

# Thread-Level Parallelism

15-213/15-503: Introduction to Computer Systems  
26<sup>th</sup> Lecture, July 29, 2025

**Instructors:**

Brian Railing

# Logistics

## ■ SFS due Friday August 1 at 11:59pm

- NO late submissions
- No extensions except for exceptional circumstances

## ■ Final Exam

- Final will be on Thursday, July 31 at 12:30-3:30pm
  - Unless 8/23 at ?
  - Unless 12/? at ?
- You can bring two 8.5"x11" / A4 cheat sheets, written or printed

# Hours and FCEs

- **Please fill out your FCEs (faculty course evaluations)**
  - Response rates have been declining in recent semesters

# Disclaimer

- **We do not have time to fully cover the following content**
  - Take -346, -410, -418 ...
- **Valuable to know as you start writing parallel programs**

# Today

## ■ Parallel Computing Hardware

- Multicore
  - Multiple separate processors on single chip
- Hyperthreading
  - Efficient execution of multiple threads on single core

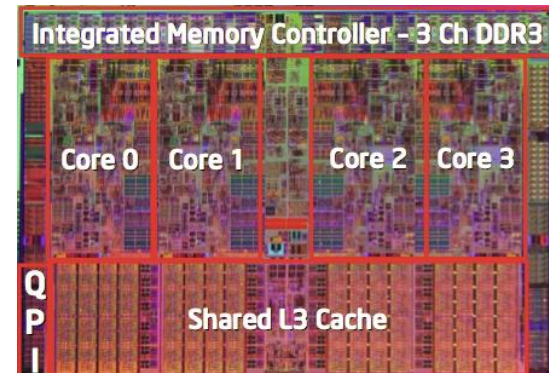
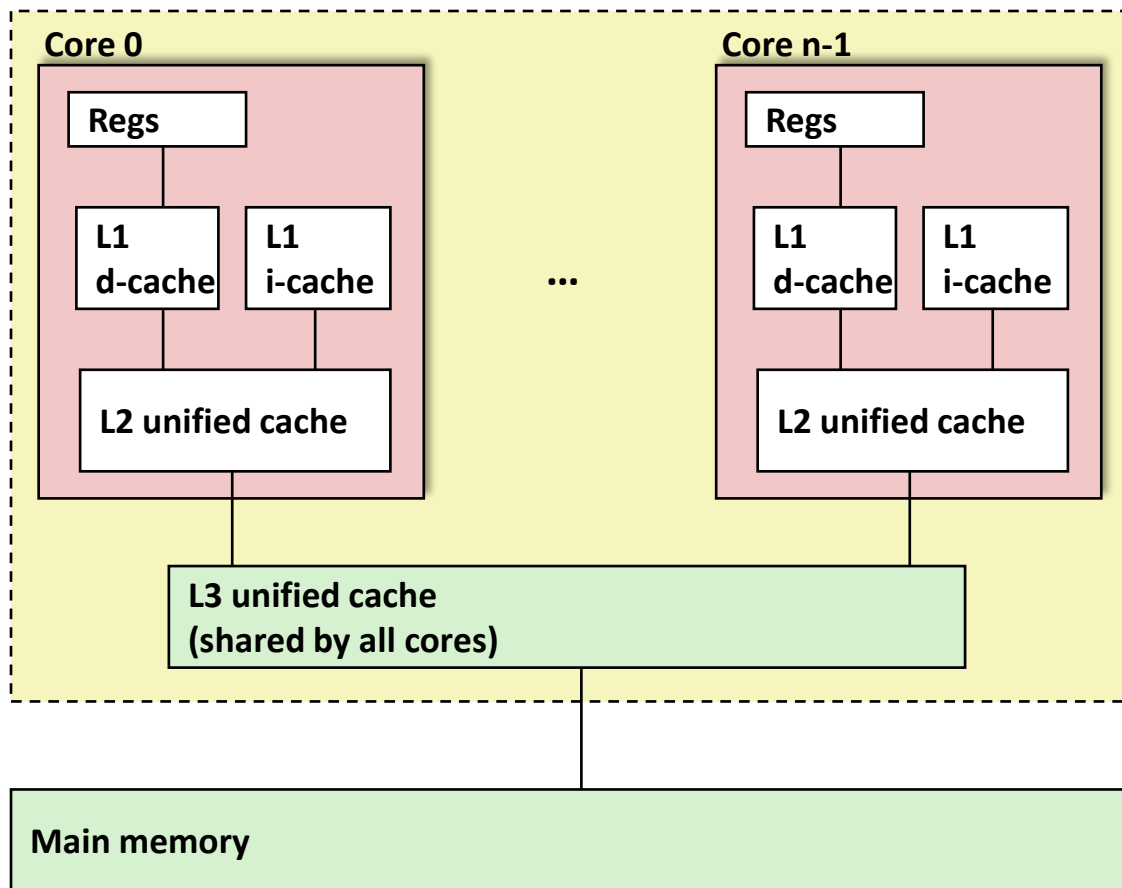
## ■ Consistency Models

- What happens when multiple threads are reading & writing shared state

## ■ Thread-Level Parallelism

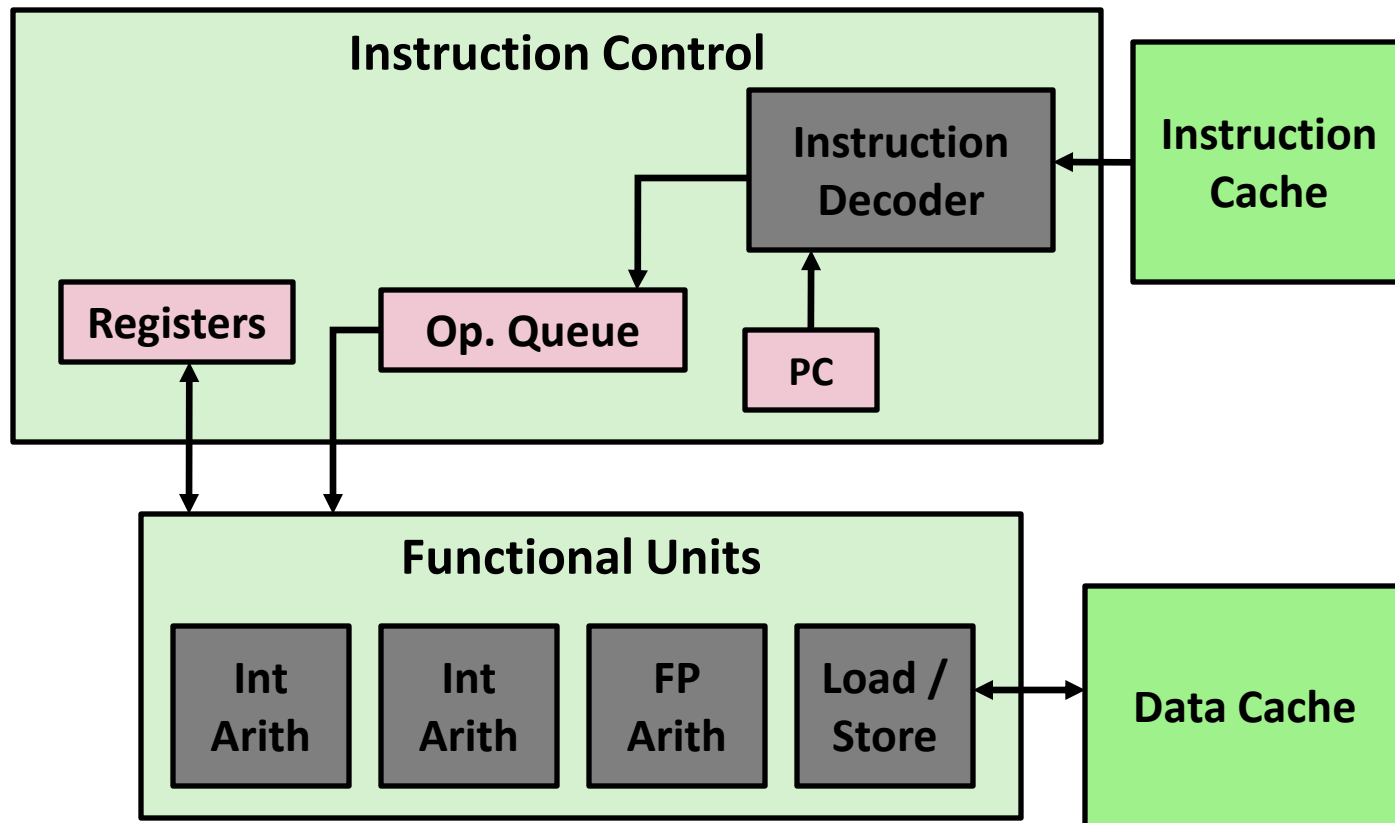
- Splitting program into independent tasks
  - Example: Parallel summation
  - Examine some performance artifacts
- Divide-and conquer parallelism
  - Example: Parallel quicksort

# Typical Multicore Processor



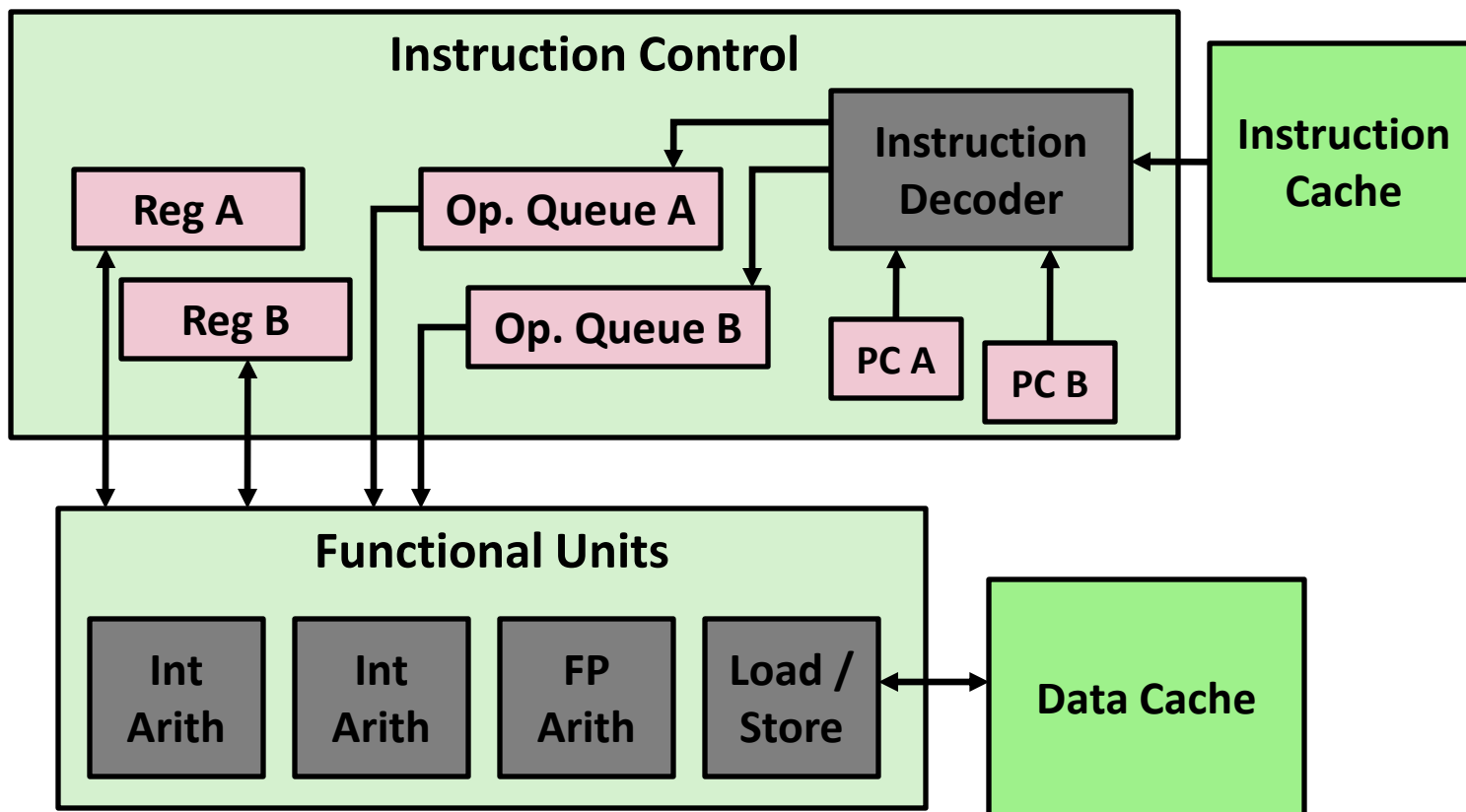
- Multiple processors operating with coherent view of memory

