

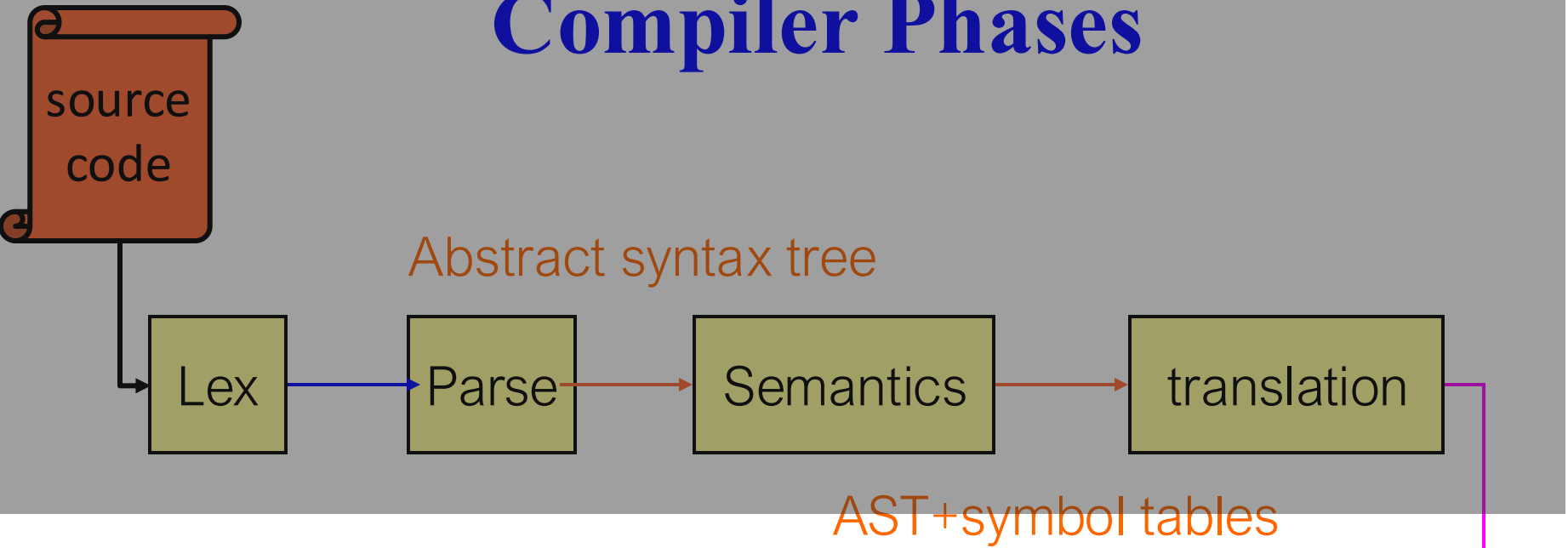
# **Functions: Calling Conventions + Frames**

**15-411/15-611 Compiler Design**

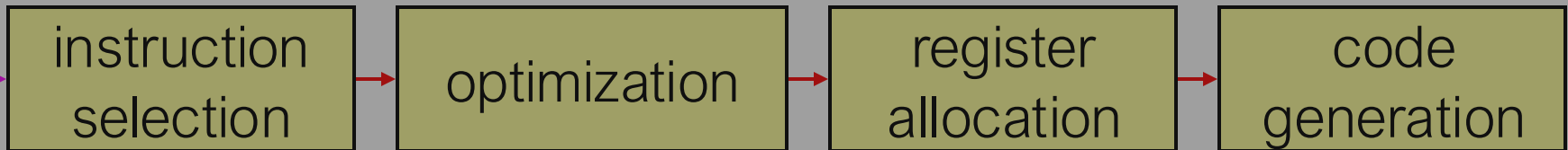
Seth Copen Goldstein

February 17, 2026

# Compiler Phases



## Intermediate Representation (tree)



## Code Triples

# Today

- Calling Conventions
- Activation Frames
- IR for Function Calls
- Putting it all together



# Lab3

- Function declarations and calls
- Typedefs
- assert

Understanding functions is the key.

# What is the role of a Function?

- Provides an independent namespace
  - Parameters
  - Local variables
- Binds a name to an executable sequence  
Can be invoked with a call
- Provides illusion of custom instruction  
Control continues after call
- Interface to rest of world
  
- Job of compiler is to create this abstraction from
  - A single PC
  - Byte addressed (single) memory space
  - Shared registers

# Function as Contract

- Contract between
  - Architects
  - Compiler writers
  - Operating System
- Supports Interoperability
- Separate Compilation
- Plug-n-Play

Most Important part of the contract is between  
callers and callees.

The abstraction of the function is the key.

# Benefits of “Function”

- Supports implementation and maintenance of large programs
  - Intellectual leverage (.e.g., decompose tasks)
  - Development efficiency  
(e.g., separate compilation)
- Supports cooperation of large independent systems  
(.e.g, O/S + Application)
- Supports Portability  
(e.g., libc)

# What is the role of a Function?

- Provides an independent namespace
  - Parameters
  - Local variables
- Binds a name to an executable sequence  
Can be invoked with a call
- **Provides illusion of custom instruction**  
Control continues after call
- Interface to rest of world
  
- Job of compiler is to create this abstraction from
  - A single PC
  - Byte addressed (single) memory space
  - Shared registers

Foo: instr1

Need to find code for bar

instr2 x,y,z

mov z,a

Bar: instr1 op1,op2

instr2 x,y,z

Abstraction supported by 3 mechanisms:

- Call instruction
- Activation Frame
- Calling Convention

add r3,r1,r2

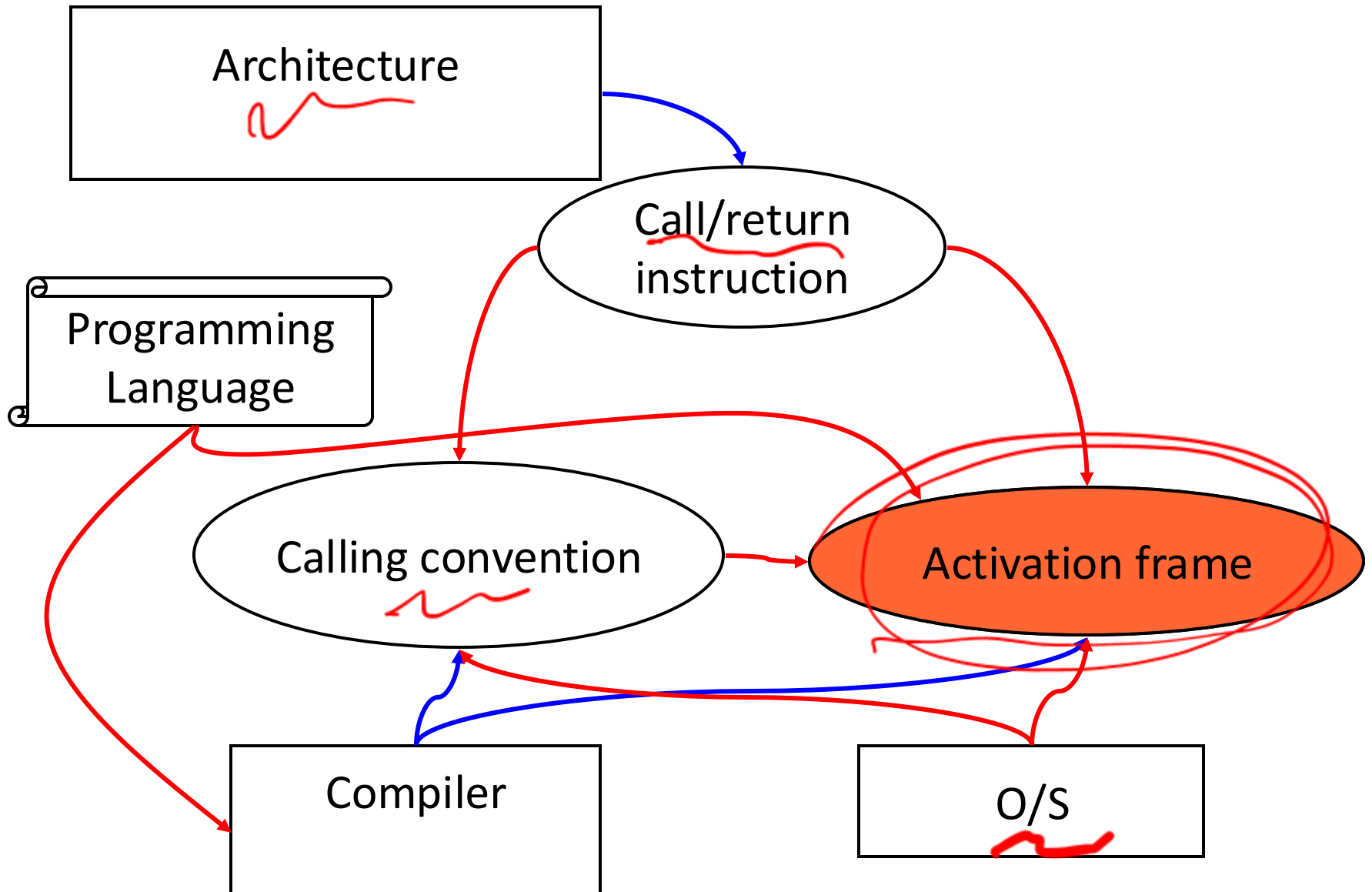
instr3

add r3,r1,r2

instr3

Need to resume Foo at correct place.

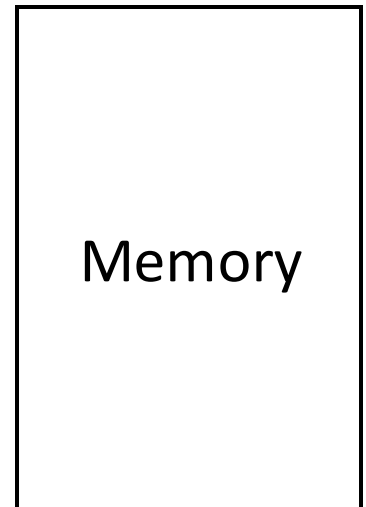
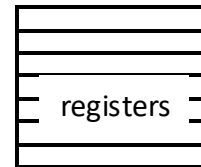
# Implementing the Function



# The Activation Frame

- Information to restore caller environment
  - Return address
  - registers
- Establishes local environment for function
  - Parameters
  - Locals
  - Temporaries
  - Dynamically allocated data?
- Support for non-locals?

PC

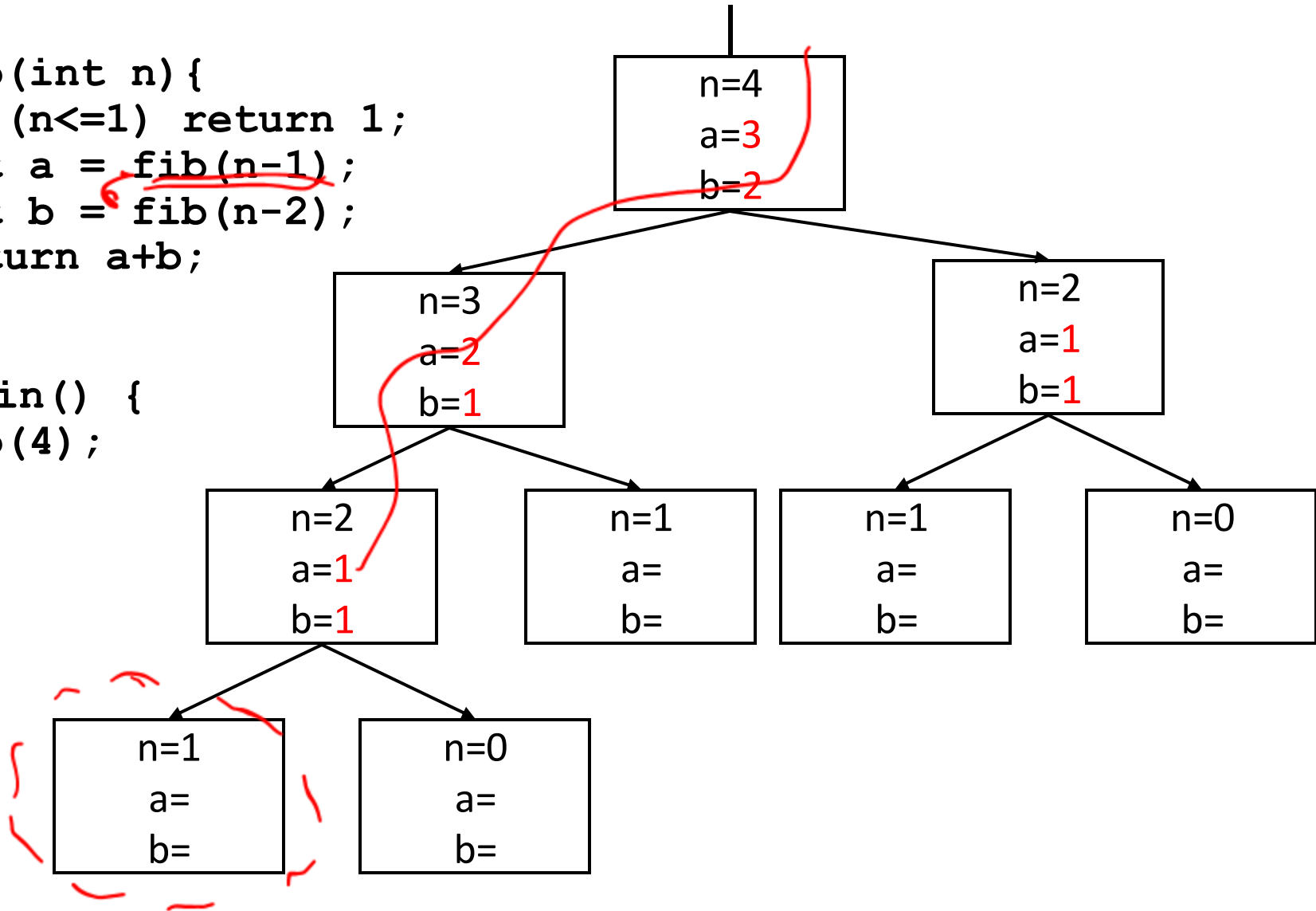


# Programming Language Issues

- Can functions be recursive?
- What is Parameter passing mechanism?
  - Call-by-name
  - Call-by-value
  - Call-by-reference
- Can (and how) are non-local names referenced?
- What happens to local variables on return from function?
- Can storage be allocated locally and dynamically in a function?
- Are functions first-class objects?

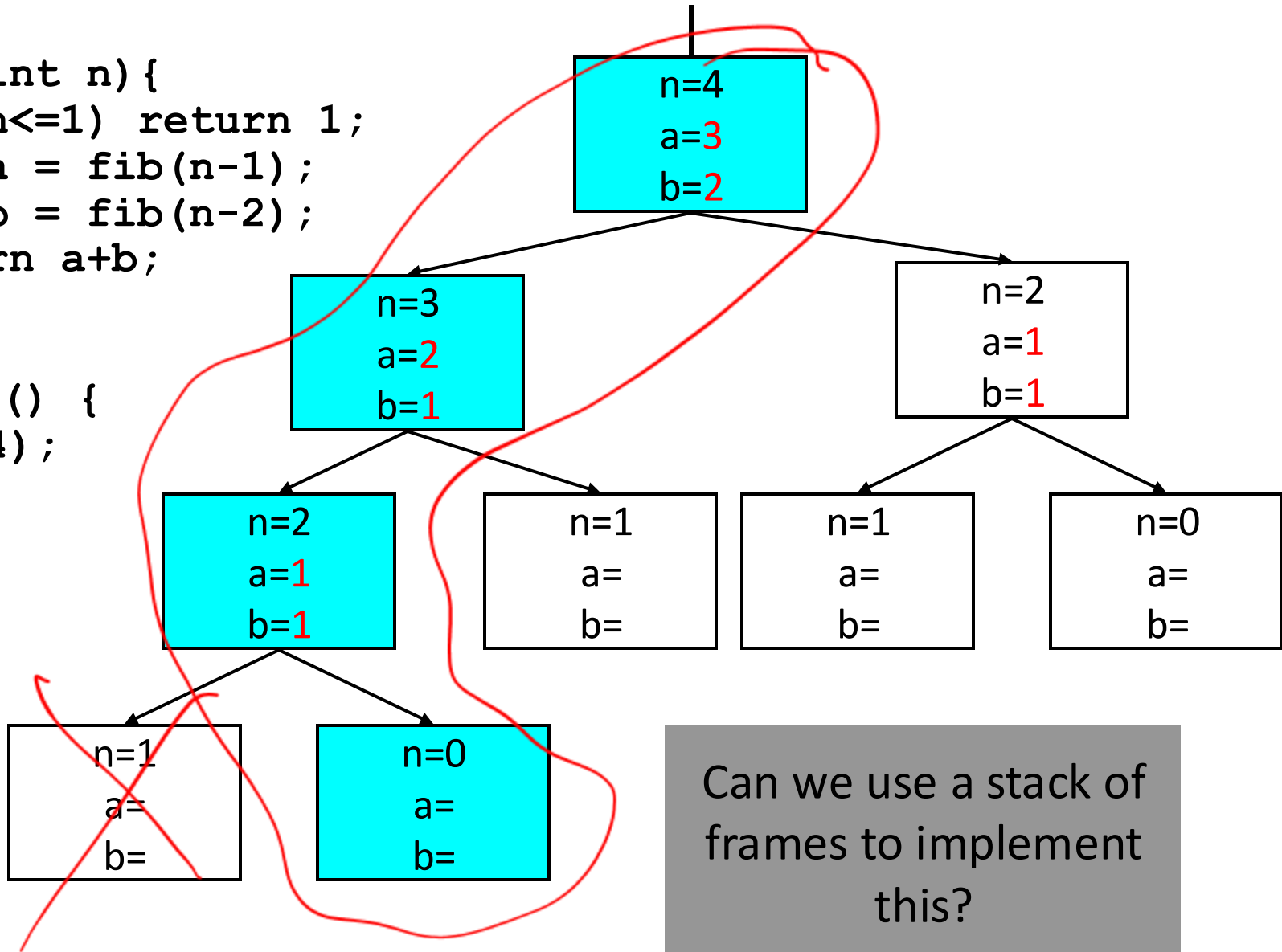
# An Activation Tree

```
int fib(int n) {  
    if (n<=1) return 1;  
    int a = fib(n-1);  
    int b = fib(n-2);  
    return a+b;  
}  
  
int main() {  
    fib(4);  
}
```



# A Control Path

```
int fib(int n) {  
    if (n<=1) return 1;  
    int a = fib(n-1);  
    int b = fib(n-2);  
    return a+b;  
}  
  
int main() {  
    fib(4);  
}
```

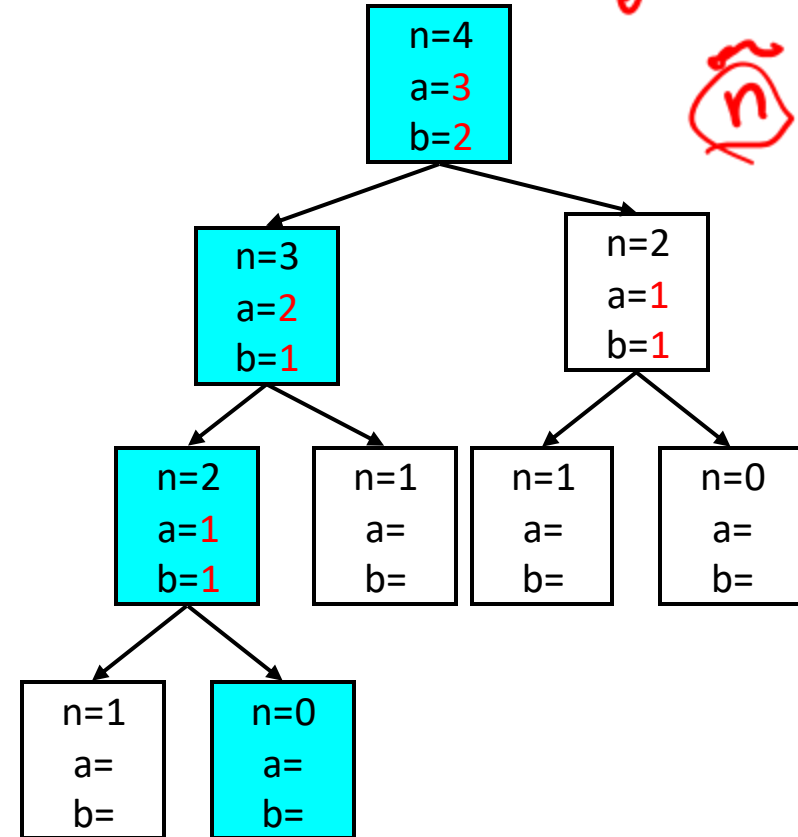


# Collection of Frames

*func() {  
  int n;  
  func(b);  
}*

*n*

- Can functions be recursive? **yes**
- What is Parameter passing mechanism?
  - Call-by-name
  - Call-by-value
  - Call-by-reference
- Can (and how) are non-local names referenced?
- What happens to local variables on return from function? **?**
- Can storage be allocated locally and dynamically in a function?
- Are functions first-class objects? **?**




# Returning references

- Can a function return a reference to a local variable?

