15-494/694: Cognitive Robotics

Dave Touretzky

Lecture 9:

Path Planning with Rapidly-exploring Random Trees

Navigating with the Pilot

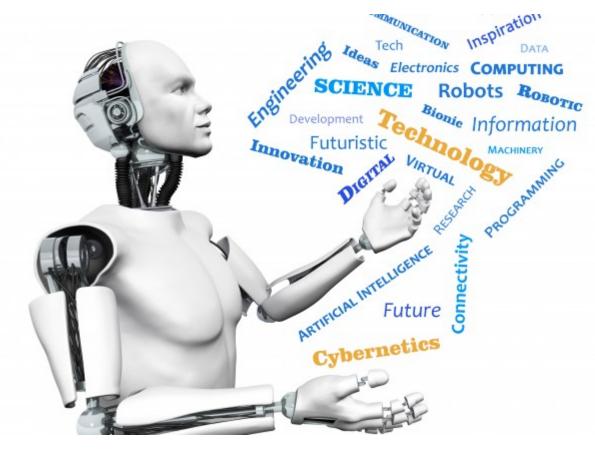


Image from http://www.futuristgerd.com/2015/09/10

Outline

- How is path planning used in robotics?
- Path planning as state space search
- RRTs: Rapidly-exploring Random Trees
- The RRT-Connect algorithm
- Collision detection
- Smoothing
- Path planning with constraints
- Navigating with the Pilot

Path Planning in Robotics

1. Navigation path planning

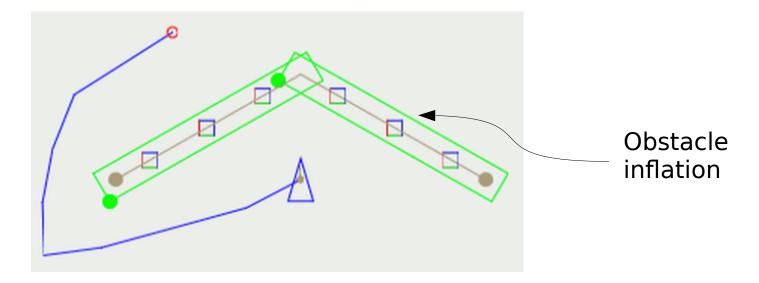
- How to get from the robot's current location to a goal.
- Avoid obstacles.
- Provide for localization.

2. Manipulation path planning

- Move an arm to grasp and manipulate an object.
- Avoid obstacles.
- Obey constraints (e.g., don't spill the coffee).

Navigation Planning

- 2D state space: (x,y) coordinates of the robot
 - Treat the robot as a point or a circle.



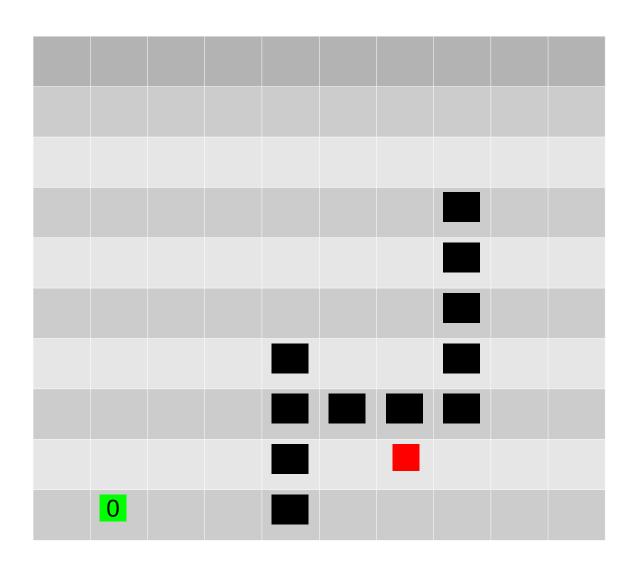
- 3D state space: (x,y,θ) pose of the robot
 - Heading matters when the robot is asymmetric
 - Heading matters when the robot's motion is constrained