# Out-of-Order Processor Structure



- Instruction control dynamically converts program into stream of operations
- Operations mapped onto functional units to execute in parallel

# Hyperthreading Implementation



- Replicate instruction control to process K instruction streams
- K copies of all registers
- Share functional units



# Benchmark Machine

- **Get data about machine from `/proc/cpuinfo`**
- **Shark Machines**
  - Intel Xeon E5520 @ 2.27 GHz
  - Nehalem, ca. 2010
  - 8 Cores
  - Each can do 2x hyperthreading

# Exploiting parallel execution

- **So far, we've used threads to deal with I/O delays**
  - e.g., one thread per client to prevent one from delaying another
- **Multi-core CPUs offer another opportunity**
  - Spread work over threads executing in parallel on N cores
  - Happens automatically, if many independent tasks
    - e.g., running many applications or serving many clients
  - Can also write code to make one big task go faster
    - by organizing it as multiple parallel sub-tasks
- **Shark machines can execute 16 threads at once**
  - 8 cores, each with 2-way hyperthreading
  - Theoretical speedup of 16X
    - never achieved in our benchmarks

# Powerful, Parallel Computing Is

- Two threads, with X and Y initialized to 0

**X = 1**

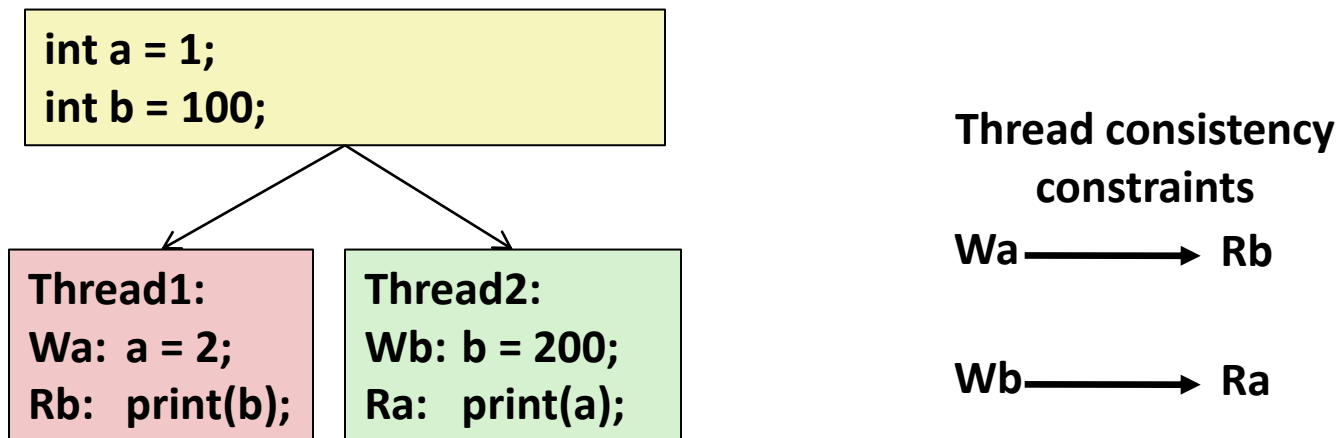
**if (Y == 0) print Hello**

**Y = 1**

**if (X == 0) print World**



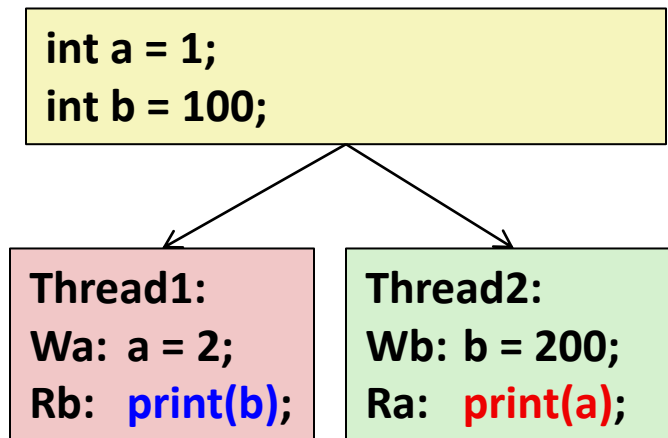
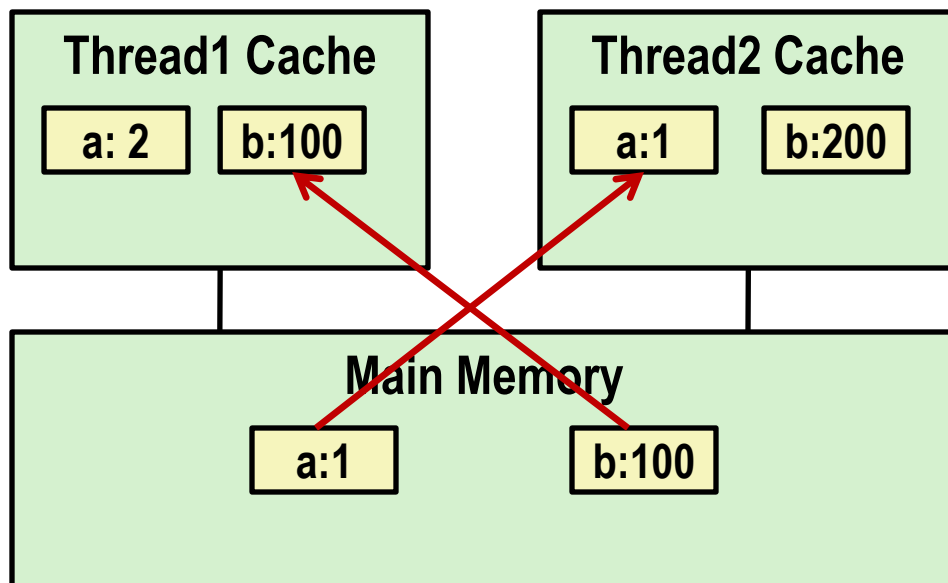
# Memory Coherence / Consistency



- **What are the possible values printed?**
  - Depends on memory consistency model
  - Abstract model of how hardware handles concurrent accesses
- **How do the two threads really see the writes?**

# Non-Coherent Cache Scenario

- Write-back caches, without coordination between them



**print 1**

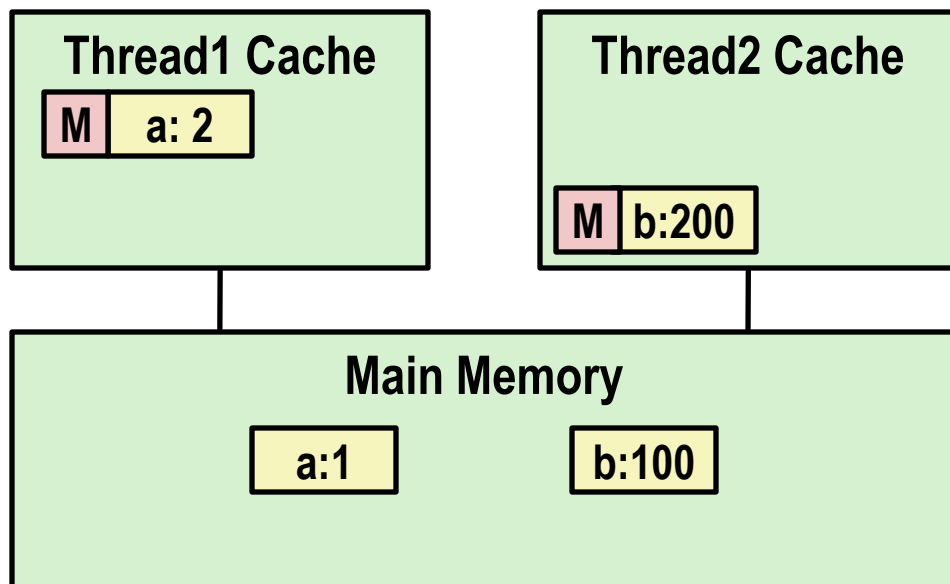
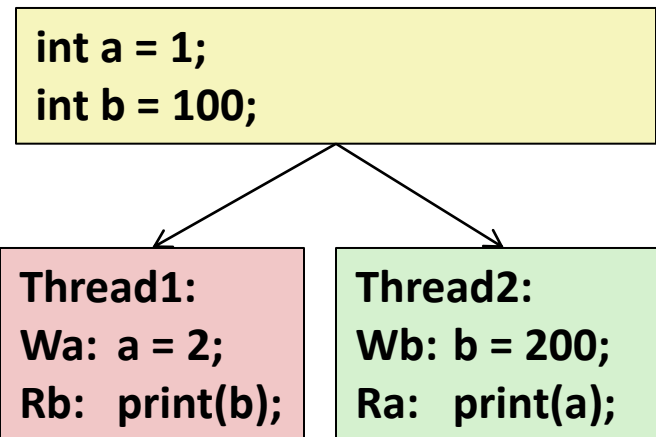
**print 100**

