

## Planning-II

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- Plan-space search
- Comparison
- Graphplan, Satplan

*These lecture slides should be complemented with the examples discussed and worked out on the blackboard during the lecture.*

## Outline: Selecting ACTIONS

- Planning algorithms
- Comparison of planning algorithms
- Learning in planning
- Planning, execution, and learning
- Behavior-based (reactive) planning
- Action selection in multiagent systems

## Plan-Space Partial-Order Nonlinear Planning

SNLP Planning Algorithm McAllester & Rosenblitt 91

1. Terminate if the goal set is empty.
2. Select a goal  $g$  from the goal set and identify the plan step that needs it,  $S_{need}$ .
3. Let  $S_{add}$  be a step (operator) that adds  $g$ , either a new step or a step that is already in the plan. Add the causal link  $S_{add} \xrightarrow{g} S_{need}$ , constrain  $S_{add}$  to come before  $S_{need}$ , and enforce bindings that make  $S_{add}$  add  $g$ .

## Plan-Space Partial-Order Nonlinear Planning

4. Update the goal set with **all** the preconditions of the step  $S_{add}$ , and delete  $g$ .
5. Identify *threats* and resolve the conflicts by adding ordering or bindings constraints.
  - A step  $S_k$  threatens a causal link  $S_i \xrightarrow{g} S_j$  when it occurs between  $S_i$  and  $S_j$ , and it adds or deletes  $p$ .
  - Resolve threats by using *promotion*, *demotion*, or *separation*.

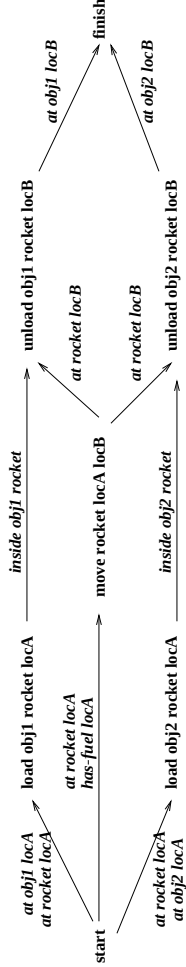
## Linking and Solving Threats

- Linking - which operator (step) adds a goal
- Threats:
  - Step  $S_1$  needs  $p$ , Step  $S_2$  deletes  $p$ .
  - Step  $S_1$  adds  $p$  (in causal link), Step  $S_2$  deletes  $p$ .

## Plan-space Planning

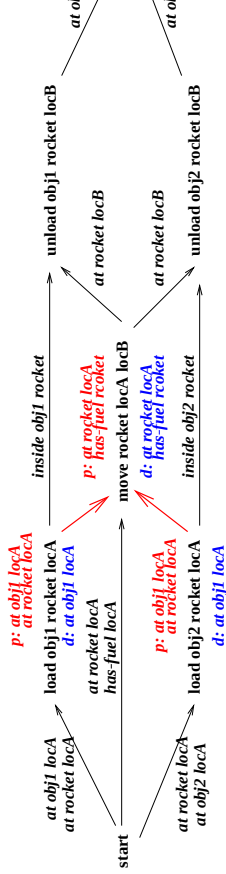
- Complete, sound, and optimal.
- Optimal handling of goal orderings.

## Plan-space Planning



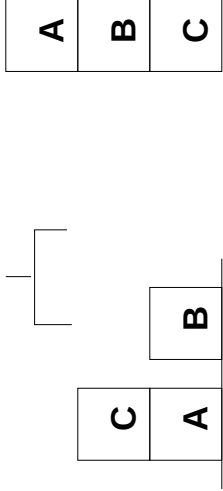
Example - LINKING

## Plan-space Planning



Example - THREATS

Sussman Anomaly



Comparison of Planning Algorithms

- Complete nonlinear state-space planning
- Plan-space planning
- Graphplan
- Satplan
- And more

Is there a *universally* best planning algorithm?