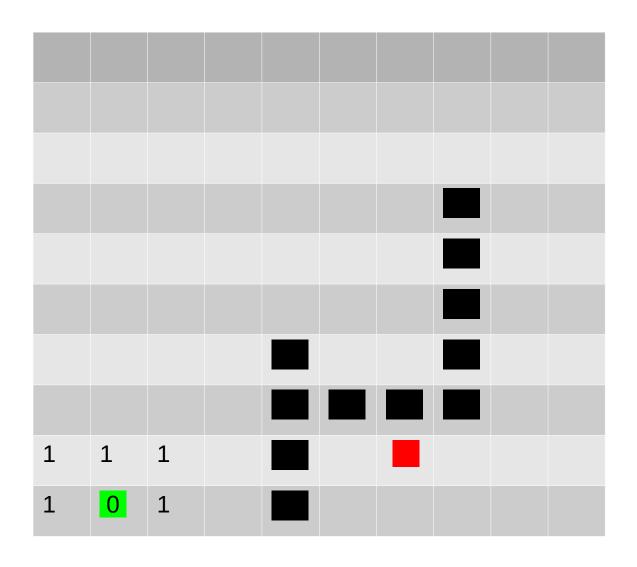
Grid-Based Path Planning

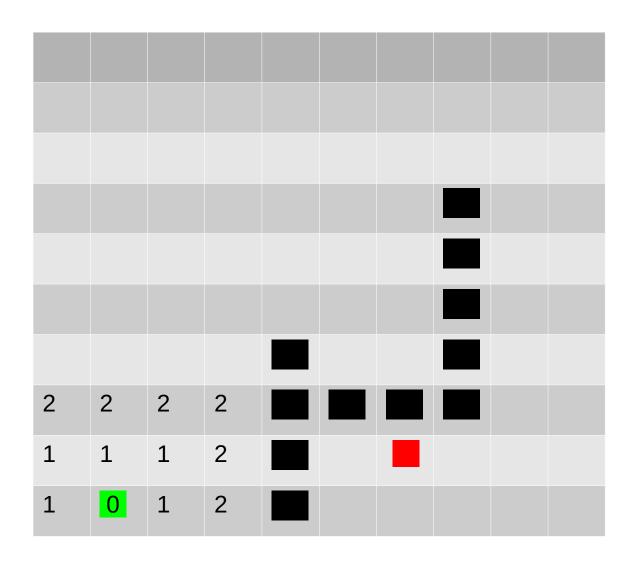
- Discretizes the environment into a 2D grid.
- Wavefront algorithm: propagate from the start location.
- Can also used best-first or A* search.
- Works okay in small spaces.

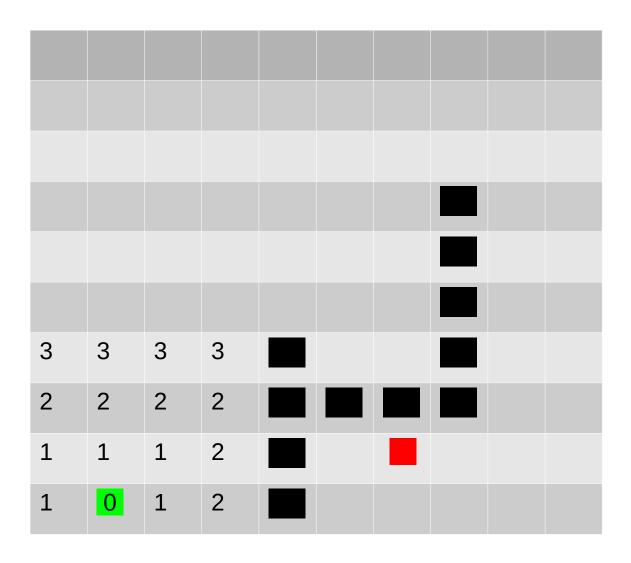
But it has its drawbacks:

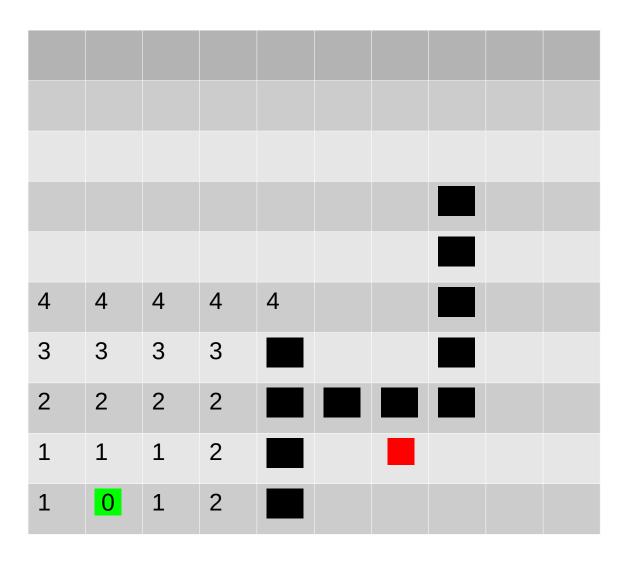
- Treats the robot as a point. Unrealistic!
- Not efficient in higher dimensional state spaces.











9	9	9	9	9	9	9	9	9	10
8	8	8	8	8	8	8	8	9	10
7	7	7	7	7	7	7	8	9	10
6	6	6	6	6	6	7		9	10
5	5	5	5	5	6	7		10	10
4	4	4	4		6	7		11	11
3	3	3	3		7	7		12	12
2	2	2	2					13	13
1	1	1	2			15	14	14	14
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Best-First or A* Search

Works okay in small spaces.

