

Semantics and First-Order Predicate Calculus

11-711 Algorithms for NLP

17 November 2016

(With thanks to Noah Smith)

Key Challenge of Meaning

- We actually say very little - much more is left unsaid, because it's assumed to be widely known.
- Examples:
 - Reading newspaper stories
 - Using restaurant menus
 - Learning to use a new piece of software

Meaning Representation Languages

- Symbolic representation that does two jobs:
 - Conveys the meaning of a **sentence**
 - Represents (some part of) the **world**
- We're assuming a very literal, context-independent, inference-free version of meaning!
 - Semantics vs. linguists' "pragmatics"
 - "Meaning representation" vs some philosophers' use of the term "semantics".
- Today we'll use **first-order logic**. Also called First-Order Predicate Calculus. Logical form.

A MRL Should Be Able To ...

- Verify a query against a knowledge base: *Do CMU students follow politics?*
- Eliminate ambiguity: *CMU students enjoy visiting Senators.*
- Cope with vagueness: *Sally heard the news.*
- Cope with many ways of expressing the same meaning (canonical forms): *The candidate evaded the question vs. The question was evaded by the candidate.*
- Draw conclusions based on the knowledge base: *Who could become the 45th president?*
- Represent all of the meanings we care about

Model-Theoretic Semantics

- Model: a simplified representation of (some part of) the world: objects, properties, relations (**domain**).
- Non-logical vocabulary
 - Each element **denotes** (maps to) a well-defined part of the model
 - Such a mapping is called an **interpretation**

A Model

- **Domain:** Noah, Karen, Rebecca, Frederick, Green Mango, Casbah, Udipi, Thai, Mediterranean, Indian
- **Properties:** Green Mango and Udipi are crowded; Casbah is expensive
- **Relations:** Karen likes Green Mango, Frederick likes Casbah, everyone likes Udipi, Green Mango serves Thai, Casbah serves Mediterranean, and Udipi serves Indian
- $n, k, r, f, g, c, u, t, m, i$
- **Crowded** = $\{g, u\}$
- **Expensive** = $\{c\}$
- **Likes** = $\{(k, g), (f, c), (n, u), (k, u), (r, u), (f, u)\}$
- **Serves** = $\{(g, t), (c, m), (u, i)\}$

Some English

- Karen likes Green Mango and Frederick likes Casbah.
- Noah and Rebecca like the same restaurants.
- Noah likes expensive restaurants.
- Not everybody likes Green Mango.

- What we want is to be able to represent these statements in a way that lets us compare them to our model.
- **Truth-conditional semantics:** need operators and their meanings, given a particular model.

First-Order Logic

- **Terms** refer to elements of the domain: **constants**, **functions**, and **variables**
 - Noah, SpouseOf(Karen), X
- **Predicates** are used to refer to sets and relations; predicate applied to a term is a **Proposition**
 - Expensive(Casbah)
 - Serves(Casbah, Mediterranean)
- Logical connectives (**operators**):
 - \wedge (and), \vee (or), \neg (not), \Rightarrow (implies), ...
- **Quantifiers** ...

Quantifiers in FOL

- Two ways to use variables:
 - refer to one anonymous object from the domain (**existential**; \exists ; “there exists”)
 - refer to all objects in the domain (**universal**; \forall ; “for all”)
- A restaurant near CMU serves Indian food
 $\exists x \text{ Restaurant}(x) \wedge \text{Near}(x, \text{CMU}) \wedge \text{Serves}(x, \text{Indian})$
- All expensive restaurants are far from campus
 $\forall x \text{ Restaurant}(x) \wedge \text{Expensive}(x) \Rightarrow \neg \text{Near}(x, \text{CMU})$

Inference

- Big idea: extend the knowledge base, or check some proposition against the knowledge base.
- **Forward chaining** with modus ponens: given α and $\alpha \Rightarrow \beta$, we know β .
- **Backward chaining** takes a query β and looks for propositions α and $\alpha \Rightarrow \beta$ that would prove β .
 - Not the same as backward reasoning (*abduction*).
 - Used by Prolog
- Both are sound, neither is complete by itself.

Inference example

- Starting with these facts:

Restaurant(Udipi)

$\forall x \text{ Restaurant}(x) \Rightarrow \text{Likes}(\text{Noah}, x)$

- We can “turn a crank” and get this *new* fact:

Likes(Noah, Udipi)

FOL: Meta-theory

- Well-defined set-theoretic semantics
- **Sound:** can't prove false things
- **Complete:** can prove everything that logically follows from a set of axioms (e.g., with “resolution theorem prover”)
- Well-behaved, well-understood
- Mission accomplished?

FOL: But there are also “Issues”

- “Meanings” of sentences are *truth values*.
- Only *first-order* (no quantifying over *predicates* [which the book does without comment]).
- Not very good for “*fluents*” (time-varying things, real-valued quantities, etc.)
- Brittle: *anything* follows from *any* contradiction(!)
- **Goedel incompleteness**: “This statement has no proof”!
 - (Finite axiom sets are incomplete w.r.t. the real world.)
- **So**: Most systems use its descriptive apparatus (with extensions) but not its inference mechanisms.

First-Order Worlds, Then and Now

- Interest in this topic (in NLP) waned during the 1990s and 2000s.
- It has come back, with the rise of semi-structured databases like Wikipedia.
 - Lay contributors to these databases may be helping us to solve the knowledge acquisition problem.
- Also, lots of research on using NLP, information extraction, and machine learning to grow and improve knowledge bases from free text data.
 - “Read the Web” project here at CMU.
- And: Semantic embedding/NN/vector approaches.

Lots More To Say About MRLs!

