## How To LaTeX

Adam Blank
February 12, 2013

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## 1 What is $\operatorname{AT}_{\mathrm{E}} \mathrm{X}$ ?

${ }^{\mathrm{E}} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ is a typesetting language that is often used in technical fields like Computer Science, Mathematics, Chemistry, and Physics. It is particularly useful to easily typeset math (like $\emptyset \subseteq \mathbb{N}$ ) and chemical formulae (like $\mathrm{H}_{2} \mathrm{O}$ ).

Unfortunately, $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ has a non-trivial learning curve associated with it. This document is intended to lessen your pain in learning how to easily typeset beautiful documents for the rest of your technical career. It is this author's belief that once you learn how to use $\mathrm{LA}_{\mathrm{E}} \mathrm{X}$, editors like Microsoft Word become obsolete, even for documents like English papers.

## 2 Installation and Editors

### 2.1 Windows

You should download MiKTeX from http://miktex.org. TeXnicCenter is a good editor to use to write LATEX documents. You can download it here: http://www.texniccenter.org/.

### 2.2 Mac

You should download MacTeX from http://www.tug.org/mactex/2012/. An editor comes with the distribution which you can use; alternatively, most of the common editors for OSX will support writing LATEX documents.

### 2.3 Linux

If you're using Debian or Ubuntu, try sudo apt-get install texlive. Otherwise, you most likely know your system well enough to figure it out.

## 3 Math Mode

One of the most useful things that $\mathrm{IATEX}_{\mathrm{E}}$ offers is the so-called "Math Mode." Let's just begin with an example. If you type the following snippet of code:

```
Let $M$ be the number of moons in the Universe, and let $E$ be the number of
moons Earth has. We know from Elementary School that $E=1$, but what can we
say about $M$? Since Earth is a part of the Universe, we know that $M \geq E$.
Furthermore, Jupiter has at least one moon; so, $M > E$.
```

LATEX parses it as:
Let $M$ be the number of moons in the Universe, and let $E$ be the number of moons Earth has. We know from Elementary School that $E=1$, but what can we say about $M$ ? Since Earth is a part of the Universe, we know that $M \geq E$. Furthermore, Jupiter has at least one moon; so, $M>E$.

Isn't that neat? The \$'s allow us to seamlessly switch between using Math and English. Sometimes, however, we want to isolate the math to display how important it is. This $\mathrm{AT}_{\mathrm{EX}}$ mode is called
"Display Mode" and is just as easy to use. Instead of a single $\$$, just double them up. ${ }^{1}$ Here's an example:

Now that we have determined that $\$ \mathrm{M}>\mathrm{E}$, we would like to find a simple unification result for physics. To do this, we must recall Newton's famous
formula: $\$ \$ F=m a \$ \$$
You see, once we realize its significance, the rest is all simple arithmetic.
And the output:
Now that we have determined that $M>E$, we would like to find a simple unification result for physics. To do this, we must recall Newton's famous formula:

$$
F=m a
$$

You see, once we realize its significance, the rest is all simple arithmetic.
By using display mode, we made several things happen: (1) we entered math mode and (2) we asked $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ to make sure the content was spaced nicely. You should be careful with math mode and display mode, because, while $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ will try its best to not let the math run off the side of the page, there are some times when it just doesn't know what else to do:

```
$$a + b + c + d + e + f + g + h + i + j + k + l + m + n +o + p + q + r + s +
t + u + v + w + x + y + z + 0 + 1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10 + 11 +
12 + 13 + 14 + 15$$
```

$a+b+c+d+e+f+g+h+i+j+k+l+m+n+o+p+q+r+s+t+u+v+w+x+y+z+0+1+2+3+4+5+6+7+8+9+10+11+$
In such a situation, the correct thing to do is use the align* environment which is discussed below.