State-space and Plan-space

- Planning is NP-hard.
- Two different planning approaches: state-space and plan-space planning

|                                       | State-space | Plan-space  |
|---------------------------------------|-------------|-------------|
| Commitments in plan step orderings    | Yes         | No          |
| Therefore, suffer with goal orderings | Yes         | No          |
| Therefore, handle goal interactions   | Poorly      | Efficiently |

Step Ordering Commitments

WHY?

Use of the STATE of the world while planning

In Prodigy4.0 advantages include:

- Means-ends analysis - plan for goals that reduce the differences between current and goal states.
- Informed selection of operators - select operators that need less planning work than others.
- State useful for learning, generation and match of conditions supporting informed decisions.
- Helpful for generating anytime planning - provide *valid*, executable, plans at any time.

Parallel between Commitments - Example

|                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                             |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Operator Polish<br>preconds: ()<br>adds: polished<br>deletes: ()                                                                                                                                                        | Operator Drill-Hole<br>preconds: ()<br>adds: has-hole<br>deletes: polished                                                                                                                                                                                                  |
| Goal: polished and has-hole<br>Initial state: empty<br>Prodigy4.0                                                                                                                                                       | Goal: polished and has-hole<br>Initial state: polished<br>SNLP                                                                                                                                                                                                              |
| - plan for goal polished<br>- select Polish<br>• order Polish as first step<br>- plan for goal has-hole<br>- select Drill-Hole<br>• order Drill-Hole > Polish<br>• polished deleted, backtrack<br>- Polish > Drill-Hole | - plan for goal polished<br>- select Initial state<br>• link Initial to polished<br>- plan for goal has-hole<br>- select Drill-Hole<br>• link Drill-Hole to has-hole<br>• threat - relink polished<br>- select Polish<br>- link Polish to polished<br>- Polish > Drill-Hole |

Serializability and Linkability

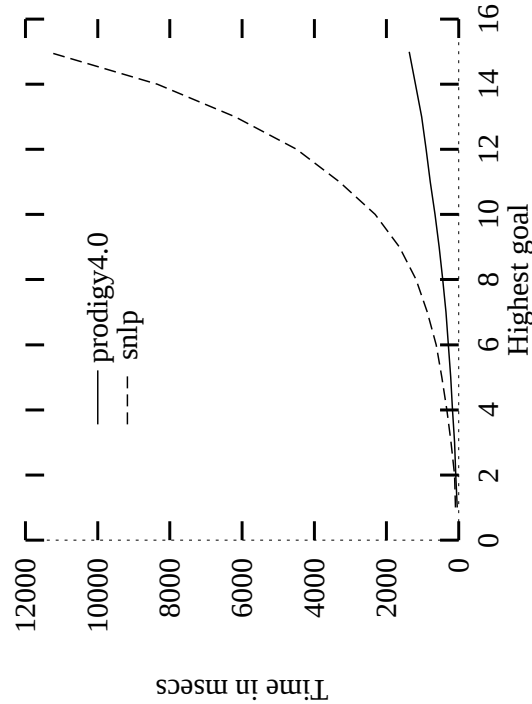
- A set of subgoals is *serializable* [Korf]:
  - If there exists some ordering whereby they can be solved sequentially,
  - without ever violating a previously solved subgoal.
- Easily serializable, laboriously serializable
- A set of subgoals is *easily linkable*:
  - If, independently of the order by which the planner links these subgoals to operators,
  - it never has to undo those links.
  - Otherwise it is *laboriously linkable*.

Laboriously Linkable Goals

operator  $A_i$       operator  $A_*$   
preconds  $g_*, g_{i-1}$       preconds ()  
adds  $g_i$       adds  $g_*$   
deletes  $g_*$       deletes ()

Initial state:  $g_*$   
Goal statement:  
 $g_*, g_5$   
Plan:  
 $A_1, A_*, A_2, A_*, A_3, A_*, A_4, A_*, A_5$