- E.g.:

```
int* dangle() {  
    int a;  
    return &a;  
}
```



- If so, can we use a stack of frames?

# Returning Functions

- Can a function return a function?

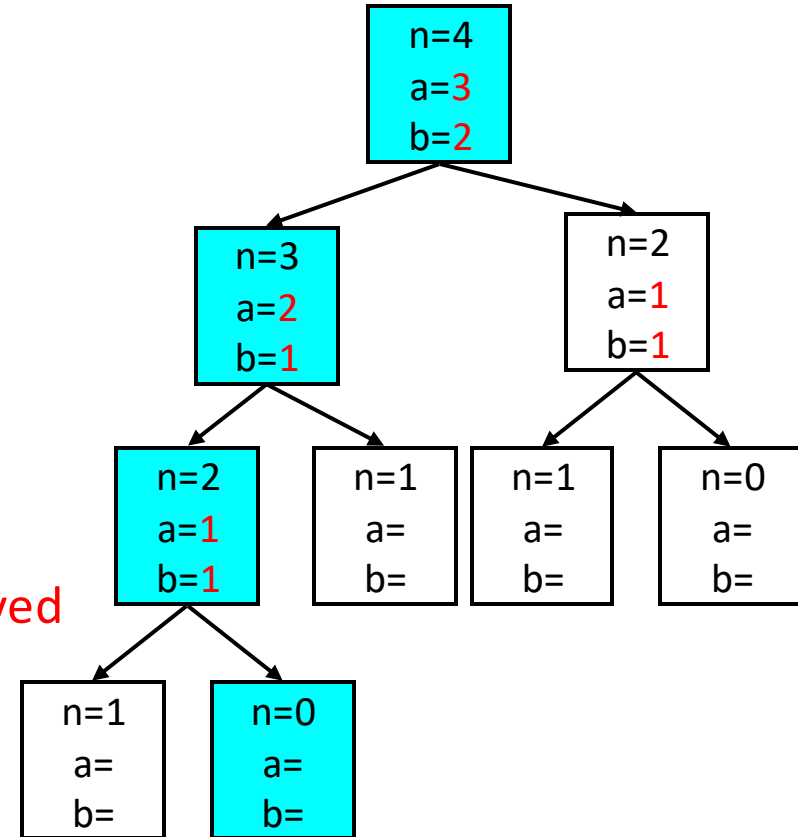
- E.g.:

```
typedef int (*p2f)(int);  
p2f hof(void) {  
    int add5(int b) {  
        return 5+b;  
    }  
    return &add5;  
}
```

- Can we use a stack of frames?

# Collection of Frames

- Can functions be recursive? **yes**
- What is Parameter passing mechanism?
  - Call-by-name
  - Call-by-value
  - Call-by-reference
- Can (and how) are non-local names referenced? **?**
- What happens to local variables on return from function? **destroyed**
- Can storage be allocated locally and dynamically in a function?
- Are functions first-class objects? **?**



# Non-local Access

- Can a function refer to variables in outer functions?

- E.g.:

```
int add2(int a, int c) {  
    int add1(int b) {  
        return b;   
    }  
    return add1(c);  
}
```

foo(b) {return b}

- Stack of Frames ok?
- There are other issues however (deal with later)

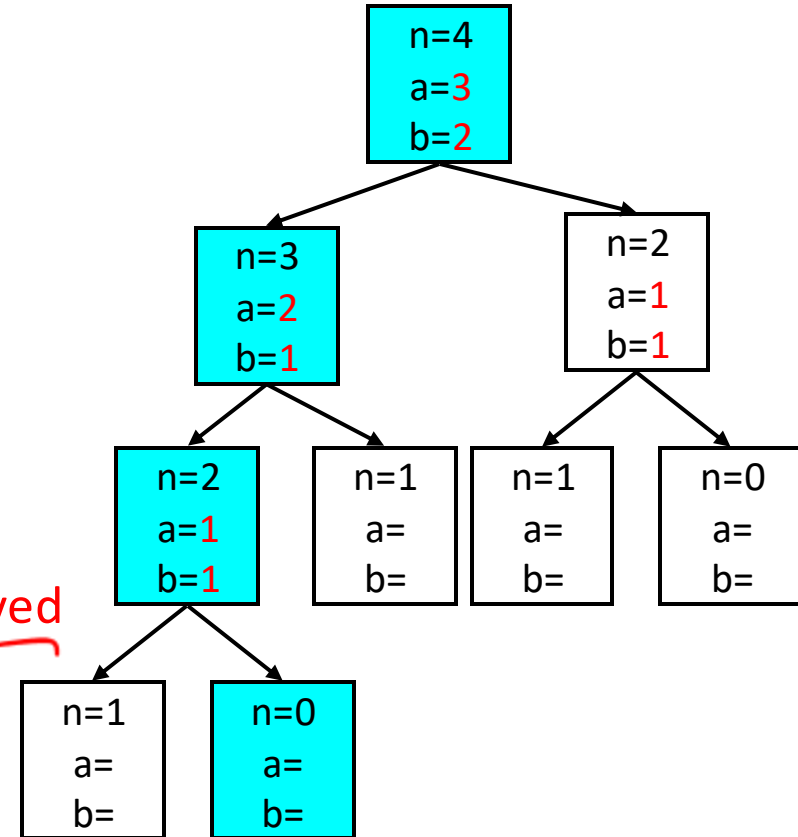
# Non-local Access vs. Global Access

```
int add2(int a, int c) {  
    int add1(int b) {  
        return a+b;  
    }  
    return add1(c);  
}
```

```
int a;  
int add2(int c) {  
    int add1(int b) {  
        return a+b;  
    }  
    return add1(c);  
}
```

# Collection of Frames

- Can functions be recursive? yes
- What is Parameter passing mechanism?
  - Call-by-name
  - Call-by-value
  - Call-by-reference
- Can (and how) are non-local names referenced? no
- What happens to local variables on return from function? destroyed
- Can storage be allocated locally and dynamically in a function?
- Are functions first-class objects? ?



# 1<sup>st</sup> Class Functions & Non-local Access

- Can a function return a function?

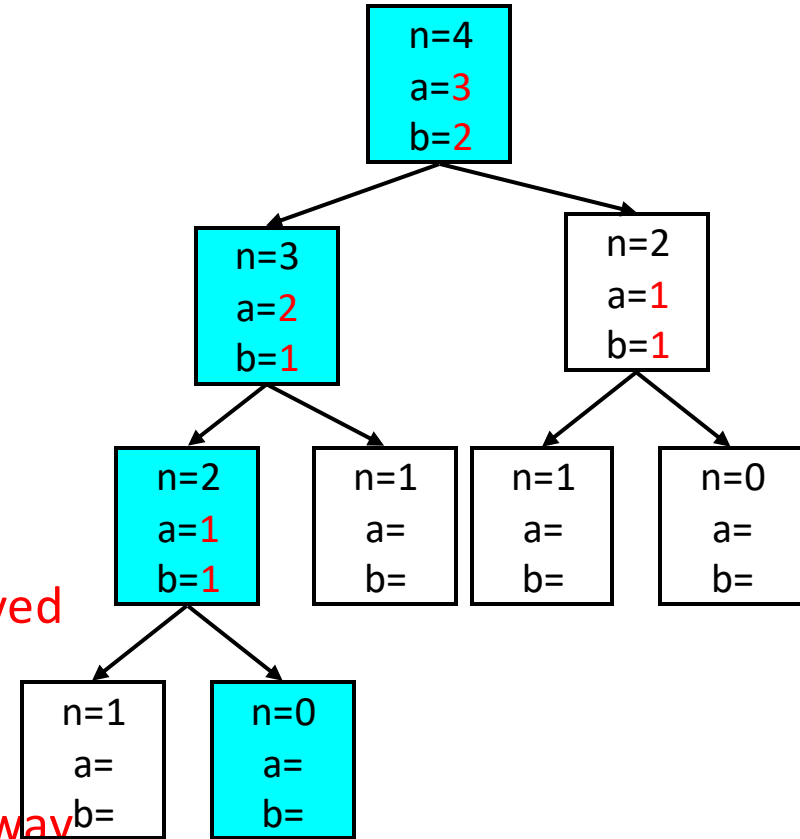
- E.g.:

```
typedef int (*p2f) (int);
p2f hof(int a) {
    int adda(int b) {
        return a+b;
    }
    return &adda;
}
```

- What is going on here?
- Combination of
  - non-local access &
  - first-class functions.

# Collection of Frames

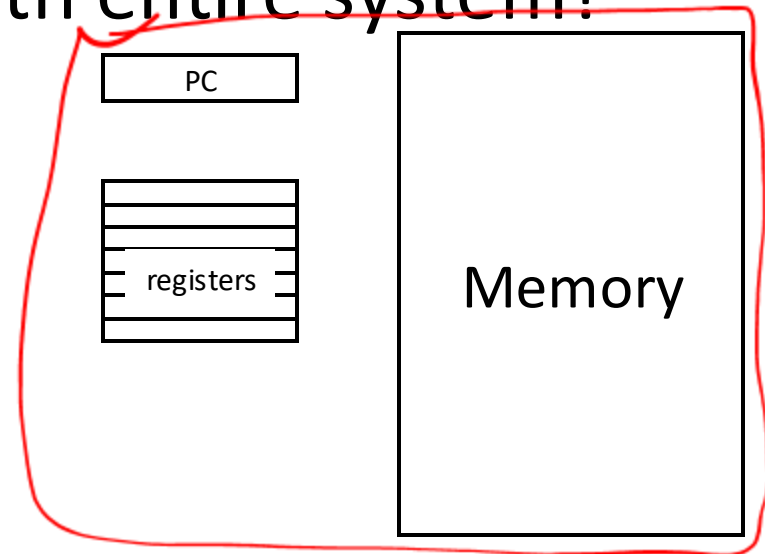
- Can functions be recursive? **yes**
- What is Parameter passing mechanism?
  - Call-by-name
  - Call-by-value
  - Call-by-reference
- Can (and how) are non-local names referenced? **yes**
- What happens to local variables on return from function? **destroyed**
- Can storage be allocated locally and dynamically in a function?
- Are functions first-class objects? **Either way**



Use a stack of activation frames.

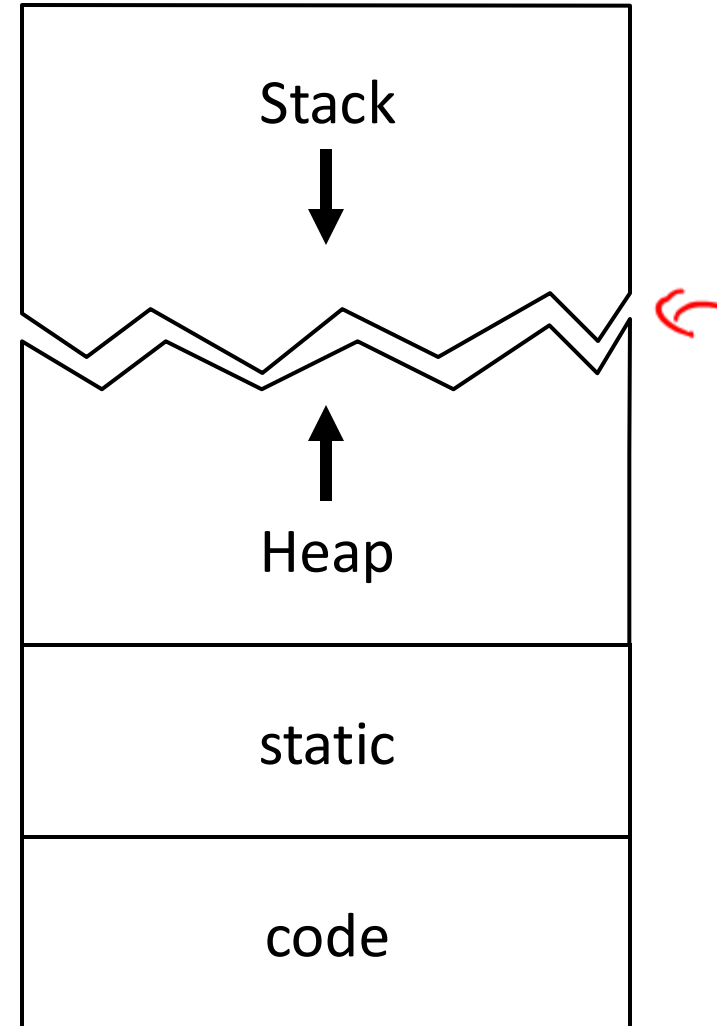
# Memory Layout

- We went through this analysis to determine the interaction of frames
- We are assuming:
  - stack is good for storing frames
  - Allows “unlimited” recursion
- How does this interact with entire system?



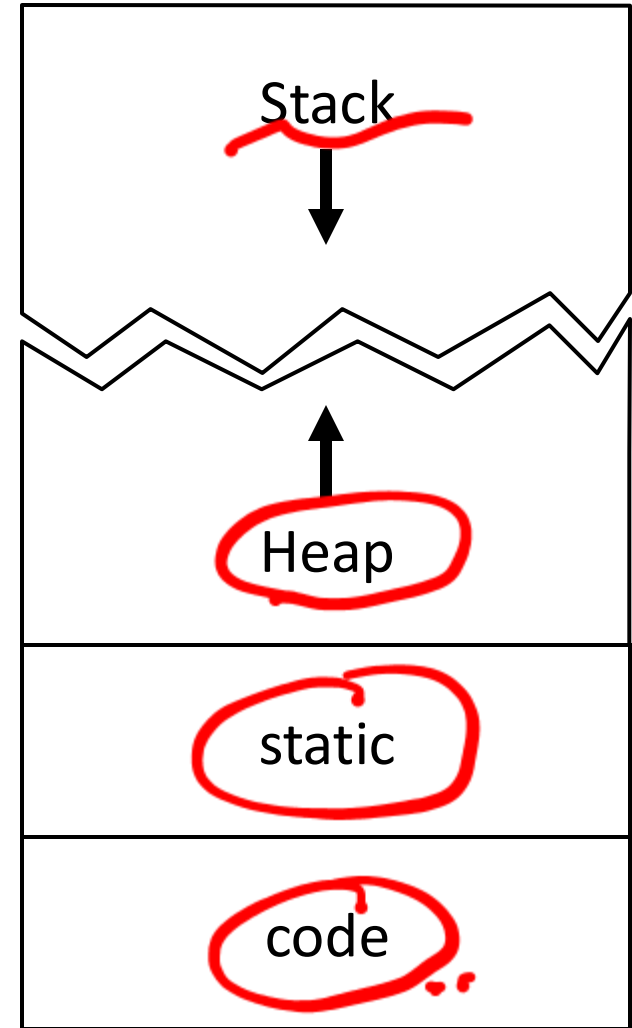
# Memory Organization

- Instructions are (usually) static and go into code.
- Static data is allocated at compile time, resolved at link-time
- Stack grows down and holds activation frames
- Heap grows up