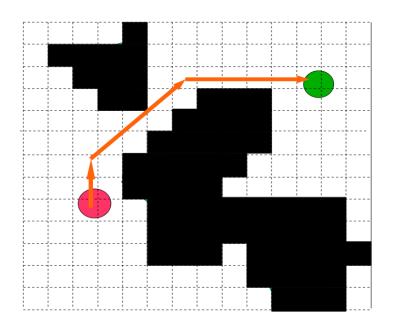


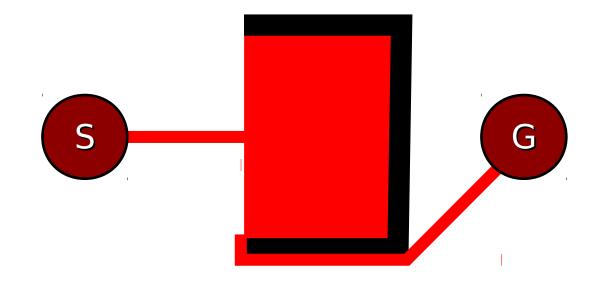
Figure from http://www.gamasutra.com/blogs/MattKlingensmith/ 20130907/199787/Overview of Motion Planning.php

Same drawbacks as wavefront:

- Treats the robot as a point. Unrealistic!
- Not efficient in higher dimensional state spaces.

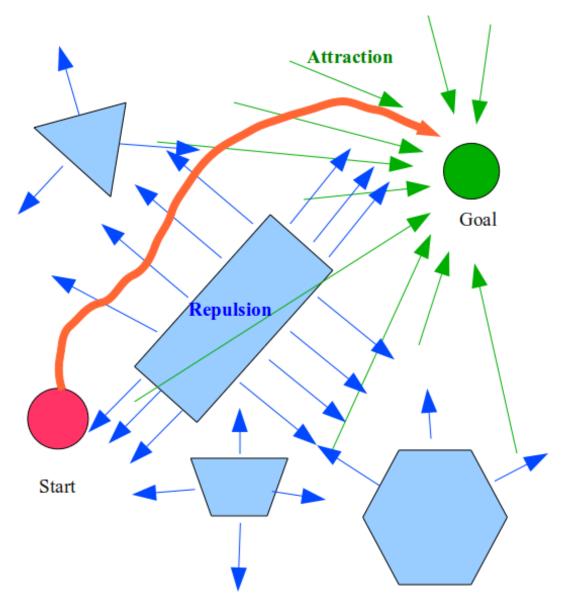
Best First or A* Search Can Be Slow

Can get trapped in a cul de sac for a long time.



- See search animation videos on YouTube.
- Random search might be faster.

Potential Field Path Planning



- Can fail due to local minima in the potential function.
- Consider a U-shaped obstacle.
- Requires careful tuning.

Cspace Transform

 The area around an obstacle that would cause a collision with the robot.

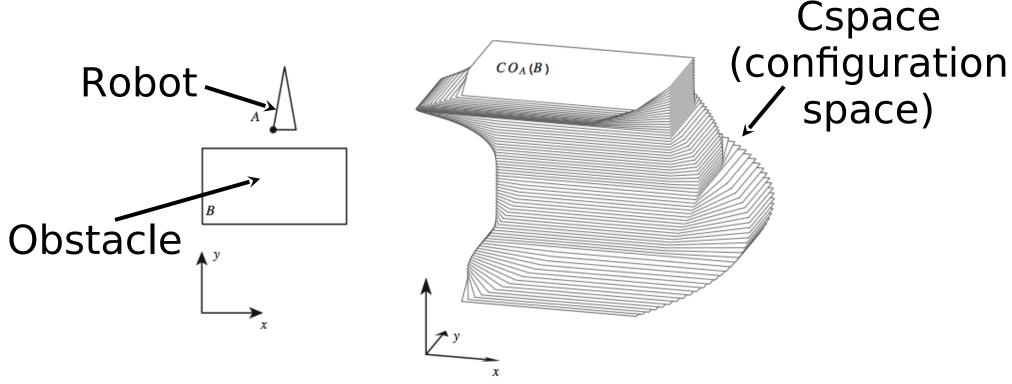
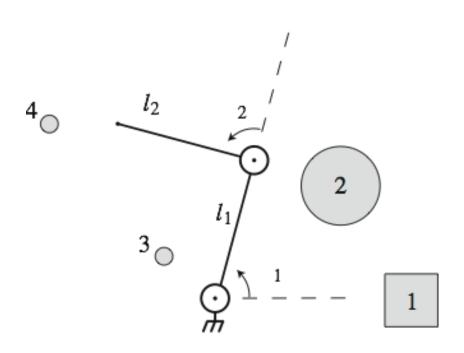


