

CARNEGIE MELLON UNIVERSITY 07-280

HOMEWORK 1

<https://www.cs.cmu.edu/~07280>

INSTRUCTIONS

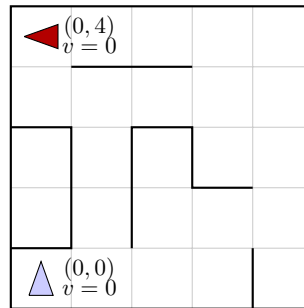
- **Format:** Use the provided LaTeX template to write your answers in the appropriate locations within the *.tex files and then compile a pdf for submission. We try to mark these areas with STUDENT SOLUTION HERE comments. Make sure that you don't change the size or location of any of the answer boxes and that your answers are within the dedicated regions for each question/part. If you do not follow this format, we may deduct points.

You may also digitally annotate the pdf. Illegible handwriting will lead to lost points. However, we suggest that try to do at least some of your work directly in LaTeX.

- **How to submit written component:** Submit to Gradescope a pdf with your answers. Again, make sure your answer boxes are aligned with the original pdf template.
- **How to submit programming component:** See section Programming Submission for details on how to submit to the Gradescope autograder.
- **Policy:** See the course website for homework policies, including late policy, and academic integrity policies.

Name	
Andrew ID	
Hours to complete all components (nearest hour)	

1 [22 pts] Search and Heuristics



Imagine a car-like agent wishes to exit a maze like the one shown above. The agent is directional and at all times faces some direction $d \in (N, S, E, W)$. With a single action, the agent can *either* move forward at an adjustable velocity v or turn.

The moving actions are *faster*, *maintain* and *slower*. For these actions, the agent then moves a number of squares equal to its **new** adjusted velocity. Let v denote the agent's current velocity and let v' denote the agent's new adjusted velocity.

- *Faster*: $v' = v + 1$
- *Slower*: $v' = v - 1$
- *Maintain*: $v' = v$

The turning actions are *left* and *right*, which change the agent's direction by 90 degrees. **Turning is only permitted when the velocity is zero.** Turning leaves the speed at zero.

- *Left*: change the agent's direction by 90 degrees counterclockwise
- *Right*: change the agent's direction by 90 degrees clockwise

For example, if the agent is currently on $(0, 0)$ facing north with velocity 0 (as pictured) and wants to get to $(2, 0)$ facing east with velocity 0, the sequence of actions will be: *right*, *faster*, *maintain*, *slower*.

Illegal actions include

- Any action that would result in a collision with a wall (i.e. there is a wall between the current position and the position you would be in if you took said action)
- Any action that would reduce v below 0 (slowing when $v=0$) or above a maximum speed V_{max}
- Maintaining a velocity of 0
- Turning when velocity $\neq 0$

The agent's goal is to find a plan which parks it ($v = 0$) in the goal direction on the exit square using as few actions (time steps) as possible. Note that the cost of a path is defined by the number of actions the agent takes.

Continued on the following page.

1. [3 pts] Suppose the agent wants to take the leftmost path (i.e., the one that passes through (1,2)) from the start (0,0) facing north to the goal (0,4) facing west. Write down the **shortest** sequence of actions for it to take.

Actions

2. [3 pts] If the grid is M by N and the maximum speed is V_{max} , what is the size of the state space? You should assume that all configurations are reachable from the start state.

State Space Size

3. [3 pts] A “child” of a state s is any other state s' reachable via a legal action from state s . Is it possible that a state in the state space has no children? If so, give an example of such a state. If not, briefly explain why every state must have at least one child.

☐ Yes ☐ No

Example State or Explanation

4. [3 pts] What is the maximum branching factor of this problem? Draw an example state (x , y , orientation, velocity) that has this branching factor, and list the set of available actions. For example, in the above picture, if the agent was in $(0, 0)$ facing North with a velocity of $v = 0$, the branching factor would be 2. The agent could turn left or right (but not go faster since it would hit a wall).

Illegal actions are simply not returned by the problem model and therefore not counted in the branching factor. You do not necessarily have to use the example grid above. If you need to include a drawing of your own, label properly and **make sure it fits in the solution box**.

Maximum Branching Factor

Maximum Branching Example State and Available Actions

5. [3 pts] Is the Manhattan distance from the agent's location to the exit's location admissible?