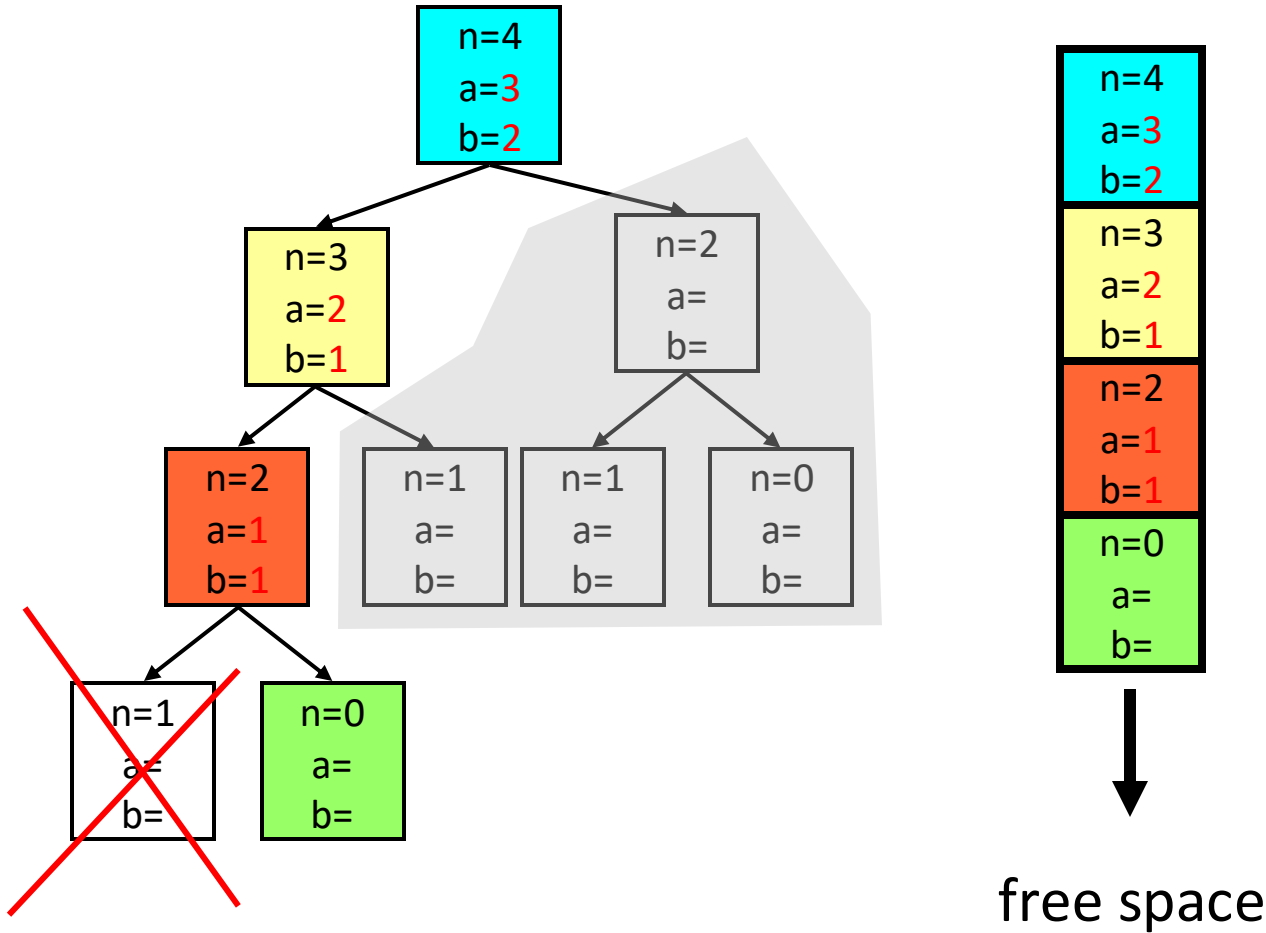


# Memory Organization

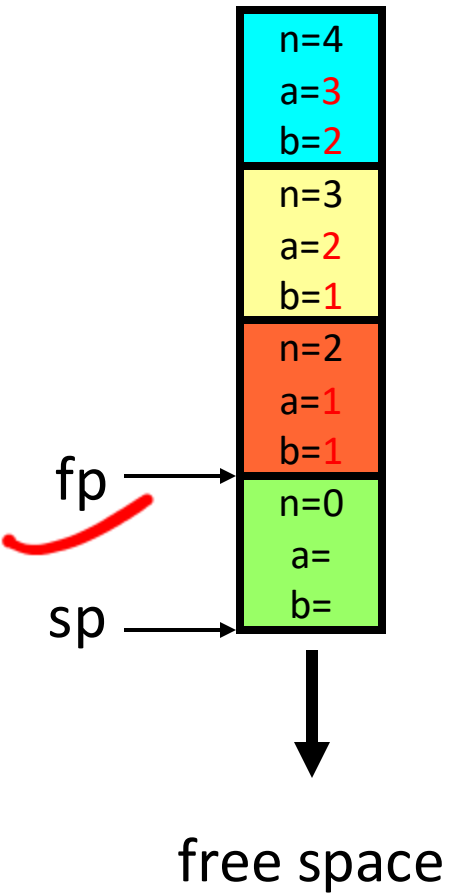
- Code and static contain fixed size statically allocated information
- Stack and data contain dynamically sized and dynamically allocated information
- Stack and heap compete for memory.
- Relates to storage classes



# The Stack



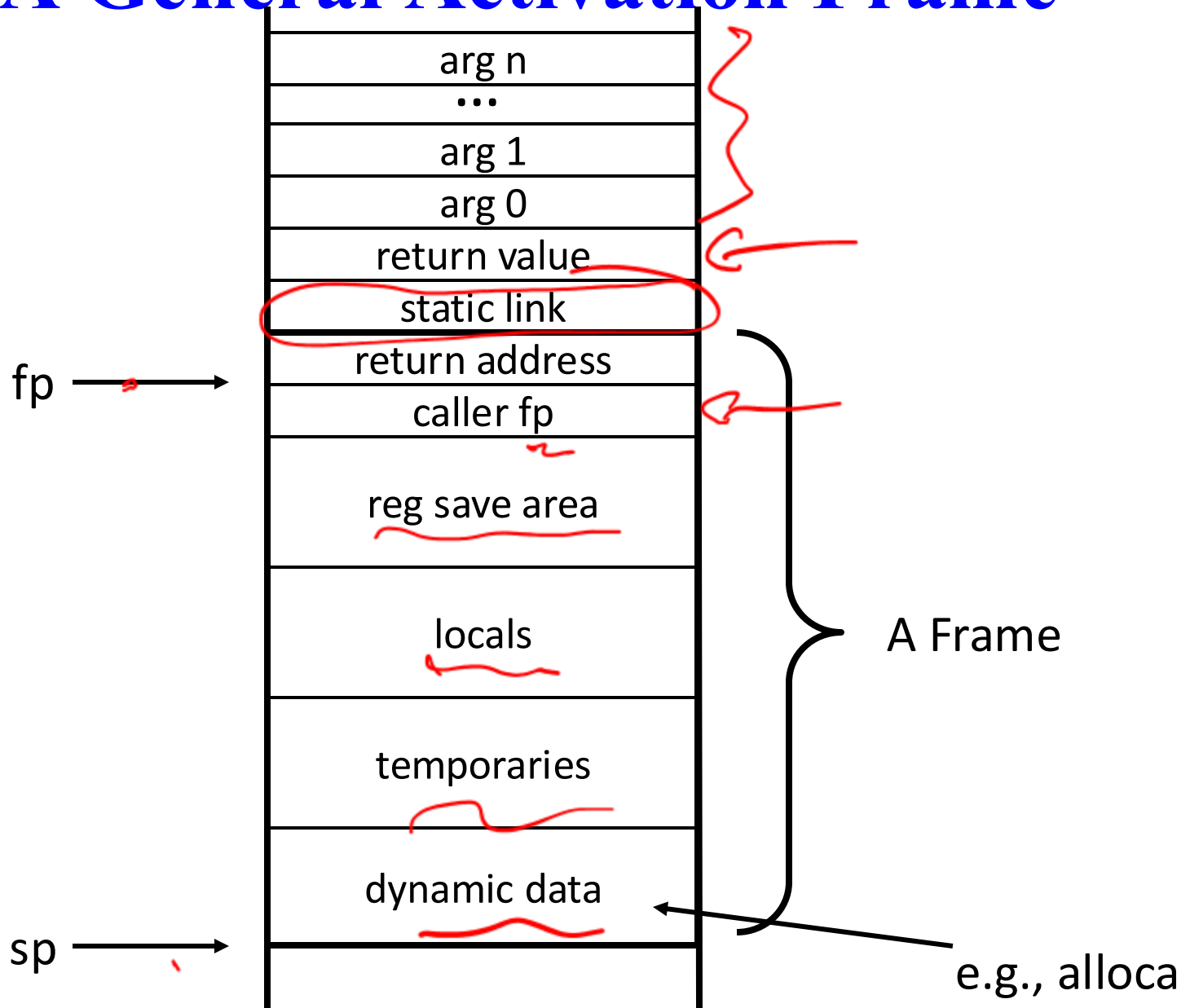
# The Stack



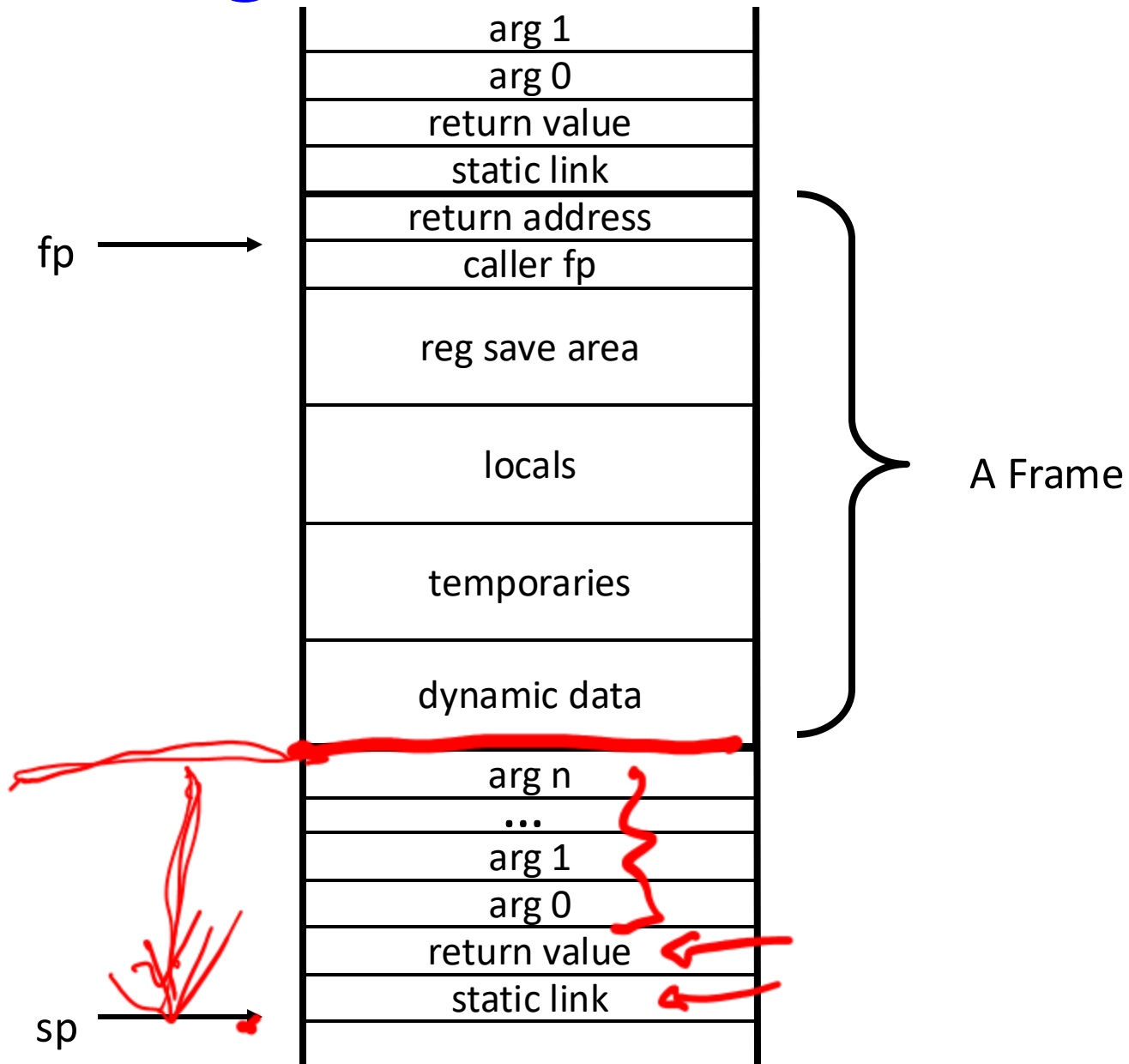
- How do we know where one frame starts and another stops?
  - How do we track return address?
  - How do we access local variables?
  - How do we access non-local variables?
- 
- Frame Pointer (fp)
  - Stack Pointer (sp)

Why not just say `%rbp`?

# A General Activation Frame



# Right Before Next Call



# Who does what?

Foo: **Prolog**

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

**setup for call**

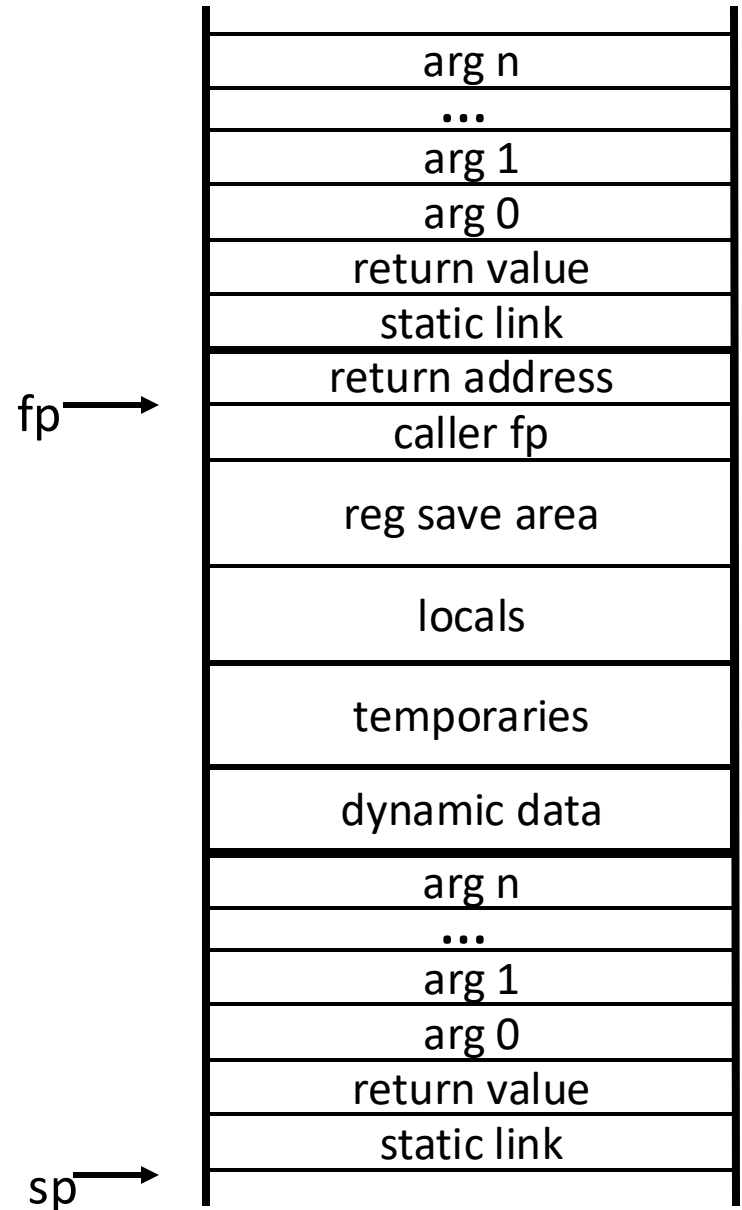
**call bar(a,b,c,d)**

**recover from call**

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

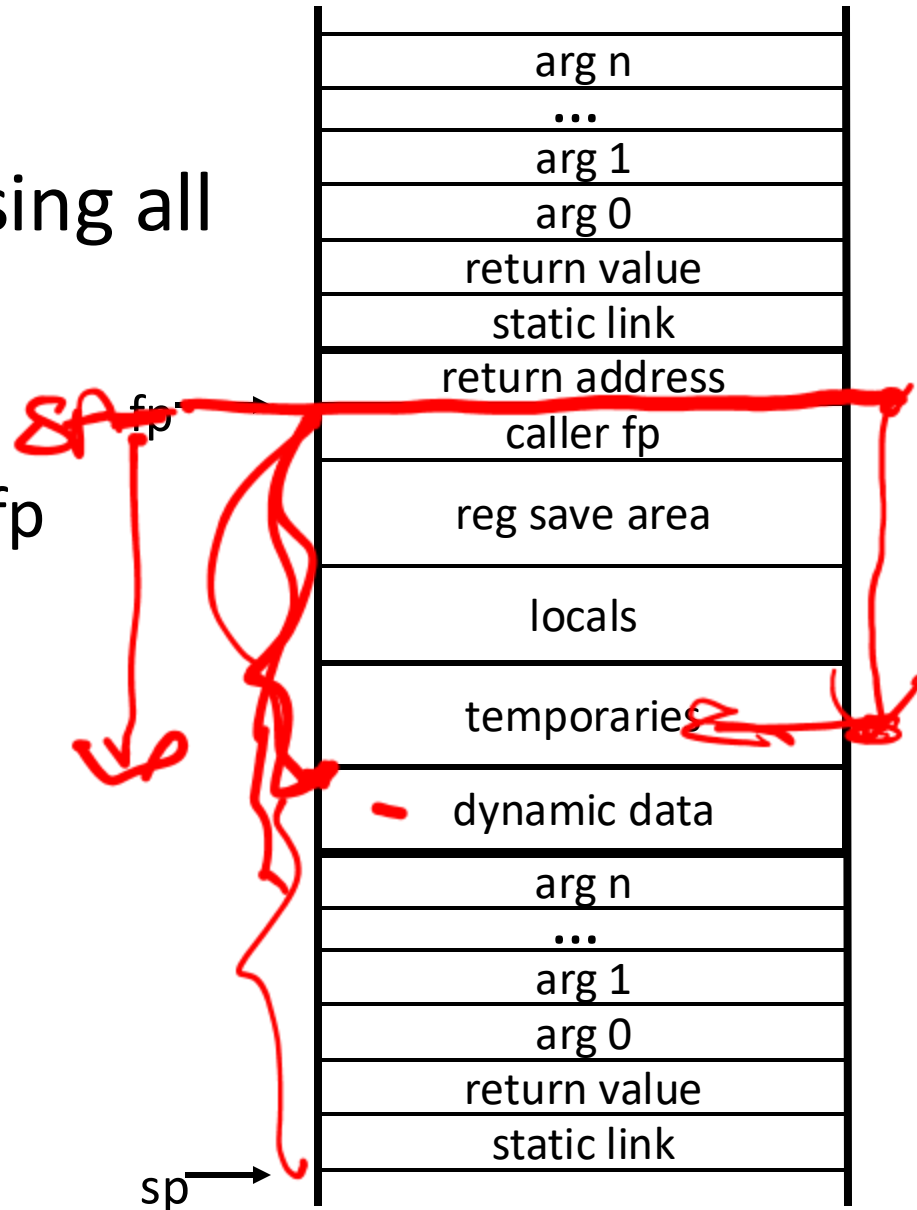
**Epilog**

The answer is: it depends!