At later points, `a:2` and `b:200` are written back to main memory

# Snoopy Caches

## ■ Tag each cache block with state

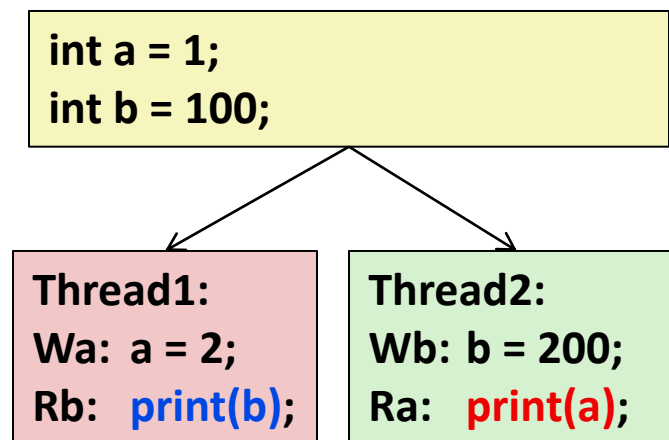
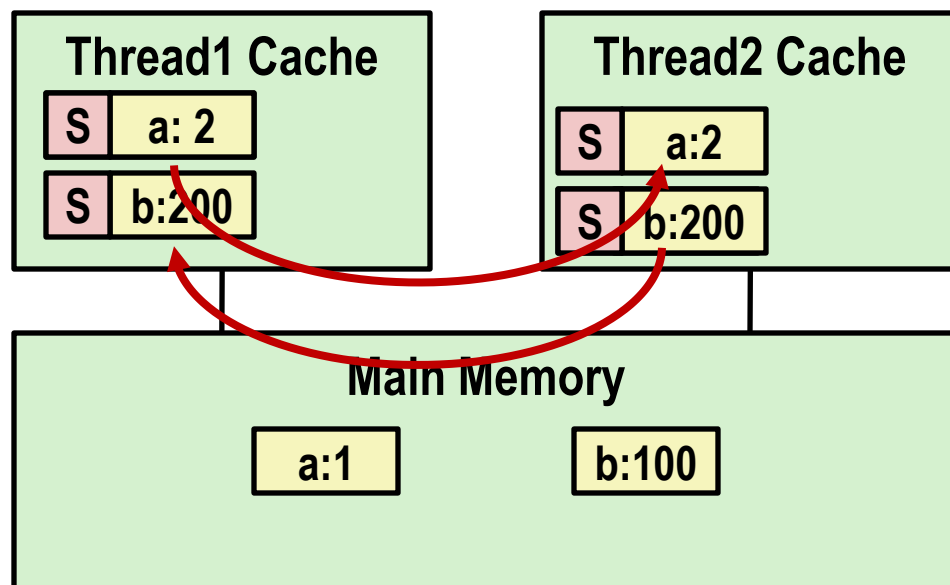
Invalid	Cannot use value
Shared	Readable copy
Modified	Writeable copy



# Snoopy Caches

## ■ Tag each cache block with state

Invalid	Cannot use value
Shared	Readable copy
Modified	Writeable copy

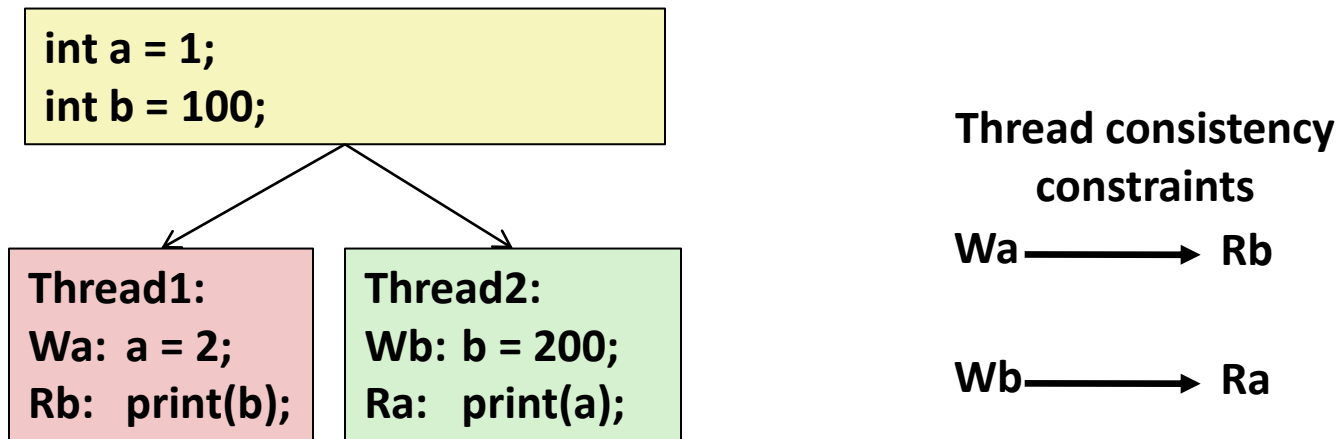


**print 2**

**print 200**

- When cache sees request for one of its M-tagged blocks
  - Supply value from cache (Note: value in memory may be stale)
  - Set tag to S

# Memory Consistency

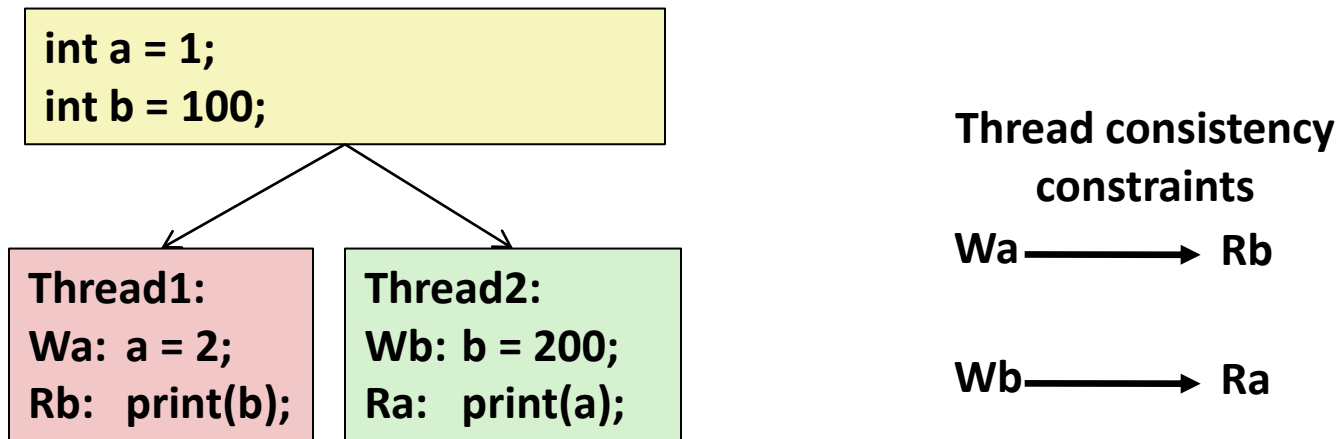


## ■ What are the possible values printed?

- Depends on memory consistency model
- Abstract model of how hardware handles concurrent accesses



# Memory Consistency



## ■ What are the possible values printed?

- Depends on memory consistency model
- Abstract model of how hardware handles concurrent accesses

## ■ Sequential consistency

- As if only one operation at a time, in an order consistent with the order of operations within each thread
- Thus, overall effect consistent with each individual thread but otherwise allows an arbitrary interleaving

# Sequential Consistency Example

```
int a = 1;
int b = 100;
```

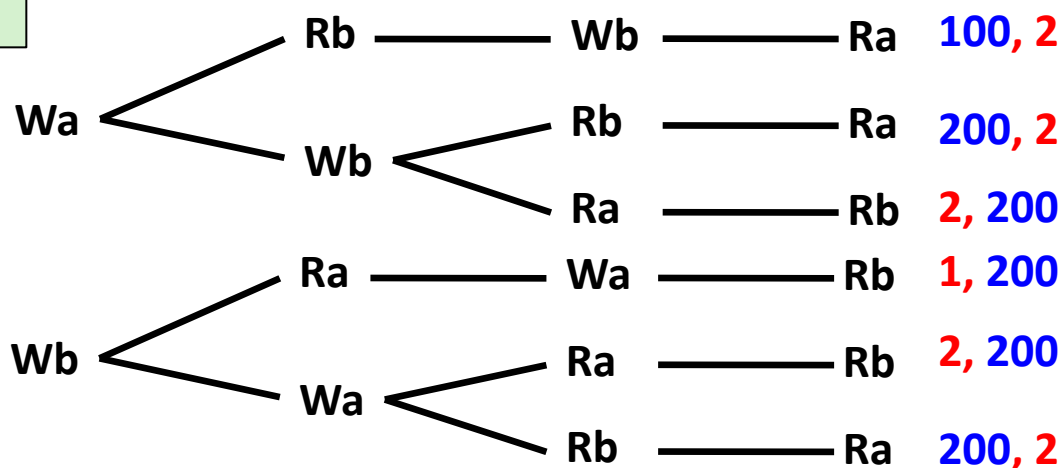
Thread1:  
Wa: a = 2;  
Rb: **print(b);**

Thread2:  
Wb: b = 200;  
Ra: **print(a);**

Thread consistency  
constraints

Wa ————— Rb

Wb ————— Ra

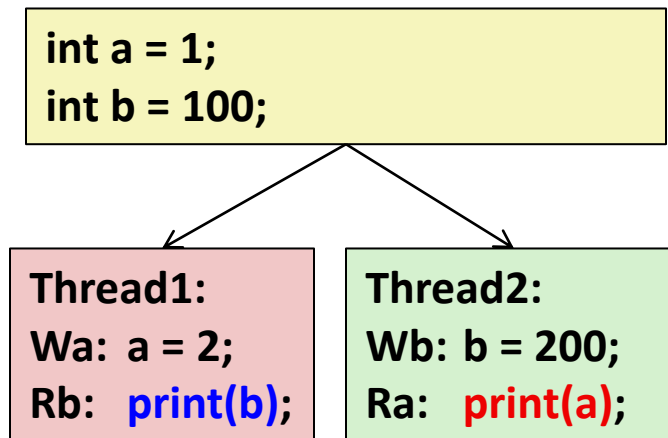
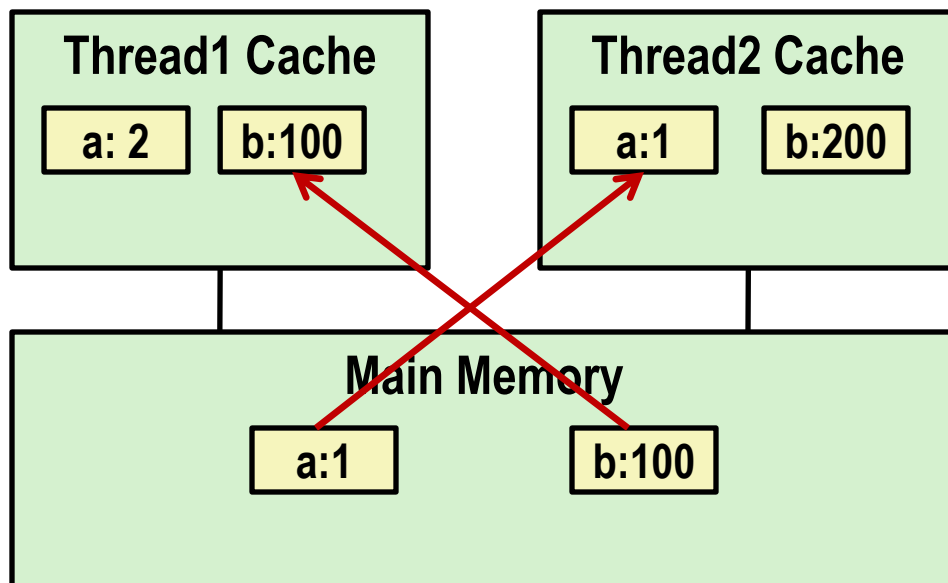


## ■ Impossible outputs

- 100, 1 and 1, 100
- Would require reaching *both* Ra and Rb before *either* Wa or Wb