If not, draw an example state (x , y , orientation, velocity) where this heuristic overestimates at that state, and specify: 1) the heuristic value at that state and 2) the actual cost from that state to the goal.

You do not necessarily have to use the example grid above. Make sure to label your drawing, including the goal state (location, orientation, speed) and action sequence, and fit it into the solution box.

☐ Yes ☐ No

Example State, Heuristic Value, Actual Cost

6. [3 pts] Is the following heuristic admissible? *Manhattan distance* / V_{max} .

If yes, state why. If not, draw an example state (x, y, orientation, velocity) where this heuristic overestimates at that state, and specify: 1) the heuristic value at that state and 2) the actual cost from that state to the goal.

You do not necessarily have to use the example grid above. Make sure to label your drawing, including the goal state (location, orientation, speed) and action sequence, and fit it into the solution box.

☐ Yes ☐ No

[illegible]

7. **[1 pts]** If we used an inadmissible heuristic in A* Tree search, could it change the completeness of the search? Assume the graph is finite and the heuristic is non-negative.

☐ Yes ☐ No

8. **[1 pts]** If we used an inadmissible heuristic in A* Tree search, could it change the optimality of the search? Assume the graph is finite and the heuristic is non-negative.

☐ Yes ☐ No

9. **[2 pts]** Which of the following may be a good reason to use an inadmissible heuristic over an admissible one? Select all that apply.

- ☐ An inadmissible heuristic may be easier to compute, leading to a faster state heuristic computation time.
- ☐ An inadmissible heuristic can be a closer estimate to the actual cost (even if it's an overestimate) than an admissible heuristic, thus exploring fewer nodes.
- ☐ An inadmissible heuristic will still find optimal paths when the actual costs are non-negative.
- ☐ An inadmissible heuristic may be used to completely block off searching part of a graph in a search algorithm.

2 [6 pts] Search Nodes

Consider the tree search (i.e. no explored set) of an arbitrary search problem with max branching factor b . Each search node n has a backward (cumulative) cost of $g(n)$, an admissible heuristic of $h(n)$, and a depth of $d(n)$. Let n_c be a minimum-cost goal node, and let n_s be a shallowest goal node.

For each of the following, give an expression that characterizes the set of nodes that are explored before the search terminates. For instance, if we asked for the set of nodes with positive heuristic value, you could say: for all n , such that $h(n) \geq 0$. Don't worry about ties (so you won't need to worry about $>$ versus $\geq$). If there are no nodes for which the expression is true, you must write "none."

Note that you are not required to use all the functions given, f , g , and h , in your inequality.

1. [2 pts] Give an inequality in terms of the functions g , h , and d , as well as the nodes n_c and n_s defined above to describe the nodes n that are explored in a **breadth-first search** before terminating.

Inequality: All n , such that:

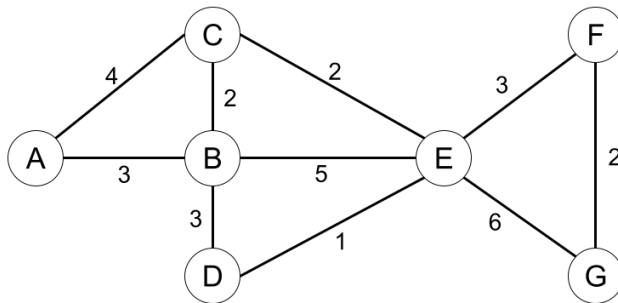
2. [2 pts] Give an inequality in terms of the functions g , h , and d , as well as the nodes n_c and n_s defined above to describe the nodes n that are explored in a **uniform cost search** before terminating.

Inequality: All n , such that:

3. [2 pts] Now for this question, assume the heuristic h is consistent. Give an inequality in terms of the functions g , h , and d , as well as the nodes n_c and n_s defined above to describe the nodes n that are explored in an **A* search** before terminating.

Inequality: All n , such that:

3 [16 pts] Searching a Graph



Node	h_1	h_2
A	12	11
B	6	7
C	9	6
D	3	4
E	3	5
F	2	1
G	0	0

Consider the graph shown above. A is the start state and G is the goal state. The costs for each edge are shown on the graph. The graph is bi-directional so each edge can be traversed from either direction. Please refer to the search algorithms **exactly as presented on the lecture slides** as the ordering of the actions matters.