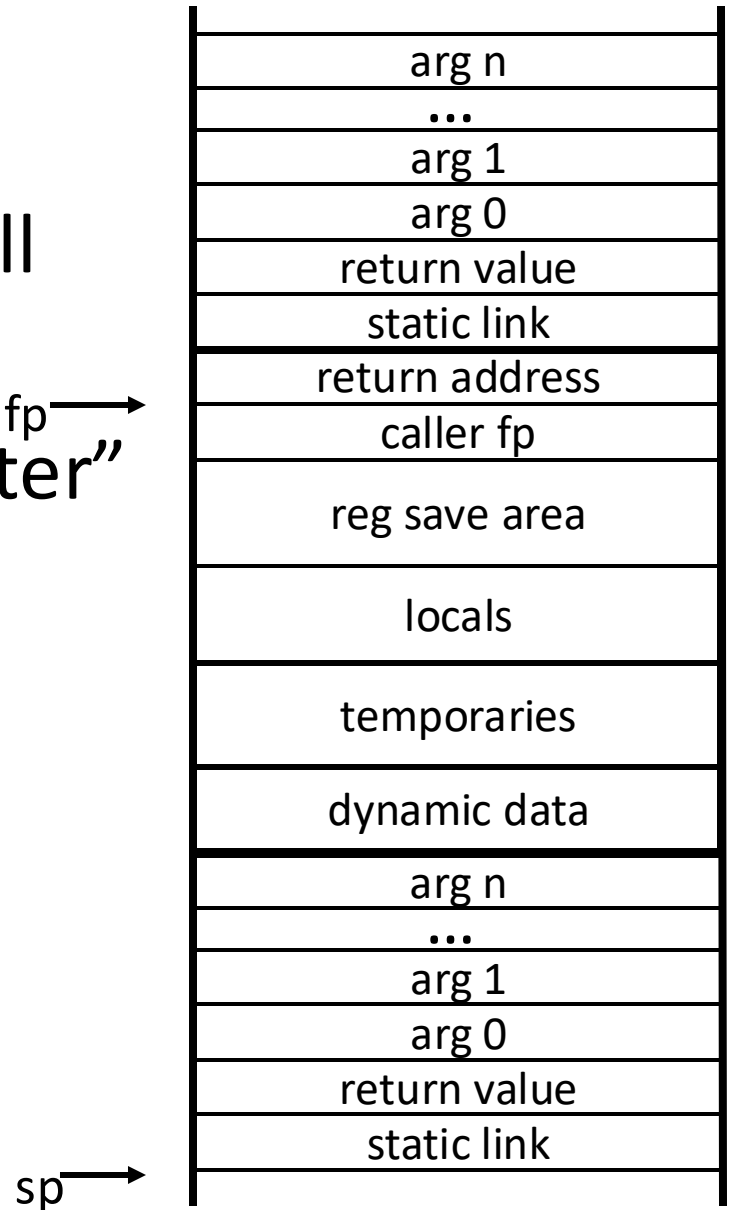
# Frame Pointer

- Used as base for accessing all elements of frame.
- In Prolog:
  - $[sp-x] = fp$ ; save caller's fp
  - $fp = sp$
  - $sp -= frameSize$
- In Epilog
  - $sp = fp$
  - $fp = [sp-x]$
- Do we always need fp?



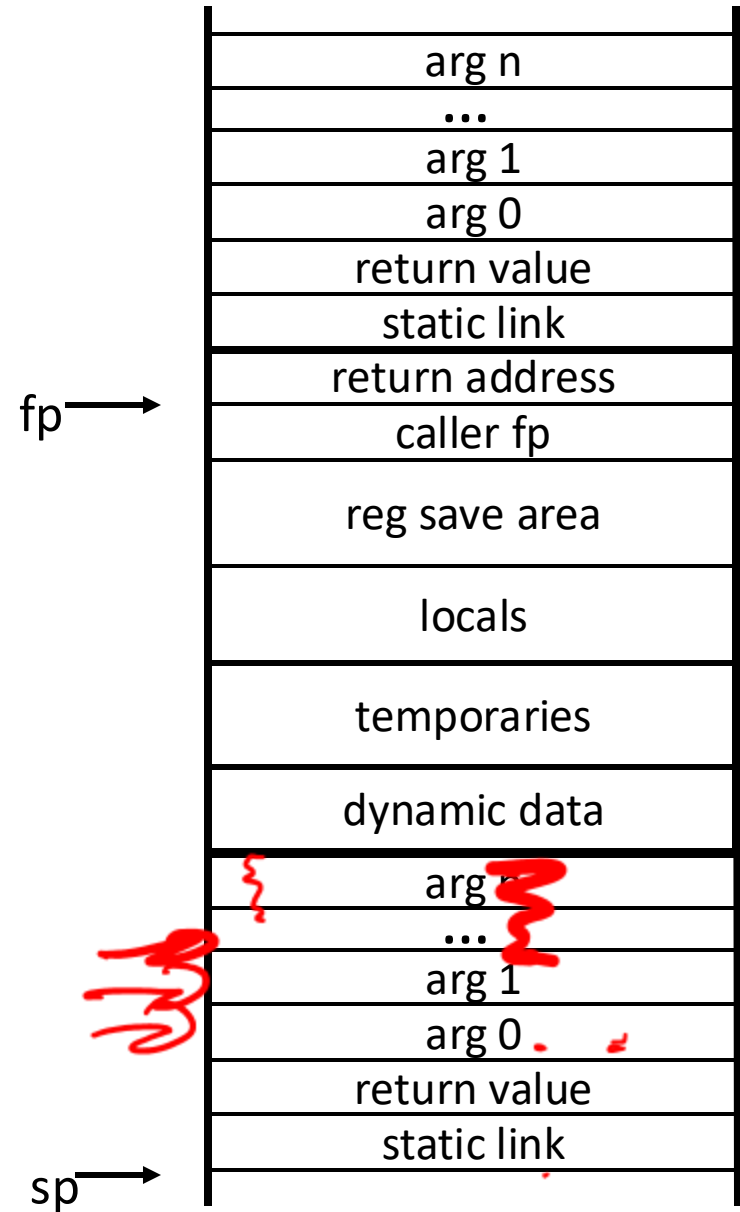
# Frame Pointer

- Used as base for accessing all elements of frame.
- Many times a “fictional register”  
fp →
- On Call
  - $sp -= \text{frameSize}$
  - $fp = sp + \text{frameSize}$
- On Return
  - $sp += \text{frameSize}$



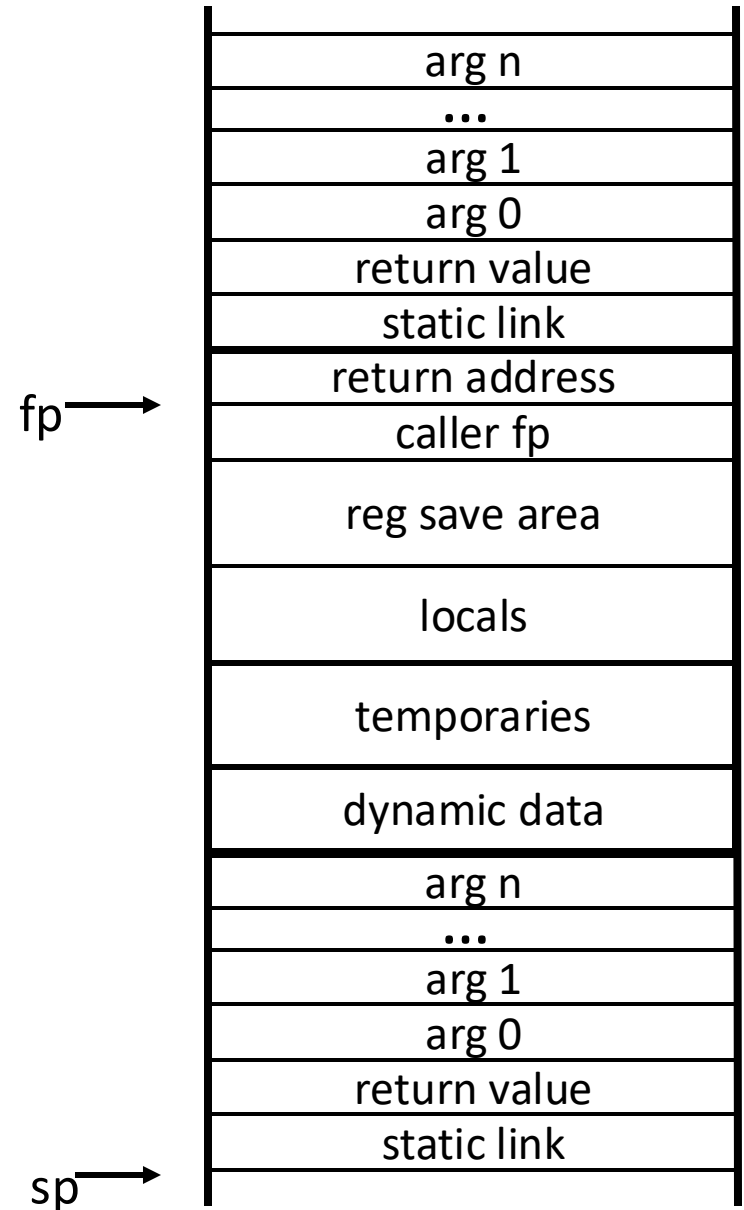
# Parameter Passing

- Caller puts parameters into stack starting at current sp
- Save space for return value
- Invoke Callee
- Actually we can do better!
  - Caller **reserves** space for first k params and return value
  - Why is this better?
  - Why bother to reserve space at all?



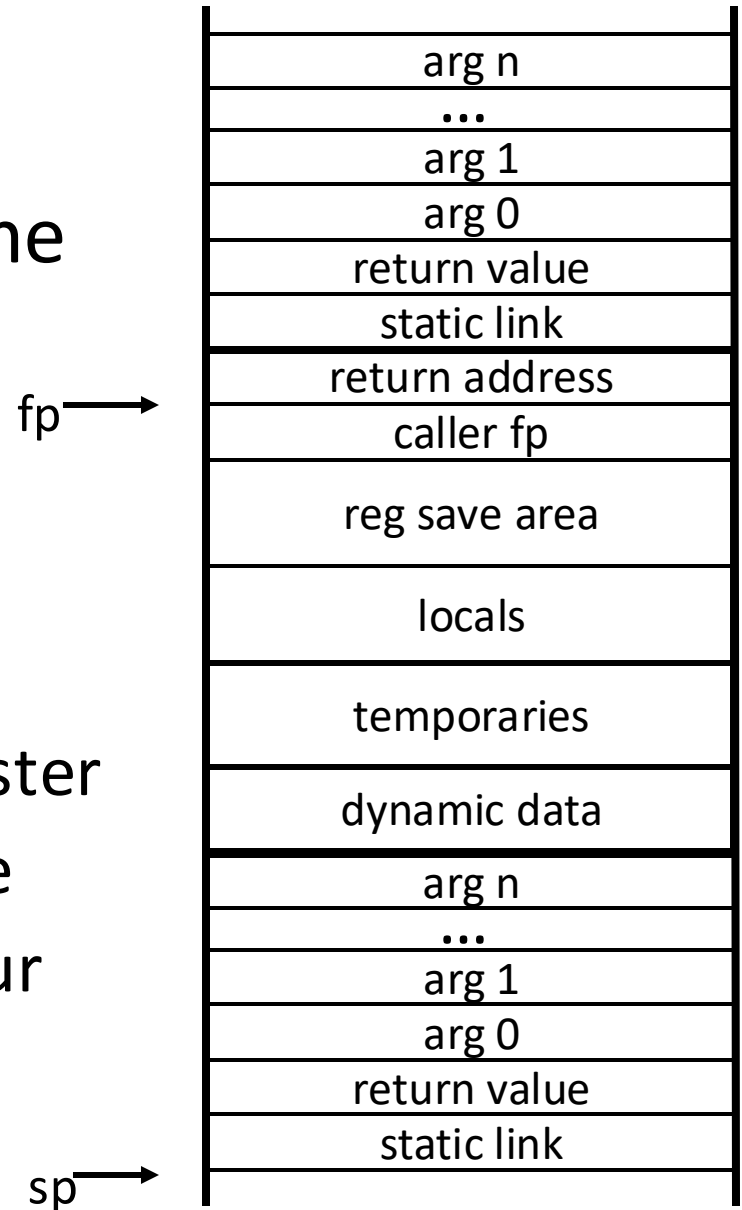
# Registers

- One set of registers
- Callee might want to use same register as caller
- Caller can save all registers
- Callee can save all registers
- Which is better?
- Issues:



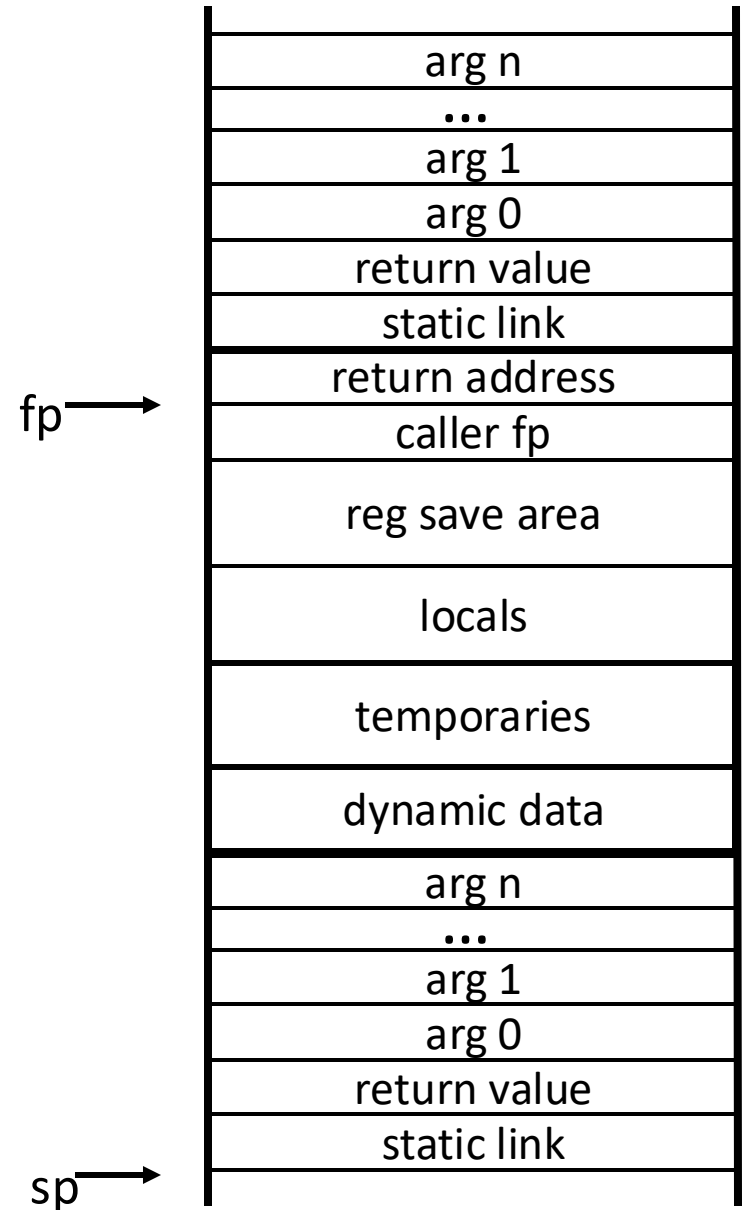
# Registers

- One set of registers
- Callee might want to use same register as caller
- Caller can save all registers
- Callee can save all registers
- Issues:
  - callee might not use your register
  - Extreme case is leaf procedure
  - caller might not have used your register



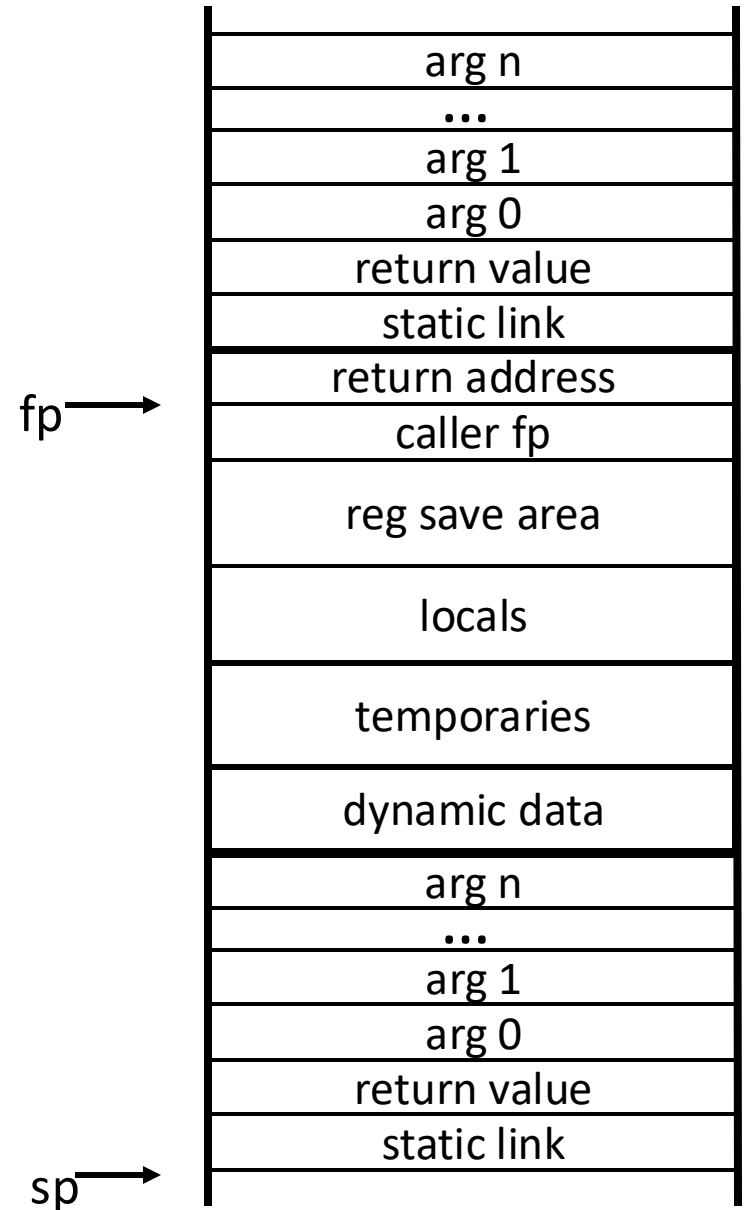
# Registers

- One set of registers
- Callee might want to use same register as caller
- Caller can save all registers
- Callee can save all registers
- Make some registers
  - caller save
  - callee save
- Or, register windows?