# Non-Coherent Cache Scenario

- Write-back caches, without coordination between them



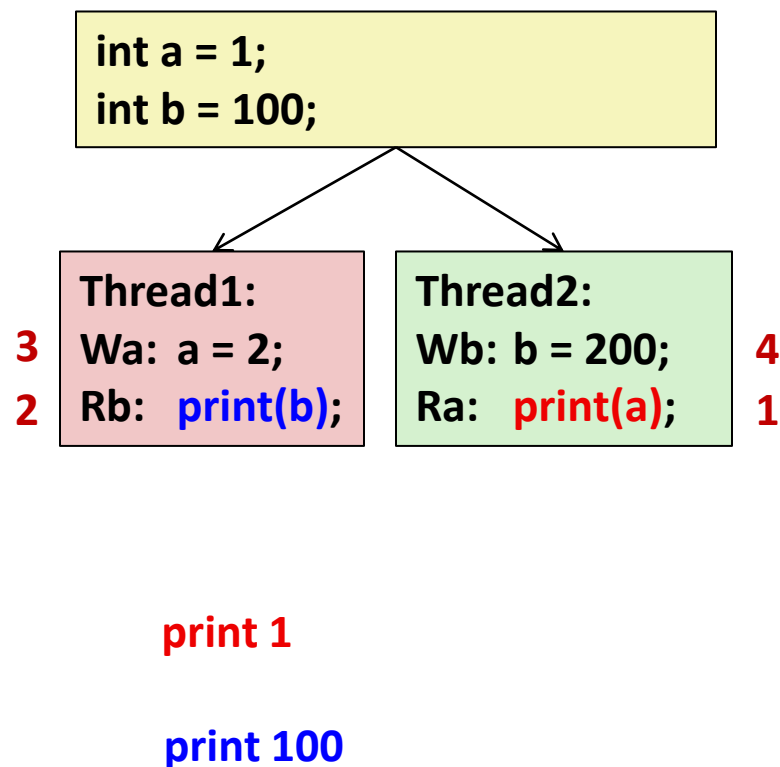
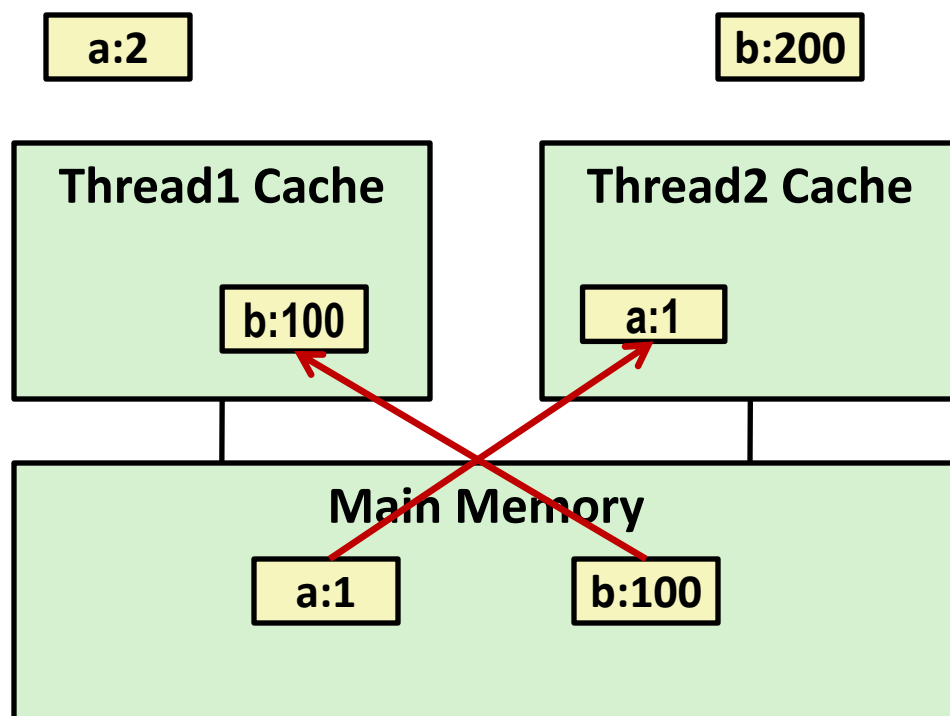
**print 1**

**print 100**

Sequentially consistent? No!

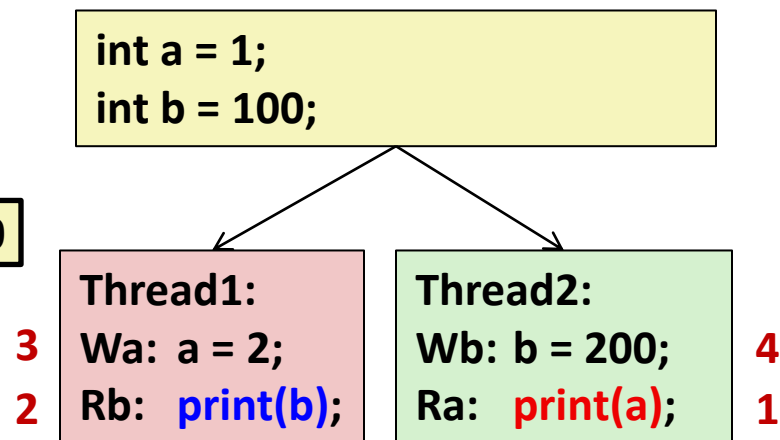
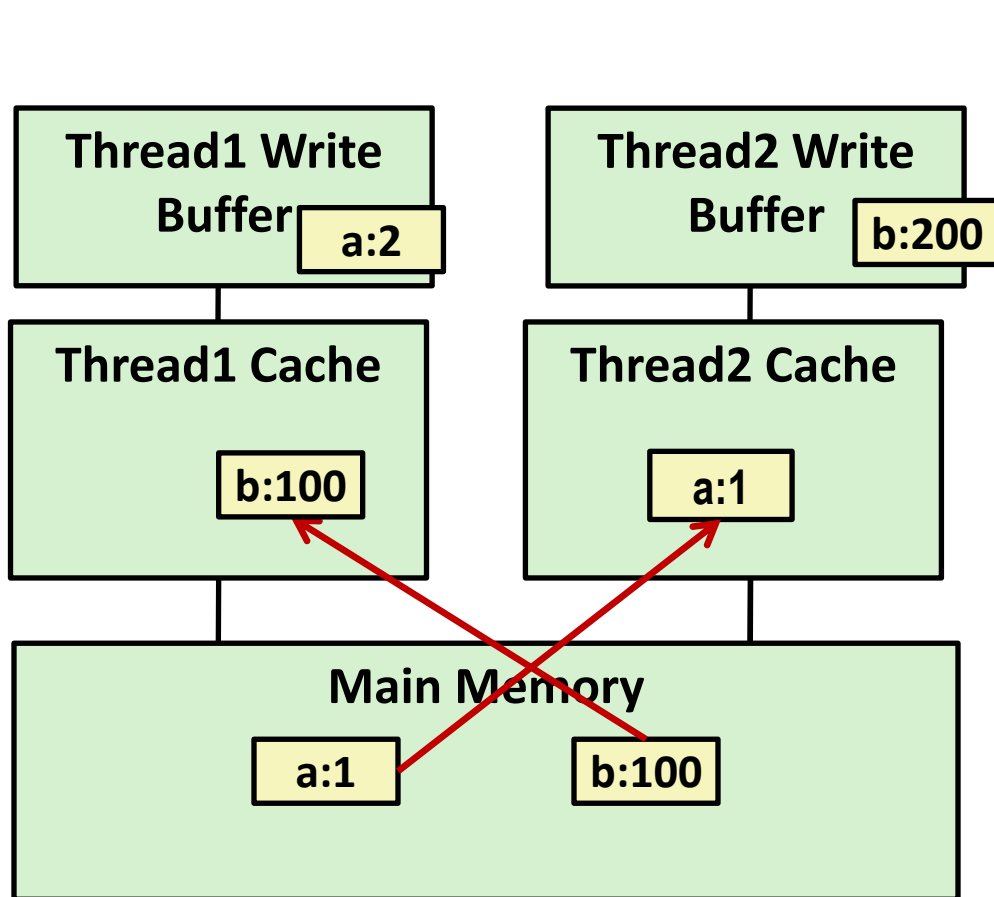
# Non-Sequentially Consistent Scenario

- Coherent caches, but thread consistency constraints violated due to *operation reordering*



- Architecture lets reads finish before writes because single thread accesses different memory locations

# Non-Sequentially Consistent Scenario



- Why Reordered? Writes take long time. Buffer write, let read go ahead. *Instruction-level parallelism*

- Fix: Add `SFENCE` instructions between `Wa & Rb` and `Wb & Ra`
- Fix: Use synchronization (properly written, it fences)

# Memory Models

- **Sequentially Consistent:**

- Each thread executes in proper order, any interleaving

- **To ensure, requires**

- Proper cache/memory behavior
- Proper intra-thread ordering constraints

- **Thread ordering constraints**

- Use synchronization to ensure the program is free of data races

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## ■ Consistency Models

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## ■ Thread-Level Parallelism

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  - Example: Parallel summation
  - Examine some performance artifacts
- Divide-and conquer parallelism
  - Example: Parallel quicksort

# Summation Example

- **Sum numbers 0, ..., N-1**
  - Should add up to  $(N-1)*N/2$
- **Partition into K ranges**
  - $\lfloor N/K \rfloor$  values each
  - Each of the  $t$  threads processes 1 range
  - Accumulate leftover values serially
- **Method #1: All threads update single global variable**
  - 1A: No synchronization
  - 1B: Synchronize with pthread semaphore
  - 1C: Synchronize with pthread mutex
    - “Binary” semaphore. Only values 0 & 1



# Accumulating in Single Global Variable: Declarations

```
typedef unsigned long data_t;  
/* Single accumulator */  
volatile data_t global_sum;
```

# Accumulating in Single Global Variable: Declarations

```
typedef unsigned long data_t;  
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volatile data_t global_sum;  
  
/* Mutex & semaphore for global sum */  
sem_t semaphore;  
pthread_mutex_t mutex;
```

# Accumulating in Single Global Variable: Declarations

```
typedef unsigned long data_t;
/* Single accumulator */
volatile data_t global_sum;

/* Mutex & semaphore for global sum */
sem_t semaphore;
pthread_mutex_t mutex;

/* Number of elements summed by each thread */
size_t nelems_per_thread;

/* Keep track of thread IDs */
pthread_t tid[MAXTHREADS];

/* Identify each thread */
int myid[MAXTHREADS];
```

# Accumulating in Single Global Variable: Operation

```
nelems_per_thread = nelems / nthreads;
```

```
/* Set global value */
```

```
global_sum = 0;
```

```
/* Create threads and wait for them to finish */
```

```
for (i = 0; i < nthreads; i++) {
```

```
    myid[i] = i;
```

```
    Pthread_create(&tid[i], NULL, thread_fun, &myid[i]);
```

```
}
```

```
for (i = 0; i < nthreads; i++)
```

```
    Pthread_join(tid[i], NULL);
```

```
result = global_sum;
```

```
/* Add leftover elements */
```

```
for (e = nthreads * nelems_per_thread; e < nelems; e++)
```

```
    result += e;
```