Occasionally, typesetting something requires being in math mode, but we don't want alltheletterstoruntogether or be in the math font. One good example of this is chemical formulae. They require us to typeset superscripts and subscripts, but we want normal letters. How do we fix this? ${ }^{2}$ We use the text command! Here's an example:

```
Little Johnny was a chemist.\\
```

He isn't any more. <br>
For what he thought was $\$ \backslash$ text $\{\mathrm{H}\} \_2 \backslash t e x t\{0\} \$$ was $\$ \backslash$ text $\{\mathrm{H}\} \_2 \backslash t e x t\{S O\} \_4 \$$.

And the output:
Johnny was a little chemist.
He isn't any more.
For what he thought was $\mathrm{H}_{2} \mathrm{O}$ was $\mathrm{H}_{2} \mathrm{SO}_{4}$.
That completes the basics of typesetting math in $\mathrm{EA}_{\mathrm{E}} \mathrm{X}$; now, we move on to some quirks that are often "gotchas" to people using $\mathrm{E}^{\mathrm{A}} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ for the first time.

[^0]
## 4 Some ATEX Quirks and Misconceptions

One of the common misconceptions that people using $\mathbb{E A}_{E} \mathrm{X}$ for the first time have is that they think of it as more like Microsoft Word than Java. $\mathrm{LAT}_{\mathrm{E}} \mathrm{X}$ is, first and foremost, a programming language, and you should think of it that way. The way $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ works is that you describe how you want your output to look and $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ figures out what it thinks will look best given your constraints.

### 4.1 Whitespace

As a direct result of $\mathrm{IAT}_{\mathrm{E} X}$ 's methodology, it is not very sensitive to whitespace. Think about when the last time Java cared if you put one or two spaces between public and void was. Take a look:

```
I like my words to have varied spaces
between them. I also
like
    lots
        of
                new
                    lines.
```

Note how $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ ignores my tastes in spacing:
I like my words to have varied spaces between them. I also like lots of new lines.
The good news is that if you are really insistent, $\mathrm{IATEX}_{\mathrm{E}}$ will let you do it:

```
A\;B\;\;\;C\quad D\qquad E
A B C D E
You can\\force new lines\\ as well.
You can
force new lines
as well.
```

If you put a blank line between two paragraphs, $\mathrm{IAT}_{\mathrm{E}} \mathrm{X}$ assumes that they are paragraphs and will correctly indent the next one. Lastly, to tell $\mathrm{AT}_{\mathrm{E}} \mathrm{X}$ you want a new page use the newpage command. That is, type 
.

### 4.2 Escape Characters?

Like most programming languages, LAT $_{\mathrm{E}} \mathrm{X}$ has a bunch of characters that must be "escaped" to be written literally, like $\backslash n$ in Java or C. Here is a list of common characters, their uses in $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ and how to write them literally:

| Character | Usage in LaTeX | Literal |
| :---: | :--- | :---: |
| $\backslash$ | Signifies that what is coming next is a command | \$backslash\$ |
| $\$$ | Enter/exit math mode | $\backslash \$$ |
| $\#$ | Macro arguments | $\backslash \#$ |
| $\&$ | Delimits cells in tabulars | $\backslash \&$ |
| $\%$ | Comments out the rest of the line after it | $\backslash \%$ |
| - | Displaying subscripts | $\backslash-$ |
| - | Displaying superscripts | $\backslash$ verb!~! |
| $\{$ | Delimits various environment and macro bodies | $\backslash\{$ |
| $\}$ | Delimits various environment and macro bodies | $\backslash\}$ |

## 4.3 "Quotes"

This oddity is easier to show than explain:

```
Using "double quotes" and 'single quotes' will not come out like you expect.
```

And the output:
Using "double quotes" and 'single quotes' will not come out like you expect.
Instead, to get the right output, use backticks, which are on the key to the left of ' 1 ', to open quotes and single quotes to close them.

## 4.4 i i

If you are seeing ; or $i$ randomly in your output, you probably meant to use $<$ or $>$. To display either of those you must be in math mode.

## 5 How Do I Make that Symbol?

This section is intended to be a reference for common symbols and constructs that you will probably use fairly often.