- See chapter 17 for more about:
 - Representing events and states in FOL
 - Dealing with optional arguments (e.g., “eat”)
 - Representing time
 - Non-FOL approaches to meaning

Connecting Syntax and Semantics

Semantic Analysis

- Goal: transform a NL statement into MRL (today, FOL).
- Sometimes called “semantic parsing.”
- As described earlier, this is the literal, context-independent, inference-free meaning of the statement

“Literal, context-independent, inference-free” semantics

- Example: *The ball is red*
- Assigning a specific, grounded meaning involves deciding *which* ball is meant
- Would have to resolve *indexical terms* including pronouns, normal NPs, etc.
- Logical form allows compact representation of such indexical terms (vs. listing all members of the set)
- To retrieve a specific meaning, we combine LF with a particular context or situation (set of objects and relations)
- So LF is a function that maps an initial discourse situation into a new discourse situation (from *situation semantics*)

Compositionality

- The meaning of an NL phrase is determined by combining the meaning of its sub-parts.
- There are obvious exceptions (“hot dog,” “straw man,” “New York,” etc.).
- Note: your book uses an event-based FOL representation, but I’m using a simpler one without events.
- Big idea: start with parse tree, build semantics on top using FOL with λ -expressions.

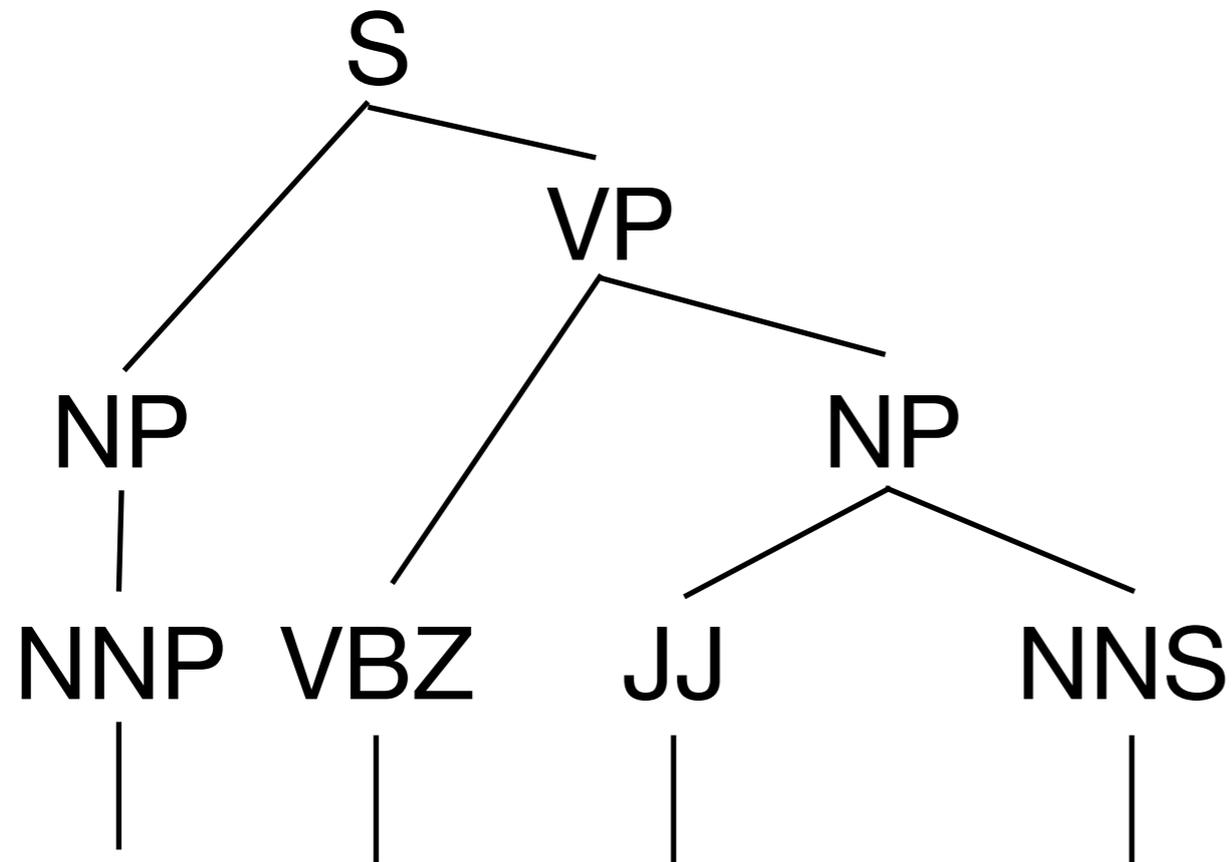
Extension: Lambda Notation

- A way of making anonymous functions.
- $\lambda x.$ (*some expression mentioning x*)
 - Example: $\lambda x.$ Near(x , CMU)
 - Trickier example: $\lambda x.$ $\lambda y.$ Serves(y , x)
- Lambda reduction: substitute for the variable.
 - $(\lambda x.$ Near(x , CMU))(LulusNoodles)
 - becomes
 - $\text{Near}(\text{LulusNoodles}, \text{CMU})$

Lambda reduction: order matters!