Laboriously Linkable Goals



# Graphplan

|                  |                                                                                                  |                                                                                           |                                                                                                                              |
|------------------|--------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|
| <b>Operator:</b> | <b>designate-roller</b><br><wall> <roller> <color><br>(clean <roller><br>(needs-painting <wall>) | <b>fill-roller</b><br><roller> <color><br>(clean <roller><br>(chosen<br><roller> <color>) | <b>paint-wall</b><br><wall> <roller> <color><br>(ready<br><wall> <roller> <color><br>(filled-with-paint<br><roller> <color>) |
| <b>preconds:</b> |                                                                                                  |                                                                                           |                                                                                                                              |
| <b>adds:</b>     | (ready<br><wall> <roller> <color><br>(chosen <roller> <color>)                                   | (filled-with-paint<br><roller> <color>)                                                   | (painted <wall> <color>)                                                                                                     |
| <b>deletes:</b>  |                                                                                                  | (clean <roller>)                                                                          | (ready<br><wall> <roller> <color><br>(needs-painting <wall>)                                                                 |

| Initial State          | Goal Statement        | An Optimal Solution                    |
|------------------------|-----------------------|----------------------------------------|
| (needs-painting wallA) | (painted wallA red)   | <Designate-Roller wallA roller1 red>   |
| (needs-painting wallB) | (painted wallB red)   | <Designate-Roller wallB roller1 red>   |
| (needs-painting wallC) | (painted wallC red)   | <Designate-Roller wallC roller1 red>   |
| (needs-painting wallD) | (painted wallD green) | <Fill-Roller roller1 red>              |
| (needs-painting wallE) | (painted wallE green) | <Paint-Wall wallA roller1 red>         |
| (clean roller1)        |                       | <Paint-Wall wallB roller1 red>         |
| (clean roller2)        |                       | <Paint-Wall wallC roller1 red>         |
|                        |                       | <Designate-Roller wallD roller2 green> |
|                        |                       | <Designate-Roller wallE roller2 green> |
|                        |                       | <Fill-Roller roller2 green>            |
|                        |                       | <Paint-Wall wallD roller2 green>       |
|                        |                       | <Paint-Wall wallE roller2 green>       |

|                   | time(sec) | solution |
|-------------------|-----------|----------|
| eager applying    | 500       | no       |
| eager subgoaling  | 500       | no       |
| variable strategy | 4         | yes      |

# Planning Graphs

- A literal may exist at level  $i + 1$  if it is an Add-Effect of some action in level  $i$ .
- Two propositions  $p$  and  $q$  are **exclusive** in a proposition-level if ALL actions that add  $p$  are exclusive of ALL actions that add  $q$ .
- Actions A and B are **exclusive** at action-level  $i$ , if:
  - ▷ **Interference:** A (or B) deletes a precondition or an Add-Effect of B (or A).
  - ▷ **Competing Needs:**  $p$  is a precondition of A and  $q$  is a precondition of B, and  $p$  and  $q$  are exclusive in proposition-level  $i - 1$ .

# Graphplan

Blum &amp; Furst 95

- Forward search combined with backward search.
- Uses planning graphs.
- Two stages:
  - ▷ **Extend**: One more time step in the planning graph.
  - ▷ **Search**: Is there a valid plan in the planning graph?
- Graphplan finds a plan or proves that no plan has fewer “time steps.”

[illegible]

## Extending a Planning Graph

- To create an action-level  $i$ :
  - ▷ Add each instantiated operator, for which all of its preconditions are present at proposition-level  $i$  AND *no two of its preconditions are exclusive*.
  - ▷ Add all the no-op actions.
- Determine the exclusive actions.
- To create a proposition-level  $i + 1$ :
  - ▷ Add all the effects of the inserted actions at action-level  $i$  - distinguishing add and delete effects.
- Determine the exclusive propositions.

## Exclusivity Examples

- Exclusive Actions: (Move A B) deletes a precondition of (Load o1 A). Therefore exclusive (existence of threats).
- Exclusive Propositions: (at R A) and (at R B) at time 2 are exclusive. (at R A) is added by a no-op and (at R B) is added by (Move A B) and no-op and (Move A B) are exclusive actions.
- Exclusive Actions: Then (Load o1 A) and (Load o2 B) are exclusive because (at R A) and (at R B) are exclusive.
- Propositions can be exclusive in some time step and not in others: If (at o1 A) and (at R A) at time 1, then (in o1 A) and (at R B) are exclusive at time 2, but not at time 3.