### 5.1 Basic Math

| Description | Example | $\mathrm{LAT}_{\text {E }} \mathrm{X}$ Code |
| :---: | :---: | :---: |
| Composition | $\bigcirc$ | \circ |
| Superscript | $x^{n+3}$ | $\mathrm{x}^{\wedge}\{\mathrm{n}+3\}$ |
| Subscript | $y_{n+4}$ | y_\{n+4\} |
| Fraction | $\frac{a+b}{c+d}$ | $\backslash f r a c\{a+b\}\{c+d\}$ |
| Binomial Coefficient | $\binom{n}{k}$ | $\backslash$ binom $\{\mathrm{n}\}\{\mathrm{k}\}$ |
| Greek Letter | $\delta, \Delta$ | \delta , \Delta |
| Greek Letters (Styled) | $\varepsilon$ | \varepsilon |
| Large Parentheses | ${ }^{\prime}\left(\frac{a-b}{c}\right)$ |  |
| Modular Equivalence | $x \equiv 1 \bmod 5$ | $\mathrm{x} \backslash$ \equiv $1 \backslash \bmod 5$ |
| Infinity | $\infty$ | \infty |
| $\leq$ | $x \leq y$ | x \leq y |
| $\geq$ | $x \geq y$ | x \geq y |
| $\neq$ | $x \neq y$ | $\mathrm{x} \backslash$ neq y |
| $\langle$, | $\langle 1,2\rangle$ | \langle 1,2 \rangle |
| ᄂ, 」 | $\left\lfloor\frac{1}{2}\right\rfloor$ | \left\lfloor \frac\{1\}\{2\} \right\rfloor |
| $\lceil$, | $\left\lceil\frac{1}{2}\right\rceil$ | \left\lceil \frac\{1\}\{2\} \right\rceil |
| $\Longrightarrow$ | $x \Longrightarrow y$ | x \implies y |
| $\Longleftrightarrow$ | $x \Longleftrightarrow y$ | x \iff y |
| $\times$ | $A \times B$ | A \times B |
| . | $A \cdot B$ | A \cdot B |

### 5.2 Logical Symbols

| Description | Example | $\mathbf{A N}_{\mathbf{E}} \mathbf{X}$ Code |
| :---: | :---: | :---: |
| And | $p \wedge q$ | p \wedge q |
| Equivalence | $p \Leftrightarrow q$ | $\mathrm{p} \backslash$ Leftrightarrow q |
| Implication | $p \Rightarrow q$ | $\mathrm{p} \backslash$ Rightarrow q |
| Not | $\neg p$ | $\backslash$ neg p |
| Or | $p \vee q$ | $\mathrm{p} \backslash$ vee q |
| Quantifiers | $\forall, \exists$ | $\backslash$ forall , \exists |

### 5.3 Set Symbols

| Description | Example | $\mathbf{I A}_{\mathbf{E} X} \mathbf{X}$ Code |
| :---: | :---: | :---: |
| Blackboard Style | $\mathbb{N}$ | $\backslash$ mathbb\{N\} |
| Difference | $A \backslash B$ | $\mathrm{~A} \backslash$ setminus B |
| Element Of | $x \in A$ | $\mathrm{x} \backslash$ in A |
| Empty Set | $\varnothing$ | $\backslash$ varnothing |
| Intersection | $A \cap B$ | $\mathrm{~A} \backslash$ cap B |
| Not Element Of | $x \notin A$ | $\mathrm{x} \backslash$ not $\backslash$ in A |
| Subset | $A \subseteq B$ | $\mathrm{~A} \backslash$ subseteq B |
| Superset | $B \supseteq A$ | $\mathrm{~B} \backslash$ supseteq A |
| Union | $A \cup B$ | $\mathrm{~A} \backslash$ cup B |

### 5.4 Sequences, Summations, and Products

| Description | Example | $\mathbf{E A T}_{\mathbf{E} X}$ Code |
| :---: | :---: | :---: |
| Centered Ellipses | $1+2+\cdots+n$ | $1+2+\backslash$ cdots +n |
| Ellipses | $1,2, \ldots, n$ | $1,2, \backslash$ dots, n |
| Product | $\prod_{k=0}^{n} k^{2}$ | $\backslash$ prod_ $\{\mathrm{k}=0\}^{\wedge}\{\mathrm{n}\}\left\{\mathrm{k}^{\wedge} 2\right\}$ |
| Summation | $\sum_{k=0}^{n} k^{2}$ | $\backslash \operatorname{sum}_{-}\{\mathrm{k}=0\}^{\wedge}\{\mathrm{n}\}\left\{\mathrm{k}^{\wedge} 2\right\}$ |