1. [10 pts] For each of the following **graph search** strategies, mark with an X which (if any) of the listed paths it could return. Note that for some search strategies the specific path returned might depend on tie-breaking behavior. In any such cases, make sure to mark **all** paths that could be returned under some tie-breaking scheme. If a graph search strategy returns a path not listed, **write out the correct path** in the *Other* column.

Algorithm	A-C-E-G	A-C-E-F-G	A-B-D-E-F-G	Other
UCS	(i)	(ii)	(iii)	(iv)
Greedy with heuristic h_1	(v)	(vi)	(vii)	(viii)
Greedy with heuristic h_2	(ix)	(x)	(xi)	(xii)
A* with heuristic h_1	(xiii)	(xiv)	(xv)	(xvi)
A* with heuristic h_2	(xvii)	(xviii)	(xix)	(xx)

2. [2 pts] What is the cost of the optimal path for uniform cost search from A to G?

Answer:

3. [2 pts] Is h_1 admissible? Is it consistent?

Admissible: ☐ Yes ☐ No

Consistent: ☐ Yes ☐ No

4. [2 pts] Is h_2 admissible? Is it consistent?

Admissible: ☐ Yes ☐ No

Consistent: ☐ Yes ☐ No

4 [8 pts] Search: Multiple Choice and Short Answer Questions

1. [5 pts] Consider the following 5 true/false questions with each question worth 1 point. For the following search problems, assume every action has a cost of at least ϵ , with $\epsilon > 0$. Assume any heuristics used are consistent.

Depth-first tree-search on a finite graph is guaranteed to be complete.

☐ True ☐ False

Breadth-first tree-search on a finite graph is guaranteed to be complete.

☐ True ☐ False

For all graphs without cycles, graph-search contains a larger frontier than tree-search.

☐ True ☐ False

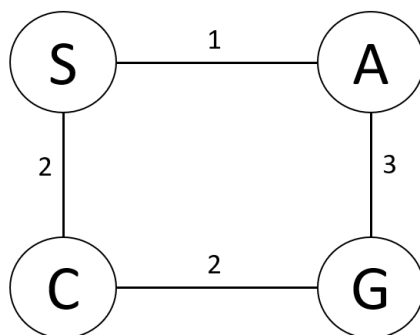
Iterative deepening graph-search has the time complexity of BFS and the space complexity of DFS.

☐ True ☐ False

If $h_1(s)$ is a consistent heuristic and $h_2(s)$ is a consistent heuristic, then $\min(h_1(s), h_2(s))$ must be consistent.

☐ True ☐ False

2. [3 pts] Consider the state space graph shown below. S is the start state and G is the goal state. The costs for each edge are shown on the graph. For the following table below, fill in potential heuristic values such that the heuristic is admissible but not consistent.



Heuristic Function	
State	$h(s)$
S	
A	
C	
G	0

5 [6 pts] Ethics

Please review this article: *This Navigation App Keeps You Out of High-crime Areas in Real Time*:

<https://www.androidauthority.com/redzone-navigation-app-avoids-high-crime-areas-686894/>

1. [2 pts] Let's assume this navigation app uses A* search with an admissible and consistent heuristic to find and return paths. Suppose you are working on this app, and your boss proposes a new heuristic. There is some crime rate metric that ranges from 0 to 5, where 5 is high crime. Your boss proposes that you add this crime rate metric to the application's current heuristic, such that **the heuristic is still admissible and consistent**.

Will the path **necessarily** change with the new heuristic? If so, will the new path be optimal? If not, under what conditions would the path change?

Answer

2. [2 pts] If for some reason you choose not to adjust the heuristic, what is one way you could modify the graph structure or edge costs so that your implementation could return paths that avoid high crime areas? Give your answer in one sentence.

Answer

3. [2 pts] In what ways could people and stores residing in high crime neighborhoods be impacted by changes in navigation algorithms, particularly focusing on the economic and/or societal impact? Please provide 2-3 sentences.

Answer

6 Collaboration Policy

After you have completed all other components of this assignment, report your answers to the following collaboration questions.

1. Did you receive any help whatsoever from anyone in solving this assignment? If so, include full details including names of people who helped you and the exact nature of help you received.

Your Answer

2. Did you give any help whatsoever to anyone in solving this assignment? If so, include full details including names of people you helped and the exact nature of help you offered.

Your Answer

3. Did you find or come across code that implements any part of this assignment? If so, include full details including the source of the code and how you used it in the assignment.

Your Answer