

Machine-Level Programming II: Arithmetic & Control

15-213 / 18-213: Introduction to Computer Systems
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Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops

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Complete Memory Addressing Modes

- **Most General Form**
- **D(Rb,Ri,S) Mem[Reg[Rb]+S*Reg[Ri]+ D]**
 - D: Constant “displacement” 1, 2, or 4 bytes
 - Rb: Base register: Any of 8 integer registers
 - Ri: Index register: Any, except for `%esp`
 - Unlikely you’d use `%ebp`, either
 - S: Scale: 1, 2, 4, or 8 (*why these numbers?*)
- **Special Cases**
- **(Rb,Ri) Mem[Reg[Rb]+Reg[Ri]]**
- **D(Rb,Ri) Mem[Reg[Rb]+Reg[Ri]+D]**
- **(Rb,Ri,S) Mem[Reg[Rb]+S*Reg[Ri]]**

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Address Computation Examples

<code>%edx</code>	<code>0xF000</code>
<code>%ecx</code>	<code>0x0100</code>

Expression	Address Computation	Address
<code>0x8(%edx)</code>		
<code>(%edx,%ecx)</code>		
<code>(%edx,%ecx,4)</code>		
<code>0x80(,%edx,2)</code>		

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Address Computation Instruction

■ `leal Src, Dest`

- `Src` is address mode expression
- Set `Dest` to address denoted by expression

■ Uses

- Computing addresses without a memory reference
 - E.g., translation of `p = &x[i];`
- Computing arithmetic expressions of the form $x + k*y$
 - $k = 1, 2, 4, \text{ or } 8$

■ Example

```
int mul12(int x)
{
    return x*12;
}
```

Converted to ASM by compiler:

```
leal (%eax,%eax,2), %eax ;t <- x+x*2
sall $2, %eax ;return t<<2
```

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Today

- Complete addressing mode, address computation (`leal`)
- Arithmetic operations
- Control: Condition codes
- Conditional branches
- While loops

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Some Arithmetic Operations

■ Two Operand Instructions:

Format **Computation**

<code>addl</code>	<code>Src, Dest</code>	$Dest = Dest + Src$
<code>subl</code>	<code>Src, Dest</code>	$Dest = Dest - Src$
<code>imull</code>	<code>Src, Dest</code>	$Dest = Dest * Src$
<code>sall</code>	<code>Src, Dest</code>	$Dest = Dest \ll Src$
<code>sarl</code>	<code>Src, Dest</code>	$Dest = Dest \gg Src$
<code>shrl</code>	<code>Src, Dest</code>	$Dest = Dest \gg Src$
<code>xorl</code>	<code>Src, Dest</code>	$Dest = Dest \wedge Src$
<code>andl</code>	<code>Src, Dest</code>	$Dest = Dest \& Src$
<code>orl</code>	<code>Src, Dest</code>	$Dest = Dest Src$

Also called `shll`

Arithmetic

Logical

■ Watch out for argument order!

■ No distinction between signed and unsigned int (why?)

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Some Arithmetic Operations

■ One Operand Instructions

<code>incl</code>	<code>Dest</code>	$Dest = Dest + 1$
<code>decl</code>	<code>Dest</code>	$Dest = Dest - 1$
<code>negl</code>	<code>Dest</code>	$Dest = -Dest$
<code>notl</code>	<code>Dest</code>	$Dest = \sim Dest$

■ See book for more instructions

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Arithmetic Expression Example