### 5.5 Text Styles

| Description | Example | $\mathrm{LA}^{\text {T }}$ E X Code |
| :---: | :---: | :---: |
| Blackboard Style | $\mathbb{N}$ | $\backslash$ mathbb \{N\} |
| Bold | OMG | \textbf \{0MG\} |
| Code | int counter | \texttt\{int counter\} |
| Italics | $O M G$ | \emph \{0MG\} |
| Script Style | $\mathcal{R}$ | $\backslash$ mathcal $\{\mathrm{R}\}$ |
| Truth Values | T, F | \textsf\{T\}, \textsf\{F\} |

### 5.6 Piecewise Functions

```
$$\text{abs}(x) =
    \begin{cases}
    x & \text{if $x \geq 0$}\\
    -x & \text{if $x < 0$}
    \end{cases}$$
```

$$
\operatorname{abs}(x)= \begin{cases}x & \text { if } x \geq 0 \\ -x & \text { if } x<0\end{cases}
$$

### 5.7 Still Can't Find It?

There is a great tool online called detexify. You draw the symbol you are looking for, and it gives you the LATEX command that it thinks most closely represents it. You can find it at http: //detexify.kirelabs.org/classify.html.

## 6 Some Useful Environments

## 6．1 Centering Text

| begin\｛center\} [〈options $\rangle]$ 〈environment contents〉 \end\｛center\} |
| :--- |
| This environment is used for centering a section of your document． <br> lbegin\｛center\} <br> This text is centered．I am a silly example．$\backslash \backslash$ <br> She sells sea shells by the sea shore． <br> \end\｛center\} <br> This text is centered．I am a silly example． <br> She sells sea shells by the sea shore． |

## 6．2 Tables

|  |  |  |  |
| :---: | :---: | :---: | :---: |
| options usage |  |  |  |
| column horizonatal alignment c，l，r separated by｜for grid lines |  |  |  |
| This environment nicely typesets tables．It allows you to choose where（and if）you want grid lines in your table． |  |  |  |
| ```\begin{tabular}{1\|c|r} First Column & Second Column & Third Column\\ \hline Cell 1,0 & Cell 1,1 & Cell 1,2\\ Cell 2,0 & Cell 2,1 & Cell 2,2 \end{tabular}``` |  |  |  |
| First Column | Second Column | Third Column |  |
| Cell 1，0 | Cell 1，1 | Cell 1，2 |  |
| Cell 2，0 | Cell 2，1 | Cell 2，2 |  |

## 6．3 Math Align

```
\begin\{align*\}[〈options〉] 〈environment contents〉ไend\{align*\} }
This environment allows you to write out aligned columns of text and math．It is particularly useful for writing out proofs with justifications to the right．Note the＊on the end of the name．Also note that each row of the align＊can have an arbitrary number of \(\mathcal{\xi}\) signs which are alignment points．
```

```
\begin{align*}
```

$$
\begin{align*}
\neg ((p \vee \neg q) \vee (q \vee \neg p)) \iff & (\neg p \wedge q)
\neg ((p \vee \neg q) \vee (q \vee \neg p)) \iff & (\neg p \wedge q)
    \wedge (\neg q \wedge p) && \text{[DeMorgan's Laws]} \\
    \wedge (\neg q \wedge p) && \text{[DeMorgan's Laws]} \\
\iff & \neg p \wedge p \wedge \neg q \wedge q && \text{[Associativity and Commutativity]}\\
\iff & \neg p \wedge p \wedge \neg q \wedge q && \text{[Associativity and Commutativity]}\\
\iff & \textsf{F} && \text{[Any value of $p$ will lead to $\textsf{F}$]}
\iff & \textsf{F} && \text{[Any value of $p$ will lead to $\textsf{F}$]}
\end{align*}
$$

```
\end{align*}
```