Figure 4.4 - Mason, Mechanics Of Robotic Manipulation

Arm Path Planning

Cspace transform blocks out regions of joint space



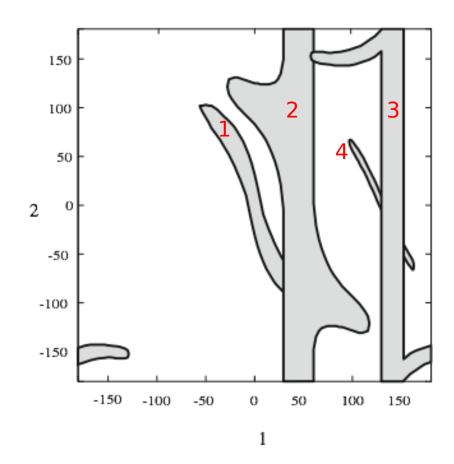


Figure 4.5 - Mason, Mechanics Of Robotic Manipulation

State Space Search

The path planning problem:

Given an n-dimensional state space and

- a start state $S = \langle s_1, s_2, ..., s_n \rangle$
- a goal state $G = \langle g_1, g_2, ..., g_n \rangle$
- an admissibility predicate P (collision test + constraints)

find a path from S to G such that every state on the path satisfies P.

Rapidly-exploring Random Trees

- Described in LaValle (1998), Kuffner & LaValle (2000)
- Create a tree with initial state S as the root.
- Repeat up to K times:

Pick a point \mathbf{q}_{rand} in configuration space:

- Sometimes \mathbf{q}_{rand} is really random
- Sometimes \mathbf{q}_{rand} is the goal G
- Find $\mathbf{q}_{\text{nearest}}$, the closest node to \mathbf{q}_{rand}
- Add a new node \mathbf{q}_{new} by extending $\mathbf{q}_{\text{nearest}}$ some distance Δ toward \mathbf{q}_{rand} .
- If \mathbf{q}_{new} is close enough to the goal G, return.

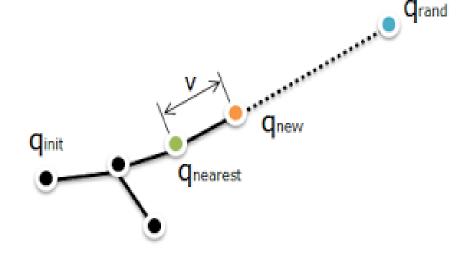
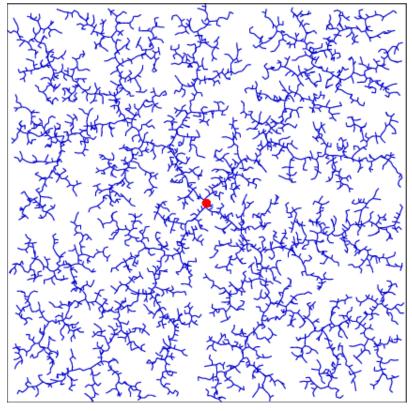


Image from http://joonlecture.blogspot.com/2011/02/improving-optimality-of-rrt-rrt.html

RRT Algorithm

- Rapidly samples the state space.
- Cannot get trapped in local minima.
- Works well in high-dimensional spaces.
- Does not generate smooth paths.
- Can't tell when no solution exists; only quits when it exceeds the iteration limit K.

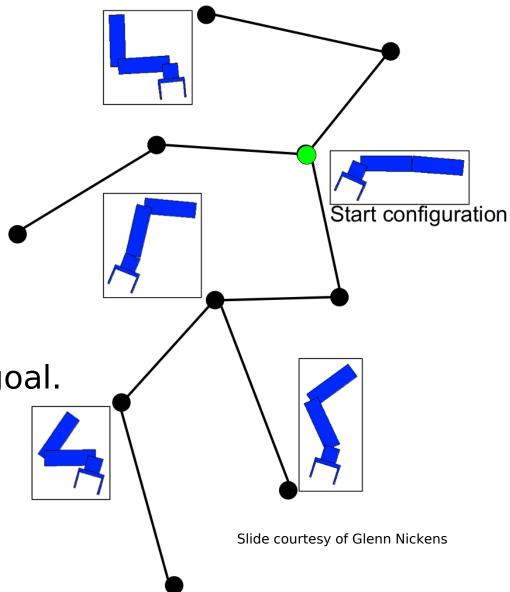


http://msl.cs.uiuc.edu/rrt/treemovie.gif

RRTs for Arm Path Planning

- Each node encodes an arm configuration in joint space.
- Only add nodes that don't cause collisions (with self or obstacles).

 Alternately (i) extend the tree in random directions and (ii) move toward the goal.