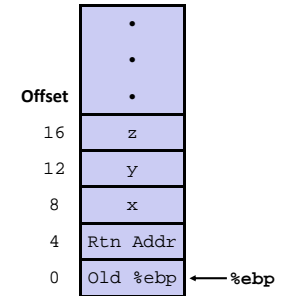
```

arith:
  pushl %ebp
  movl  %esp, %ebp
  {
    int t1 = x+y;
    int t2 = z+t1;
    int t3 = x+4;
    int t4 = y * 48;
    int t5 = t3 + t4;
    int rval = t2 * t5;
    return rval;
  }
  movl  8(%ebp), %ecx
  movl  12(%ebp), %edx
  leal  (%edx,%edx,2), %eax
  sall  $4, %eax
  leal  4(%ecx,%eax), %eax
  addl  %ecx, %edx
  addl  16(%ebp), %edx
  imull %edx, %eax
  popl  %ebp
  ret
  } Set Up
  } Body
  } Finish
    
```

Understanding arith

```

int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
    
```



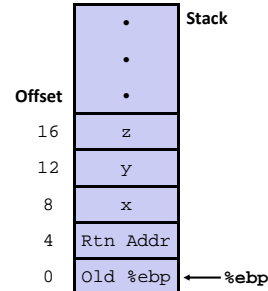
```

movl  8(%ebp), %ecx
movl  12(%ebp), %edx
leal  (%edx,%edx,2), %eax
sall  $4, %eax
leal  4(%ecx,%eax), %eax
addl  %ecx, %edx
addl  16(%ebp), %edx
imull %edx, %eax
    
```

Understanding arith

```

int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
    
```



```

movl  8(%ebp), %ecx      # ecx = x
movl  12(%ebp), %edx     # edx = y
leal  (%edx,%edx,2), %eax # eax = y*3
sall  $4, %eax          # eax *= 16 (t4)
leal  4(%ecx,%eax), %eax # eax = t4 +x+4 (t5)
addl  %ecx, %edx        # edx = x+y (t1)
addl  16(%ebp), %edx     # edx += z (t2)
imull %edx, %eax        # eax = t2 * t5 (rval)
    
```

Observations about arith

```

int arith(int x, int y, int z)
{
  int t1 = x+y;
  int t2 = z+t1;
  int t3 = x+4;
  int t4 = y * 48;
  int t5 = t3 + t4;
  int rval = t2 * t5;
  return rval;
}
    
```

- Instructions in different order from C code
- Some expressions require multiple instructions
- Some instructions cover multiple expressions
- Get exact same code when compile:
 - $(x+y+z) * (x+4+48*y)$

```

movl  8(%ebp), %ecx      # ecx = x
movl  12(%ebp), %edx     # edx = y
leal  (%edx,%edx,2), %eax # eax = y*3
sall  $4, %eax          # eax *= 16 (t4)
leal  4(%ecx,%eax), %eax # eax = t4 +x+4 (t5)
addl  %ecx, %edx        # edx = x+y (t1)
addl  16(%ebp), %edx     # edx += z (t2)
imull %edx, %eax        # eax = t2 * t5 (rval)
    
```

Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
  pushl %ebp          } Set
  movl %esp,%ebp     } Up
                                     }
  movl 12(%ebp),%eax }
  xorl 8(%ebp),%eax  } Body
  sarl $17,%eax      }
  andl $8185,%eax    }
                                     }
  popl %ebp          } Finish
  ret
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax     # eax = t1>>17 (t2)
andl $8185,%eax  # eax = t2 & mask (rval)
```

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Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
  pushl %ebp          } Set
  movl %esp,%ebp     } Up
                                     }
  movl 12(%ebp),%eax }
  xorl 8(%ebp),%eax  } Body
  sarl $17,%eax      }
  andl $8185,%eax    }
                                     }
  popl %ebp          } Finish
  ret
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax     # eax = t1>>17 (t2)
andl $8185,%eax  # eax = t2 & mask (rval)
```

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Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
  pushl %ebp          } Set
  movl %esp,%ebp     } Up
                                     }
  movl 12(%ebp),%eax }
  xorl 8(%ebp),%eax  } Body
  sarl $17,%eax      }
  andl $8185,%eax    }
                                     }
  popl %ebp          } Finish
  ret
```

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax     # eax = t1>>17 (t2)
andl $8185,%eax  # eax = t2 & mask (rval)
```

