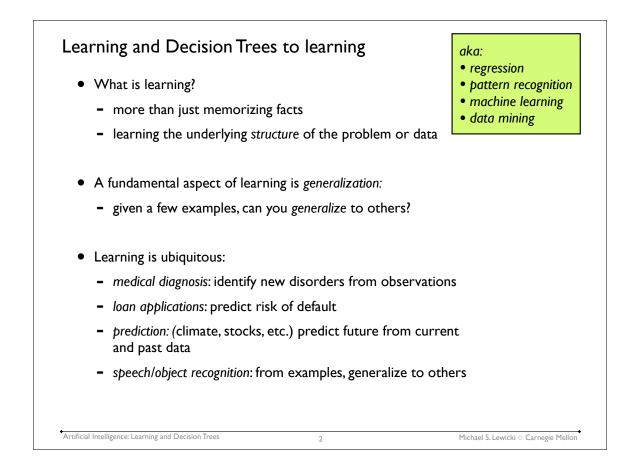
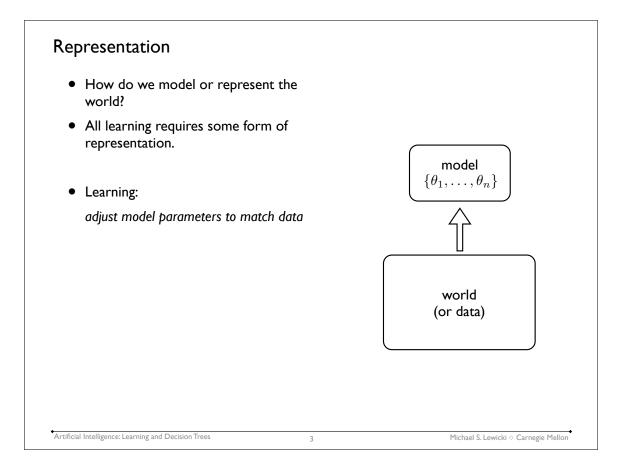
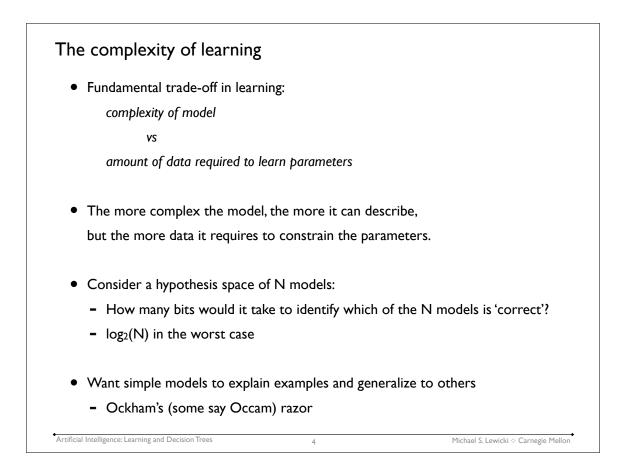
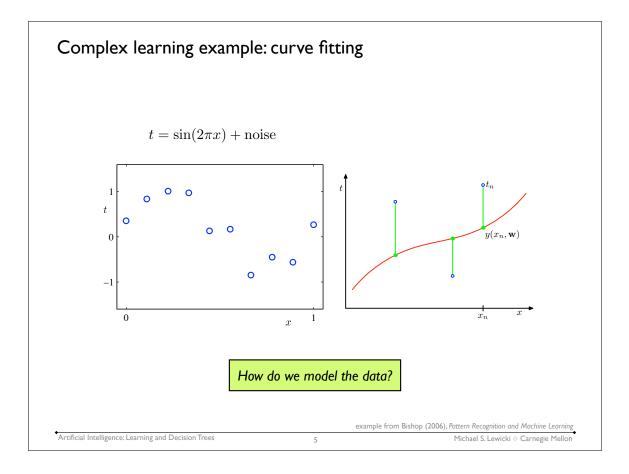
Artificial Intelligence: Representation and Problem Solving 15-381 April 10, 2007