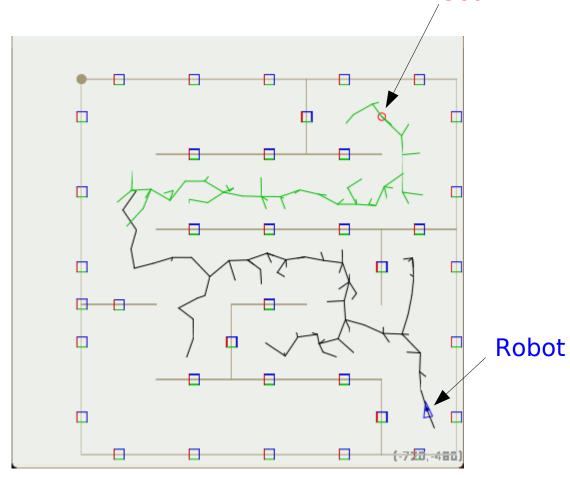


Implementation Notes

- Finding $\mathbf{q}_{\text{nearest}}$, the nearest node in the tree to \mathbf{q}_{rand} , is the most expensive part of the algorithm.
 - Use K-D trees to efficiently find $\mathbf{q}_{\text{nearest}}$?
 - In practice, K-D trees are slower unless you have a huge number of nodes (several thousand).
- Why only go a distance Δ toward the goal state G? Why not go as far as we can, in steps of Δ ?
 - With no obstacles, this reaches the goal very quickly, but random search will get there nearly as quickly as we keep extending the nearest node to the goal.
 - But when obstacles are present, this can waste time filling out branches that will ultimately fail.
 - Generating lots of extra nodes bloats the tree, which slows down the algorithm.

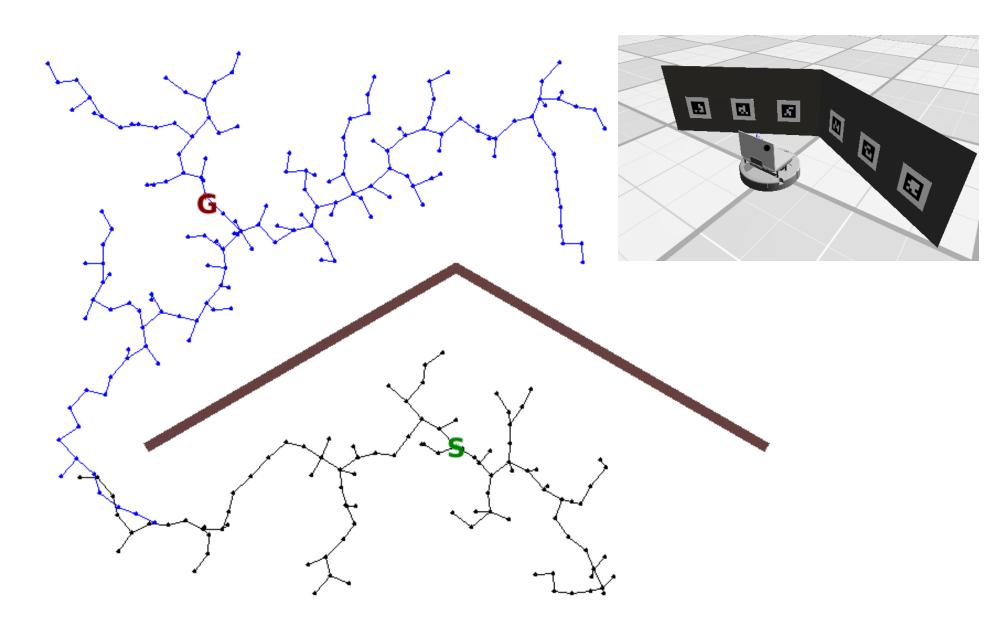
RRT-Connect Algorithm

- Variant of RRT that grows two trees:
 - one from the start state toward the goal
 - one from the goal state toward the start
- When the two trees connect, a solution has been found.
- Not guaranteed to be better than RRT, but often helps.



Goal

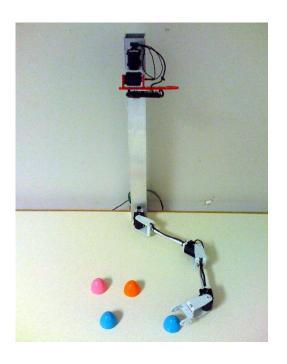
RRTs in An Open Field

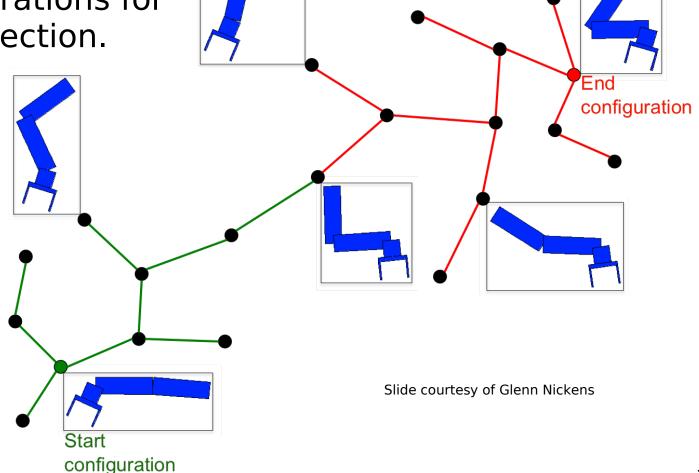


RRT-Connect For Arms

 Use IK to calculate the goal configuration.

 Use FK to calculate arm configurations for collision detection.