**Thread ID**

**Thread routine**

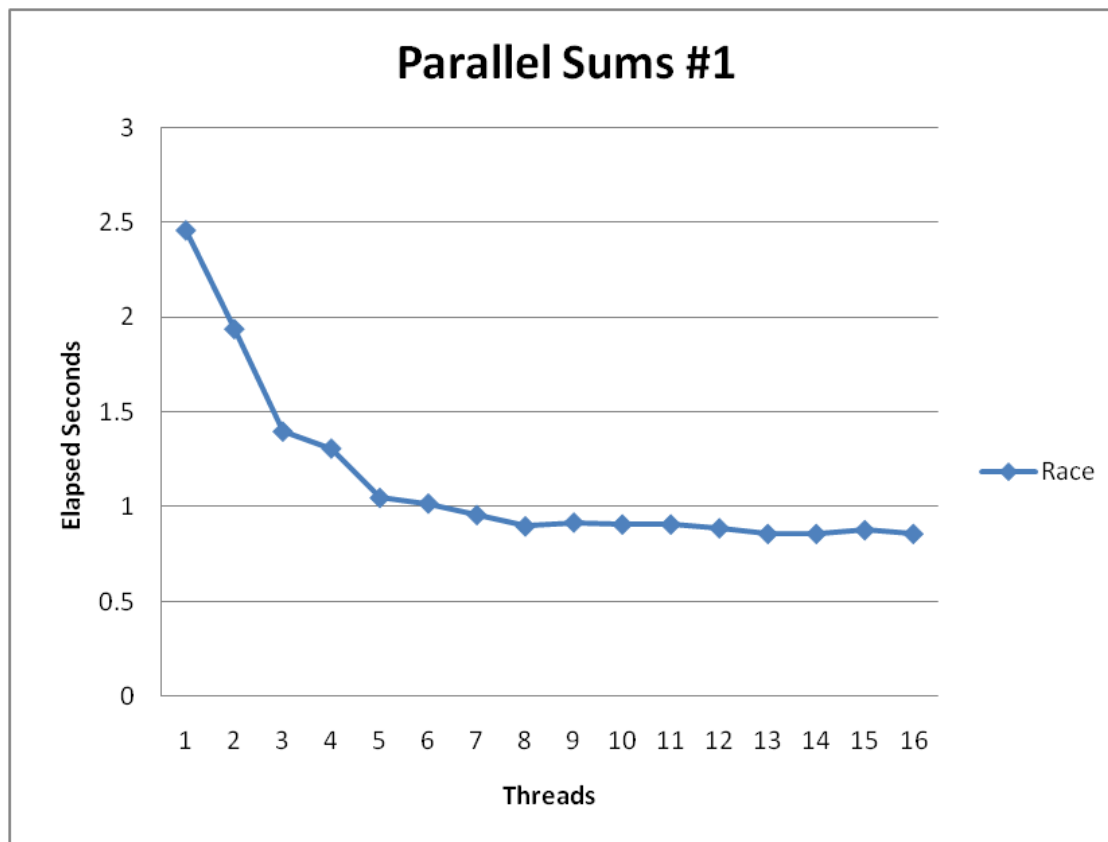
**Thread arguments  
(void \*p)**

# Thread Function: No Synchronization

```
void *sum_race(void *vargp)
{
    int myid = *((int *)vargp);
    size_t start = myid * nelems_per_thread;
    size_t end = start + nelems_per_thread;
    size_t i;

    for (i = start; i < end; i++) {
        global_sum += i;
    }
    return NULL;
}
```

# Unsynchronized Performance



- $N = 2^{30}$
- Best speedup = 2.86X
- Gets **wrong answer** when  $> 1$  thread! Why?

# Thread Function: Semaphore / Mutex

## Semaphore

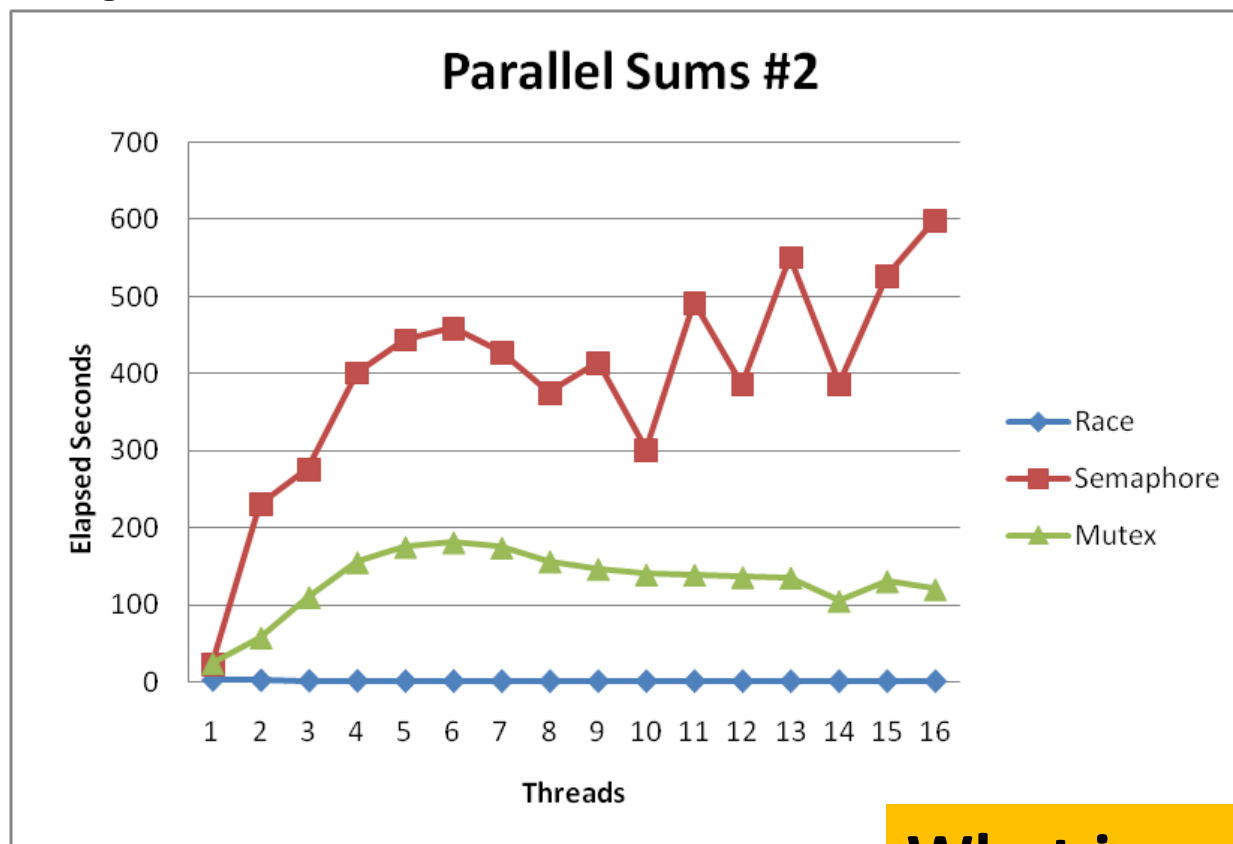
```
void *sum_sem(void *vargp)
{
    int myid = *((int *)vargp);
    size_t start = myid * nelems_per_thread;
    size_t end = start + nelems_per_thread;
    size_t i;

    for (i = start; i < end; i++) {
        sem_wait(&semaphore);
        global_sum += i;
        sem_post(&semaphore);
    }
    return NULL;
}
```

## Mutex

```
pthread_mutex_lock(&mutex);
global_sum += i;
pthread_mutex_unlock(&mutex);
```

# Semaphore / Mutex Performance



- **Terrible Performance**
  - 2.5 seconds → ~10 minutes
- **Mutex 3X faster than semaphore**
- **Clearly, neither is successful**

**What is main reason for poor performance?**



# Separate Accumulation

- **Method #2: Each thread accumulates into separate variable**
  - 2A: Accumulate in contiguous array elements
  - 2B: Accumulate in spaced-apart array elements
  - 2C: Accumulate in registers

```
/* Partial sum computed by each thread */  
data_t psum[MAXTHREADS*MAXSPACING];  
  
/* Spacing between accumulators */  
size_t spacing = 1;
```

# Separate Accumulation: Operation

```
nelems_per_thread = nelems / nthreads;

/* Create threads and wait for them to finish */
for (i = 0; i < nthreads; i++) {
    myid[i] = i;
    psum[i*spacing] = 0;
    Pthread_create(&tid[i], NULL, thread_fun, &myid[i]);
}
for (i = 0; i < nthreads; i++)
    Pthread_join(tid[i], NULL);

result = 0;

/* Add up the partial sums computed by each thread */
for (i = 0; i < nthreads; i++)
    result += psum[i*spacing];

/* Add leftover elements */
for (e = nthreads * nelems_per_thread; e < nelems; e++)
    result += e;
```

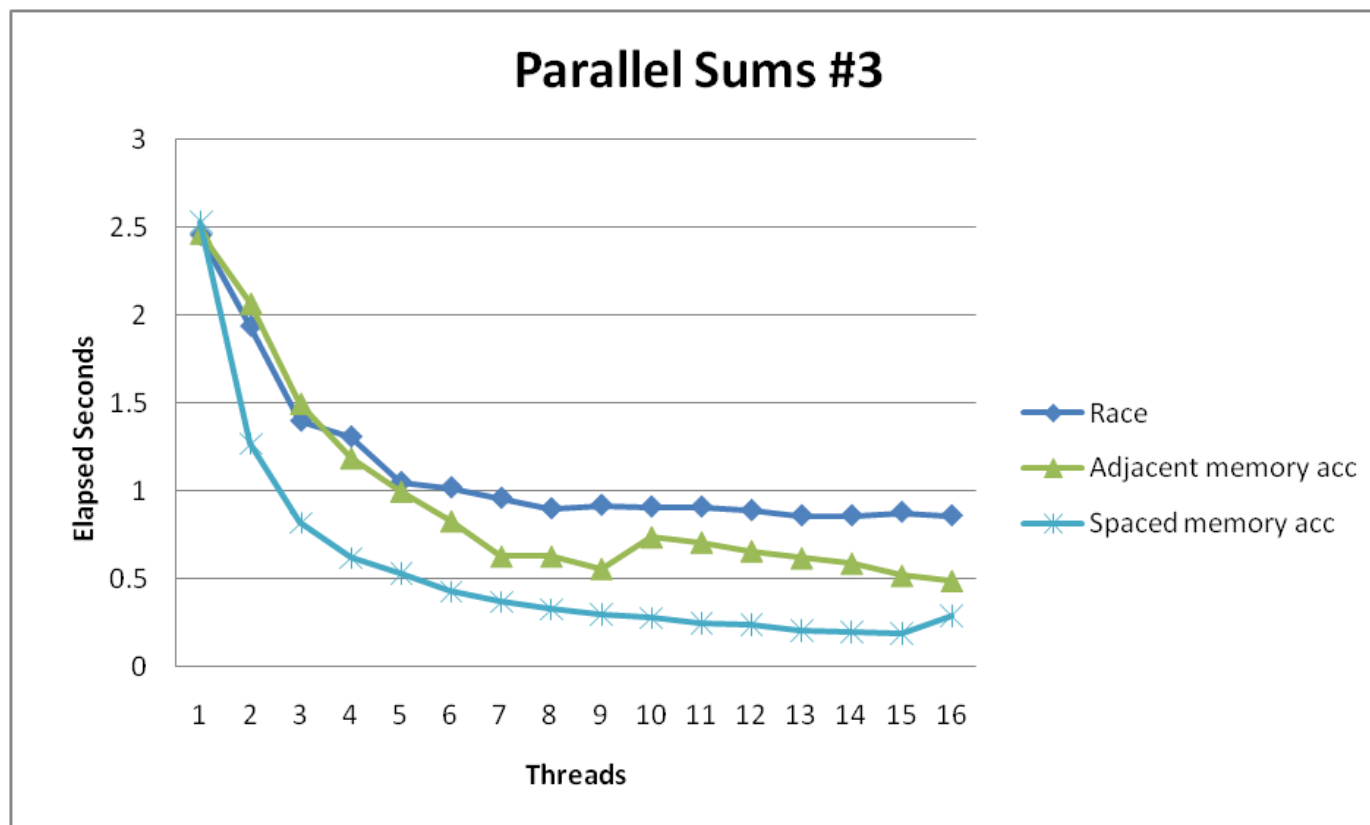
# Thread Function: Memory Accumulation

Where is the mutex?

```
void *sum_global(void *vargp)
{
    int myid = *((int *)vargp);
    size_t start = myid * nelems_per_thread;
    size_t end = start + nelems_per_thread;
    size_t i;

    size_t index = myid*spacing;
    psum[index] = 0;
    for (i = start; i < end; i++) {
        psum[index] += i;
    }
    return NULL;
}
```