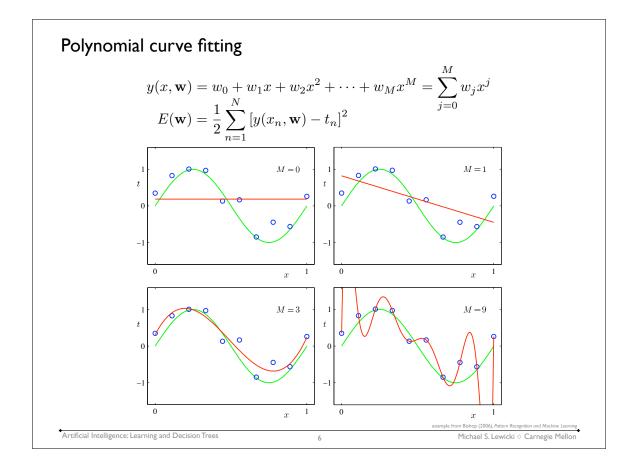
Introduction to Learning & Decision Trees

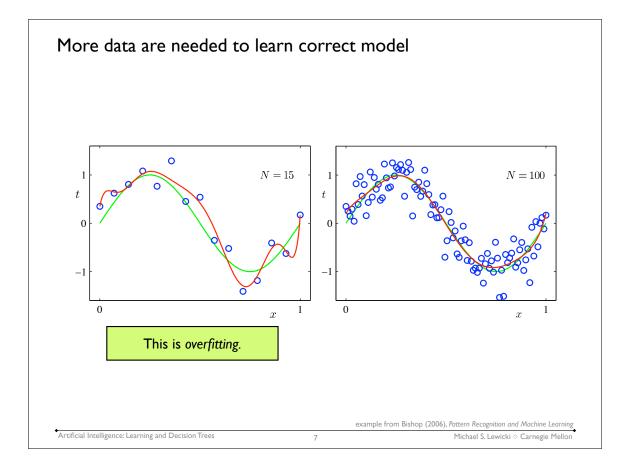


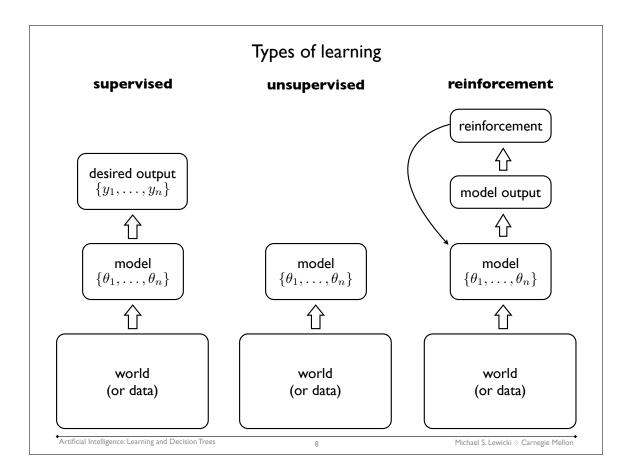


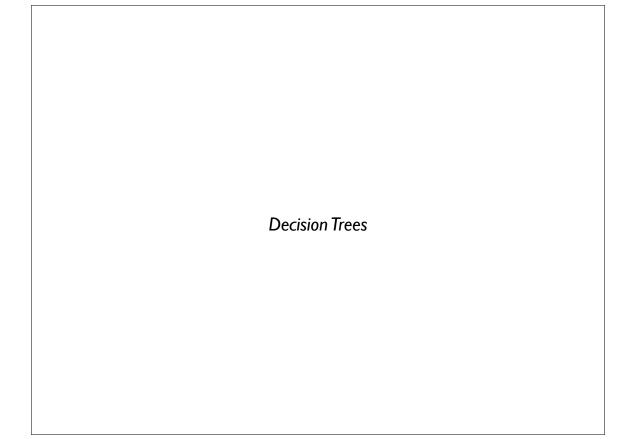


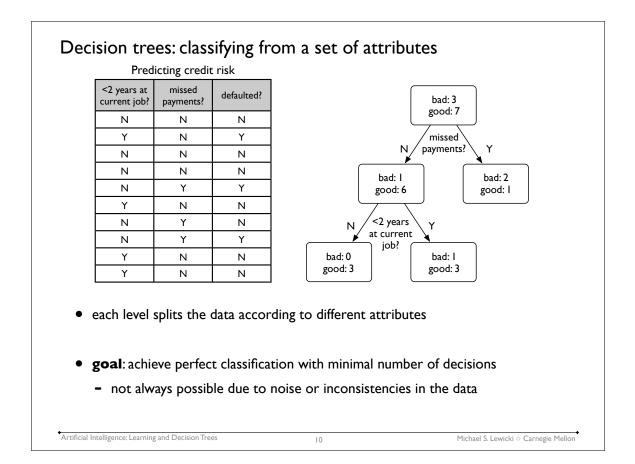




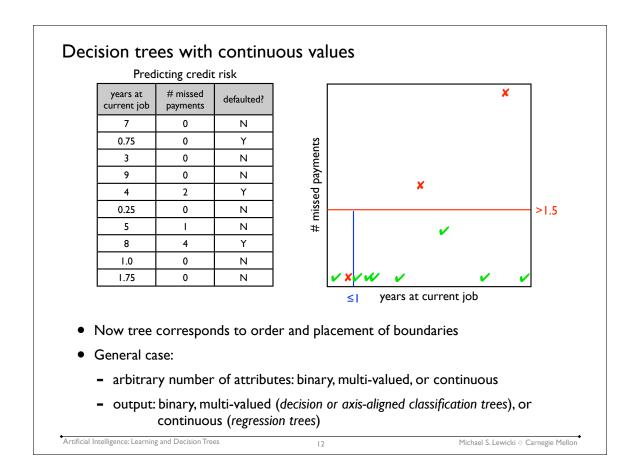








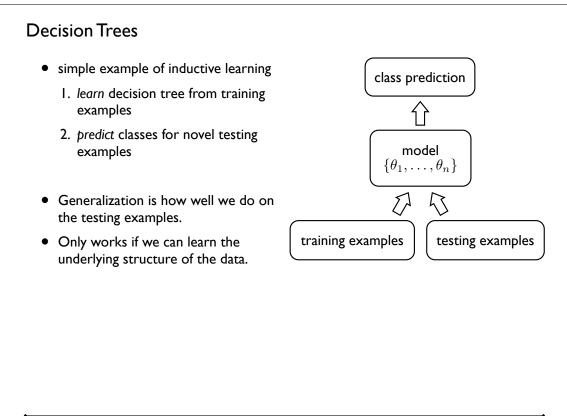
Observations		
 Any boolean function can be an not good for all functions, e.g. parity function: return 1 iff majority function: return 1 best when a small number of Note: finding optimal tree for 	an even number of inpu if more than half inputs attributes provide a lot o	its are I are I of information
		-
Artificial Intelligence: Learning and Decision Trees	II	Michael S. Lewicki \diamond Carnegie Mellor