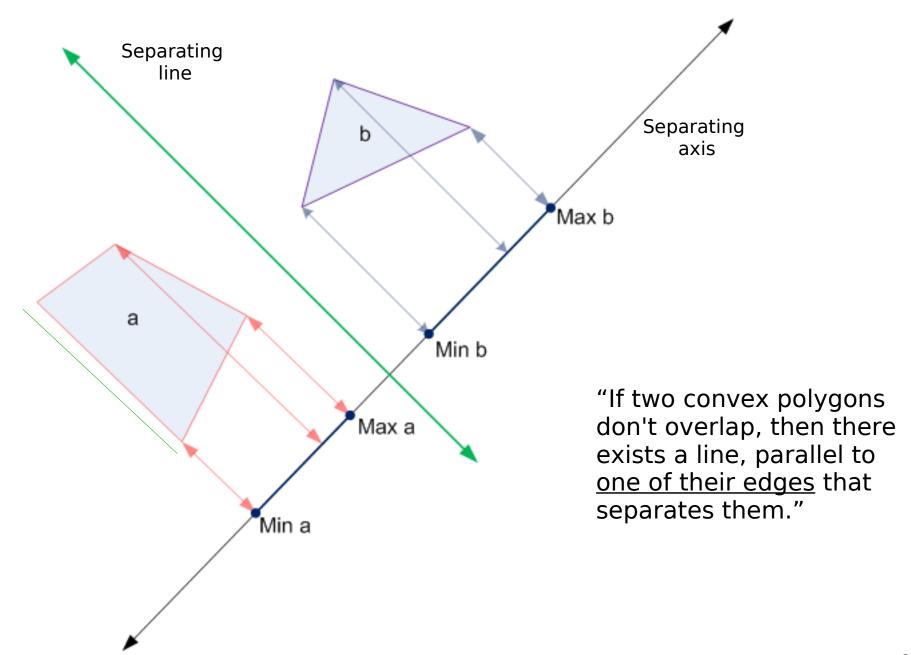
Collision Detection

- Represent the robot and the obstacles as convex polygons.
- In 2D, use the Separating Axis Theorem to check for collisions.
 - Easy to code
 - Fast to compute
- In 3D, things get more complex.
 - Tekkotsu uses the GJK (Gilbert-Johnson-Keerthi) algorithm, used in many physics engines for video games.

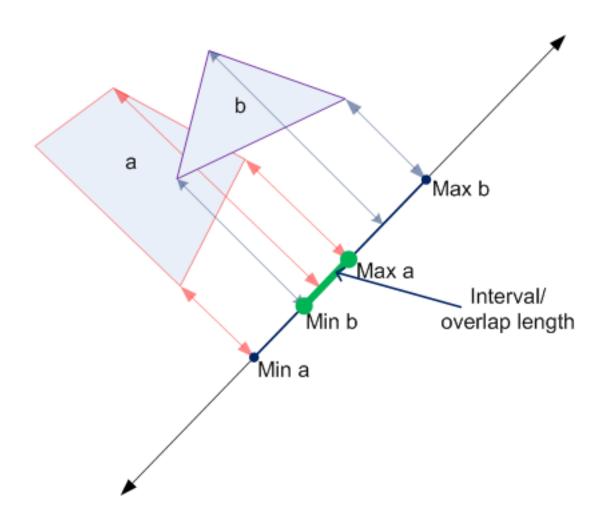
Algorithm to Apply the SAT

- For every edge of polygon A and of polygon B:
 - Project all the vertices onto the line normal to that edge.
 - Calculate the min and max coordinates for each polygon
 - If minA < minB and maxA > minB OR if minB < minA and maxB > minA then the polygons collide.
- If you find any edge projection in which the ranges don't overlap, the polygons do not collide.

Separating Axis Theorem

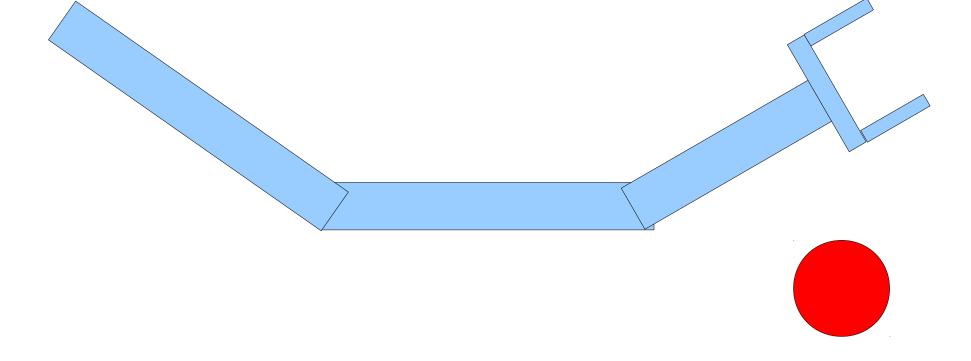


Separating Axis Theorem



Arm Collision Detection

- Represent each link as a separate polygon.
- · Check for:
 - Self-collisions other than link n with link n+1
 - Collisions of a link with an obstacle