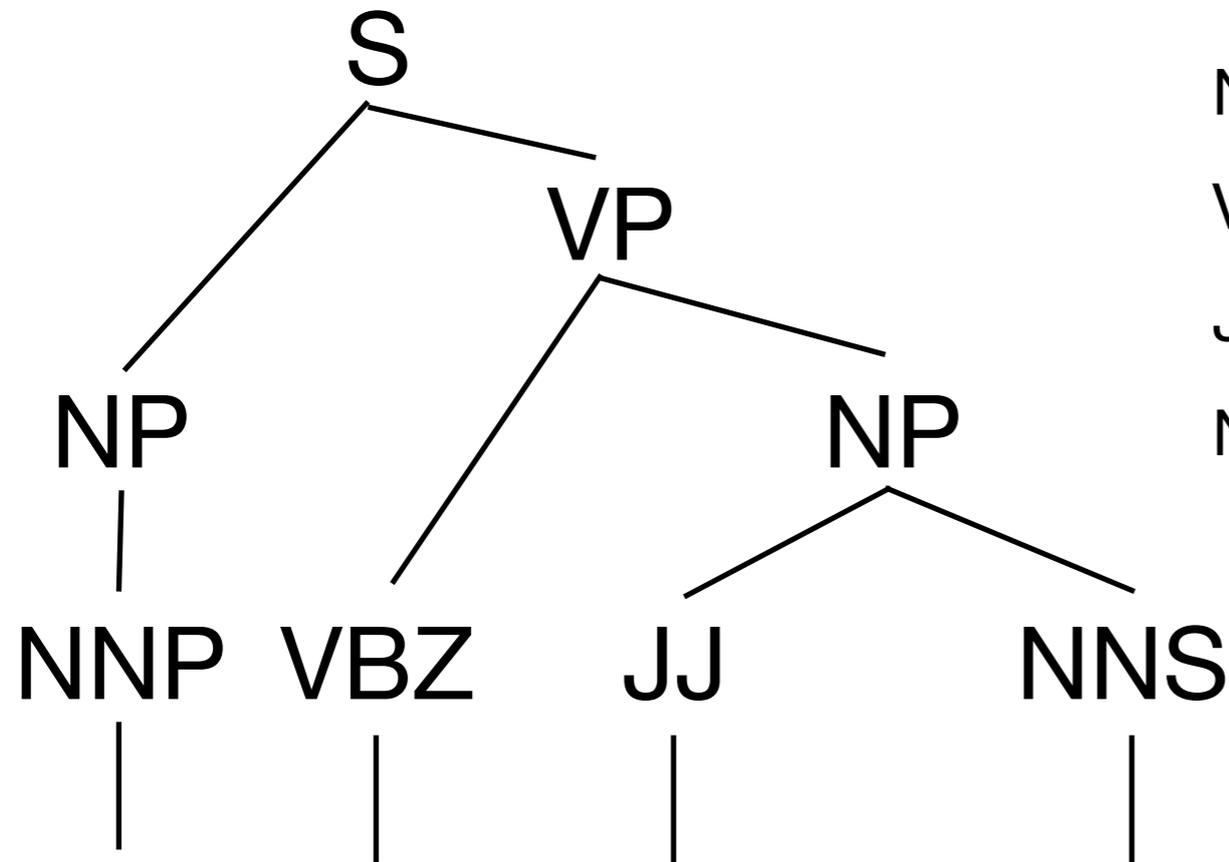
- $\lambda x.\lambda y.$ Serves(y, x) (Bill)(Jane) becomes $\lambda y.$ Serves(y, Bill)(Jane)
Then $\lambda y.$ Serves(y, Bill) (Jane) becomes Serves(Jane, Bill)
- $\lambda y.\lambda x.$ Serves(y, x) (Bill)(Jane) becomes $\lambda x.$ Serves(Bill, x)(Jane)
Then $\lambda x.$ Serves(Bill, x) (Jane) becomes Serves(Bill, Jane)

An Example



- Noah likes expensive restaurants.
- $\forall x \text{ Restaurant}(x) \wedge \text{Expensive}(x) \Rightarrow \text{Likes}(\text{Noah}, x)$

An Example



NNP \rightarrow Noah { Noah }

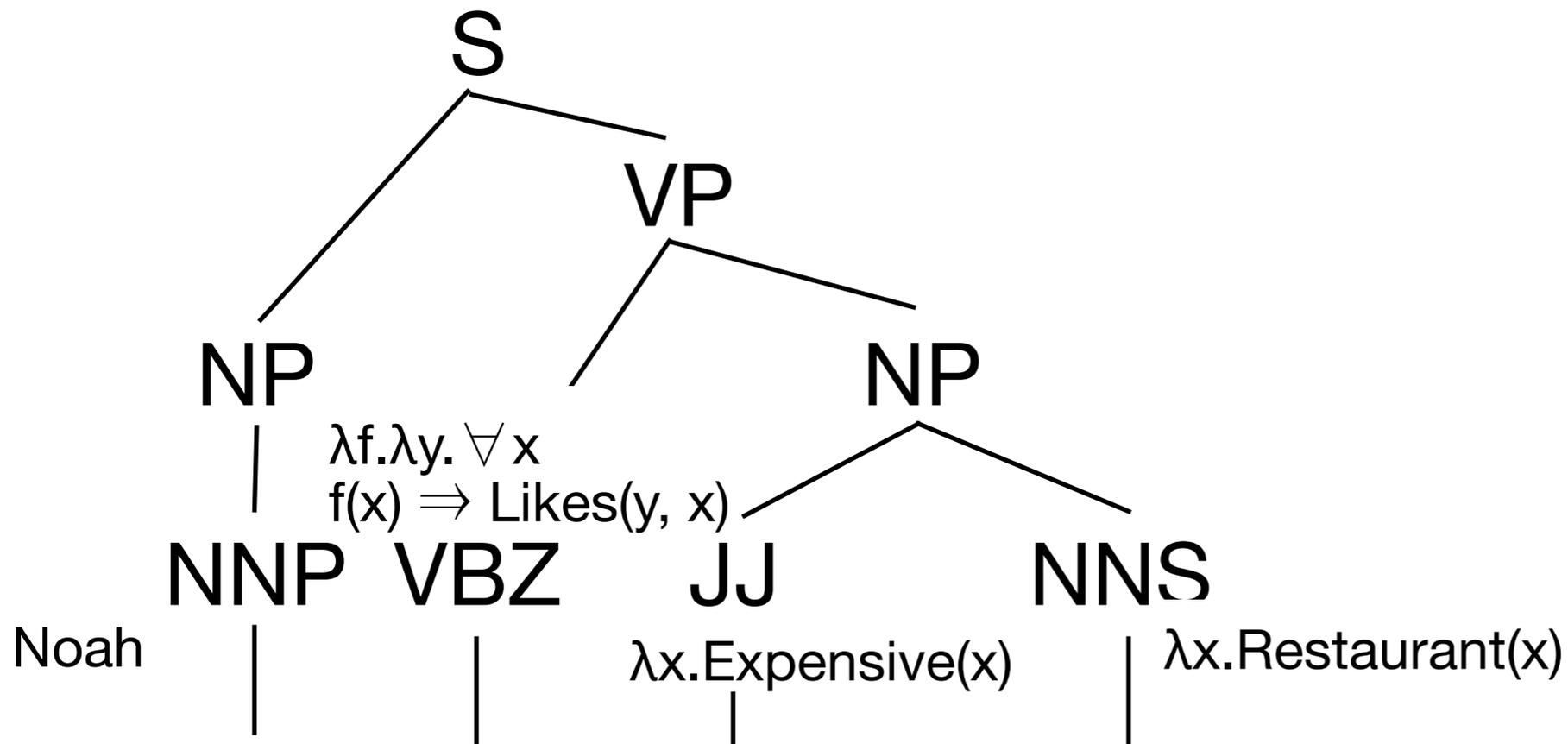
VBZ \rightarrow likes { $\lambda f.\lambda y.\forall x f(x) \Rightarrow \text{Likes}(y, x)$ }