# Memory Accumulation Performance

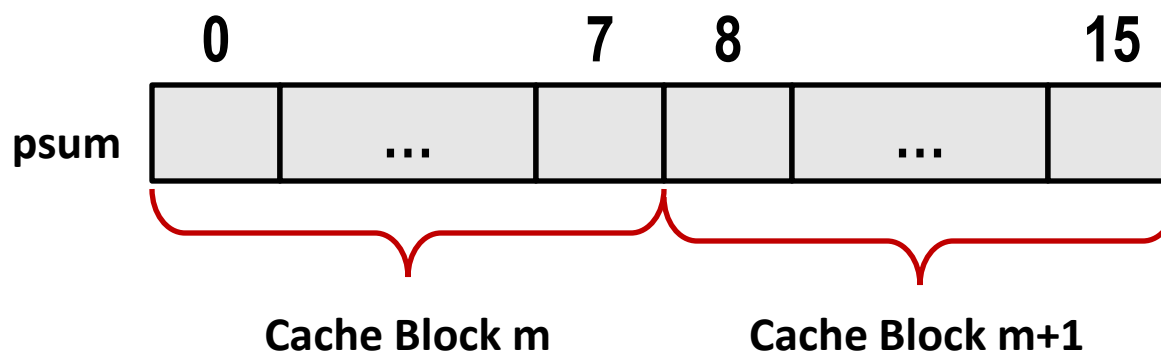


## ■ Clear threading advantage

- Adjacent speedup: 5 X
- Spaced-apart speedup: 13.3 X (Only observed speedup > 8)

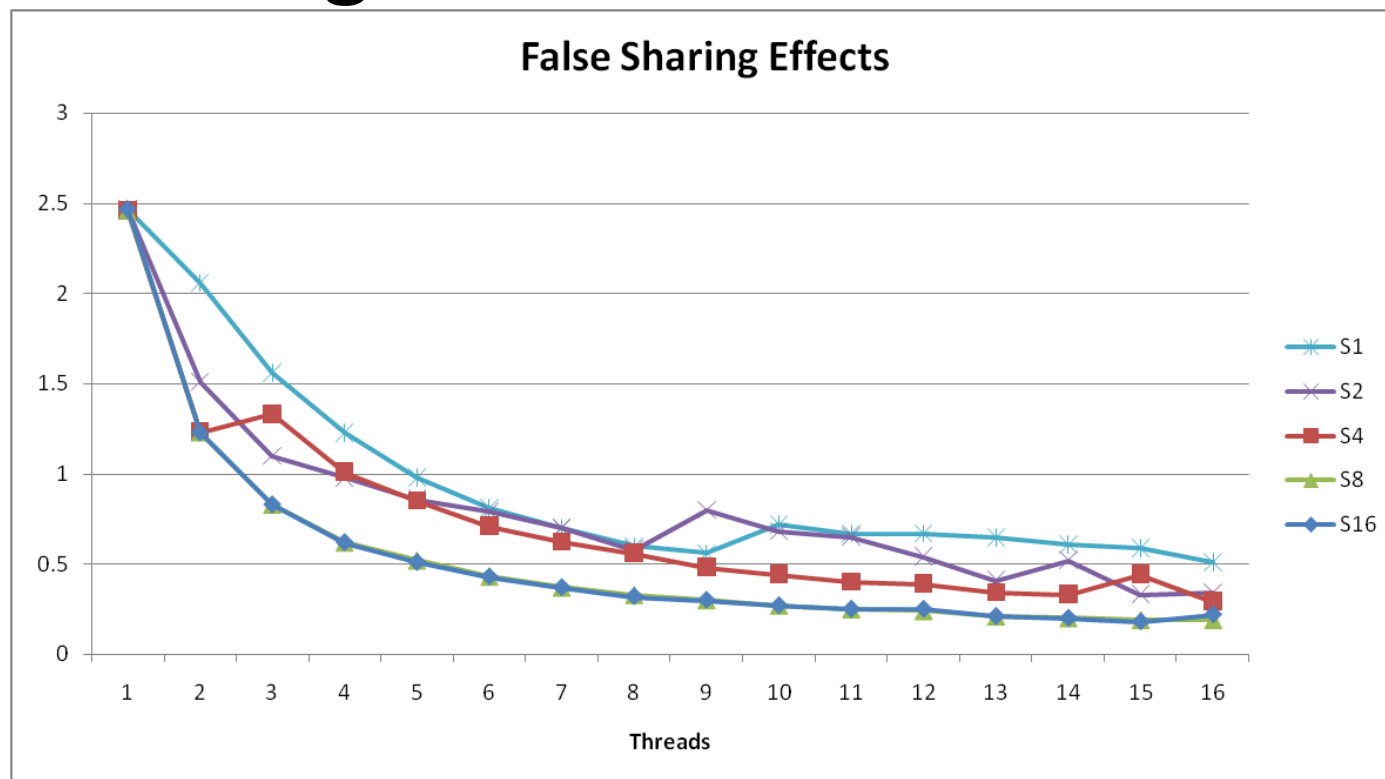
## ■ Why does spacing the accumulators apart matter?

# False Sharing



- **Coherence maintained on cache blocks**
- **To update `psum[i]`, thread `i` must have exclusive access**
  - Threads sharing common cache block will keep fighting each other for access to block

# False Sharing Performance

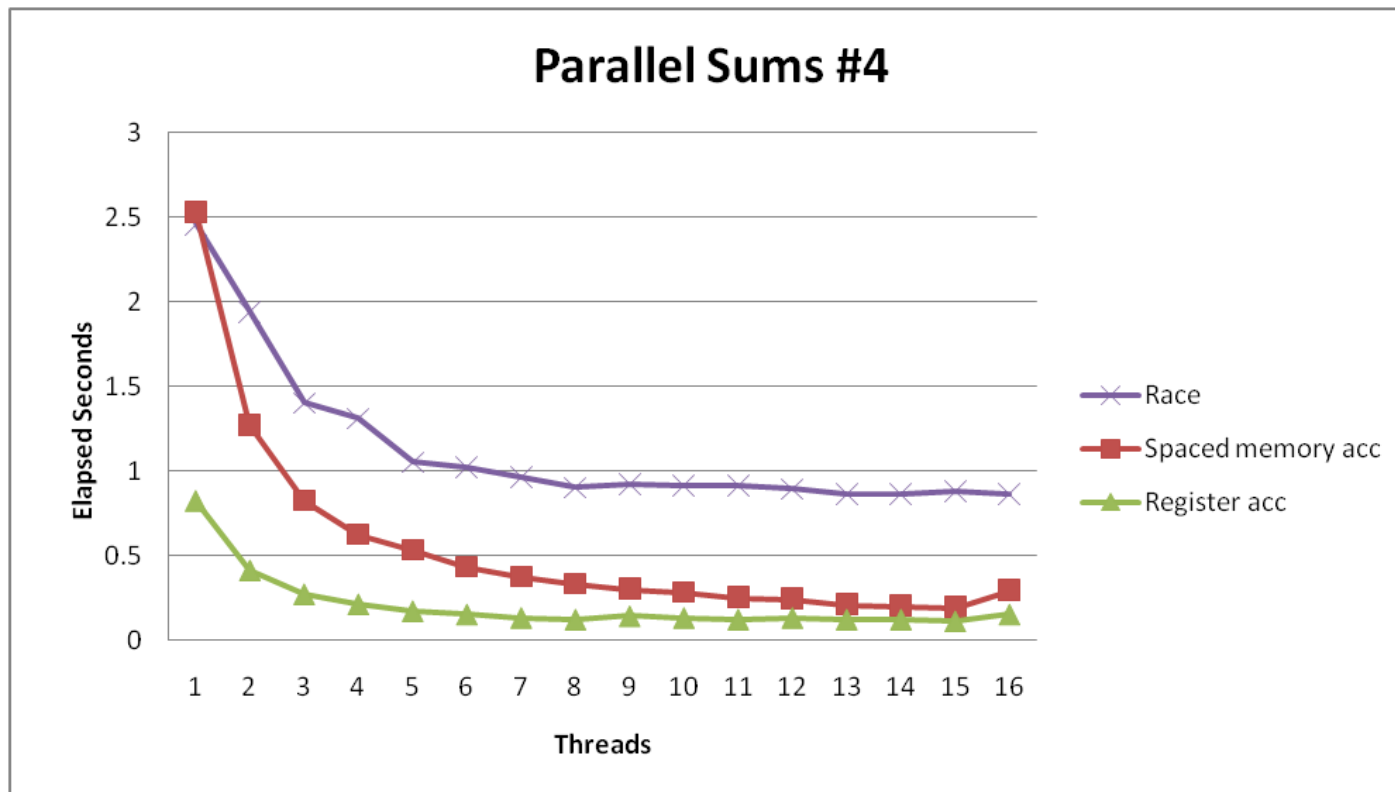


- Best spaced-apart performance 2.8 X better than best adjacent
- **Demonstrates cache block size = 64**
  - 8-byte values
  - No benefit increasing spacing beyond 8

# Thread Function: Register Accumulation

```
void *sum_local(void *vargp)
{
    int myid = *((int *)vargp);
    size_t start = myid * nelems_per_thread;
    size_t end = start + nelems_per_thread;
    size_t i;
    size_t index = myid*spacing;
    data_t sum = 0;
    for (i = start; i < end; i++) {
        sum += i;
    }
    psum[index] = sum;
    return NULL;
}
```