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Another Example

```
int logical(int x, int y)
{
  int t1 = x^y;
  int t2 = t1 >> 17;
  int mask = (1<<13) - 7;
  int rval = t2 & mask;
  return rval;
}
```

```
logical:
  pushl %ebp          } Set
  movl %esp,%ebp     } Up
                                     }
  movl 12(%ebp),%eax }
  xorl 8(%ebp),%eax  } Body
  sarl $17,%eax      }
  andl $8185,%eax    }
                                     }
  popl %ebp          } Finish
  ret
```

$$2^{13} = 8192, 2^{13} - 7 = 8185$$

```
movl 12(%ebp),%eax # eax = y
xorl 8(%ebp),%eax # eax = x^y (t1)
sarl $17,%eax     # eax = t1>>17 (t2)
andl $8185,%eax  # eax = t2 & mask (rval)
```

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Today

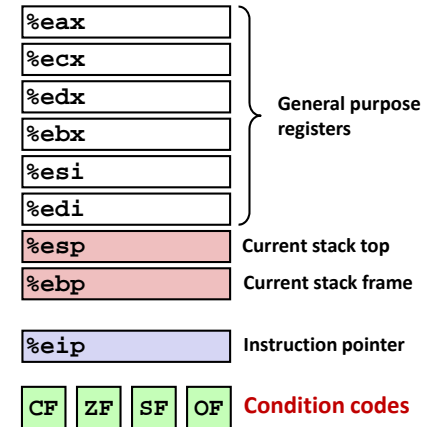
- Complete addressing mode, address computation (leal)
- Arithmetic operations
- **Control: Condition codes**
- Conditional branches
- Loops

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Processor State (IA32, Partial)

Information about currently executing program

- Temporary data (%eax, ...)
- Location of runtime stack (%ebp, %esp)
- Location of current code control point (%eip, ...)
- Status of recent tests (CF, ZF, SF, OF)



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Condition Codes (Implicit Setting)

- **Single bit registers**
 - **CF** Carry Flag (for unsigned) **SF** Sign Flag (for signed)
 - **ZF** Zero Flag **OF** Overflow Flag (for signed)
- **Implicitly set (think of it as side effect) by arithmetic operations**
 Example: `addl/addq Src, Dest` \leftrightarrow `t = a+b`
 - **CF set** if carry out from most significant bit (unsigned overflow)
 - **ZF set** if `t == 0`
 - **SF set** if `t < 0` (as signed)
 - **OF set** if two's-complement (signed) overflow
 $(a > 0 \ \&\& \ b > 0 \ \&\& \ t < 0) \ || \ (a < 0 \ \&\& \ b < 0 \ \&\& \ t \geq 0)$
- **Not set by `leal` instruction**
- [Full documentation \(IA32\)](#), link on course website

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Condition Codes (Explicit Setting: Compare)

Explicit Setting by Compare Instruction

- `cmpl / cmpq Src2, Src1`
- `cmpl b, a` like computing `a-b` without setting destination
 - **CF set** if carry out from most significant bit (used for unsigned comparisons)
 - **ZF set** if `a == b`
 - **SF set** if `(a-b) < 0` (as signed)
 - **OF set** if two's-complement (signed) overflow
 $(a > 0 \ \&\& \ b < 0 \ \&\& \ (a-b) < 0) \ || \ (a < 0 \ \&\& \ b > 0 \ \&\& \ (a-b) > 0)$

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Condition Codes (Explicit Setting: Test)

■ Explicit Setting by Test instruction

- `testl/testq Src2, Src1`
`testl b, a` like computing `a&b` without setting destination

- Sets condition codes based on value of `Src1` & `Src2`
- Useful to have one of the operands be a mask