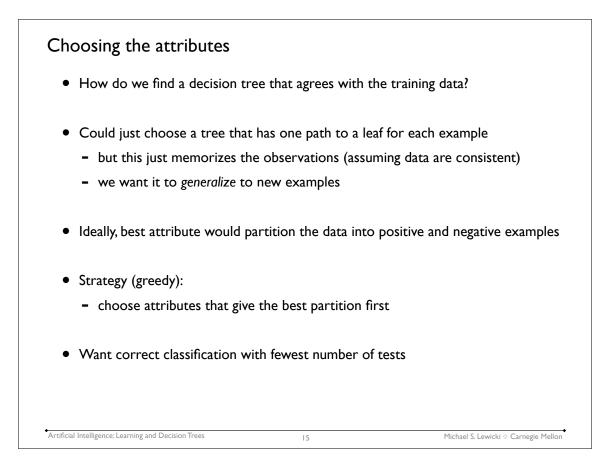


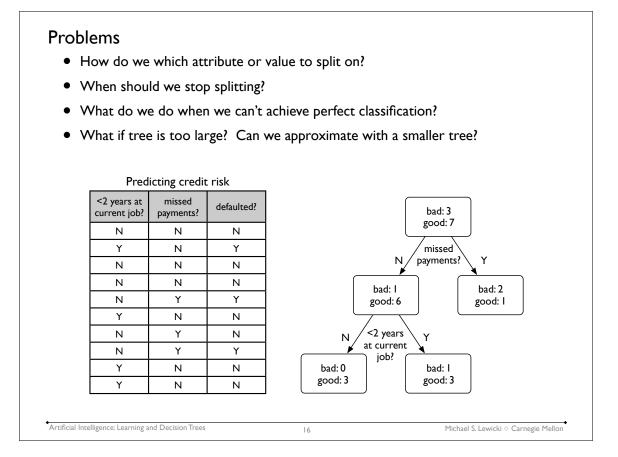
Examples

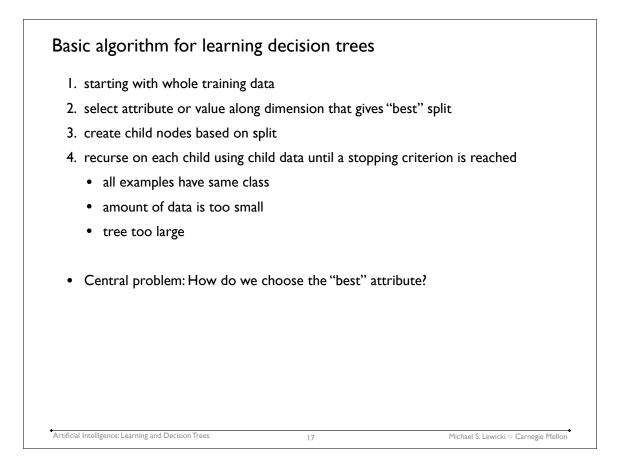
- loan applications
- medical diagnosis
- movie preferences (Netflix contest)
- spam filters
- security screening
- many real-word systems, and AI success
- In each case, we want
 - accurate classification, i.e. minimize error
 - efficient decision making, i.e. fewest # of decisions/tests
- decision sequence could be further complicated
 - want to minimize false negatives in medical diagnosis or minimize cost of test sequence
 - don't want to miss important email