JJ \rightarrow expensive { $\lambda x.\text{Expensive}(x)$ }

NNS \rightarrow restaurants { $\lambda x.\text{Restaurant}(x)$ }

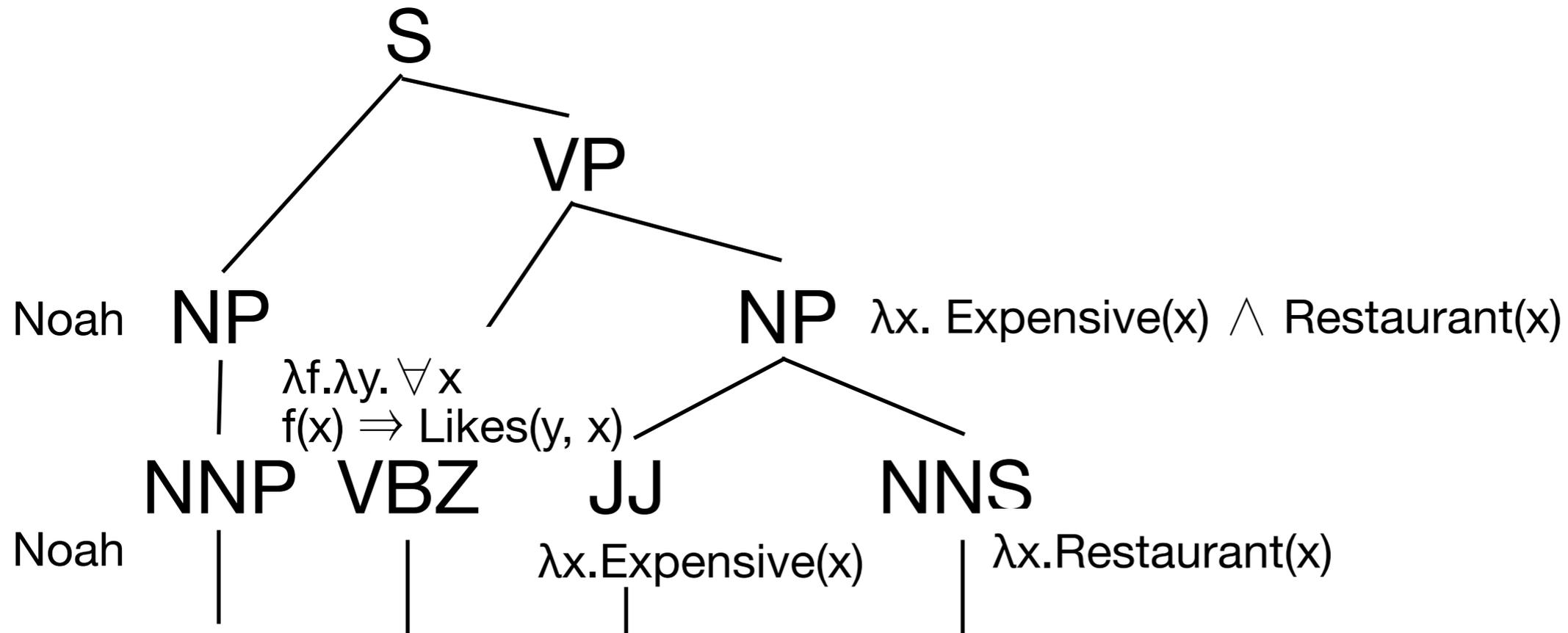