## Searching a Planning Graph

- Level-by-level backward-chaining approach to use the exclusivity constraints.
- Given a set of goals at time  $t$ , identify all the sets of actions (including no-ops) at time  $t - 1$  who add those goals and are not exclusive. The preconditions of these actions are new goals for  $t - 1$ .

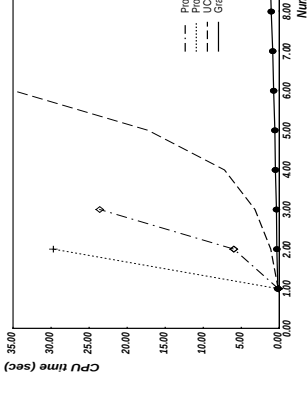
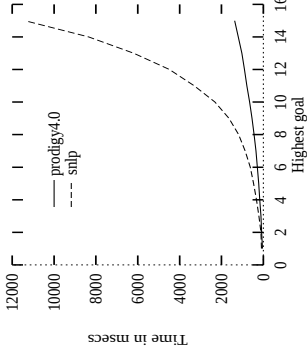
## Planning as Satisfiability

- One interpretation: “first-order deductive theorem-proving does not scale well.”
- One solution: “propositional satisfiability”
- Uniform clausal representation for goals and operators.
- Stochastic local search is a powerful technique for planning.

## SatPlan

- Assume the plan has  $n$  (time-parallel) steps. (*strong assumption*)
- Initial state:** completely specified at time 0.  
at-o1-A<sub>0</sub>  $\wedge$  at-o2-A<sub>0</sub>  $\wedge$  at-R-A<sub>0</sub>
- Goal:** specified at time  $2n$ .  
at-o1-B<sub>6</sub>  $\wedge$  at-o2-B<sub>6</sub>
- Actions:** specified at *odd* times; An action implies its preconditions and effects.  
 $(\neg\text{load-o1-A}_1 \vee \text{at-o1-A}_0) \wedge (\neg\text{load-o1-A}_1 \vee \text{at-R-A}_0) \wedge (\neg\text{load-o1-A}_1 \vee \text{in-R-A}_2) \wedge (\neg\text{load-o1-A}_1 \vee \neg\text{at-o1-A}_2)$

## Performance



Nonlinear state-space planning can suffer from goal orderings, but can use state information to reduce the search space

Graph-based planning forward state expansion and exclusivity analysis with backwards goal set

*Veloso et al.*

*Blum et al.*

## Performance (cont.)

| Prob | UMOP<br>OBDDs | Prodigy4.0<br>NL state | STAN<br>graphplan | HSP<br>A* heuristics | IPP<br>graphplan | Blackbox<br>satplan |
|------|---------------|------------------------|-------------------|----------------------|------------------|---------------------|
| 1    | 20            | 11                     | 46                | 11                   | 50               | 15                  |
| 2    | 150           | 17                     | 1075              | 17                   | 380              | 23                  |
| 3    | 710           | 23                     | 54693             | 23                   | 3270             | 31                  |
| 4    | 1490          | 29                     | 3038381           | 29                   | 26680            | 39                  |
| 5    | 3600          | 35                     | 430               | 47                   | 226460           | 47                  |
| 6    | 7260          | 41                     | 590               | 55                   | -                | -                   |
| 7    | 13750         | 47                     | 800               | 63                   | -                | -                   |
| 8    | 23840         | 53                     | 960               | 71                   | -                | -                   |
| 9    | 36220         | 59                     | 1240              | 79                   | -                | -                   |
| 10   | 56200         | 65                     | 1560              | 87                   | -                | -                   |
| 11   | 84930         | 71                     | 1820              | 95                   | -                | -                   |
| 12   | 127870        | 77                     | 2240              | 103                  | -                | -                   |
| 13   | 197170        | 83                     | 2660              | 111                  | -                | -                   |
| 14   | 290620        | 89                     | 3200              | 119                  | -                | -                   |
| 15   | 411720        | 95                     | 3740              | 127                  | -                | -                   |
| 16   | 549610        | 101                    | 4350              | 135                  | -                | -                   |
| 17   | 746920        | 107                    | 5030              | 143                  | -                | -                   |
| 18   | 971420        | 113                    | 5900              | 151                  | -                | -                   |
| 19   | 1361580       | 119                    | 6810              | 159                  | -                | -                   |
| 20   | 1838110       | 125                    | 7710              | 167                  | -                | -                   |