$$
\begin{aligned}
\neg((p \vee \neg q) \vee(q \vee \neg p)) & \Longleftrightarrow(\neg p \wedge q) \wedge(\neg q \wedge p) & & \text { [DeMorgan's Laws] } \\
& \Longleftrightarrow \neg p \wedge p \wedge \neg q \wedge q & & \text { [Associativity and Commutativity] } \\
& \Longleftrightarrow \mathrm{F} & & \text { [Any value of } p \text { will lead to } \mathrm{F} \text { ] }
\end{aligned}
$$

## 6.4 a，b，c，1，2， 3

|  |  |  |  |
| :---: | :---: | :---: | :---: |
| options | default | usage |  |
| item display | 1. | Use this argument to change You can use 1，i，a，etc． | e appearance of the item． |

This environment allows you to typeset numbered or lettered lists．Make sure to use enumerate\}ifyouwanttochangethelookoftheitemdisplay.undefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefinedundefined

```
\usepackage{enumerate} %Put this line at the beginning of your document
\begin{enumerate}[(a)]
\item This is the first item.
\item This is the second item.
\item This is the third item.
\end{enumerate}
```

（a）This is the first item．
（b）This is the second item．
（c）This is the third item．

## 6．5 Bullet Points

## $\backslash$ begin\｛itemize\}[\{options $\rangle$ ］〈environment contents $\rangle$ \end\｛itemize\}

This environment allows you to typeset bullet pointed lists．

```
\begin{itemize}
\item This is the first item.
\item This is the second item.
\item This is the third item.
\end{itemize}
```

－This is the first item．
－This is the second item．
－This is the third item．

## 6．6 Custom Lists

## \begin\｛description\}[〈options〉] 〈environment contents〉 \end\{description\} 

}This environment allows you to typeset lists with completely custom items displays．This is really nice for induction proofs．
\begin\｛description\}
- ［First Item．］This is the first item．
- ［Second Item．］This is the second item．
- ［Third Item．］This is the third item．
\end\｛description\}
First Item．This is the first item．
Second Item．This is the second item．
Third Item．This is the third item．


## 6．7 Matrices

| begin\｛bbmatrix\} $[\langle$ options $\rangle]$ | environment contents $\rangle \backslash$ end\｛bbmatrix\} |
| :--- | :--- | :--- |

This environment allows you to typeset matrices．Note that the matrix must be in math mode！
$\$ \backslash$ begin $\{$ bmatrix $\}$
$1 \& 2$ \＆3<br>
4 \＆ 5 \＆ $6 \backslash \backslash 7 \& 8 \& 9$
\end\｛bmatrix\}\$
$\left[\begin{array}{lll}1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9\end{array}\right]$

## 6．8 Code and WYSIWYG

```
\begin\{verbatim\}[〈options〉] 〈environment contents〉\end\{verbatim\} }
This environment allows you to typeset words in a WYSIWYG fashion．Note that it will ignore all tabs，so you will want to use spaces instead．
\begin\{verbatim\} }
    I want this text
        to look
            exactly as I put it.
def hello():
        return "Goodbye"
\end\{verbatim\} }
        I want this text
        to look
            exactly as I put it.
def hello():
        return "Goodbye"
```


## 7 Using the Homework Template



## \begin\｛part\}[〈options $\rangle$ ］〈environment contents〉 \end\｛part\}

You should use this environment to surround the individual parts of questions we assign you．
\begin\｛question\}\{This is a test question\}
\begin\｛part\}
This is the solution to the first part
\end\｛part\}
\begin\｛part\}
This is a solution to the second part
\end\｛part\}
\end\｛question\}

## 1：This is a test question

（a）This is the solution to the first part
（b）This is a solution to the second part