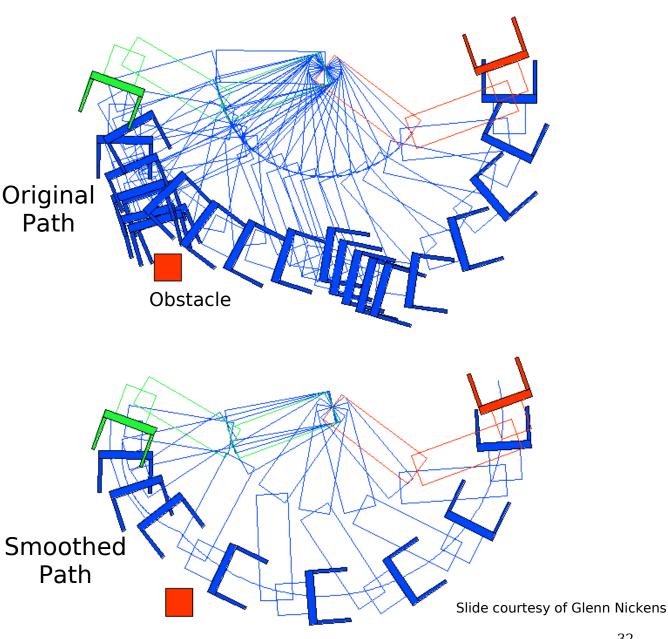


Path Smoothing

- The random component of RRT-Connect search often results in a jerky and meandering solution.
- Solution: apply a path smoothing algorithm.
- Repeat N times:
 - Pick two points on the path at random
 - See if we can linearly interpolate between those points without collisions.
 - If so, then snip out that segment of the path.

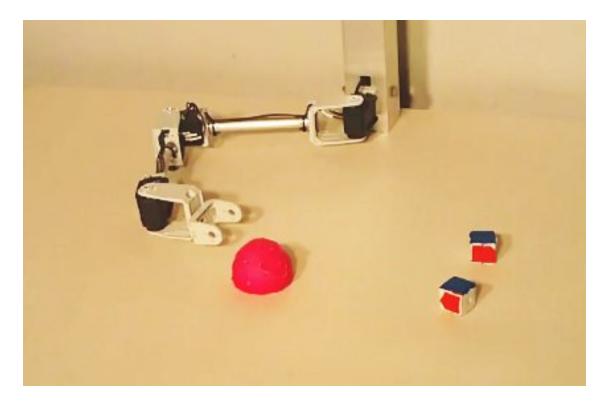
Smoothing An Arm Trajectory

- Start state
- Intermed. states
- End state



Path Planning With Constraints

 With no closeable fingers, arm motion is constrained to be within about 60° of finger direction or we'll lose the object.



(video)

http://www.youtube.com/watch?v=9oDQ754YVoc

Implementing Constraints

- Each time we generate a new state q_{new}:
 - Check to see if \mathbf{q}_{new} obeys the constraint.
 - For finger motion constraint, check if the direction of motion from parent state q_{nearest} to new state q_{new} is within 60° of the finger direction.
- What if q_{new} doesn't obey the constraint?
 - Reject it and pick a new \mathbf{q}_{rand} from which we'll generate a new \mathbf{q}_{new} .
 - Or try to "fix" \mathbf{q}_{new} by perturbing its value slightly so as to satisfy the constraint.

Path Planning Failure

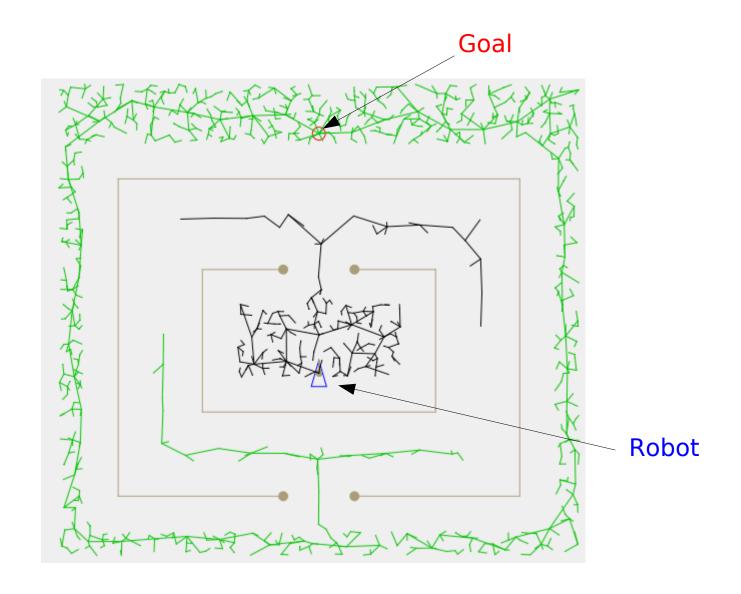
RRT path planning can legitimately fail if:

- There is no route to the goal due to obstacles blocking every path from start to goal.
- The paths to the goal don't lie entirely within the allowed world bounds (world map too small).