planning time in ms; number of plan steps

**UMOP:** Jensen & Veloso (CMU); **HSP:** Geffner & Bonet (Simon Bolivar Univ, Venezuela);  
**STAN:** Long & Fox (Durham Univ, UK); **IPP:** Köhler (Freiburg Univ, Germany);  
**Blackbox:** Kautz & Selman (AT&T, Cornell Univ)

## Performance (cont.)

| Prob | UMOP<br>OBDDs | Prodigy4.0<br>NL state | STAN<br>graphplan | HSP<br>A* heuristics | IPP<br>graphplan | Blackbox<br>satplan |
|------|---------------|------------------------|-------------------|----------------------|------------------|---------------------|
| 1    | 20            | 7                      | 19                | 7                    | 10               | 7                   |
| 2    | 20            | 7                      | 18                | 7                    | 10               | 7                   |
| 3    | 20            | 7                      | 19                | 7                    | 10               | 7                   |
| 4    | 20            | 7                      | 20                | 7                    | 10               | 7                   |
| 5    | 20            | 7                      | 21                | 7                    | 10               | 7                   |
| 6    | 20            | 7                      | 22                | 7                    | 10               | 7                   |
| 7    | 30            | 7                      | 22                | 7                    | 20               | 7                   |
| 8    | 10            | 7                      | 23                | 7                    | 24               | 7                   |
| 9    | 20            | 7                      | 25                | 7                    | 2357             | 7                   |
| 10   | 30            | 7                      | 26                | 7                    | 2511             | 7                   |
| 11   | 10            | 7                      | 27                | 7                    | 2427             | 7                   |
| 12   | 20            | 7                      | 28                | 7                    | 2456             | 7                   |
| 13   | 20            | 7                      | 29                | 7                    | 3070             | 7                   |
| 14   | 20            | 7                      | 31                | 7                    | 2573             | 7                   |
| 15   | 20            | 7                      | 32                | 7                    | 2577             | 7                   |
| 16   | 20            | 7                      | 34                | 7                    | 2699             | 7                   |
| 17   | 20            | 7                      | 35                | 7                    | 2645             | 7                   |
| 18   | 20            | 7                      | 37                | 7                    | 2686             | 7                   |
| 19   | 20            | 7                      | 39                | 7                    | 2727             | 7                   |
| 20   | 20            | 7                      | 40                | 7                    | 2787             | 7                   |

planning time in ms; number of plan steps

## Performance (cont.)

| Prob | STAN<br><a href="#">graphplan</a> | HSP<br><a href="#">A* heuristics</a> | IPP<br><a href="#">graphplan</a> | Blackbox<br><a href="#">saplan</a> |
|------|-----------------------------------|--------------------------------------|----------------------------------|------------------------------------|
| 1    | 767                               | 27                                   | 43                               | 26                                 |
| 2    | 4319                              | 32                                   | 900                              | 2062                               |
| 5    | 364932                            | 29                                   | 44                               | -                                  |
| 7    | -                                 | 26                                   | -                                | 6436                               |
| 11   | 12806                             | 24                                   | 2400                             | -                                  |
|      | 34                                | 112                                  | 33                               | -                                  |
|      | 86195                             | -                                    | 6940                             | 6544                               |
|      | 30                                | -                                    | 32                               | 32                                 |

*planning time in ms; number of plan steps*

- ▷ UMOP needs tractable representation (on-going research).
- ▷ Prodigy needs control knowledge (planning by analogy or control rules).

## Summary – Planning

- Several different planning algorithms.
- **There is not a planning strategy that is universally better than the others.**
- Even for a particular planning algorithm: **There is no single domain-independent search heuristic that performs more efficiently than others for all problems or in all domains.**

Learning is appropriate for **ANY** planner.