We complete this tutorial with a real-world example:

```
\begin{question}{Little Gauss' Formula}
    \begin{part}
    We use small examples to attempt to derive a formula for the sum of
    first $n$ numbers. Listing out the first few examples, we see the
    following:
    \begin{center}
    \begin{tabular}{|c|r|c|}
            \hline
            $n$ & \multicolumn{2}{c|}{Sum} \\\hline
            O & 0 & 0\\\hline
            1 & $0+1$ & 1\\\hline
            2 & $0+1+2$ & 3\\\hline
            3 & $0+1+2+3$ & 6\\\hline
            4 & $0+1+2+3+4$ & 10\\\hline
        \end{tabular}
        \end{center}
        Clearly, this increases more quickly than a linear function; so,
        we guess that it might be quadratic. A function that matches
        these values and is quadratic is $\frac{n(n+1)}{2}$. That is,
        we guess that the following equation holds:
        $$\sum_{i=0}^{n}{i} = \frac{n(n+1)}{2}$$
    \end{part}
    \begin{part}
        Now, we prove the equality using induction as follows:
        \begin{description}
            \item[Base Case.] $n=0$: $0 = \frac{0(1)}{2}=0$.
            \item[Induction Hypothesis.] Assume the equality holds for some
                $k \geq 0$.
            \item[Induction Step.] For $n=k+1$, we have
                $$\sum_{i=1}^{k+1} i = (k+1) + \sum_{i=1}^{k}{i}$$
                Using the induction hypothesis, we can substitute for the
                second term on the right-hand side:
                \begin{eqnarray*}
                    \sum_{i=1}^{k+1}{i} &=& (k+1) + \frac{k(k+1)}{2}\\
                                    &=& \frac{2k+2 + k(k+1)}{2}\\
                                    &=& \frac{k^2 + 3k + 2}{2}\\
                                    &=& \frac{(k+1)(k+2)}{2}
                \end{eqnarray*}
            \end{description}
            The last line shows that when $n=k+1$, the equality that we guessed
            holds. Since we proved the base case, and we've shown that if it
            holds for $n=k$ it must hold for $n=k+1$, it must hold for all $n$.
    \end{part}
\end{question}
```


## 2: Little Gauss' Formula

(a) We use small examples to attempt to derive a formula for the sum of first $n$ numbers. Listing out the first few examples, we see the following:

| $n$ | Sum |  |
| ---: | ---: | :---: |
| 0 | 0 | 0 |
| 1 | $0+1$ | 1 |
| 2 | $0+1+2+3$ | 3 |
| 3 | 6 |  |
| 4 | $0+1+2+3+4$ | 10 |

Clearly, this increases more quickly than a linear function; so, we guess that it might be quadratic. A function that matches these values and is quadratic is $\frac{n(n+1)}{2}$. That is, we guess that the following equation holds:

$$
\sum_{i=0}^{n} i=\frac{n(n+1)}{2}
$$

(b) Now, we prove the equality using induction as follows:

Base Case. $n=0: 0=\frac{0(1)}{2}=0$.
Induction Hypothesis. Assume the equality holds for some $k \geq 0$.
Induction Step. For $n=k+1$, we have

$$
\sum_{i=1}^{k+1} i=(k+1)+\sum_{i=1}^{k} i
$$

Using the induction hypothesis, we can substitute for the second term on the right-hand side:

$$
\begin{aligned}
\sum_{i=1}^{k+1} i & =(k+1)+\frac{k(k+1)}{2} \\
& =\frac{2 k+2+k(k+1)}{2} \\
& =\frac{k^{2}+3 k+2}{2} \\
& =\frac{(k+1)(k+2)}{2}
\end{aligned}
$$

The last line shows that when $n=k+1$, the equality that we guessed holds. Since we proved the base case, and we've shown that if it holds for $n=k$ it must hold for $n=k+1$, it must hold for all $n$.


[^0]:    1 The $\mathrm{AT}_{\mathrm{E}} \mathrm{X}$ purist might yell at me here. Using $\$ \$$ is not actually the accepted way to enter and leave display mode. It is in fact deprecated, and, instead, you can delimit it by using $\backslash[$ and $\backslash]$.
    2 It is worthy of note that $\mathrm{H} \$ 2 \$$ SO\$_ $4 \$$ would also work, but text is also useful in other places.