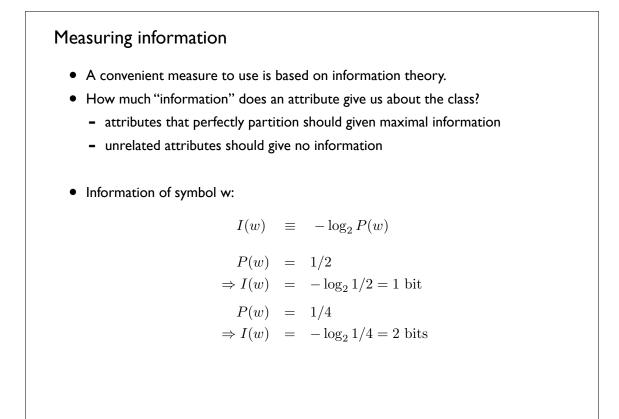




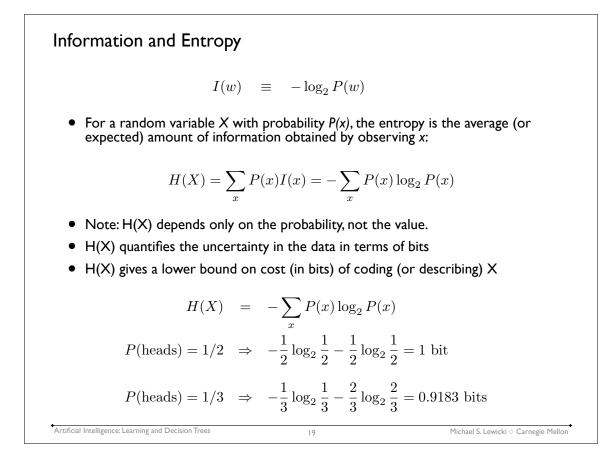


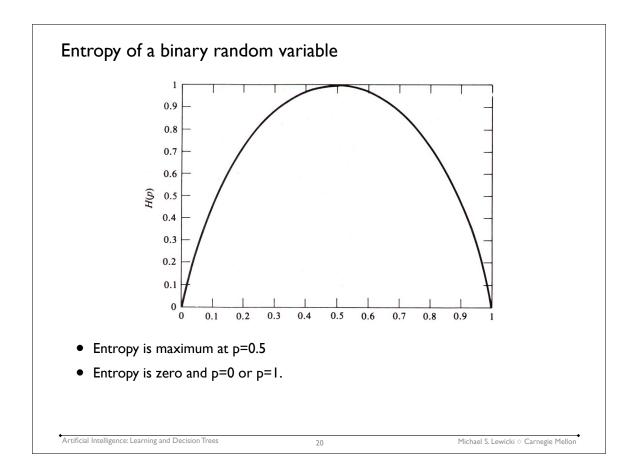


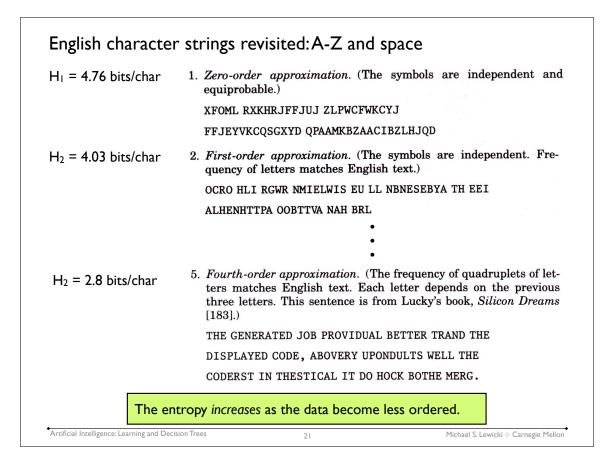


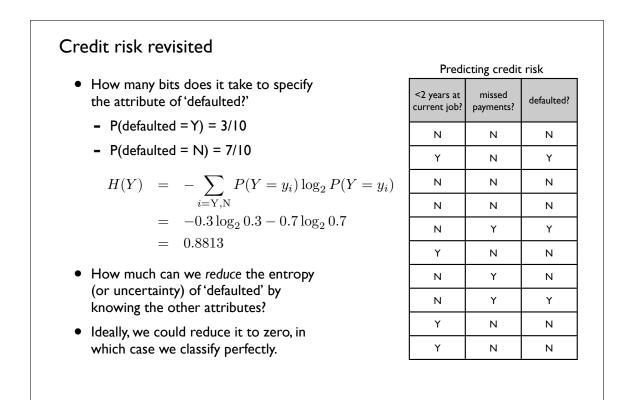


18









Artificial Intelligence: Learning and Decision Trees

Conditional entropy

• H(Y|X) is the remaining entropy of Y given X

or

The expected (or average) entropy of P(y|x)

$$H(Y|X) \equiv -\sum_{x} P(x) \sum_{y} P(y|x) \log_2 P(y|x)$$
$$= -\sum_{x} P(x) \sum_{y} P(Y=y|X=x) \log_2 P(Y=y|X=x)$$
$$= -\sum_{x} P(x) \sum_{y} H(Y|X=x)$$

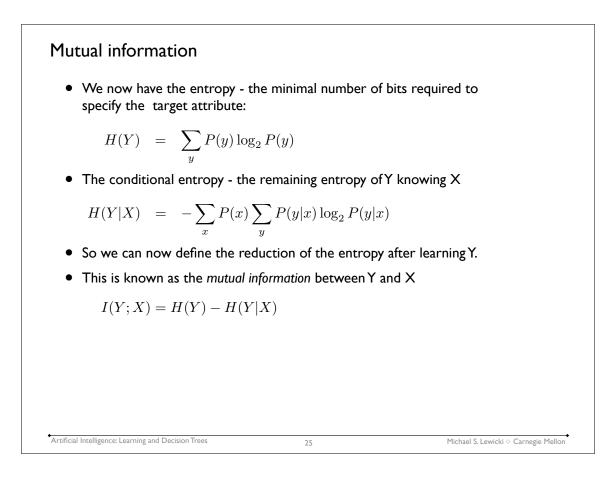
• H(Y|X=x) is the specific conditional entropy, i.e. the entropy of Y knowing the value of a specific attribute x.