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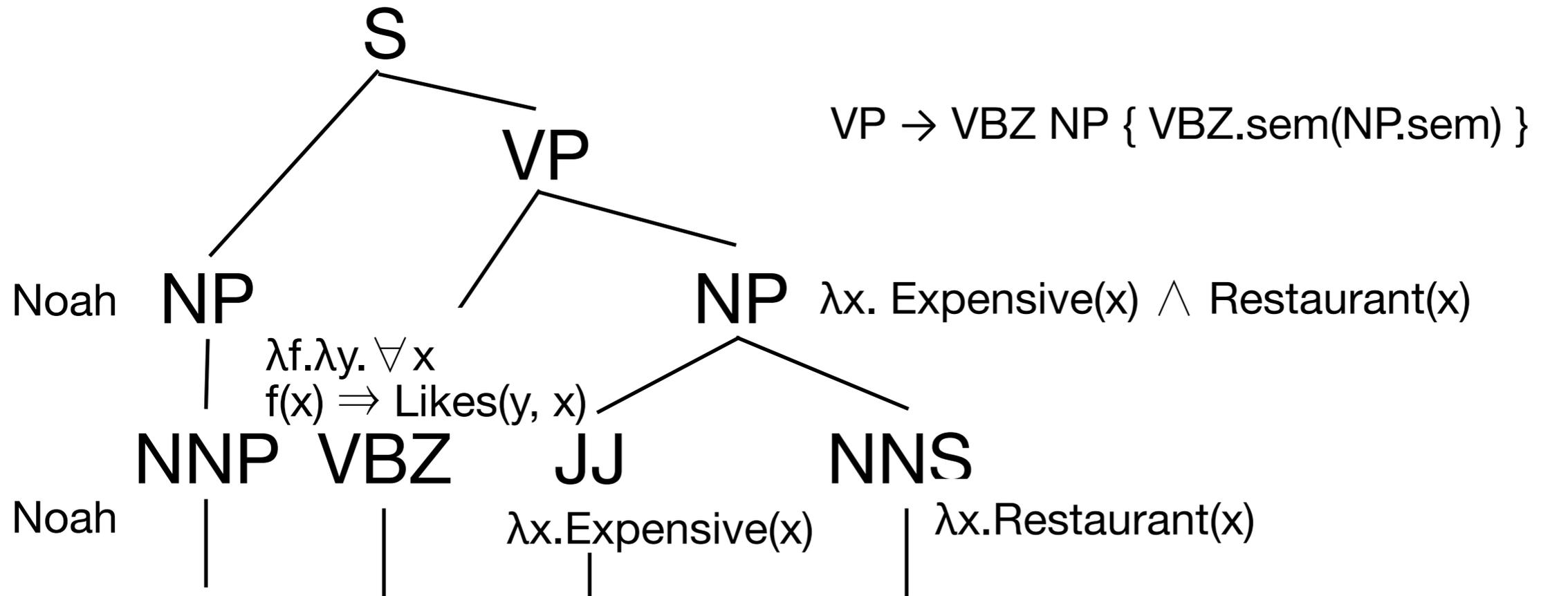
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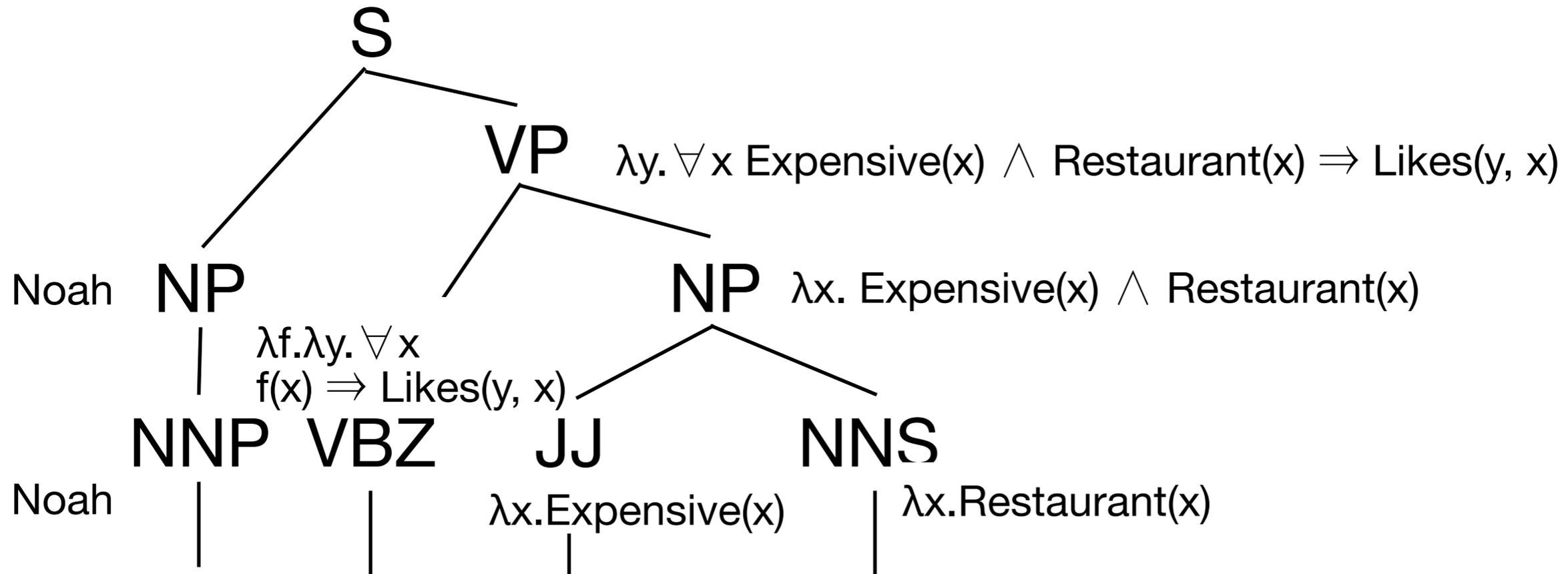