# Register Accumulation Performance



- Clear threading advantage

- Speedup = 7.5 X

**Beware the speedup metric!**

- 2X better than fastest memory accumulation



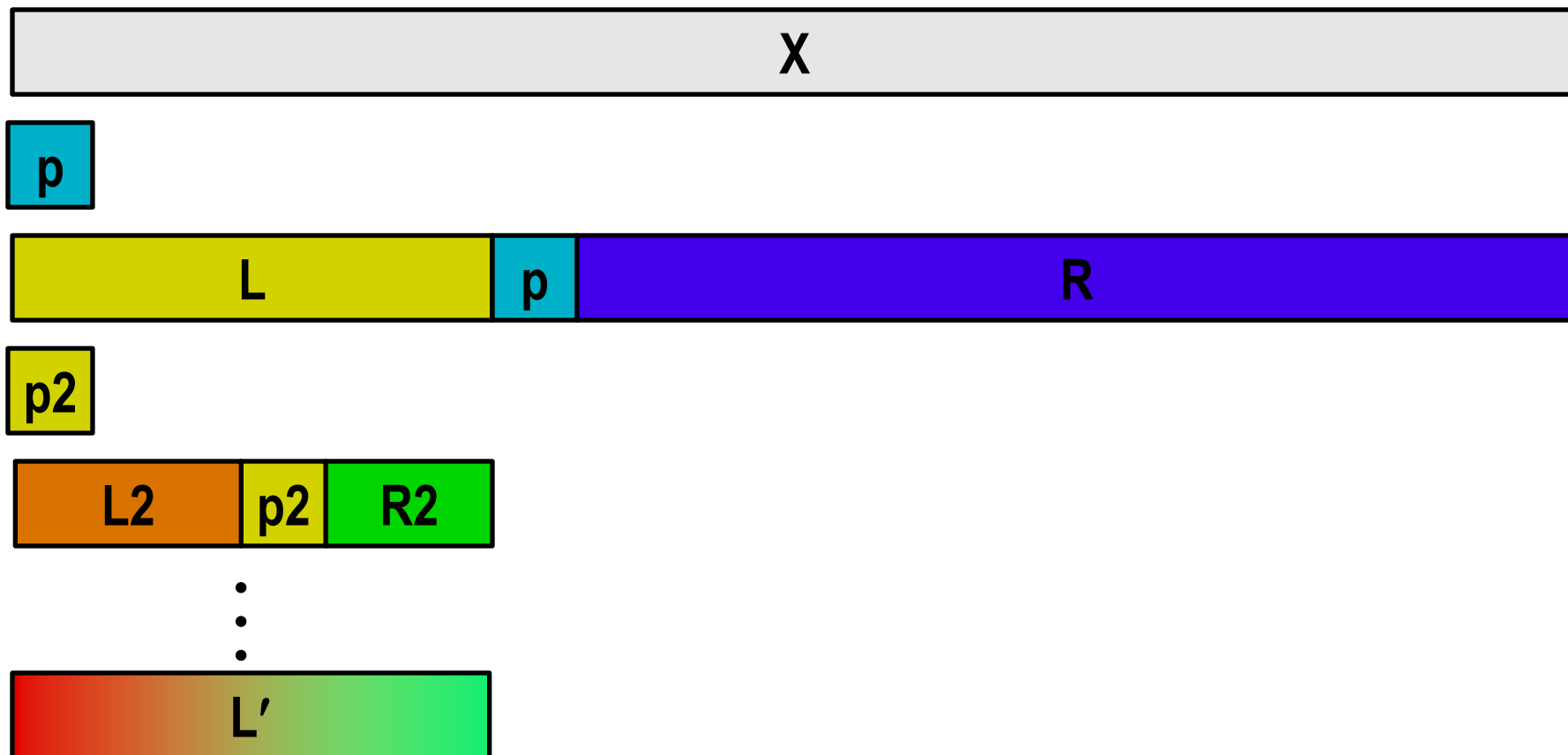
# Lessons learned

- **Sharing memory can be expensive**
  - Pay attention to true sharing
  - Pay attention to false sharing
- **Use registers whenever possible**
  - (Remember cachelab)
  - Use local cache whenever possible
- **Deal with leftovers**
- **When examining performance, compare to best possible sequential implementation**

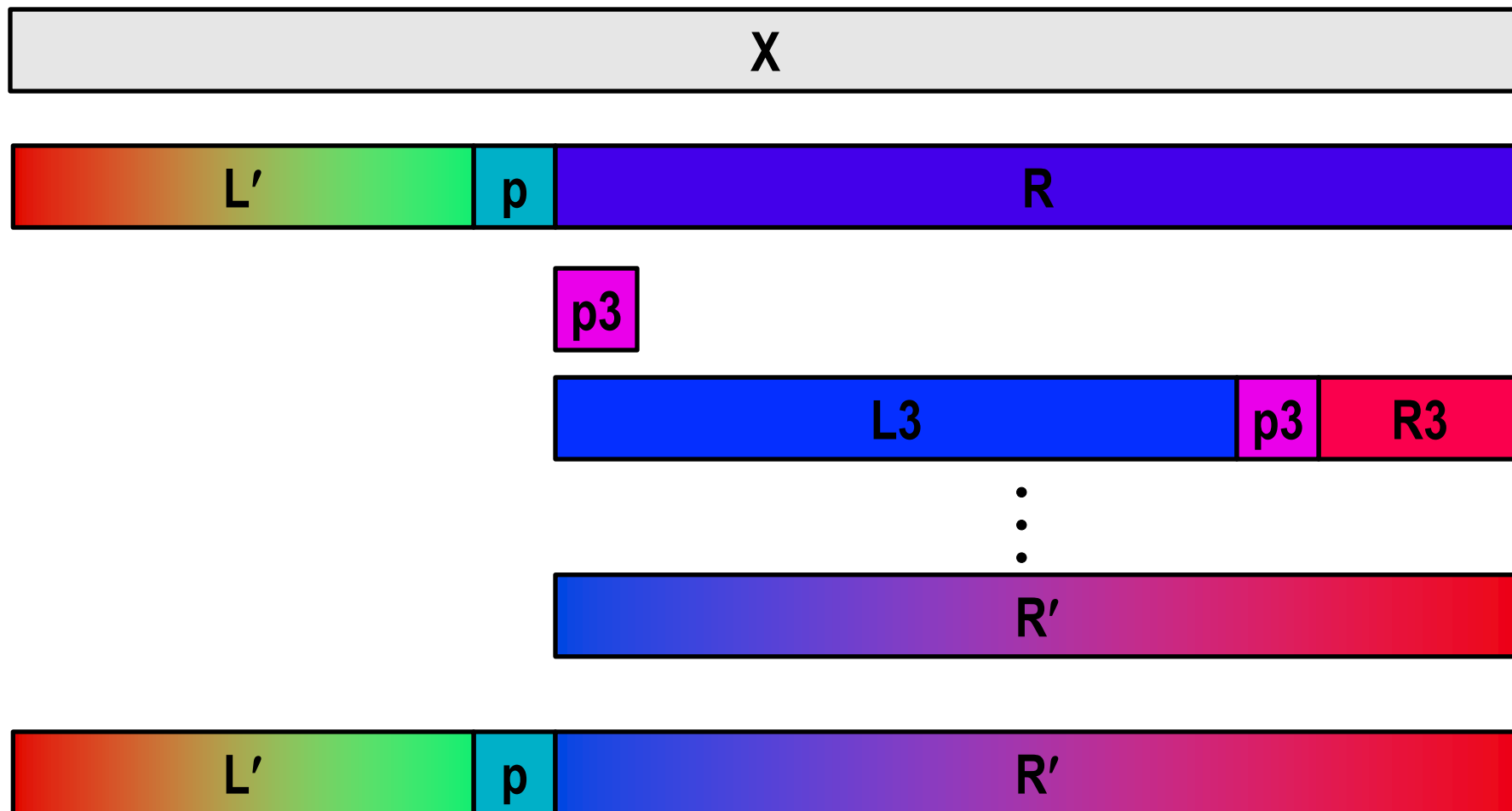
# A More Substantial Example: Sort

- Sort set of  $N$  random numbers
- Multiple possible algorithms
  - Use parallel version of quicksort
- Sequential quicksort of set of values  $X$ 
  - Choose “pivot”  $p$  from  $X$
  - Rearrange  $X$  into
    - $L$ : Values  $\leq p$
    - $R$ : Values  $\geq p$
  - Recursively sort  $L$  to get  $L'$
  - Recursively sort  $R$  to get  $R'$
  - Return  $L' : p : R'$

# Sequential Quicksort Visualized



# Sequential Quicksort Visualized



# Sequential Quicksort Code

```
void qsort_serial(data_t *base, size_t nele) {  
    if (nele <= 1)  
        return;  
    if (nele == 2) {  
        if (base[0] > base[1])  
            swap(base, base+1);  
        return;  
    }  
  
    /* Partition returns index of pivot */  
    size_t m = partition(base, nele);  
    if (m > 1)  
        qsort_serial(base, m);  
    if (nele-1 > m+1)  
        qsort_serial(base+m+1, nele-m-1);  
}
```

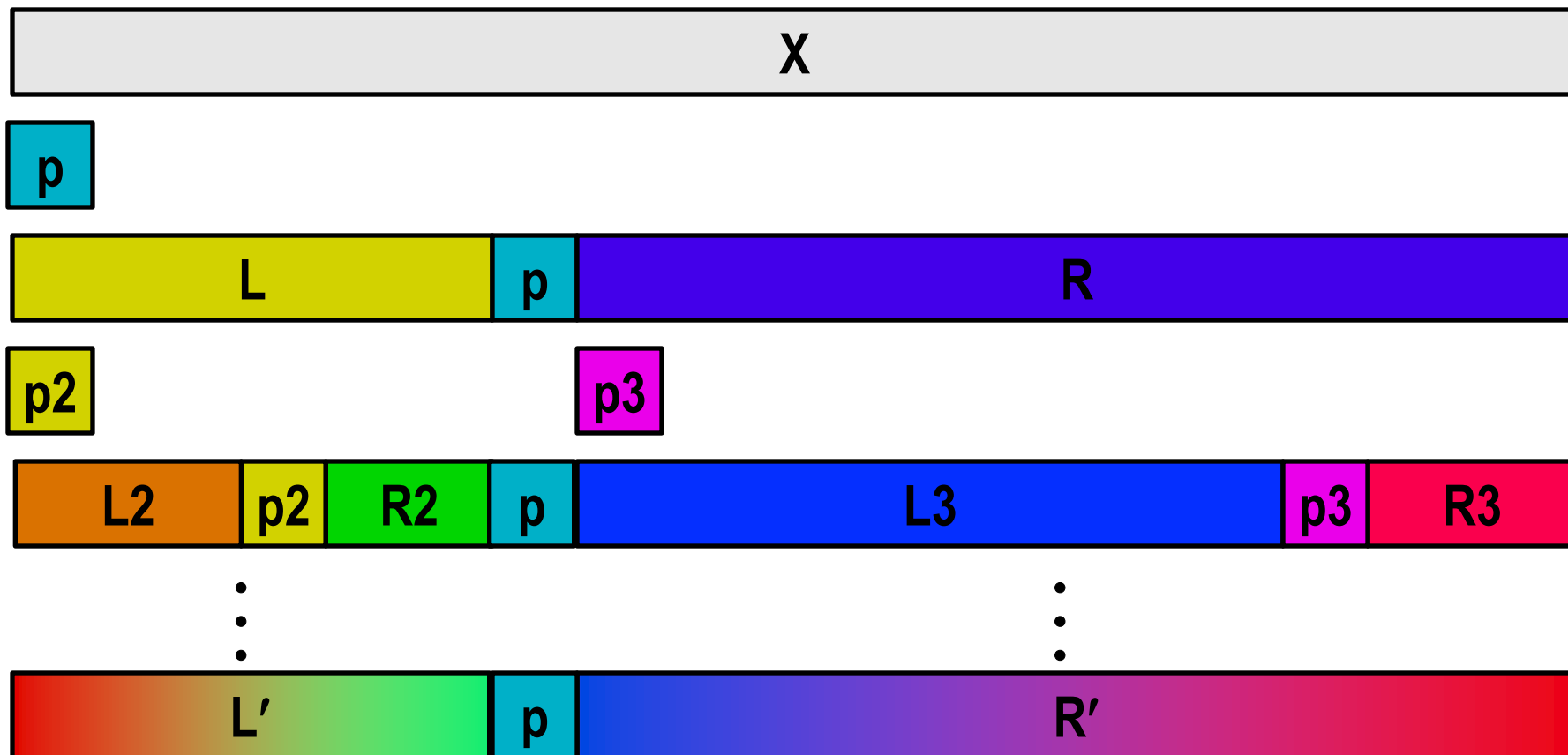
- Sort nele elements starting at base
  - Recursively sort L or R if has more than one element

