Translating between Decimal and binary floating point Hunter Pitelka January 24, 2010

From Binary to Decimal

Fill in	the table below with th	હ binary num	nber						
S	exponent		fra	ction					_
1. Fill	in the following values:								
•	number of exponent bi	ts: $k = _{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_{_$		_					
•	unsigned value of the e	exponent: exp	$\rho = 0$						
	Bias value for exponen								
2. Is th	e exponent (exp) :								
•	All 1's ?								
	– If the fraction is al	ll 0's the valu	ie is =	Ł∞					
	- if the fraction is no	onzero, the va	alue i	s NaN	V				
•	All 0's? Denormal	ized							
	- Exponent is $e = 1$	– Bias =							
	- Fraction is $frac =$	$0.\{fractional\}$	l Com	nponen	at fro	m ab	$ove \}$		
	Your answer is:	$0.frac \times 2^e$							
•	Something else: Norm	ıalized							
	$-e = exp$ -Bias $=$ _								
	- Fraction has implied	ed leading on	e: 1.{	[fracti	on al	comp	onen	t from	above
	Your answer is:	$1.frac \times 2^e$							

From Decimal to Binary

Wri	te	do	wn	$th\epsilon$	e bi	naı	у е	equ	iliva	len	t o	fу	ou	r nu	ıml	er	(the	ere :	sho	uld	be a	decir	nal	poin	ıt soı	newh	ere h	iere)	
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1.																										$\times 2$			_
• N	o	w fi	ll iı	n th	ne f	ollo	wi	ng	valı	ies:																			
	-	- N	um	ber	of	ex	poi	nen	t bi	ts a	val	ial	ole	<i>k</i> =						_									
	_	- N	ow	cal	cul	ate	yc	ur	exp	one	ent:																		
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														$= e^{-\frac{1}{2}}$								_							
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You're all set! Now just write out the binary number as:

Sign bit - exponent bits - fractional bits

Round to Even: Put a decimal place between the last bit you can keep and the first bit you have to throw away. You'll have x.5, you have to end up with y.0. Where y must be even. Just round towards the nearest even number. $2.5 \rightarrow 2.0$, $3.5 \rightarrow 4.0$, $.5 \rightarrow 0.0$.