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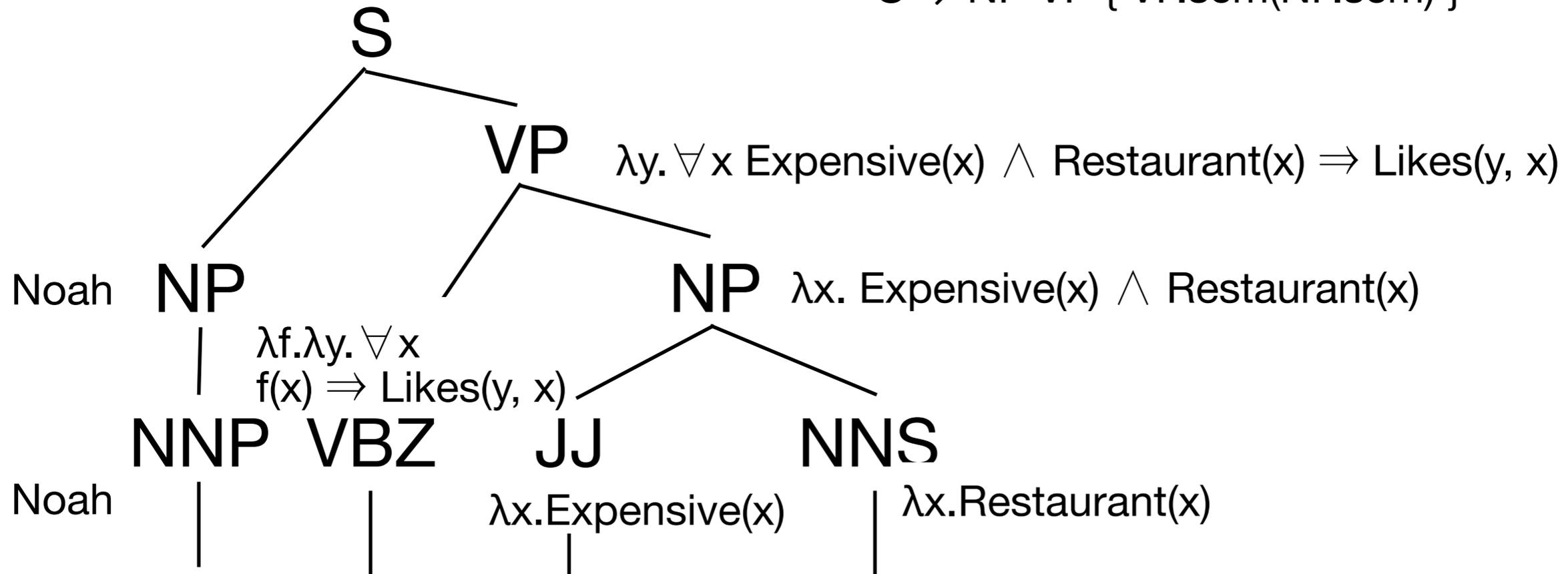
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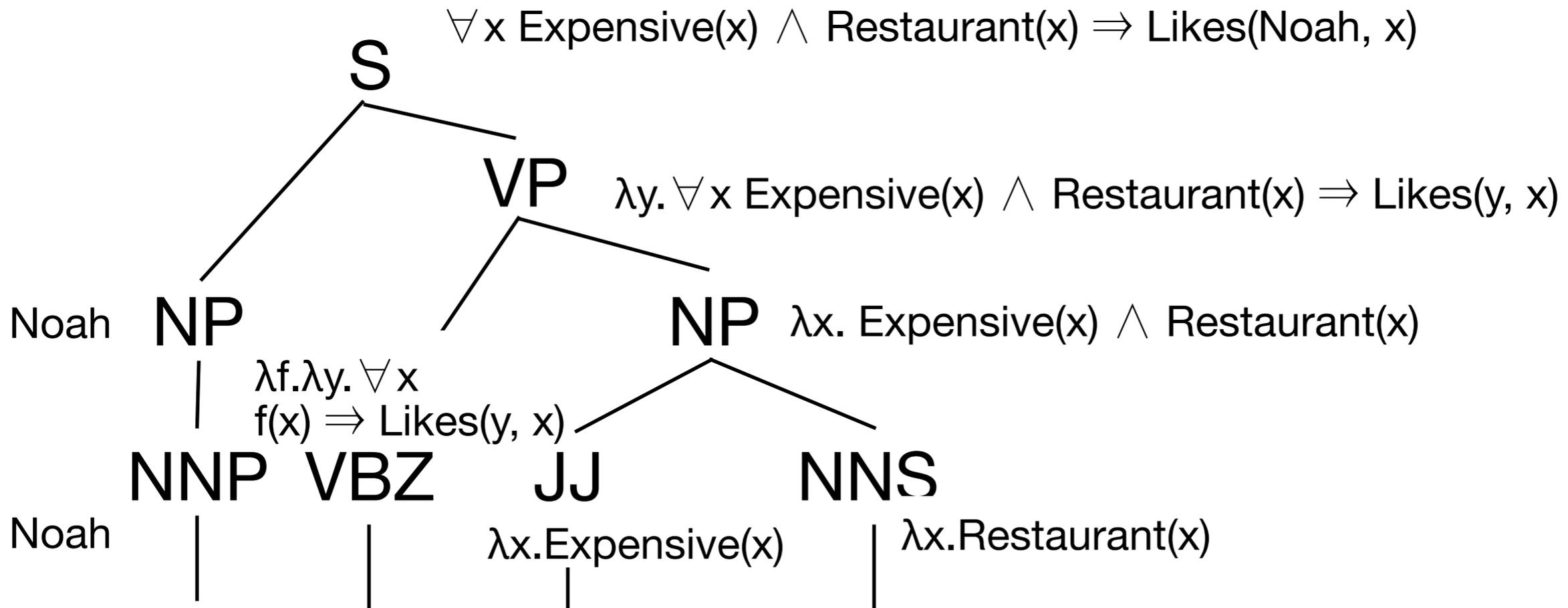
An Example