- **ZF set** when `a&b == 0`
- **SF set** when `a&b < 0`

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Reading Condition Codes

■ SetX Instructions

- Set single byte based on combinations of condition codes

SetX	Condition	Description
<code>sete</code>	ZF	Equal / Zero
<code>setne</code>	\sim ZF	Not Equal / Not Zero
<code>sets</code>	SF	Negative
<code>setns</code>	\sim SF	Nonnegative
<code>setg</code>	\sim (SF^OF)& \sim ZF	Greater (Signed)
<code>setge</code>	\sim (SF^OF)	Greater or Equal (Signed)
<code>setl</code>	(SF^OF)	Less (Signed)
<code>setle</code>	(SF^OF) ZF	Less or Equal (Signed)
<code>seta</code>	\sim CF& \sim ZF	Above (unsigned)
<code>setb</code>	CF	Below (unsigned)

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Reading Condition Codes (Cont.)

■ SetX Instructions:

- Set single byte based on combination of condition codes

■ One of 8 addressable byte registers

- Does not alter remaining 3 bytes
- Typically use `movzbl` to finish job

```
int gt (int x, int y)
{
    return x > y;
}
```

Body

```
movl 12(%ebp),%eax # eax = y
cmpl %eax,8(%ebp) # Compare x : y
setg %al          # al = x > y
movzbl %al,%eax  # Zero rest of %eax
```

%eax	%ah	%al
------	-----	-----

%ecx	%ch	%cl
------	-----	-----

%edx	%dh	%dl
------	-----	-----

%ebx	%bh	%bl
------	-----	-----

%esi

%edi

%esp

%ebp

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Reading Condition Codes: x86-64

■ SetX Instructions:

- Set single byte based on combination of condition codes
- Does not alter remaining 3 bytes

```
int gt (long x, long y)
{
    return x > y;
}
```

```
long lgt (long x, long y)
{
    return x > y;
}
```

Bodies

```
cmpl %esi, %edi
setg %al
movzbl %al, %eax
```

```
cmpq %rsi, %rdi
setg %al
movzbl %al, %eax
```

Is %rax zero?

Yes: 32-bit instructions set high order 32 bits to 0!

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Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- Control: Condition codes
- Conditional branches & Moves
- Loops

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Jumping

■ jX Instructions

- Jump to different part of code depending on condition codes

jX	Condition	Description
jmp	1	Unconditional
je	ZF	Equal / Zero
jne	~ZF	Not Equal / Not Zero
js	SF	Negative
jns	~SF	Nonnegative
jg	~(SF^OF) & ~ZF	Greater (Signed)
jge	~(SF^OF)	Greater or Equal (Signed)
jl	(SF^OF)	Less (Signed)
jle	(SF^OF) ZF	Less or Equal (Signed)
ja	~CF & ~ZF	Above (unsigned)
jb	CF	Below (unsigned)

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Conditional Branch Example

```

int absdiff(int x, int y)
{
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
absdiff:
    pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %edx
    movl 12(%ebp), %eax
    cmpl %eax, %edx
    jle .L6
    subl %eax, %edx
    movl %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax
.L7:
    popl %ebp
    ret

```

Setup }
Body1 }
Body2a }
Body2b }
Finish }

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Conditional Branch Example (Cont.)

```

int goto_ad(int x, int y)
{
    int result;
    if (x <= y) goto Else;
    result = x-y;
    goto Exit;
Else:
    result = y-x;
Exit:
    return result;
}
absdiff:
    pushl %ebp
    movl %esp, %ebp
    movl 8(%ebp), %edx
    movl 12(%ebp), %eax
    cmpl %eax, %edx
    jle .L6
    subl %eax, %edx
    movl %edx, %eax
    jmp .L7
.L6:
    subl %edx, %eax
.L7:
    popl %ebp
    ret

