

15-745 Lecture 3

Basic Blocks
Local Opts
Control Flow Graphs

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Optimizations

- Register Allocation
- Common subexpression elimination
- Constant Propagation
- Copy propagation
- Dead-code elimination
- Loop optimizations
 - Hoisting
 - Induction variable elimination

Scope of Optimization

- Local
Within a basic block
- Global
Within a function, across basic blocks
- Interprocedural
The entire program, across functions and basic blocks.

Basic Blocks

- What is a basic block?
- How do we create basic blocks?
 - leaders
 - Other definitions of leaders

Local Opts: E.g., CSE

```

B5: t6   = 4*i
     x   = a[t6]
     t7   = 4 * i
     t8   = 4 * j
     t9   = a[t8]
     a[t7] = t9
     t10  = 4*j
     a[t10] = x
     jump B2
  
```

Local Opts: E.g., CSE

```

B5: t6   = 4*i           t8   = 4 * j
     x   = a[t6]         t9   = a[t8]
     t7   = 4 * i         a[t6] = t9
     t8   = 4 * j
     t9   = a[t8]
     a[t7] = t9
     t10  = 4*j
     a[t10] = x
     jump B2           a[t8] = x
                       jump B2
  
```

Dags & Stmtns

$a + a * (b - c) + (b - c) * d$

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Dags & Blocks

```

a = b + c;
b = a - d;
c = b + c;
d = a - d;
    
```

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Dags & Blocks

```

a = b + c;
b = a - d;
c = b + c;
d = a - d;
    
```

- Must track assignments
- Must keep track of **time**

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Build a DAG

```

B5: t6 = 4*i
x = a[t6]
t7 = 4 * i
t8 = 4 * j
t9 = a[t8]
a[t7] = t9
t10 = 4*j
a[t10] = x
jump B2
    
```

- For each var & constant not seen before create a leaf
- For each op, create a node and label with lvalue

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Build a DAG

```

B5: t6 = 4*i
x = a[t6]
t7 = 4 * i
t8 = 4 * j
t9 = a[t8]
a[t7] = t9
t10 = 4*j
a[t10] = x
jump B2
    
```

- For each var & constant not seen before create a leaf
- For each op, create a node and label with lvalue

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Build a DAG

```

B5: t6 = 4*i
x = a[t6]
t7 = 4 * i
t8 = 4 * j
t9 = a[t8]
a[t7] = t9
t10 = 4*j
a[t10] = x
jump B2
    
```

- If you have seen all rvalues before see if an interior node with same "op" and operands has already been created. If so, add a label.

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Build a DAG

```

B5: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
    t8 = 4 * j
    t9 = a[t8]
    a[t7] = t9
    t10 = 4*j
    a[t10] = x
    jump B2
    
```

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Build a DAG

```

B5: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
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    t9 = a[t8]
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    a[t10] = x
    jump B2
    
```

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Build a DAG

```

B5: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
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    t9 = a[t8]
    a[t7] = t9
    t10 = 4*j
    a[t10] = x
    jump B2
    
```

- Assigning to array or pointer "kills" all possible memory lvalues. (I.e., they can't get any more labels.)

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Memory References

```

x = a[i]
a[j] = y
z = a[i]
a[j] = y
    
```

Becomes:

```

x, z
a[j] = y
    
```

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Build a DAG

```

B5: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
    t8 = 4 * j
    t9 = a[t8]
    a[t7] = t9
    t10 = 4*j
    a[t10] = x
    jump B2
    
```

Assignment to an array creates a new node with children:

- index
- old value of array
- value assigned

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Build a DAG

```

B5: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
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    a[t10] = x
    jump B2
    
```

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Build a DAG

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```

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Other uses for DAGs

- Can determine those variables that *can* be live at end of a block.
- Can determine those variables that are live at start of block.

```

B8: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
    x = 4 * j
    t9 = a[x]
    ...
    
```

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Dead code too?

- Can determine those variables that *can* be live at end of a block.
- Can determine those variables that are live at start of block.

```

B8: t6 = 4*i
    x = a[t6]
    t7 = 4 * i
    x = 4 * j
    t9 = a[x]
    ...
    
```

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Using the DAG to recreate blocks

- Order of evaluation is any topological sort
- We pick a node. Assign it to ONE of the labels (hopefully one needed later in the program)
- If we end up with identifiers that are needed after this block, insert move statements.
- If a node has no identifiers, make up a new one.
- Caveats:
 - Procedure calls kill nodes
 - A[] = and *p = kill nodes

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Memory References

In general,

- No memory references may cross each other
- No instructions can move across a procedure call

```

x = a[i]
a[j] = y
z = a[i]
    
```

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Value Numbering

- Don't actually build DAG
- Track value of variable in time as a "value number"
- compute `valueOf(var)` and `valueOf(val, op, val)`
- Scan stmts: `d ← a op b`, computing
 - $a_n = \text{valueOf}(a)$
 - $b_n = \text{valueOf}(b)$
 - $op_n = \text{valueOf}(a_n, op, b_n)$
 - set $\text{valueOf}(d) = op_n$

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VN example

```

a = b + c;
b = a - d;
c = b + c;
d = a - d;
    
```

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VN uses

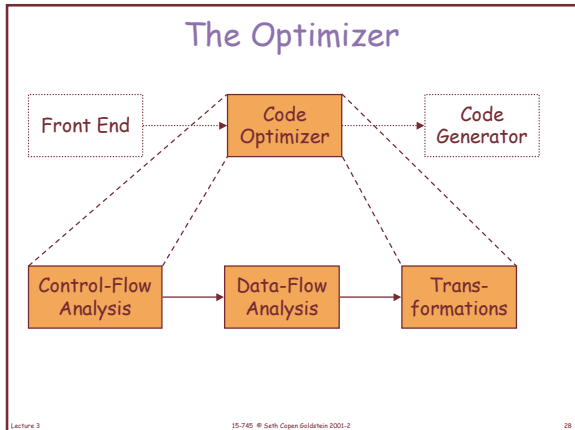
- Same as DAGs (live in, live out, CSE)
- How about constant folding?
 - a = 1
 - b = 2
 - c = a + b

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The entire program, across functions and basic blocks.

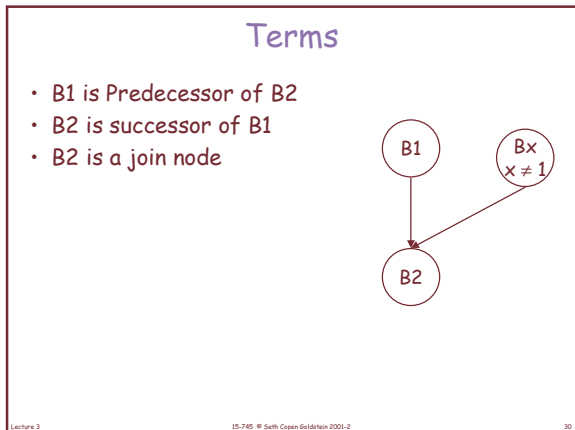
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Control Flow Graph

- Each BB is a node in the graph
- Distinguished nodes: Entry & Exit
- Edge between B1 & B2 iff
 - B2 can follow B1 in some execution of the program
 - B2 is a target of a jump/branch at end of B1
 - B2 follows B1 and B1 does not end with an unconditional jump
 - B1 is Entry and B2 is first instruction
 - B2 is Exit and B1 can exit procedure

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Unreachable Code Elimination

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Straightening

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