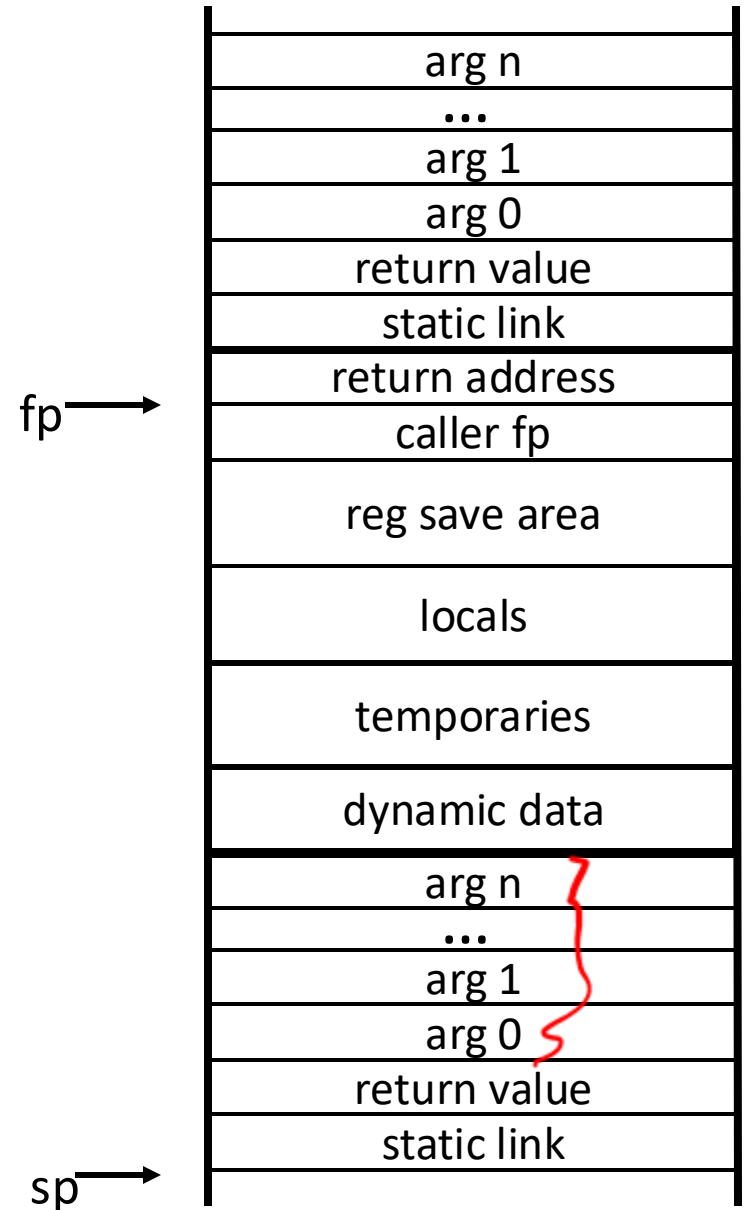
# Return Address

- Who should save it?
- Should it be saved?



# Locals/Temps/Dynamic

- Allocated by callee
- Dynamic data (e.g., alloca) requires fp and sp



# Activation Frame C0

- No ~~nested functions, so no static link~~
- return value is not stored on stack:

**%rax**

- First 6 arguments stored in registers:

**%rdi, %rsi, %rdx, %rcx, %r8, %r9**

- Divides registers into caller save:

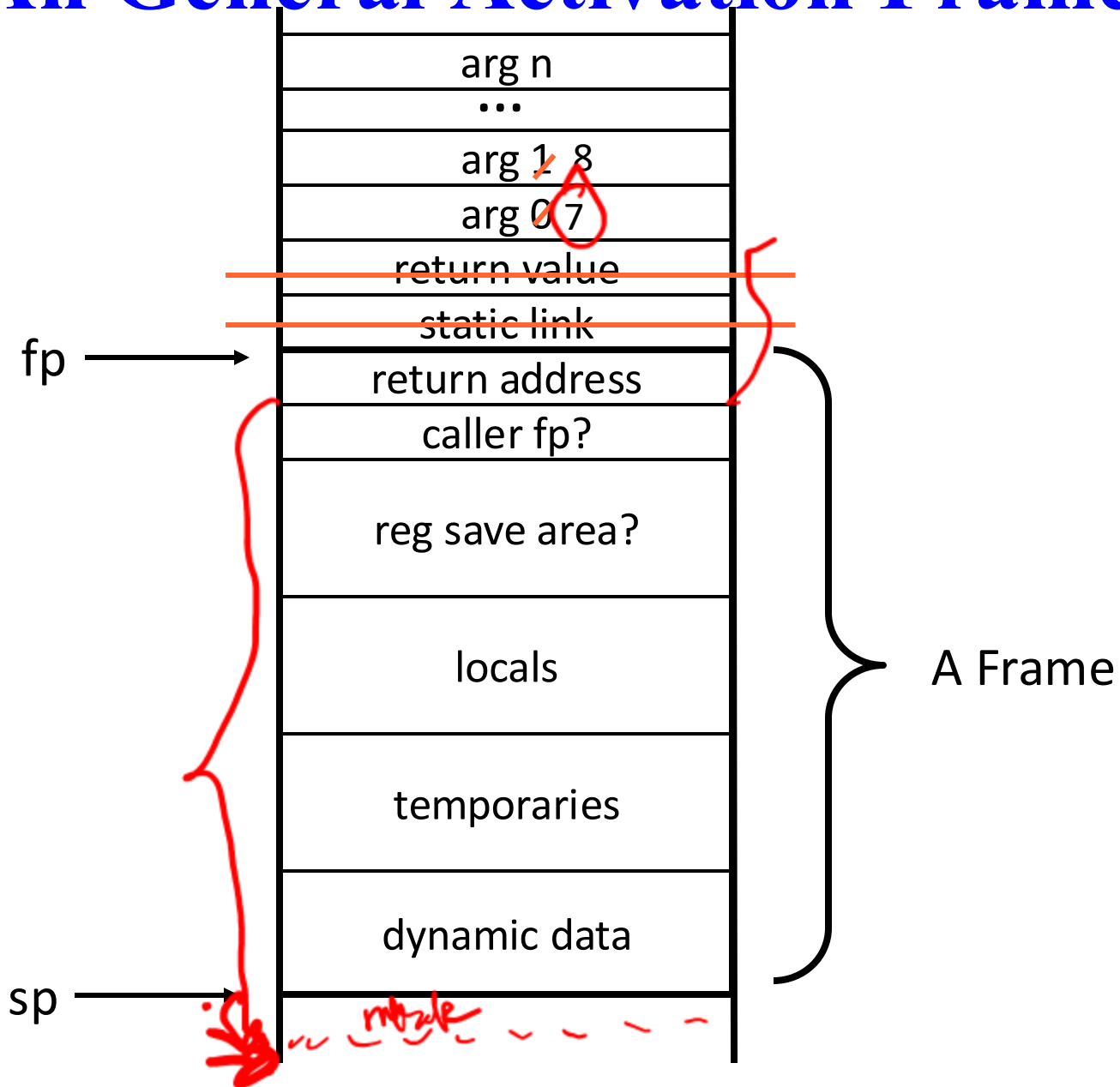
**%r10, %r11**

- And, callee save:

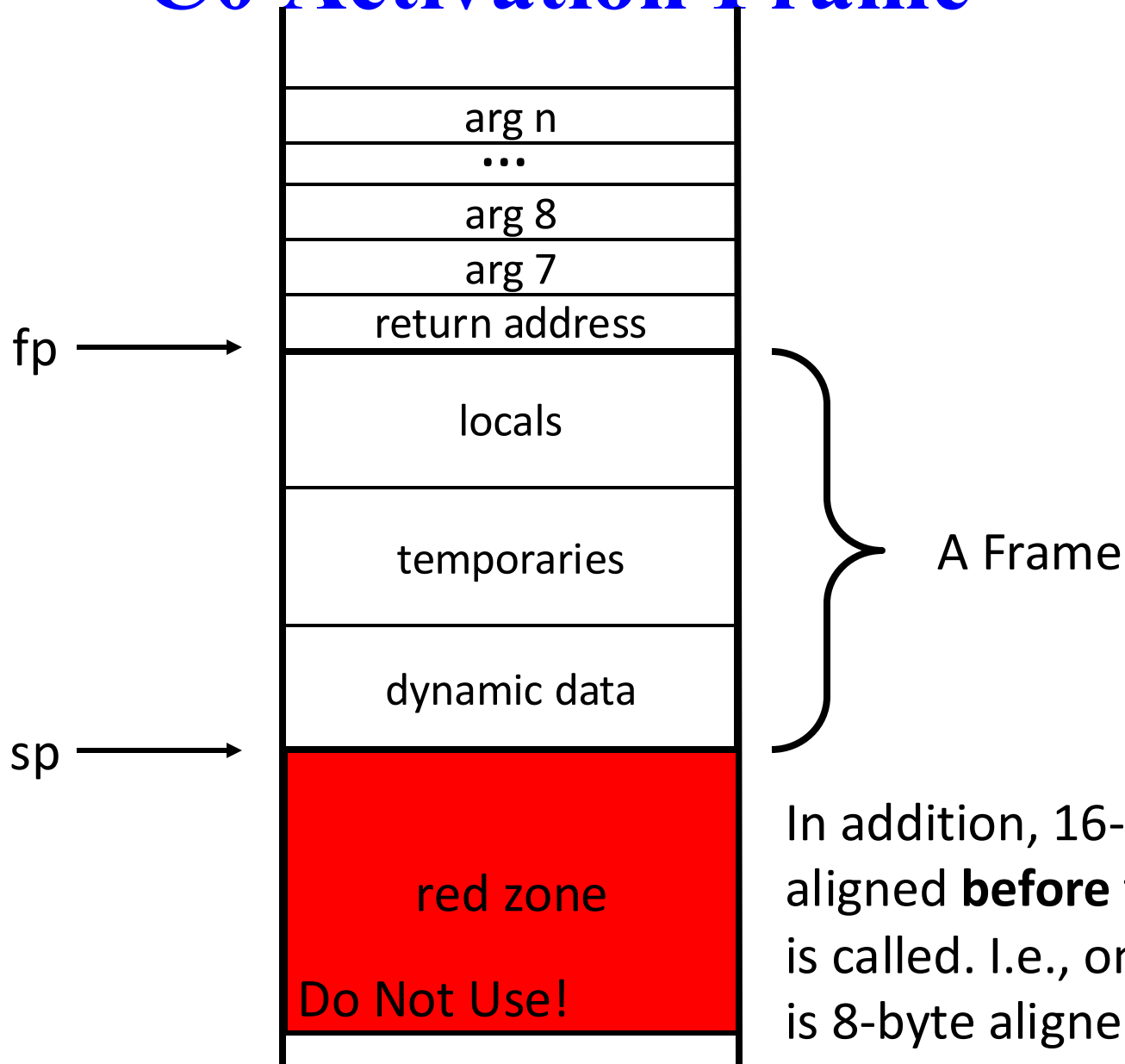
**%rbx, %rbp, %r12, %r13, %r14, %r15**

This is a part of C's calling convention

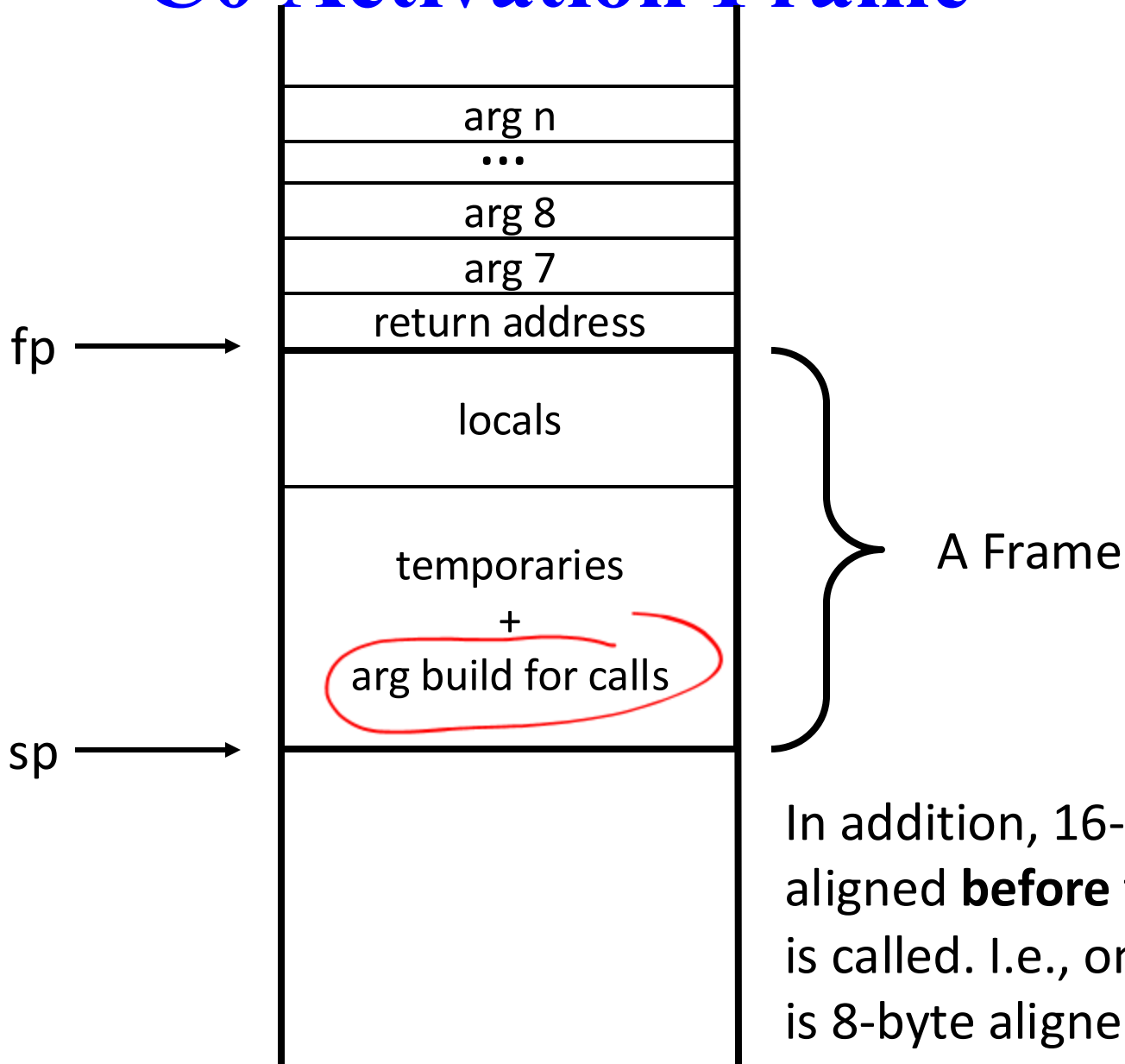
# An General Activation Frame



# C0 Activation Frame



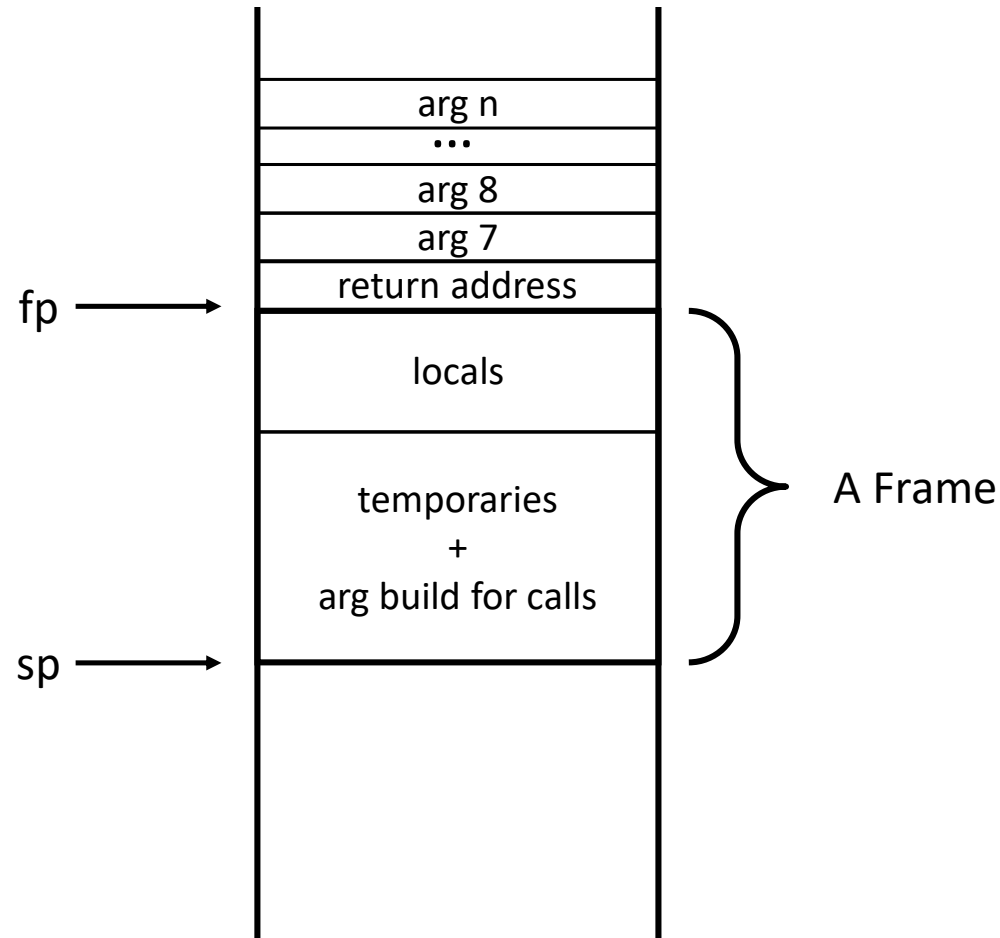
# C0 Activation Frame



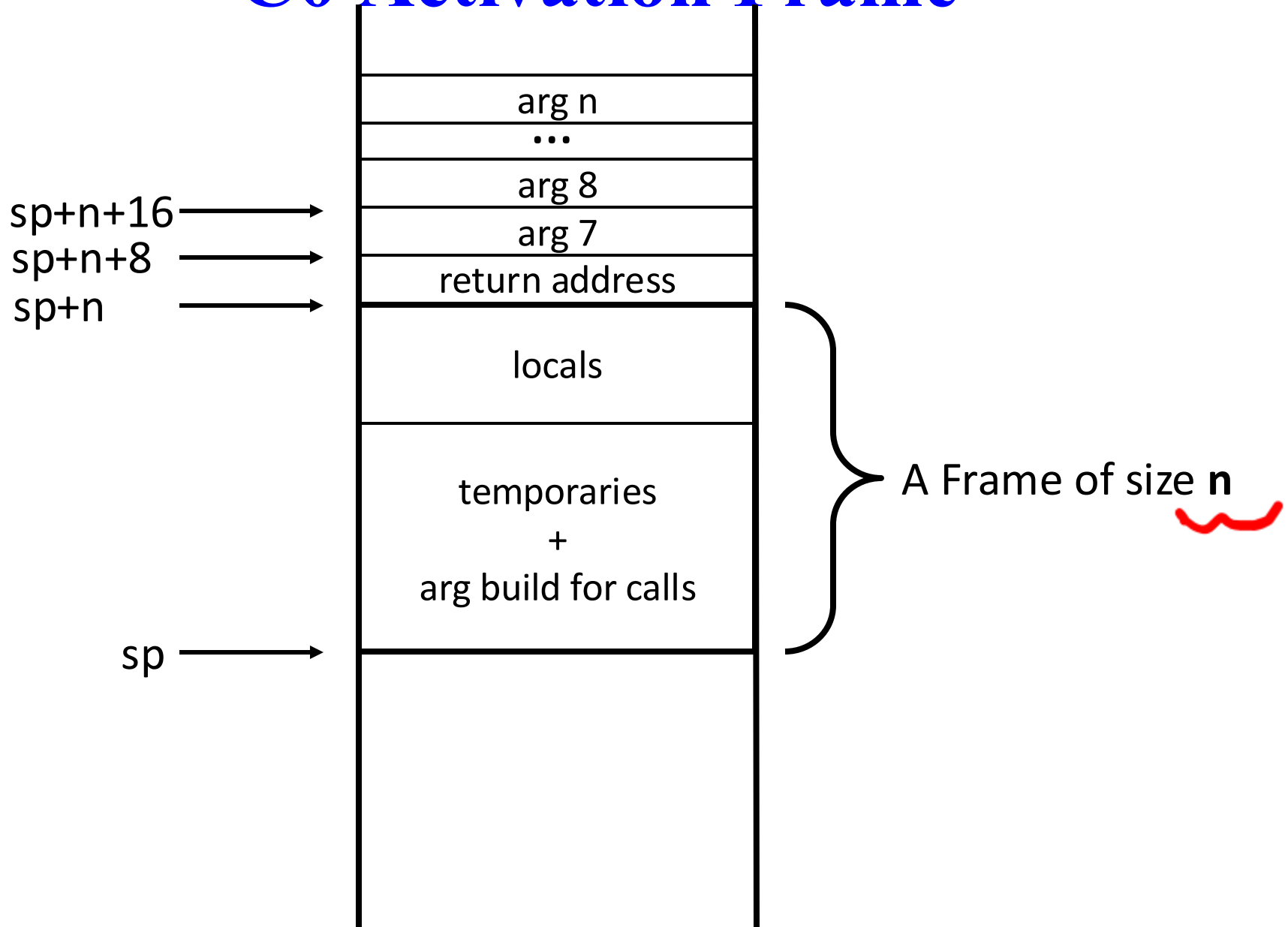
In addition, 16-byte aligned **before** function is called. I.e., on entry it is 8-byte aligned.