$S \rightarrow NP VP \{ VP.sem(NP.sem) \}$



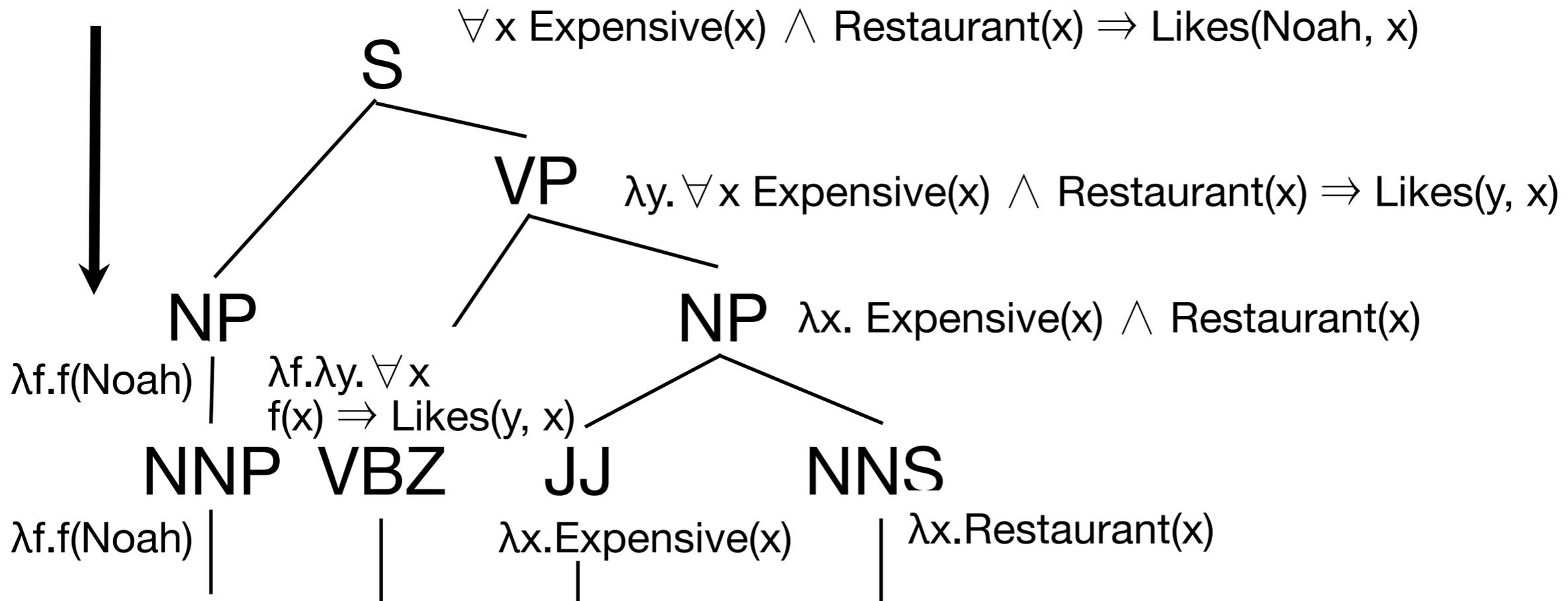
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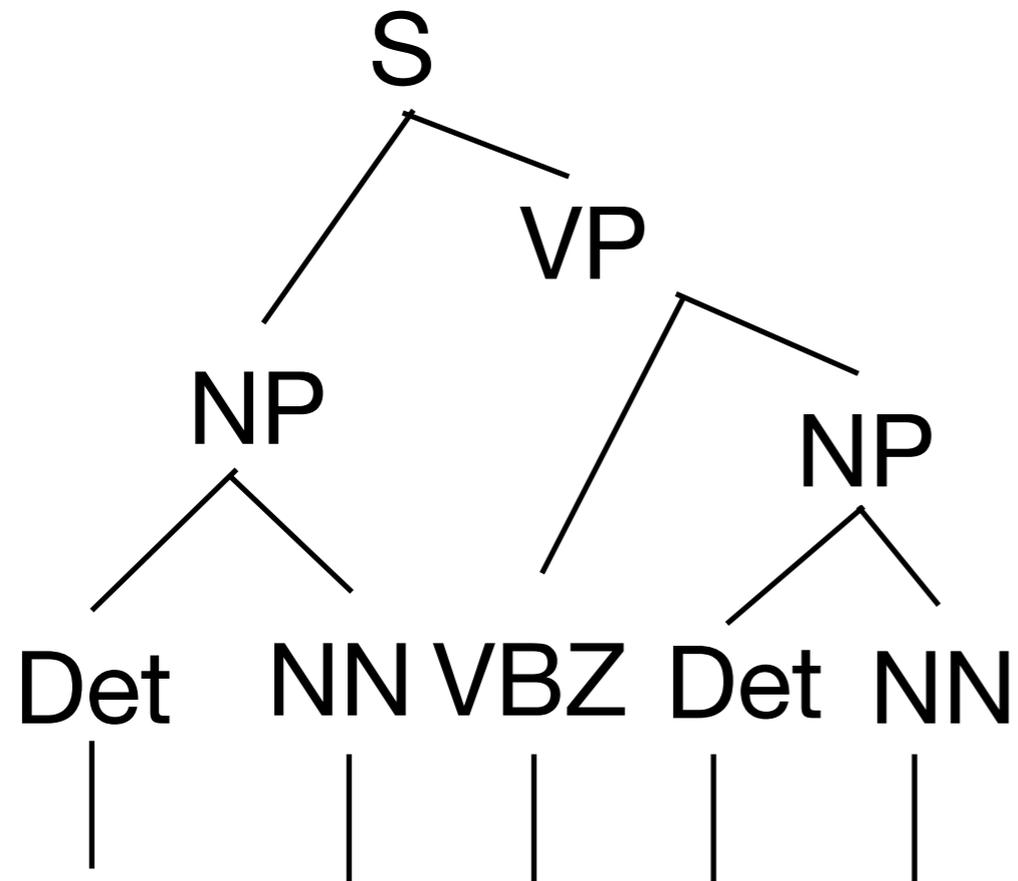
Alternative (Following *SLP*)



