What is  $A^*$  without heuristic values?). This is because we'll be working together to come up with heuristics ourselves!

In groups, design both an admissible heuristic and a consistent heuristic for the graph below by annotating each node with a heuristic value. (Note: you do NOT need to find a closed form way to represent the heuristic function.)

When you have completed your heuristics, work together to answer the questions below.



- What are the definitions of an admissible heuristic and a consistent heuristic?
- Write down the path found by running  $A^*$  using your heuristic on the graph above.
- Work with your group to come up with a heuristic that's admissible but not consistent.

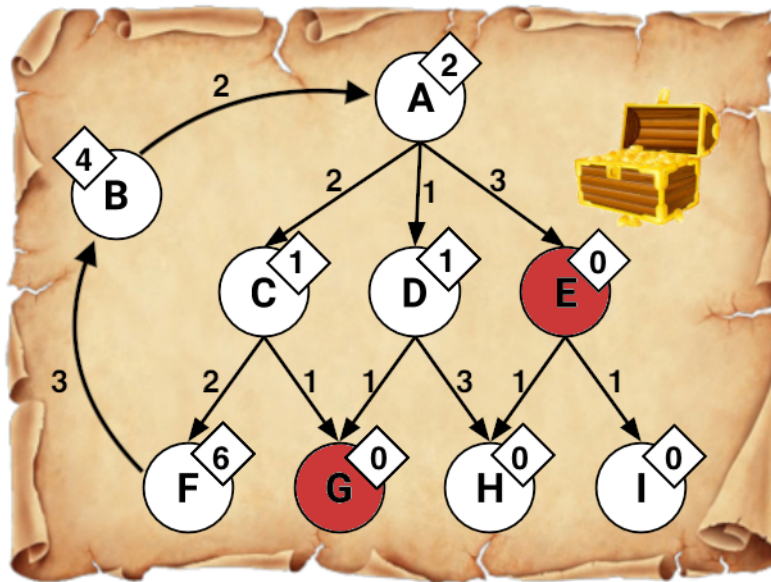
Node	Heuristic
S	
A	
B	
C	
D	
G	

- Explain why a consistent heuristic must also be admissible. You may assume that the heuristic value at a goal node is always 0.



## 4 Treasure Hunting

We are lost at sea, trying to find a hidden treasure. We have a treasure map that tells us which paths we can take and approximately how far away the treasure is but it's not very accurate. We do know that the map will never overestimate the distance to the treasure. There is treasure on two different islands (but we only need to reach one of them).



A is the the island where we are currently and the shaded **red states** are the locations of the treasure. Arrows encode possible actions from each island, and numbers by the arrows represent action costs. Note that arrows are directed; for example,  $A \rightarrow C$  is a valid action, but  $C \rightarrow A$  is not. Numbers shown in diamonds are heuristic values that estimate the optimal (minimal) cost to get from that island to any treasure.

Run each of the following search algorithms with graph search and write down the nodes that are added to the explored set during the course of the search, as well as the final path returned and the corresponding cost of the final path, if applicable. When popping off of the frontier, assume that ties are broken alphabetically.

### (a) Depth-First Search

Explored set:

Path returned:

(b) **Breadth-First Search**

Explored set:

Path returned:

(c) **Uniform-Cost Search**

Explored set:

Path returned and cost:

(d) **Greedy Search**

Explored set:

Path returned and cost:

(e) **A\* Search**

Explored set:

Path returned and cost:

## 5 True/False Section

For each of the following questions, answer true or false and provide a brief explanation (or counterexample, if applicable).

- (a) Depth-first search always expands at least as many nodes as  $A^*$  search with an admissible heuristic.
- (b) Assume that for a single move, a rook can move any number of squares on a chessboard in a straight line, either vertically or horizontally, but cannot jump over other pieces. Manhattan distance is an admissible heuristic for the smallest number of moves to move the rook from square A to square B.
- (c) Euclidean distance is an admissible heuristic for Pacman path-planning problems.
- (d) The sum of several admissible heuristics is still an admissible heuristic.
- (e) Admissibility of a heuristic for  $A^*$  search implies consistency as well.
- (f)  $A^*$  with graph search is always optimal with an admissible heuristic.