# Parallel Quicksort

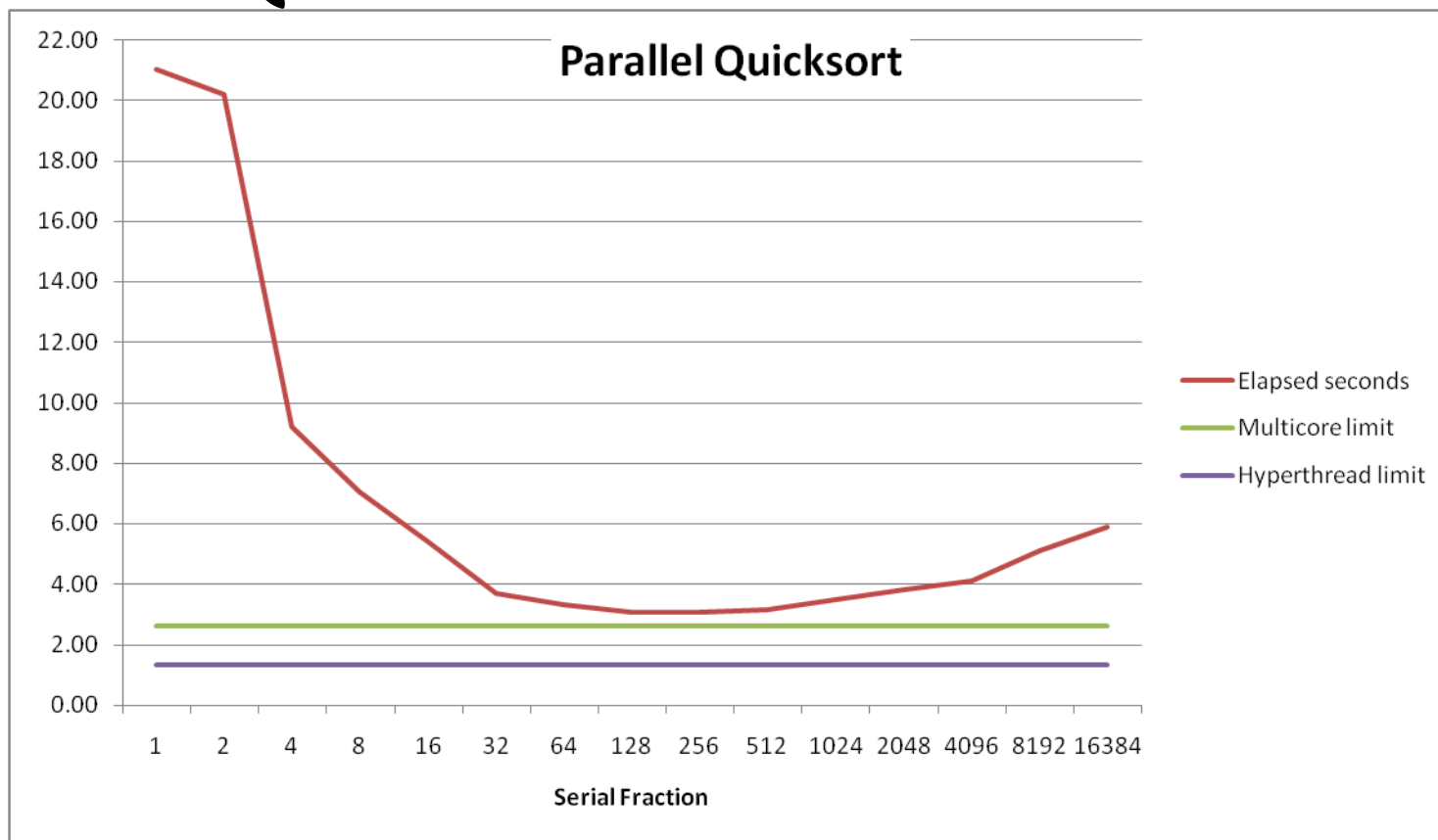
## ■ Parallel quicksort of set of values $X$

- If  $N \leq N_{\text{thresh}}$ , do sequential quicksort
- Else
  - Choose “pivot”  $p$  from  $X$
  - Rearrange  $X$  into
    - $L$ : Values  $\leq p$
    - $R$ : Values  $\geq p$
  - Recursively spawn separate threads
    - Sort  $L$  to get  $L'$
    - Sort  $R$  to get  $R'$
  - Return  $L' : p : R'$

# Parallel Quicksort Visualized



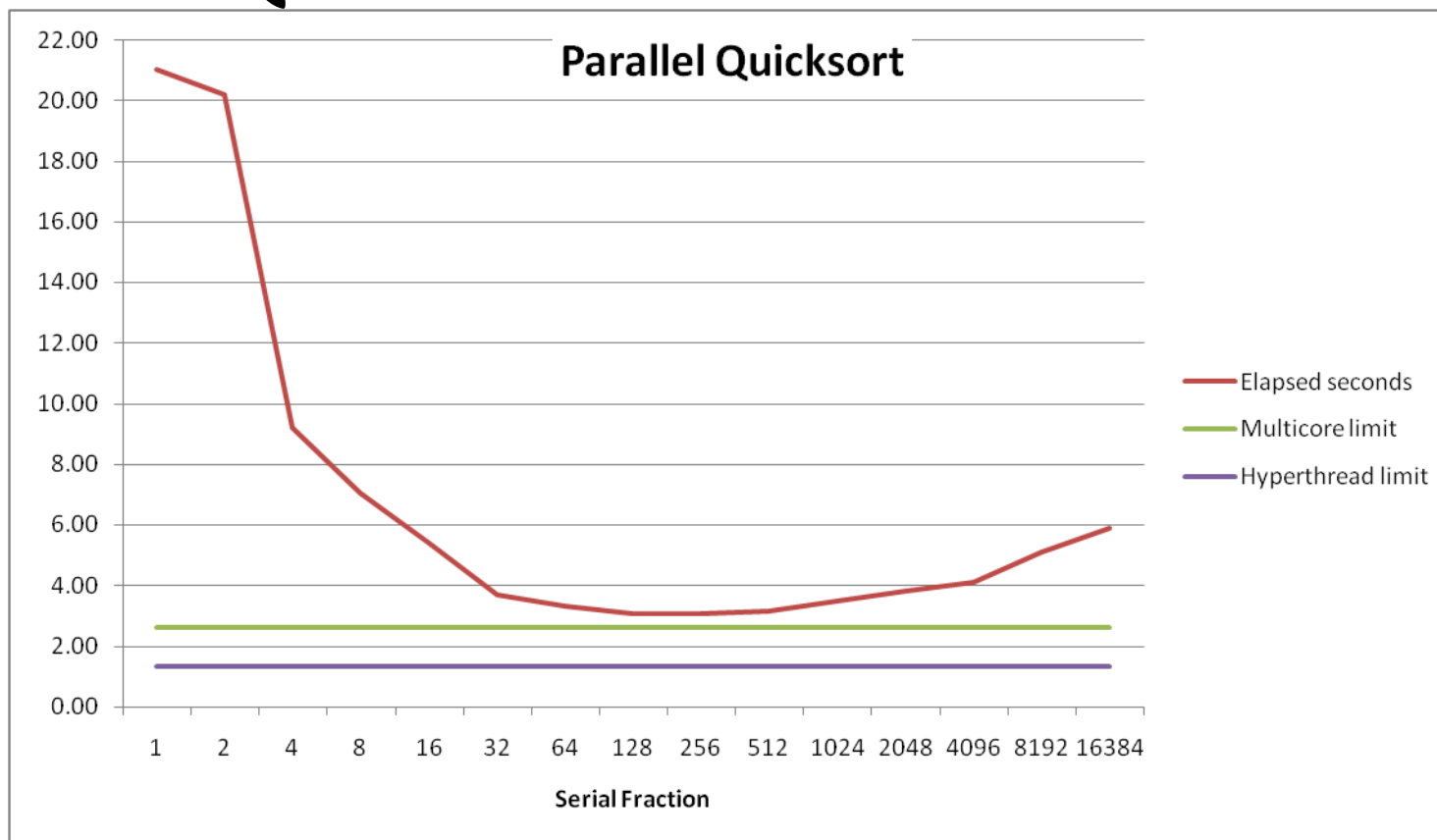
# Parallel Quicksort Performance



- Serial fraction: Fraction of input at which do serial sort
- Sort  $2^{27}$  (134,217,728) random values
- Best speedup = 6.84X



# Parallel Quicksort Performance



- **Good performance over wide range of fraction values**
  - F too small: Not enough parallelism
  - F too large: Thread overhead too high

# Amdahl's Law (Travel Analogy)

		Speed-Up
■ Flying jet non-stop from PIT -> LHR:	7.5 Hours	1
■ Or, old fashioned SST way:		
■ Fly jet from PIT -> JFK: 1.5 Hours		
■ Fly SST from JFK -> LHR: 3.5 Hours	5 Hours	1.5x
■ Or, Using FTL:		
■ Fly jet from PIT -> JFK: 1.5 Hours		
■ Fly FTL from JFK -> LHR: .01 Hours	1.51 Hours	~5x
■ Best possible speed up is 5X, even with FTL because have to get to New York.		

# Amdahl's Law

## ■ Overall problem

- $T$  Total sequential time required
- $p$  Fraction of total that can be sped up ( $0 \leq p \leq 1$ )
- $k$  Speedup factor

## ■ Resulting Performance

- $T_k = pT/k + (1-p)T$ 
  - Portion which can be sped up runs  $k$  times faster
  - Portion which cannot be sped up stays the same
- Maximum possible speedup
  - $k = \infty$
  - $T_\infty = (1-p)T$

# Amdahl's Law (Travel Analogy)

		Speed-Up
■ Flying jet non-stop from PIT -> LHR:	7.5 Hours	1
■ Or, old fashioned SST way:		
■ Fly jet from PIT -> JFK: 1.5 Hours		
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■ Or, Using FTL:		
■ Fly jet from PIT -> JFK: 1.5 Hours		
■ Fly FTL from JFK -> LHR: .01 Hours	1.51 Hours	~5x
■ Best possible speed up is 5X, even with FTL because have to get to New York.		
■ $T=7.5, p=6/7.5=.8, k=\infty \Rightarrow T_{\infty} = (1-p)T=1.5$		max speed-up =5x

# Amdahl's Law Example

## ■ Overall problem

- $T = 10$  Total time required
- $p = 0.9$  Fraction of total which can be sped up
- $k = 9$  Speedup factor

## ■ Resulting Performance

- $T_9 = 0.9 * 10/9 + 0.1 * 10 = 1.0 + 1.0 = 2.0$  (a 5x speedup)

## ■ Maximum possible speedup

- $T_\infty = 0.1 * 10.0 = 1.0$  (a 10x speedup)
  - With **infinite** parallel computing resources!
- Limit speedup shows **algorithmic** limitation

# Amdahl's Law & Parallel Quicksort

## ■ Sequential bottleneck

- Top-level partition: No speedup
- Second level:  $\leq 2X$  speedup
- $k^{\text{th}}$  level:  $\leq 2^{k-1}X$  speedup

## ■ Implications

- Good performance for small-scale parallelism
- Would need to parallelize partitioning step to get large-scale parallelism
  - Parallel Sorting by Regular Sampling
    - H. Shi & J. Schaeffer, J. Parallel & Distributed Computing, 1992

# Lessons Learned

## ■ **Must have parallelization strategy**

- Partition into  $K$  independent parts
- Divide-and-conquer

## ■ **Inner loops must be synchronization free**

- Synchronization operations very expensive

## ■ **Watch out for hardware artifacts**

- Need to understand processor & memory structure
- Sharing and false sharing of global data

## ■ **Beware of Amdahl's Law**

- Serial code can become bottleneck

## ■ **You can do it!**

- Achieving modest levels of parallelism is not difficult
- Set up experimental framework and test multiple strategies