# to fp or not to fp?

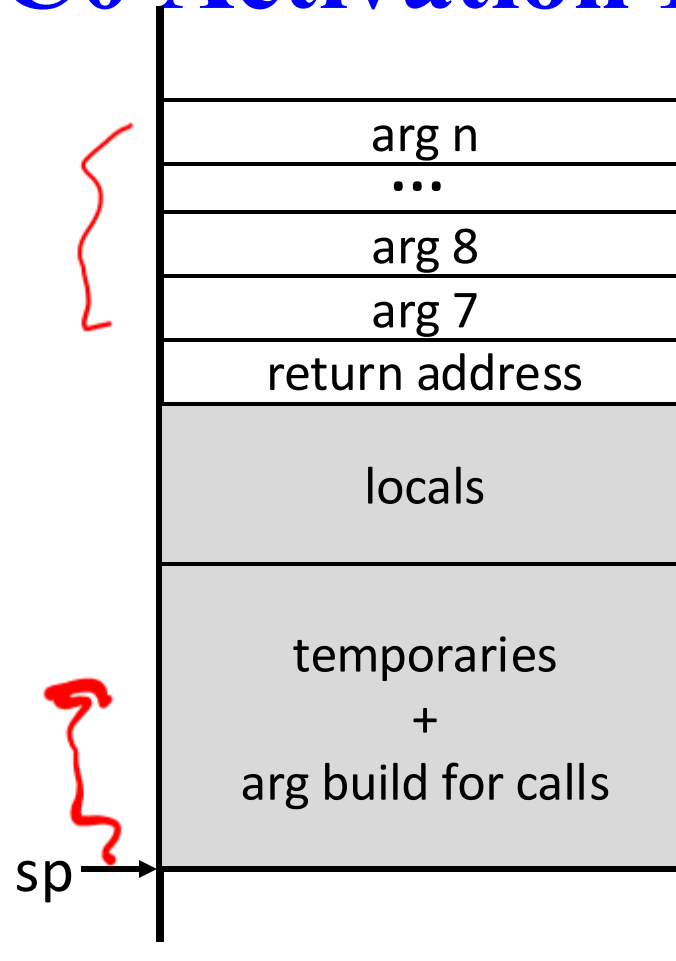
- Do we need a frame pointer?



# C0 Activation Frame



# C0 Activation Frame



# Who does what?

## Foo: Prolog

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

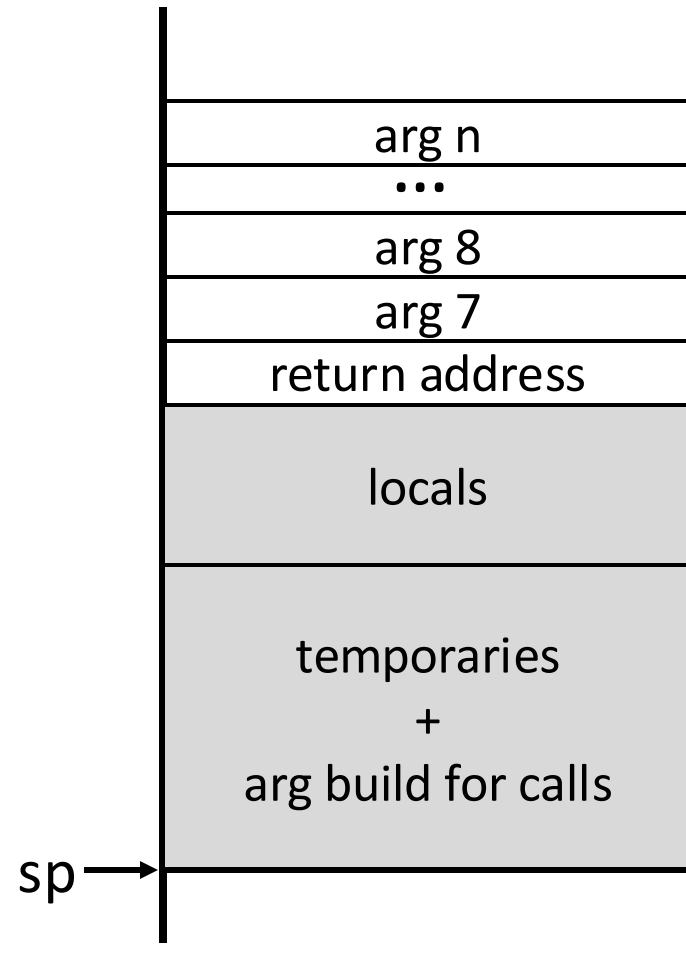
**setup for call**

**call bar(a,b,c,d)**

**recover from call**

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

## Epilog



The answer is: it depends!

# Prolog

## Foo: Prolog

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

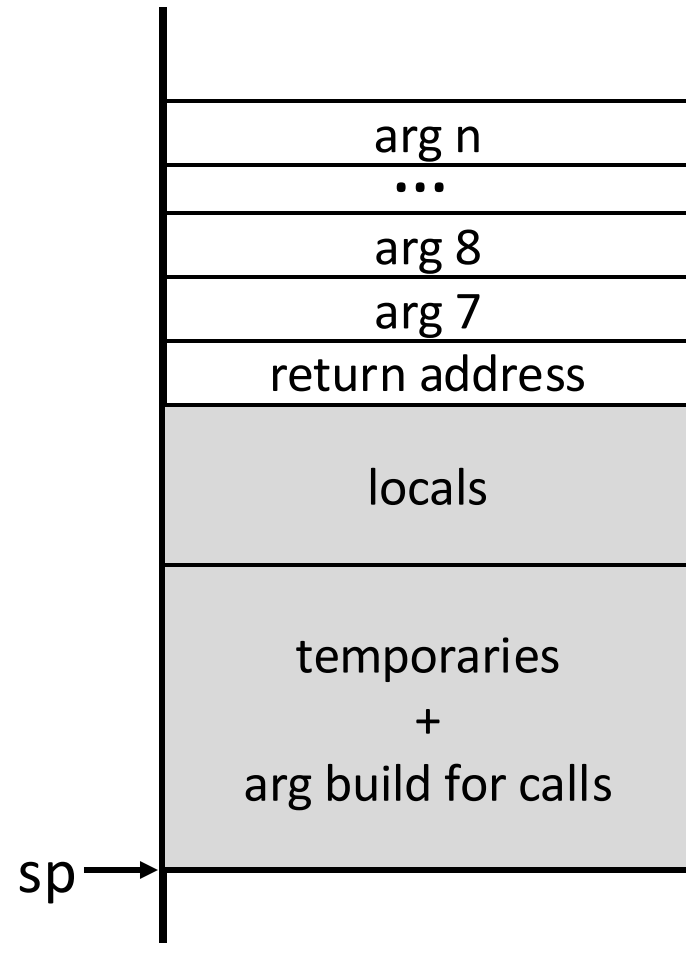
**setup for call**

**call bar(a,b,c,d)**

**recover from call**

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

## Epilog



Prolog: adjust sp

save any necessary callee-save registers

# Epilog

## Foo: Prolog

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

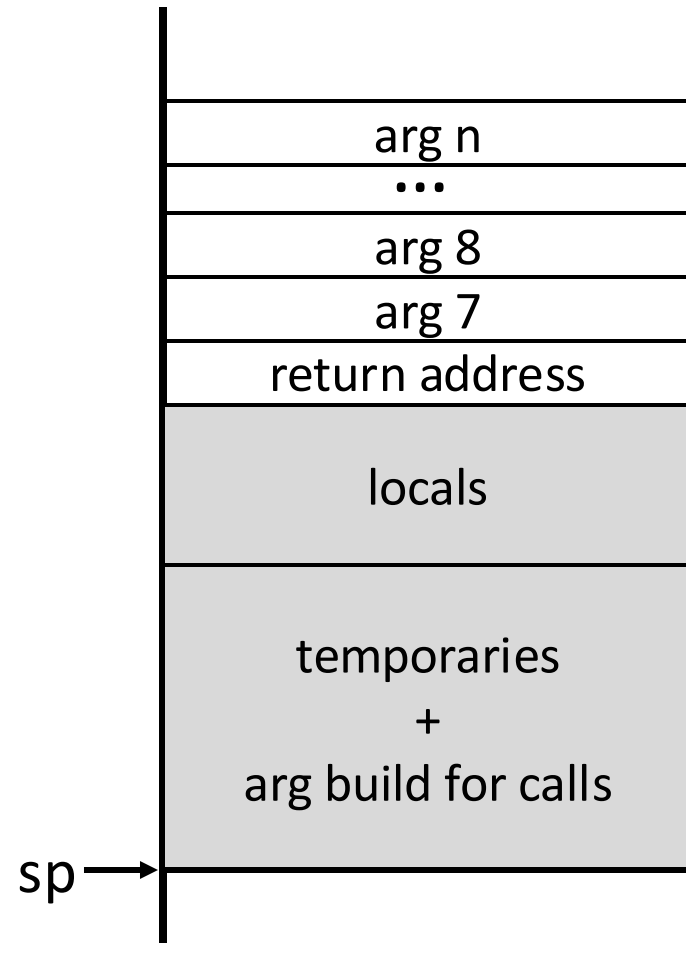
**setup for call**

**call bar(a,b,c,d)**

**recover from call**

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

## Epilog



epilog: re-adjust sp  
restore any saved callee-save registers

# setup for call

## Foo: Prolog

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

### setup for call

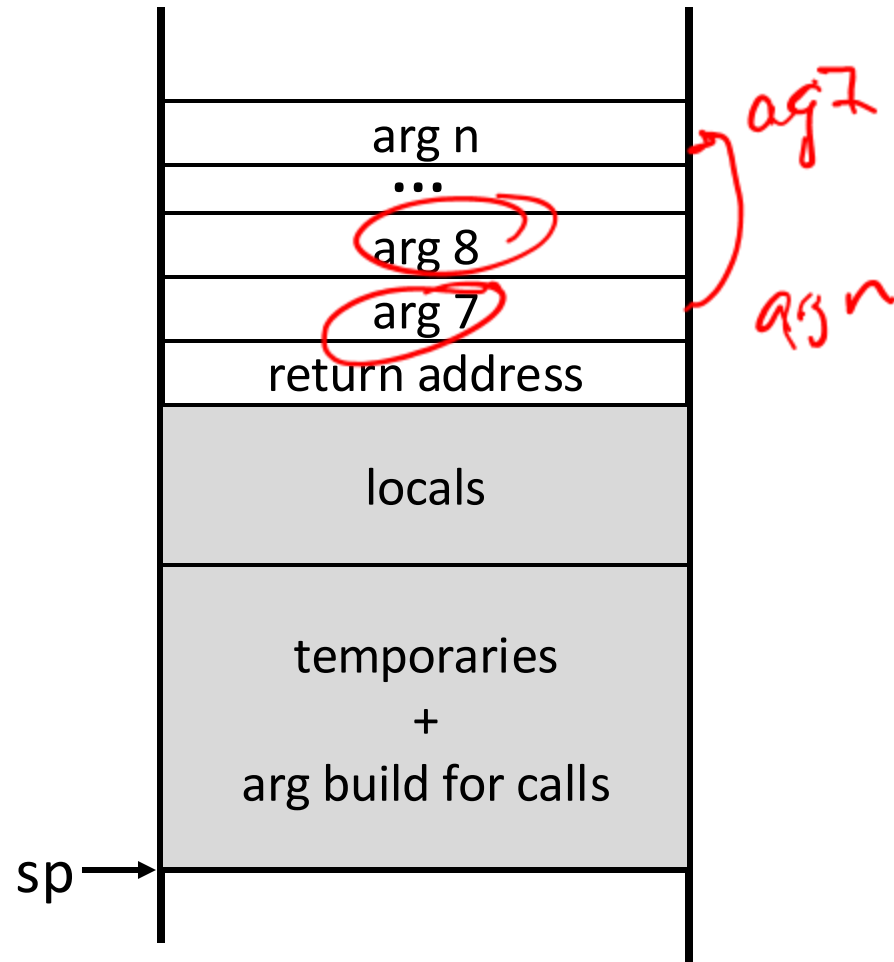
```
call bar(a,b,c,d)
```

### recover from call

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

## Epilog

before call: save any necessary caller-save registers  
setup arg registers  
possibly store 7<sup>th</sup>, ..., nth arg on stack



# recover from call

## Foo: Prolog

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

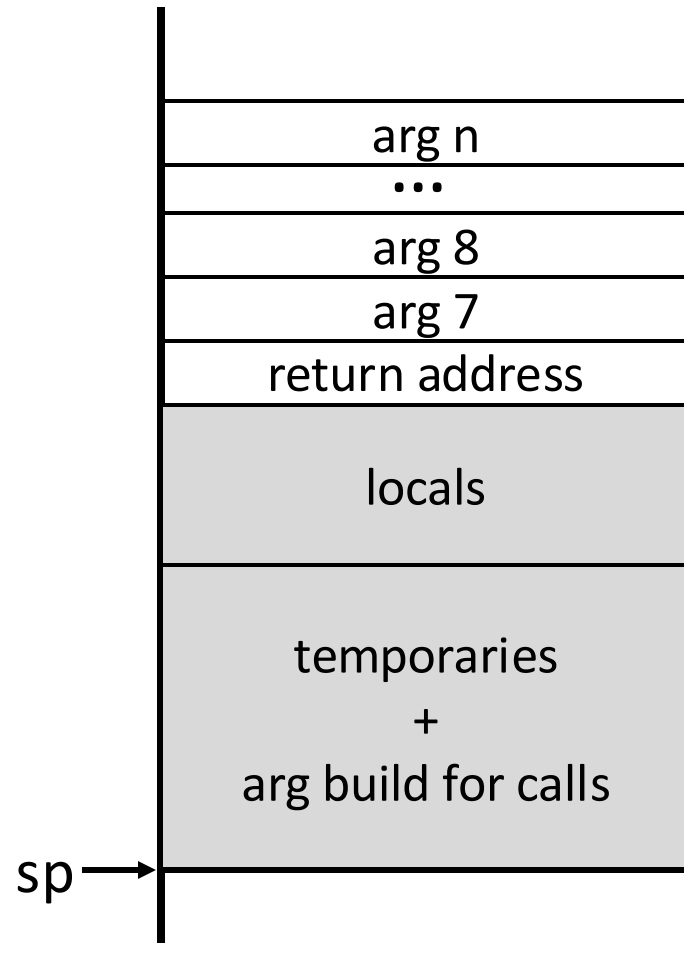
→ setup for call

call bar(a,b,c,d)

→ recover from call 2

```
instr1  op1,op2
instr2  x,y,z
mov     z,a
add     r3,r1,r2
```

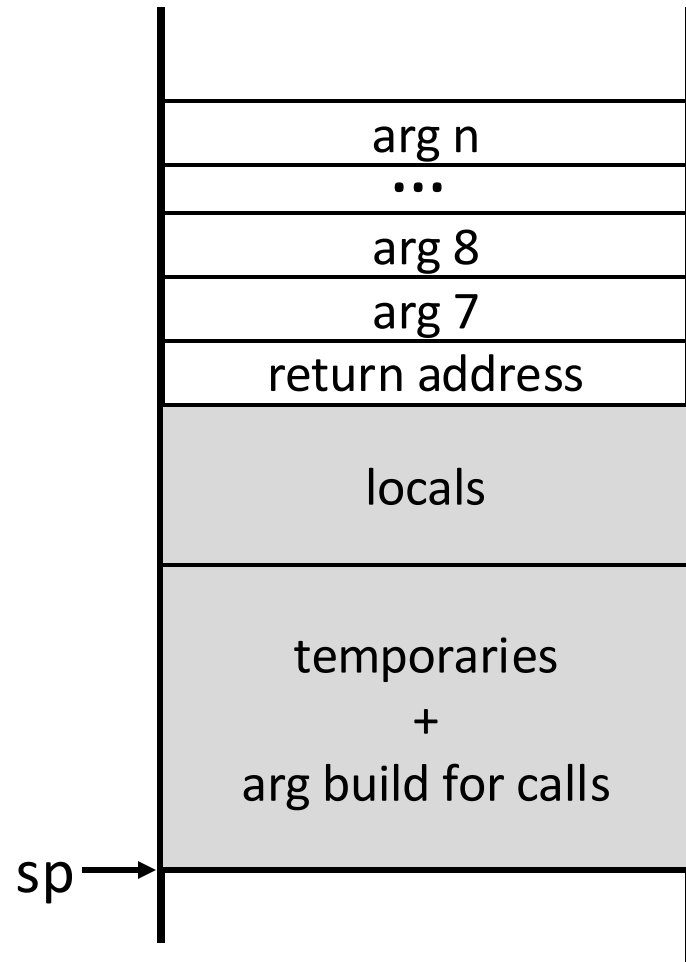
## Epilog



after call: restore any saved caller-save registers

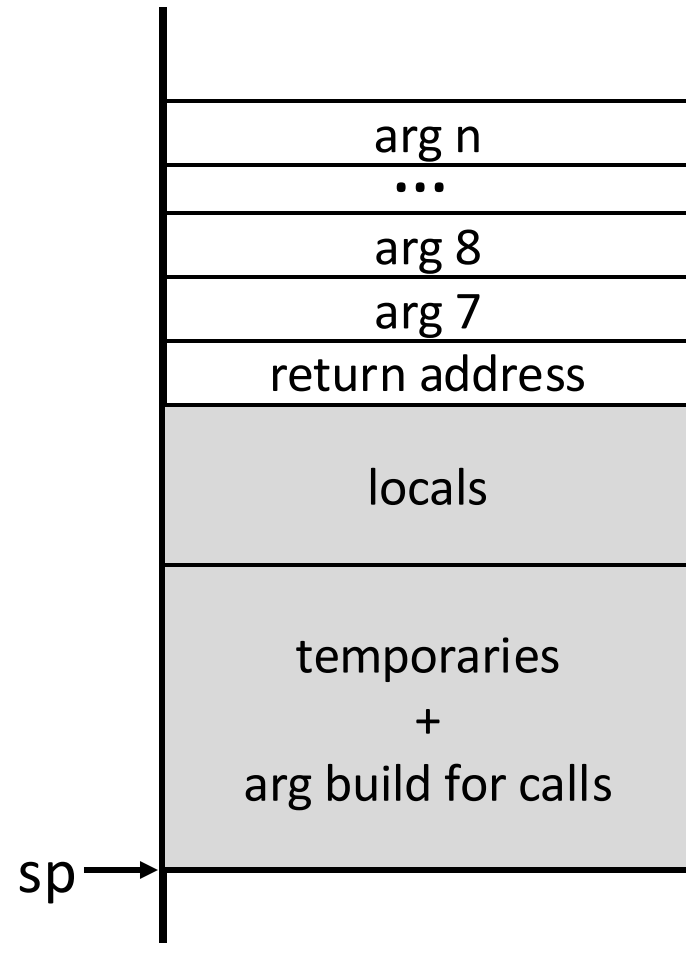
# What are “locals” and “temps”?