- Noah likes expensive restaurants.
- $\forall x \text{ Restaurant}(x) \wedge \text{Expensive}(x) \Rightarrow \text{Likes}(\text{Noah}, x)$

$S \rightarrow \text{NP VP } \{ \text{NP.sem}(\text{VP.sem}) \}$

Quantifier Scope Ambiguity



$S \rightarrow NP VP \{ NP.sem(VP.sem) \}$

$NP \rightarrow Det NN \{ Det.sem(NN.sem) \}$

$VP \rightarrow VBZ NP \{ VBZ.sem(NP.sem) \}$

$Det \rightarrow \text{every} \{ \lambda f.\lambda g.\forall u f(u) \Rightarrow g(u) \}$

$Det \rightarrow \text{a} \{ \lambda m.\lambda n.\exists x m(x) \wedge n(x) \}$

$NN \rightarrow \text{man} \{ \lambda v.Man(v) \}$

$NN \rightarrow \text{woman} \{ \lambda y.Woman(y) \}$

$VBZ \rightarrow \text{loves} \{ \lambda h.\lambda k.h(\lambda w.Loves(k, w)) \}$

- Every man loves a woman.
- $\forall u Man(u) \Rightarrow \exists x Woman(x) \wedge Loves(u, x)$

This Isn't Quite Right!

- “Every man loves a woman” really is ambiguous.
 - $\forall u \text{ Man}(u) \Rightarrow \exists x \text{ Woman}(x) \wedge \text{Loves}(u, x)$
 - $\exists x \text{ Woman}(x) \wedge \forall u \text{ Man}(u) \Rightarrow \text{Loves}(u, x)$
- This gives only one of the two meanings.
 - Extra ambiguity on top of syntactic ambiguity
- One approach is to delay the quantifier processing until the end, then permit any ordering.

Quantifier Scope

- A seat was available for every customer.
- A toll-free number was available for every customer.
- A secretary called each director.
- A letter was sent to each customer.
- Every man loves a woman
 who works at the candy store.
- Every 5 minutes a man gets knocked down
 and he's not too happy about it.

What Else?

- Chapter 18 discusses how you can get this to work for other parts of English (e.g., prepositional phrases).
- Remember attribute-value structures for parsing with more complex things than simple symbols?
 - You can extend those with semantics as well.
- No time for ...
 - Statistical models for semantics
 - Parsing algorithms augmented with semantics
 - Handling idioms

Generalized Quantifiers

- In FOL, we only have universal and existential quantifiers
- One formal extension is type-restriction of the quantified variable: *Everyone likes Udipi*:

$\forall x \text{ Person}(x) \Rightarrow \text{Likes}(x, \text{Udipi})$ becomes

$\forall x | \text{Person}(x). \text{Likes}(x, \text{Udipi})$

- English and other languages have a much larger set of quantifiers: *all, some, most, many, a few, the, ...*
- These have the same *form* as the original FOL quantifiers with type restrictions:

$\langle \text{quant} \rangle \langle \text{var} \rangle | \langle \text{restriction} \rangle . \langle \text{body} \rangle$

Generalized Quantifier examples

- *Most dogs bark*

Most $x \mid \text{Dog}(x) . \text{Barks}(x)$

- *Most barking things are dogs*

Most $x \mid \text{Barks}(x) . \text{Dog}(x)$

- *The dog barks*

The $x \mid \text{Dog}(x) . \text{Barks}(x)$

- *The happy dog barks*

The $x \mid (\text{Happy}(x) \wedge \text{Dog}(x)) . \text{Barks}(x)$

- ***Interpretation*** and ***inference*** using these are harder...

Speech Acts

- ***Mood*** of a sentence indicates relation between speaker and the concept (proposition) defined by the LF
- There can be operators that represent these relations:
 - ASSERT: the proposition is proposed as a fact
 - YN-QUERY: the truth of the proposition is queried
 - COMMAND: the proposition describes a requested action
 - WH-QUERY: the proposition describes an object to be identified

ASSERT (Declarative mood)

- *The man eats a peach*

ASSERT(The x | Man(x) . (A y | Peach(y) . Eat(x,y)))

YN-QUERY (Interrogative mood)

- *Does the man eat a peach?*

YN-QUERY(The x | Man(x) . (A y | Peach(y) . Eat(x,y)))

COMMAND (Imperative mood)

- *Eat a peach, (man).*

COMMAND(A y | Peach(y) . Eat(*HEARER*,y))

WH-QUERY

- *What did the man eat?*

WH-QUERY(The x | Man(x) . (WH y | Thing(y) . Eat(x,y)))

- One of a whole set of new quantifiers for wh-questions:
 - *What*: WH x | Thing(x)
 - *Which dog*: WH x | Dog(x)
 - *Who*: WH x | Person(x)
 - *How many men*: HOW-MANY x | Man(x)

Other complications

- Relative clauses are propositions embedded in an NP
 - Restrictive versus non-restrictive: *the dog that barked all night* vs. *the dog, which barked all night*
- Modal verbs: non-transparency for truth of subordinate clause: *Sue thinks that John loves Sandy*
- Tense/Aspect
- Plurality
- Etc.