```

Setup }
Body1 }
Body2a }
Body2b }
Finish }

■ C allows "goto" as means of transferring control

- Closer to machine-level programming style

■ Generally considered bad coding style

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Conditional Branch Example (Cont.)

```

int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
absdiff:
  pushl %ebp
  movl %esp, %ebp
  movl 8(%ebp), %edx
  movl 12(%ebp), %eax
  cmpl %eax, %edx
  jle .L6
  subl %eax, %edx
  movl %edx, %eax
  jmp .L7
.L6:
  subl %edx, %eax
.L7:
  popl %ebp
  ret

```

Setup
Body1
Body2a
Body2b
Finish

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Conditional Branch Example (Cont.)

```

int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
absdiff:
  pushl %ebp
  movl %esp, %ebp
  movl 8(%ebp), %edx
  movl 12(%ebp), %eax
  cmpl %eax, %edx
  jle .L6
  subl %eax, %edx
  movl %edx, %eax
  jmp .L7
.L6:
  subl %edx, %eax
.L7:
  popl %ebp
  ret

```

Setup
Body1
Body2a
Body2b
Finish

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Conditional Branch Example (Cont.)

```

int goto_ad(int x, int y)
{
  int result;
  if (x <= y) goto Else;
  result = x-y;
  goto Exit;
Else:
  result = y-x;
Exit:
  return result;
}
absdiff:
  pushl %ebp
  movl %esp, %ebp
  movl 8(%ebp), %edx
  movl 12(%ebp), %eax
  cmpl %eax, %edx
  jle .L6
  subl %eax, %edx
  movl %edx, %eax
  jmp .L7
.L6:
  subl %edx, %eax
.L7:
  popl %ebp
  ret

```

Setup
Body1
Body2a
Body2b
Finish

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General Conditional Expression Translation

C Code

```
val = Test ? Then_Expr : Else_Expr;
```

```
val = x>y ? x-y : y-x;
```

- Test is expression returning integer
 - = 0 interpreted as false
 - ≠ 0 interpreted as true
- Create separate code regions for then & else expressions
- Execute appropriate one

Goto Version

```

nt = !Test;
if (nt) goto Else;
val = Then_Expr;
goto Done;
Else:
  val = Else_Expr;
Done:
  . . .

```

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Using Conditional Moves

Conditional Move Instructions

- Instruction supports:
if (Test) Dest ← Src
- Supported in post-1995 x86 processors
- GCC does not always use them
 - Wants to preserve compatibility with ancient processors
 - Enabled for x86-64
 - Use switch `-march=686` for IA32

C Code

```
val = Test
  ? Then_Expr
  : Else_Expr;
```

Goto Version

```
tval = Then_Expr;
result = Else_Expr;
t = Test;
if (t) result = tval;
return result;
```

Why?

- Branches are very disruptive to instruction flow through pipelines
- Conditional move do not require control transfer

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Conditional Move Example: x86-64

```
int absdiff(int x, int y) {
    int result;
    if (x > y) {
        result = x-y;
    } else {
        result = y-x;
    }
    return result;
}
```

```
absdiff:
x in %edi      movl  %edi, %edx
y in %esi      subl  %esi, %edx # tval = x-y
               movl  %esi, %eax
               subl  %edi, %eax # result = y-x
               cmpl  %esi, %edi # Compare x:y
               cmovg %edx, %eax # If >, result = tval
               ret
```

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Bad Cases for Conditional Move

Expensive Computations

```
val = Test(x) ? Hard1(x) : Hard2(x);
```

- Both values get computed
- Only makes sense when computations are very simple

Risky Computations

```
val = p ? *p : 0;
```

- Both values get computed
- May have undesirable effects

Computations with side effects

```
val = x > 0 ? x*=7 : x+=3;
```

- Both values get computed
- Must be side-effect free

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Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- x86-64
- Control: Condition codes
- Conditional branches and moves
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“Do-While” Loop Example

C Code

```
int pcount_do(unsigned x)
{
    int result = 0;
    do {
        result += x & 0x1;
        x >>= 1;
    } while (x);
    return result;
}
```