- What gets saved in the frame?



# What are “locals” and “temps”?

- What gets saved in the frame?
  - spilled automatic variables
  - escaping variables
- Escaping variables:
  - referenced in inner function
  - address taken
  - passed by reference
  - Can determine at semantic analysis time with recursive walk of AST
- When do we know?



# How to Represent locations

- Various kinds of locations
  - automatic variables: temp
  - parameters: temp
  - hard registers: register
  - spill: frame slot
  - global: memory?
  - static: memory?



- When do we know size of frame?
- When do we generate loads and stores?
- How do we simplify our compiler?

# Variables

- Three kinds of variables
    - globals & statics
    - local variables
    - formal parameters
  - Issues:
    - where are they stored
    - How much space do they take
    - How are they accessed
  - This is both
    - machine dependent
    - and, language dependent
- Use an abstract Access type to represent all variables.
  - It will end up being:
    - a Temp
    - a HardReg
    - a Slot
    - a MemoryLocation

# Today

- Calling Conventions
- Activation Frames
- IR for Function Calls
- Putting it all together

# Translating Function Calls

- function call is an expression in grammar, e.g.,  
    `int a = foo(bar(1), 2)+4;`
- AST?

# Translating Function Calls

- function call is an expression in grammar, e.g.,  
`int a = foo(bar(1), 2)+4;`

- AST?

- Translation?

*(→ C code;  $t_1 \leftarrow C m_2$ ;  $f(b_1, t_2)$ )*

- From munching,

$$\text{tr}(f(e_1, \dots, e_n)) = \langle (e_1; \dots; e_n; t \leftarrow f(\hat{e}_1, \dots, \hat{e}_n)), t \rangle$$

*(Handwritten annotations: red circles around  $e_1, \dots, e_n$  and  $f(\hat{e}_1, \dots, \hat{e}_n)$ ; red arrows pointing from  $t$  to the arguments and from the function call to  $t$ )*

- Evaluate all arguments first so we can use pure expressions in call.
- treat call itself as a “statement” and assign (if needed) return value to a fresh temp

# IR for a function call

- Choices:

*e<sub>1</sub>* ←  
*e<sub>2</sub>* ←  
*e<sub>3</sub>* ←  
 $d \leftarrow f(s_1, \dots, s_n)$   
 $\text{call } f$   
 $\%rax \leftarrow \text{call } f$

*more detail*

- The latter two assume that  $s_1, \dots, s_n$  have either been moved to appropriate arg register or put in proper place on stack.
- Side note on SSA and precolored registers:
  - Explicitly representing  $\%rax$  will mean not in SSA form. So, `call f` may be preferred (deal with  $\%rax$  as with `div/mult/etc.`)

# defs and uses

- Each triple has a potential 'dest' and 'src's
- It also will have a set of uses and defs (which will include the 'dest' and 'src's)
- For `call f`
  - defines %rax
  - uses all arg registers needed for the call, e.g.,  $s_1, \dots, s_n$
  - ?

# defs and uses at call site

- Each triple has a potential 'dest' and 'src's
- It also will have a set of uses and defs (which will include the 'dest' and 'src's)
- For `call f`
  - defines %rax
  - uses all arg registers needed for the call, e.g.,  $s_1, \dots, s_n$
  - It also defines all caller-save registers!
  - So, call defines:  
%rax, %rdi, %rsi, %rdx, %rcx, %r8, %r9, %r10, %r11



# Register

| Abstract form           | x86-64 Register | Usage         | Preserved accross function calls |
|-------------------------|-----------------|---------------|----------------------------------|
| <i>res<sub>0</sub></i>  | %rax            | return value* | No                               |
| <i>arg<sub>1</sub></i>  | %rdi            | argument 1    | No                               |
| <i>arg<sub>2</sub></i>  | %rsi            | argument 2    | No                               |
| <i>arg<sub>3</sub></i>  | %rdx            | argument 3    | No                               |
| <i>arg<sub>4</sub></i>  | %rcx            | argument 4    | No                               |
| <i>arg<sub>5</sub></i>  | %r8             | argument 5    | No                               |
| <i>arg<sub>6</sub></i>  | %r9             | argument 6    | No                               |
| <i>ler<sub>7</sub></i>  | %r10            | caller-saved  | No                               |
| <i>ler<sub>8</sub></i>  | %r11            | caller-saved  | No                               |
| <i>lee<sub>9</sub></i>  | %rbx            | callee-saved  | Yes                              |
| <i>lee<sub>10</sub></i> | %rbp            | callee-saved  | Yes                              |
| <i>lee<sub>11</sub></i> | %r12            | callee-saved  | Yes                              |
| <i>lee<sub>12</sub></i> | %r13            | callee-saved  | Yes                              |
| <i>lee<sub>13</sub></i> | %r14            | callee-saved  | Yes                              |
| <i>lee<sub>14</sub></i> | %r15            | callee-saved  | Yes                              |
|                         | %rsp            | stack pointer | Yes                              |

# What about callee?

- Function must preserve callee-save registers
- Could just save them all in prolog, restore them all at epilog

# What about callee?

- Function must preserve callee-save registers
- Could just save them all in prolog, restore them all at epilog
- Wasted work for leaf functions, etc.
- Instead use power of register allocator (i.e., spilling and coalescing)

– if they are not used, they become nops

– If there is register pressure, then they will be spilled. (assuming spilling cost is calculated right.)

f:  $t1 \leftarrow lee_9$   
 $t2 \leftarrow lee_{10}$

...  
 $lee_{10} \leftarrow t2$

$lee_9 \leftarrow t1$

# What about callee?

- Function must preserve callee-save registers
- Could just save them all in prolog, restore them all at epilog
- Wasted work for leaf functions, etc.
- Instead use power of register allocator (i.e., spilling and coalescing)
- What this means for 'ret'?

# What about callee?

- Function must preserve callee-save registers
- Could just save them all in prolog, restore them all at epilog
- Wasted work for leaf functions, etc.
- Instead use power of register allocator (i.e., spilling and coalescing)
- What this means for `ret`: All callee-registers are considered used by ret.

# Coloring Order?

| Abstract form            | x86-64 Register | Usage         | Preserved accross function calls |
|--------------------------|-----------------|---------------|----------------------------------|
| <i>res</i> <sub>0</sub>  | %rax            | return value* | No                               |
| <i>arg</i> <sub>1</sub>  | %rdi            | argument 1    | No                               |
| <i>arg</i> <sub>2</sub>  | %rsi            | argument 2    | No                               |
| <i>arg</i> <sub>3</sub>  | %rdx            | argument 3    | No                               |
| <i>arg</i> <sub>4</sub>  | %rcx            | argument 4    | No                               |
| <i>arg</i> <sub>5</sub>  | %r8             | argument 5    | No                               |
| <i>arg</i> <sub>6</sub>  | %r9             | argument 6    | No                               |
| <i>ler</i> <sub>7</sub>  | %r10            | caller-saved  | No                               |
| <i>ler</i> <sub>8</sub>  | %r11            | caller-saved  | No                               |
| <i>lee</i> <sub>9</sub>  | %rbx            | callee-saved  | Yes                              |
| <i>lee</i> <sub>10</sub> | %rbp            | callee-saved* | Yes                              |
| <i>lee</i> <sub>11</sub> | %r12            | callee-saved  | Yes                              |
| <i>lee</i> <sub>12</sub> | %r13            | callee-saved  | Yes                              |
| <i>lee</i> <sub>13</sub> | %r14            | callee-saved  | Yes                              |
| <i>lee</i> <sub>14</sub> | %r15            | callee-saved  | Yes                              |
|                          | %rsp            | stack pointer | Yes                              |

# **%rax? %eax? %al**

- So, far 32-bits in %eax
- Spilling callee-save registers, however, requires saving %rax.

# Coloring Order?

| Abstract form            | x86-64 Register | Usage         | Preserved accross function calls |
|--------------------------|-----------------|---------------|----------------------------------|
| <i>res</i> <sub>0</sub>  | %rax            | return value* | No                               |
| <i>arg</i> <sub>1</sub>  | %rdi            | argument 1    | No                               |
| <i>arg</i> <sub>2</sub>  | %rsi            | argument 2    | No                               |
| <i>arg</i> <sub>3</sub>  | %rdx            | argument 3    | No                               |
| <i>arg</i> <sub>4</sub>  | %rcx            | argument 4    | No                               |
| <i>arg</i> <sub>5</sub>  | %r8             | argument 5    | No                               |
| <i>arg</i> <sub>6</sub>  | %r9             | argument 6    | No                               |
| <i>ler</i> <sub>7</sub>  | %r10            | caller-saved  | No                               |
| <i>ler</i> <sub>8</sub>  | %r11            | caller-saved  | No                               |
| <i>lee</i> <sub>9</sub>  | %rbx            | callee-saved  | Yes                              |
| <i>lee</i> <sub>10</sub> | %rbp            | callee-saved* | Yes                              |
| <i>lee</i> <sub>11</sub> | %r12            | callee-saved  | Yes                              |
| <i>lee</i> <sub>12</sub> | %r13            | callee-saved  | Yes                              |
| <i>lee</i> <sub>13</sub> | %r14            | callee-saved  | Yes                              |
| <i>lee</i> <sub>14</sub> | %r15            | callee-saved  | Yes                              |
|                          | %rsp            | stack pointer | Yes                              |

# Today

- Calling Conventions
- Activation Frames
- IR for Function Calls
- **Putting it all together**

# The power function

```
int pow(int b, int e)
//@requires e >= 0;
{
    if (e == 0)
        return 1;
    else
        return b * pow(b, e-1);
}
```

```
pow(b,e):
    if (e == 0) then done else recurse
done:
    ret 1
recurse:
    t0 <- e - 1
    t1 <- pow(b, t0)
    t2 <- b * t1
    ret t2
```

# Initial Translation with def/use

| program                                | def    | use      |
|--|--------|----------|
| pow( $b, e$ ) :                        | $b, e$ |          |
| if ( $e == 0$ ) then done else recurse |        | $e$      |
| done :                                 |        |          |
| ret 1                                  |        |          |
| recurse :                              |        |          |
| $t_0 \leftarrow e - 1$                 | $t_0$  | $e$      |
| $t_1 \leftarrow \text{pow}(b, t_0)$    | $t_1$  | $b, t_0$ |
| $t_2 \leftarrow b * t_1$               | $t_2$  | $b, t_1$ |
| ret $t_2$                              |        | $t_2$    |



# Calculating liveness

| program                                | def    | use      | live-in  |
|--|--------|----------|----------|
| pow( $b, e$ ):                         | $b, e$ |          |          |
| if ( $e == 0$ ) then done else recurse |        | $e$      |          |
| done:                                  |        |          |          |
| ret 1                                  |        |          |          |
| recurse:                               |        |          |          |
| $t_0 \leftarrow e - 1$                 | $t_0$  | $e$      |          |
| $t_1 \leftarrow \text{pow}(b, t_0)$    | $t_1$  | $b, t_0$ |          |
| $t_2 \leftarrow b * t_1$               | $t_2$  | $b, t_1$ | $b, t_1$ |
| ret $t_2$                              |        | $t_2$    | $t_2$    |

# Calculating liveness

| program                                    | def                 | use              | live-in          |
|--|---------------------|------------------|------------------|
| <code>pow(<i>b</i>, <i>e</i>) :</code>     | <i>b</i> , <i>e</i> |                  |                  |
| if ( <i>e</i> == 0) then done else recurse |                     | <i>e</i>         |                  |
| done :                                     |                     |                  |                  |
| ret 1                                      |                     |                  |                  |
| recurse :                                  |                     |                  |                  |
| $t_0 \leftarrow e - 1$                     | $t_0$               | <i>e</i>         |                  |
| $t_1 \leftarrow \text{pow}(b, t_0)$        | $t_1$               | <i>b</i> , $t_0$ | <i>b</i> , $t_0$ |
| $t_2 \leftarrow b * t_1$                   | $t_2$               | <i>b</i> , $t_1$ | <i>b</i> , $t_1$ |
| ret $t_2$                                  |                     | $t_2$            | $t_2$            |



# Calculating liveness

| program                                | def    | use      | live-in  |
|--|--------|----------|----------|
| pow( $b, e$ ) :                        | $b, e$ |          |          |
| if ( $e == 0$ ) then done else recurse |        | $e$      | $b, e$   |
| done :                                 |        |          |          |
| ret 1                                  |        |          |          |
| recurse :                              |        |          | $b, e$   |
| $t_0 \leftarrow e - 1$                 | $t_0$  | $e$      | $b, e$   |
| $t_1 \leftarrow \text{pow}(b, t_0)$    | $t_1$  | $b, t_0$ | $b, t_0$ |
| $t_2 \leftarrow b * t_1$               | $t_2$  | $b, t_1$ | $b, t_1$ |
| ret $t_2$                              |        | $t_2$    | $t_2$    |

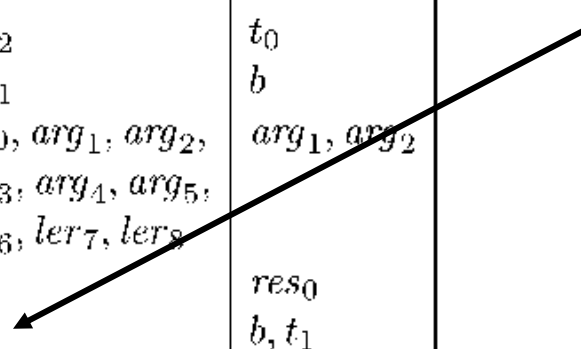
# Next: Arguments & retval explicit

| program                                | def    | use      | live-in  |
|--|--------|----------|----------|
| <code>pow(b, e) :</code>               | $b, e$ |          |          |
| if ( $e == 0$ ) then done else recurse |        | $e$      | $b, e$   |
| done :                                 |        |          |          |
| ret 1                                  |        |          |          |
| recurse :                              |        |          | $b, e$   |
| $t_0 \leftarrow e - 1$                 | $t_0$  | $e$      | $b, e$   |
| $t_1 \leftarrow \text{pow}(b, t_0)$    | $t_1$  | $b, t_0$ | $b, t_0$ |
| $t_2 \leftarrow b * t_1$               | $t_2$  | $b, t_1$ | $b, t_1$ |
| ret $t_2$                              |        | $t_2$    | $t_2$    |

# Making argument's Explicit

| program  | def   | use   |
|--|---|---|
| pow :  | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>   |   |
| <i>b</i> ← <i>arg</i> <sub>1</sub>                       | <i>b</i>  | <i>arg</i> <sub>1</sub>                           |
| <i>e</i> ← <i>arg</i> <sub>2</sub>                       | <i>e</i>  | <i>arg</i> <sub>2</sub>                           |
| if ( <i>e</i> == 0) then done else recurse               |   |   |
| done :   |   |   |
| <i>res</i> <sub>0</sub> ← 1                              | <i>res</i> <sub>0</sub>   |   |
| ret  |   | <i>res</i> <sub>0</sub>                           |
| recurse :  |   |   |
| <i>t</i> <sub>0</sub> ← <i>e</i> - 1                     | <i>t</i> <sub>0</sub>   | <i>e</i>  |
| <i>arg</i> <sub>2</sub> ← <i>t</i> <sub>0</sub>          | <i>arg</i> <sub>2</sub>   | <i>t</i> <sub>0</sub>                             |
| <i>arg</i> <sub>1</sub> ← <i>b</i>                       | <i>arg</i> <sub>1</sub>   | <i>b</i>  |
| call pow   | <i>res</i> <sub>0</sub> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> ,<br><i>arg</i> <sub>3</sub> , <i>arg</i> <sub>4</sub> , <i>arg</i> <sub>5</sub> ,<br><i>arg</i> <sub>6</sub> , <i>ler</i> <sub>7</sub> , <i>ler</i> <sub>8</sub> | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> |
| <i>t</i> <sub>1</sub> ← <i>res</i> <sub>0</sub>          | <i>t</i> <sub>1</sub>   | <i>res</i> <sub>0</sub>                           |
| <i>t</i> <sub>2</sub> ← <i>b</i> * <i>t</i> <sub>1</sub> | <i>t</i> <sub>2</sub>   | <i>b</i> , <i>t</i> <sub>1</sub>                  |
| <i>res</i> <sub>0</sub> ← <i>t</i> <sub>2</sub>          | <i>res</i> <sub>0</sub>   | <i>t</i> <sub>2</sub>                             |
| ret  |   | <i>res</i> <sub>0</sub>                           |

Missing a def



Where are callee save regs?