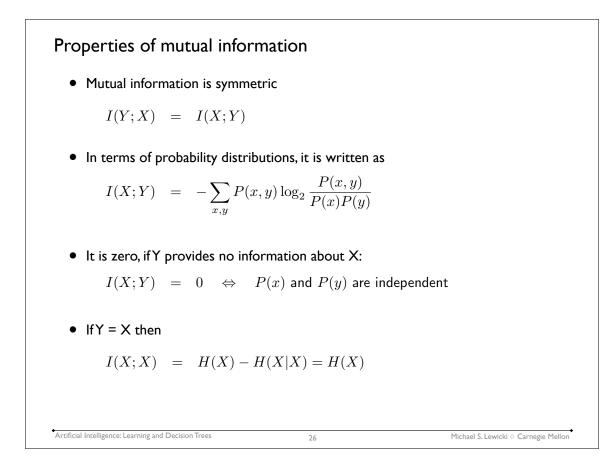
Artificial Intelligence: Learning and Decision Trees

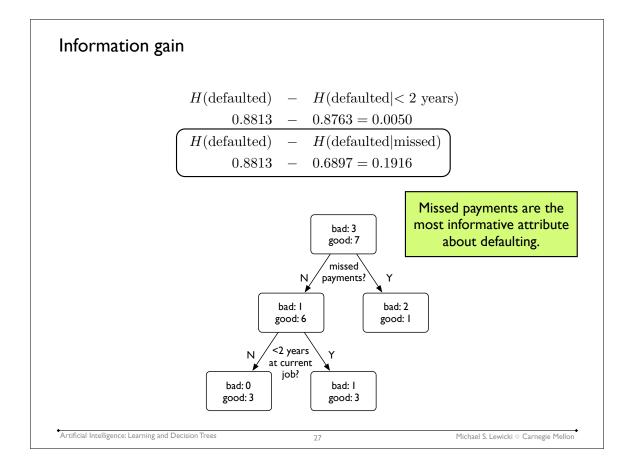
23

Michael S. Lewicki \diamond Carnegie Mellon

Back to the credit risk	example	Predicting credit risk
$= -\sum_{x}^{\overline{x}} P(x) \sum_{y}^{\overline{y}} H$ $H(\text{defaulted} < 2\text{years} = N) =$ $H(\text{defaulted} < 2\text{years} = Y) =$	$P(Y = y X = x) \log_2 P(Y = y X = x)$ $P(Y X = x)$ $-\frac{4}{4+2} \log_2 \frac{4}{4+2} - \frac{2}{6} \log_2 \frac{2}{6} = 0.9183$	<2 yrs missed def? N N N Y N Y N N N N N N N N N N N N N Y Y Y N N N Y Y Y N N N Y N N Y Y Y N N
H(defaulted missed = Y) =	$-\frac{6}{7}\log_2\frac{6}{7} - \frac{1}{7}\log_2\frac{1}{7} = 0.5917$ $-\frac{1}{3}\log_2\frac{1}{3} - \frac{2}{3}\log_2\frac{2}{3} = 0.9183$ $\frac{7}{10}0.5917 + \frac{3}{10}0.9183 = 0.6897$	Michael S. Lewicki ◊ Carnegie Mellon







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mpg	cylinders	displacement	horsepower	weight	acceleration	modelyear	maker
good	4	low	low	low	high	75to78	asia
bad	6	medium	medium	medium	medium	70to74	america
bad	4	medium	medium	medium	low	75to78	europe
bad	8	high	high	high	low	70to74	america
bad	6	medium	medium	medium	medium	70to74	america
bad	4	low	medium	low	medium	70to74	asia
bad	4	low	medium	low	low	70to74	asia
bad	8	high	high	high	low	75to78	america
:	:	:	:	:	:	:	:
:	•	:	:	:	:	:	:
:	:	:	:	:	:	:	:
bad	8	high	high	high	low	70to74	america
good	8	high	medium	high	high	79to83	america
bad	8	high	high	high	low	75to78	america
good	4	low	low	low	low	79to83	america
bad	6	medium	medium	medium	high	75to78	america
good	4	medium	low	low	low	79to83	america
good	4	low	low	medium	high	79to83	america
bad	8	high	high	high	low	70to74	america
good	4	low	medium	low	medium	75to78	europe
bad	5	medium	medium	medium	medium	75to78	europe