Goto Version

```
int pcount_do(unsigned x)
{
    int result = 0;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
    return result;
}
```

- Count number of 1’s in argument x (“popcount”)
- Use conditional branch to either continue looping or to exit loop

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“Do-While” Loop Compilation

Goto Version

```
int pcount_do(unsigned x) {
    int result = 0;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
    return result;
}
```

```

movl $0, %ecx    # result = 0
.L2:
movl %edx, %eax  # loop:
andl $1, %eax    # t = x & 1
addl %eax, %ecx  # result += t
shrl %edx        # x >>= 1
jne .L2          # If !0, goto loop

```

Registers:
%edx x
%ecx result

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General “Do-While” Translation

C Code

```
do
    Body
while (Test);
```

Goto Version

```
loop:
    Body
    if (Test)
        goto loop
```

- Body:
 - Statement₁;
 - Statement₂;
 - ...
 - Statement_n;
- Test returns integer
 - = 0 interpreted as false
 - ≠ 0 interpreted as true

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“While” Loop Example

C Code

```
int pcount_while(unsigned x) {
    int result = 0;
    while (x) {
        result += x & 0x1;
        x >>= 1;
    }
    return result;
}
```

Goto Version

```
int pcount_do(unsigned x) {
    int result = 0;
    if (!x) goto done;
loop:
    result += x & 0x1;
    x >>= 1;
    if (x)
        goto loop;
done:
    return result;
}
```

- Is this code equivalent to the do-while version?

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General “While” Translation

While version

```
while ( Test )
  Body
```



Do-While Version

```
if (!Test)
  goto done;
do
  Body
while(Test);
done:
```



Goto Version

```
if (!Test)
  goto done;
loop:
  Body
  if (Test)
    goto loop;
done:
```

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“For” Loop Example

C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
  int i;
  int result = 0;
  for (i = 0; i < WSIZE; i++) {
    unsigned mask = 1 << i;
    result += (x & mask) != 0;
  }
  return result;
}
```

- Is this code equivalent to other versions?

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“For” Loop Form

General Form

```
for ( Init; Test; Update )
  Body
```

```
for (i = 0; i < WSIZE; i++) {
  unsigned mask = 1 << i;
  result += (x & mask) != 0;
}
```

Init

```
i = 0
```

Test

```
i < WSIZE
```

Update

```
i++
```

Body

```
{
  unsigned mask = 1 << i;
  result += (x & mask) != 0;
}
```

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“For” Loop → While Loop

For Version

```
for ( Init; Test; Update )
  Body
```



While Version

```
Init;
while ( Test ) {
  Body
  Update;
}
```

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“For” Loop → ... → Goto

For Version

```
for ( Init; Test; Update )
    Body
```



While Version

```
Init;
while ( Test ) {
    Body
    Update;
}
```



```
Init;
if (!Test)
    goto done;
do
    Body
    Update
while( Test );
done:
```

```
Init;
if (!Test)
    goto done;
loop:
    Body
    Update
    if ( Test )
        goto loop;
done:
```



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“For” Loop Conversion Example

C Code

```
#define WSIZE 8*sizeof(int)
int pcount_for(unsigned x) {
    int i;
    int result = 0;
    for (i = 0; i < WSIZE; i++) {
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    return result;
}
```

Goto Version

```
int pcount_for_gt(unsigned x) {
    int i;
    int result = 0;
    i = 0;
    if (! (i < WSIZE)) !Test
        goto done;
    loop:
        Body
        unsigned mask = 1 << i;
        result += (x & mask) != 0;
    }
    i++;
    if (i < WSIZE) Test
        goto loop;
done:
    return result;
}
```

- Initial test can be optimized away

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Summary

Today

- Complete addressing mode, address computation (leal)
- Arithmetic operations
- Control: Condition codes
- Conditional branches & conditional moves
- Loops

Next Time

- Switch statements
- Stack
- Call / return
- Procedure call discipline

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