# Liveness

| program                                | def   | use            | live-in |
|--|---|----------------|---------|
| pow :                                  | $arg_1, arg_2$  |                |         |
| $b \leftarrow arg_1$                   | $b$   | $arg_1$        |         |
| $e \leftarrow arg_2$                   | $e$   | $arg_2$        |         |
| if ( $e == 0$ ) then done else recurse |   |                |         |
| done :                                 |   |                |         |
| $res_0 \leftarrow 1$                   | $res_0$   |                |         |
| ret                                    |   | $res_0$        |         |
| recurse :                              |   |                |         |
| $t_0 \leftarrow e - 1$                 | $t_0$   | $e$            |         |
| $arg_2 \leftarrow t_0$                 | $arg_2$   | $t_0$          |         |
| $arg_1 \leftarrow b$                   | $arg_1$   | $b$            |         |
| call pow                               | $res_0, arg_1, arg_2,$<br>$arg_3, arg_4, arg_5,$<br>$arg_6, ler_7, ler_8$ | $arg_1, arg_2$ |         |
| $t_1 \leftarrow res_0$                 | $t_1$   | $res_0$        |         |
| $t_2 \leftarrow b * t_1$               | $t_2$   | $b, t_1$       |         |
| $res_0 \leftarrow t_2$                 | $res_0$   | $t_2$          |         |
| ret                                    |   | $res_0$        | $res_0$ |

# Liveness

| program                                | def   | use            | live-in           |
|--|---|----------------|-------------------|
| pow :                                  | $arg_1, arg_2$  |                |                   |
| $b \leftarrow arg_1$                   | $b$   | $arg_1$        | $arg_1, arg_2$    |
| $e \leftarrow arg_2$                   | $e$   | $arg_2$        | $b, arg_2$        |
| if ( $e == 0$ ) then done else recurse |   |                | $b, e$            |
| done :                                 |   |                |                   |
| $res_0 \leftarrow 1$                   | $res_0$   |                |                   |
| ret                                    |   | $res_0$        | $res_0$           |
| recurse :                              |   |                | $b, e$            |
| $t_0 \leftarrow e - 1$                 | $t_0$   | $e$            | $b, e$            |
| $arg_2 \leftarrow t_0$                 | $arg_2$   | $t_0$          | $b, t_0$          |
| $arg_1 \leftarrow b$                   | $arg_1$   | $b$            | $b, arg_2$        |
| call pow                               | $res_0, arg_1, arg_2,$<br>$arg_3, arg_4, arg_5,$<br>$arg_6, ler_7, ler_8$ | $arg_1, arg_2$ | $b, arg_1, arg_2$ |
| <br>                                   |   |                |                   |
| $t_1 \leftarrow res_0$                 | $t_1$   | $res_0$        | $b, res_0$        |
| $t_2 \leftarrow b * t_1$               | $t_2$   | $b, t_1$       | $b, t_1$          |
| $res_0 \leftarrow t_2$                 | $res_0$   | $t_2$          | $t_2$             |
| ret                                    |   | $res_0$        | $res_0$           |

# Calculating Interference Graph

| program  | def   | use   | live-in  |   |
|--|---|---|--|---|
| pow :  | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>   |   |  |   |
| <i>b</i> ← <i>arg</i> <sub>1</sub>                       | <i>b</i>  | <i>arg</i> <sub>1</sub>                           | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>            | <i>b</i> — <i>arg</i> <sub>1</sub> — <i>arg</i> <sub>2</sub>  |
| <i>e</i> ← <i>arg</i> <sub>2</sub>                       | <i>e</i>  | <i>arg</i> <sub>2</sub>                           | <i>b</i> , <i>arg</i> <sub>2</sub>                           |   |
| if ( <i>e</i> == 0) then done else recurse               |   |   | <i>b</i> , <i>e</i>  |   |
| done :   |   |   |  | <i>b</i> — <i>e</i>   |
| <i>res</i> <sub>0</sub> ← 1                              | <i>res</i> <sub>0</sub>   |   |  |   |
| ret  |   | <i>res</i> <sub>0</sub>                           | <i>res</i> <sub>0</sub>                                      | <i>b</i> — <i>res</i> <sub>0</sub>  |
| recurse :  |   |   | <i>b</i> , <i>e</i>  |   |
| <i>t</i> <sub>0</sub> ← <i>e</i> - 1                     | <i>t</i> <sub>0</sub>   | <i>e</i>  | <i>b</i> , <i>e</i>  | <i>b</i> — <i>t</i> <sub>0</sub>  |
| <i>arg</i> <sub>2</sub> ← <i>t</i> <sub>0</sub>          | <i>arg</i> <sub>2</sub>   | <i>t</i> <sub>0</sub>                             | <i>b</i> , <i>t</i> <sub>0</sub>                             |   |
| <i>arg</i> <sub>1</sub> ← <i>b</i>                       | <i>arg</i> <sub>1</sub>   | <i>b</i>  | <i>b</i> , <i>arg</i> <sub>2</sub>                           |   |
| call pow   | <i>res</i> <sub>0</sub> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> ,<br><i>arg</i> <sub>3</sub> , <i>arg</i> <sub>4</sub> , <i>arg</i> <sub>5</sub> ,<br><i>arg</i> <sub>6</sub> , <i>ler</i> <sub>7</sub> , <i>ler</i> <sub>8</sub> | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> | <i>b</i> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> | <i>b</i> — <i>arg</i> <sub>3</sub> — <i>arg</i> <sub>4</sub> — <i>arg</i> <sub>5</sub><br>— <i>arg</i> <sub>6</sub> — <i>ler</i> <sub>7</sub> — <i>ler</i> <sub>8</sub> |
| <br>   |   |   |  |   |
| <i>t</i> <sub>1</sub> ← <i>res</i> <sub>0</sub>          | <i>t</i> <sub>1</sub>   | <i>res</i> <sub>0</sub>                           | <i>b</i> , <i>res</i> <sub>0</sub>                           | <i>b</i> — <i>t</i> <sub>1</sub>  |
| <i>t</i> <sub>2</sub> ← <i>b</i> * <i>t</i> <sub>1</sub> | <i>t</i> <sub>2</sub>   | <i>b</i> , <i>t</i> <sub>1</sub>                  | <i>b</i> , <i>t</i> <sub>1</sub>                             |   |
| <i>res</i> <sub>0</sub> ← <i>t</i> <sub>2</sub>          | <i>res</i> <sub>0</sub>   | <i>t</i> <sub>2</sub>                             | <i>t</i> <sub>2</sub>  |   |
| ret  |   | <i>res</i> <sub>0</sub>                           | <i>res</i> <sub>0</sub>                                      |   |

| temp                  | interfering with   |
|-----------------------|--|
| <i>b</i>              | <i>res</i> <sub>0</sub> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> , <i>arg</i> <sub>3</sub> , <i>arg</i> <sub>4</sub> , <i>arg</i> <sub>5</sub> , <i>arg</i> <sub>6</sub> , <i>ler</i> <sub>7</sub> , <i>ler</i> <sub>8</sub> , <i>e</i> , <i>t</i> <sub>0</sub> , <i>t</i> <sub>1</sub> |
| <i>e</i>              | <i>b</i>   |
| <i>t</i> <sub>0</sub> | <i>b</i>   |
| <i>t</i> <sub>1</sub> | <i>b</i>   |
| <i>t</i> <sub>2</sub> |  |

# Where to put b?

| program  | def   | use   | live-in  |
|--|---|---|--|
| pow :  | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>   |   |  |
| <i>b</i> ← <i>arg</i> <sub>1</sub>                       | <i>b</i>  | <i>arg</i> <sub>1</sub>                           | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>            |
| <i>e</i> ← <i>arg</i> <sub>2</sub>                       | <i>e</i>  | <i>arg</i> <sub>2</sub>                           | <i>b</i> , <i>arg</i> <sub>2</sub>                           |
| if ( <i>e</i> == 0) then done else recurse               |   |   | <i>b</i> , <i>e</i>  |
| done :   |   |   |  |
| <i>res</i> <sub>0</sub> ← 1                              | <i>res</i> <sub>0</sub>   |   |  |
| ret  |   | <i>res</i> <sub>0</sub>                           | <i>res</i> <sub>0</sub>                                      |
| recurse :  |   |   | <i>b</i> , <i>e</i>  |
| <i>t</i> <sub>0</sub> ← <i>e</i> - 1                     | <i>t</i> <sub>0</sub>   | <i>e</i>  | <i>b</i> , <i>e</i>  |
| <i>arg</i> <sub>2</sub> ← <i>t</i> <sub>0</sub>          | <i>arg</i> <sub>2</sub>   | <i>t</i> <sub>0</sub>                             | <i>b</i> , <i>t</i> <sub>0</sub>                             |
| <i>arg</i> <sub>1</sub> ← <i>b</i>                       | <i>arg</i> <sub>1</sub>   | <i>b</i>  | <i>b</i> , <i>arg</i> <sub>2</sub>                           |
| call pow   | <i>res</i> <sub>0</sub> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> ,<br><i>arg</i> <sub>3</sub> , <i>arg</i> <sub>4</sub> , <i>arg</i> <sub>5</sub> ,<br><i>arg</i> <sub>6</sub> , <i>ler</i> <sub>7</sub> , <i>ler</i> <sub>8</sub> | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> | <i>b</i> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> |
| <i>t</i> <sub>1</sub> ← <i>res</i> <sub>0</sub>          | <i>t</i> <sub>1</sub>   | <i>res</i> <sub>0</sub>                           | <i>b</i> , <i>res</i> <sub>0</sub>                           |
| <i>t</i> <sub>2</sub> ← <i>b</i> * <i>t</i> <sub>1</sub> | <i>t</i> <sub>2</sub>   | <i>b</i> , <i>t</i> <sub>1</sub>                  | <i>b</i> , <i>t</i> <sub>1</sub>                             |
| <i>res</i> <sub>0</sub> ← <i>t</i> <sub>2</sub>          | <i>res</i> <sub>0</sub>   | <i>t</i> <sub>2</sub>                             | <i>t</i> <sub>2</sub>  |
| ret  |   | <i>res</i> <sub>0</sub>                           | <i>res</i> <sub>0</sub>                                      |

| temp                  | interfering with   |
|-----------------------|--|
| <i>b</i>              | <i>res</i> <sub>0</sub> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> , <i>arg</i> <sub>3</sub> , <i>arg</i> <sub>4</sub> , <i>arg</i> <sub>5</sub> , <i>arg</i> <sub>6</sub> , <i>ler</i> <sub>7</sub> , <i>ler</i> <sub>8</sub> , <i>e</i> , <i>t</i> <sub>0</sub> , <i>t</i> <sub>1</sub> |
| <i>e</i>              | <i>b</i>   |
| <i>t</i> <sub>0</sub> | <i>b</i>   |
| <i>t</i> <sub>1</sub> | <i>b</i>   |
| <i>t</i> <sub>2</sub> |  |

# Where to put b?

| program  | live-in   |
|--|---|
| pow :  | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> , <i>lee</i> <sub>9</sub> |
| push <i>lee</i> <sub>9</sub>                             | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub> , <i>lee</i> <sub>9</sub> |
| <i>b</i> ← <i>arg</i> <sub>1</sub>                       | <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>                           |
| <i>e</i> ← <i>arg</i> <sub>2</sub>                       | <i>b</i> , <i>arg</i> <sub>2</sub>  |
| if ( <i>e</i> == 0) then done else recurse               | <i>b</i> , <i>e</i>   |
| done :   |   |
| <i>res</i> <sub>0</sub> ← 1                              |   |
| goto exitpow   | <i>res</i> <sub>0</sub>   |
| recurse :  | <i>b</i> , <i>e</i>   |
| <i>t</i> <sub>0</sub> ← <i>e</i> - 1                     | <i>b</i> , <i>e</i>   |
| <i>arg</i> <sub>2</sub> ← <i>t</i> <sub>0</sub>          | <i>b</i> , <i>t</i> <sub>0</sub>  |
| <i>arg</i> <sub>1</sub> ← <i>b</i>                       | <i>b</i> , <i>arg</i> <sub>2</sub>  |
| call pow   | <i>b</i> , <i>arg</i> <sub>1</sub> , <i>arg</i> <sub>2</sub>                |
| <i>t</i> <sub>1</sub> ← <i>res</i> <sub>0</sub>          | <i>b</i> , <i>res</i> <sub>0</sub>  |
| <i>t</i> <sub>2</sub> ← <i>b</i> * <i>t</i> <sub>1</sub> | <i>b</i> , <i>t</i> <sub>1</sub>  |
| <i>res</i> <sub>0</sub> ← <i>t</i> <sub>2</sub>          | <i>t</i> <sub>2</sub>   |
| goto exitpow   | <i>res</i> <sub>0</sub>   |
| exitpow :  | <i>res</i> <sub>0</sub>   |
| pop <i>lee</i> <sub>9</sub>                              | <i>res</i> <sub>0</sub>   |
| ret  | <i>lee</i> <sub>9</sub> , <i>res</i> <sub>0</sub>                           |

- We added epilogs
- save and restore *lee*<sub>9</sub>
- Make all returns goto epilogs

# Post coloring

```
pow :  
  push lee9  
  lee9 ← arg1  
  res0 ← arg2  
  if (res0 == 0) then done else recurse  
done :  
  res0 ← 1  
  goto exitpow  
recurse :  
  res0 ← res0 - 1  
  arg2 ← res0  
  arg1 ← lee9 (redundant)  
  call pow  
  res0 ← res0 (redundant)  
  res0 ← lee9 * res0  
  res0 ← res0 (redundant)  
  goto exitpow  
exitpow :  
  pop lee9  
  ret
```

# Final

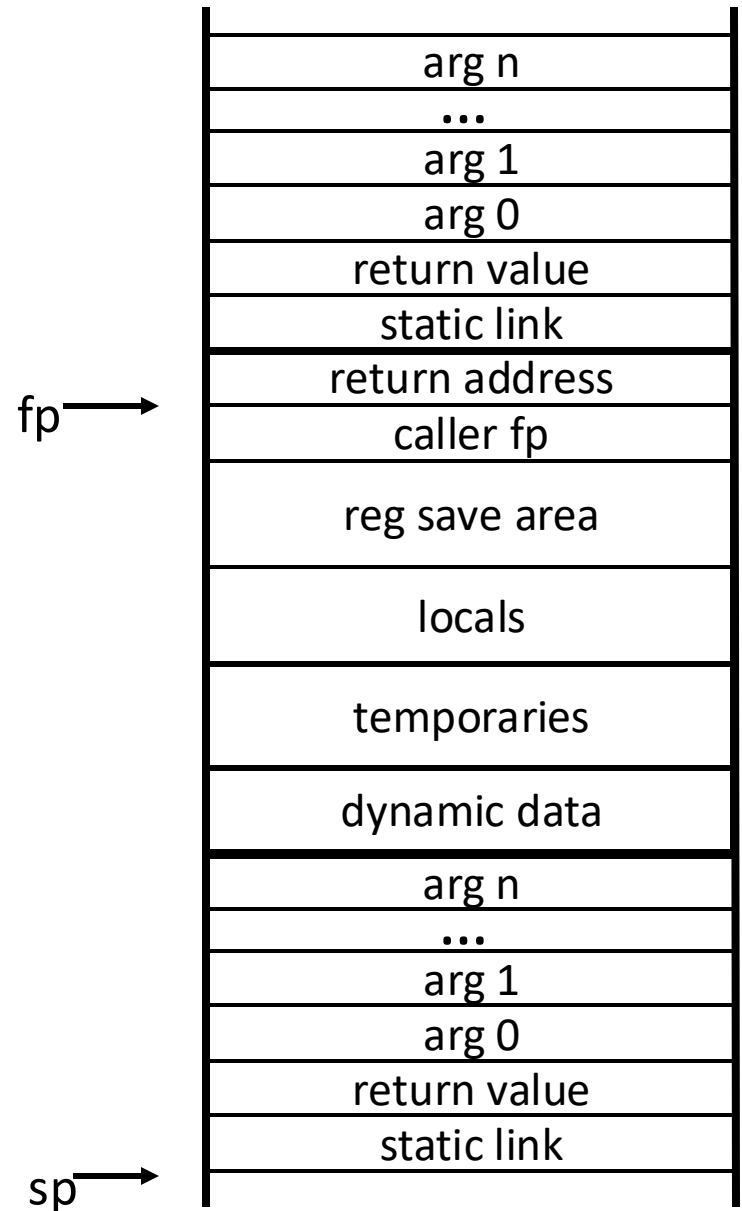
```
pow :
  push lee9
  lee9 ← arg1
  res0 ← arg2
  if (res0 == 0) then done else recurse
done :
  res0 ← 1
  goto exitpow
recurse :
  res0 ← res0 - 1
  arg2 ← res0
  arg1 ← lee9
  call pow
  res0 ← res0
  res0 ← lee9 * res0
  res0 ← res0
  goto exitpow
exitpow :
  pop lee9
  ret
```

```
pow:   pushq   %rbx
       movl   %edi, %ebx
       movl   %esi, %eax
       cmpl  $0, %eax
       jne   L1
       movl  $1, %eax
       goto  L2
L1:    subl  $1, %eax
       movl  %eax, %esi
       call  pow
       imull %ebx, %eax
L2:    popq  %rbx
       ret
```

**See you Thursday**

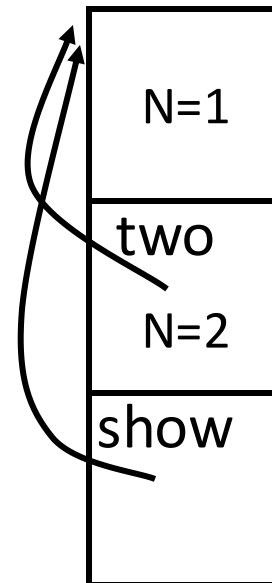
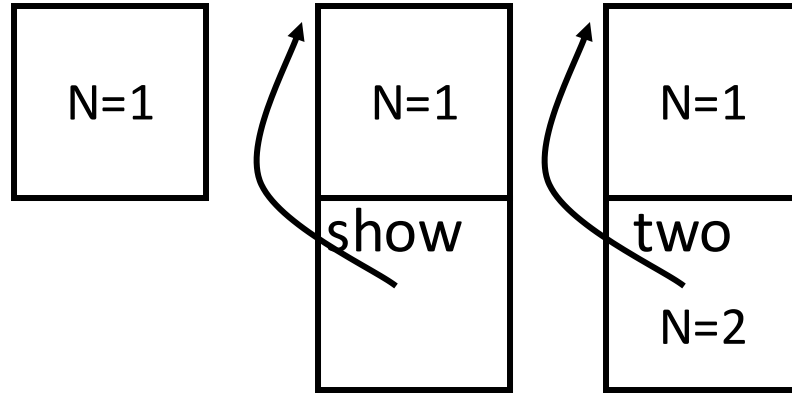
# The Static Link

- Static link used to access non-local variables for nested procedures.



# Nested Functions\*

```
void outer(void) {  
    int N = 1;  
    void show(void) {  
        print(N);  
        print(" ");  
    }  
  
    void two(void) {  
        int N = 2;  
        show();  
    }  
  
    show(); two();  
    show(); two()  
}
```



\*Lexically scoped

# Implementing Nested Functions

- Non-local names are referenced by their **level** and **offset**.
  - level is lexical nesting depth
  - offset is offset into activation frame
- During compilation names must be translated into <level,offset> pair.
  - Use block structured symbol tables
  - Track difference between current function's nesting depth and referenced names nesting depth
- At runtime, either
  - static links
  - displays

# Static Links

- Keep a link list which follows the lexical nesting depth (NOT THE SAME AS PARENT FP!)
- Can follow chain to find frame at level  $k$
- On call/return setup and teardown chain
- Caller passes pointer to lexically enclosing frame of callee.
- Maintenance cost: store (on call)
- Access cost from frame at level  $l$  to one at level  $k$ :  $(k-l)$  extra loads

# Display

- Maintain global table with size = maximum lexical nesting in program
- In prolog:
  - save  $k^{\text{th}}$  entry in display for call to function at level  $k$ .
  - Store FP in  $k^{\text{th}}$  entry in display
- In epilog:
  - restore display
- On access: one load from display to get proper frame.