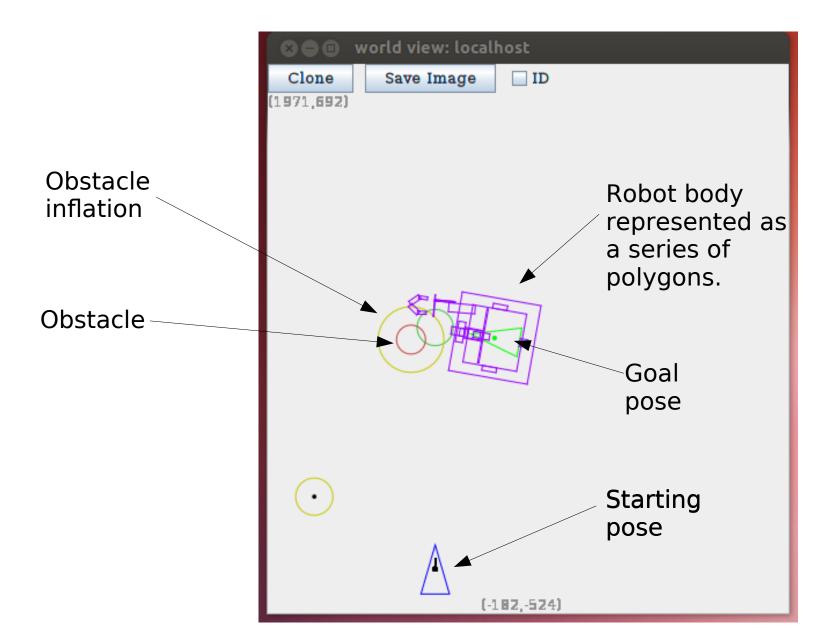
But it can also fail if:

- The iteration limit was set too low.
- The start state is already in collision with something.
- The goal state is in collision with something.

Running Out of Iterations



Path Planning Failure: Goal State Is In Collision



Full 3D Path Planning: The Piano Movers Problem



Figure from http://www.gamasutra.com/blogs/MattKlingensmith/20130907/199787/Overview of Motion Planning.php

Open Motion Planning Library: http://ompl.kavrakilab.org

The Pilot

- Navigation utility defined in cozmo fsm/pilot.fsm
- How to go from A to B:
 - Generate obstacle list from current world map.
 - Use RRT-Connect to plan a path from A to B?
 - Good in open spaces; has trouble with doorways.
 - Formulate a navigation plan to follow the path.
 - Straight segments
 - Turns
 - Arcs
 - Landmark checks
 - Execute the navigation plan, correcting as necessary.
 - Report success or failure.

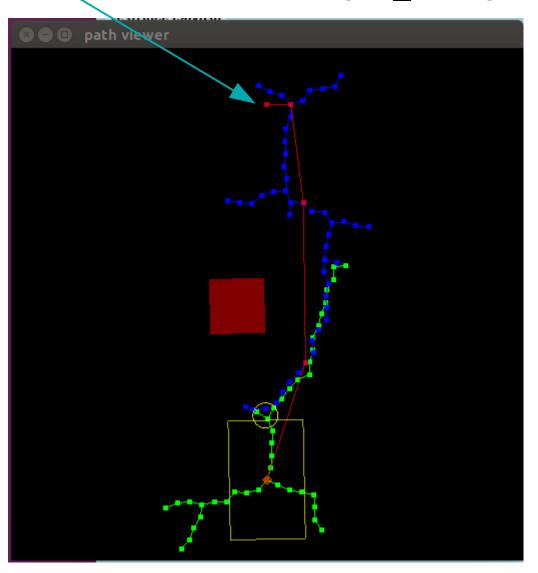
PilotToPose Node

- State node for invoking the Pilot.
- Tell it where you want to go, and (optionally) the desired heading at the destination.
- Use a heading of NaN if you don't care.
- =PILOT=> transition can check for errors.

```
go: PilotToPose(Pose(500, 0, 0, angle_z=degrees(90)))
go =C=> Say("Success")
go =PILOT(StartCollides)=> Say("Start collides!")
```

Path Viewer

PilotToPose(Pose(300, 0, 0, angle_z=degrees(90)))



Hybrid Path-Planner

- cozmo-tools now uses a hybrid path planner.
- Check for StartCollides condition and use RRT to find a maneuver that disengages from the obstacle, e.g., move away from a wall.
- Wavefront algorithm finds a route to the goal using large obstacle inflation. Easily goes through doorways.
- RRT post-processing:
 - Check for collisions using actual robot shape and less inflation
 - Generate a condensed path with fewer steps
- Check for doorway crossing and insert "doorpass" steps in the navigation plan.