

The Memory Hierarchy

15-213/14-513/15-513: Introduction to Computer Systems
9th Lecture, Summer 2025

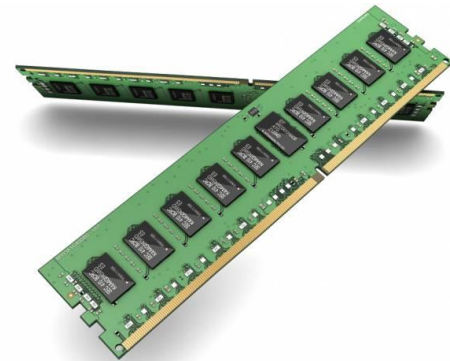
Announcements

- **Attack lab due June 10**

Today

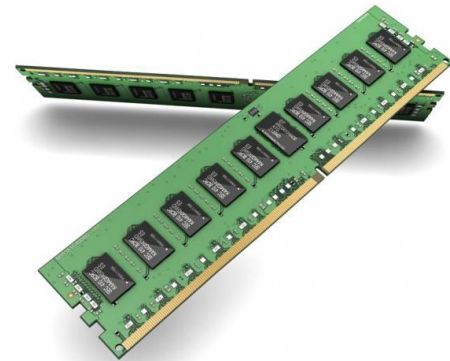
- **The memory abstraction**
- RAM : main memory building block
- Locality of reference
- The memory hierarchy
- Storage technologies and trends

```
movq 8(%rsp), %rax
```



Read from memory to CPU: “Load”

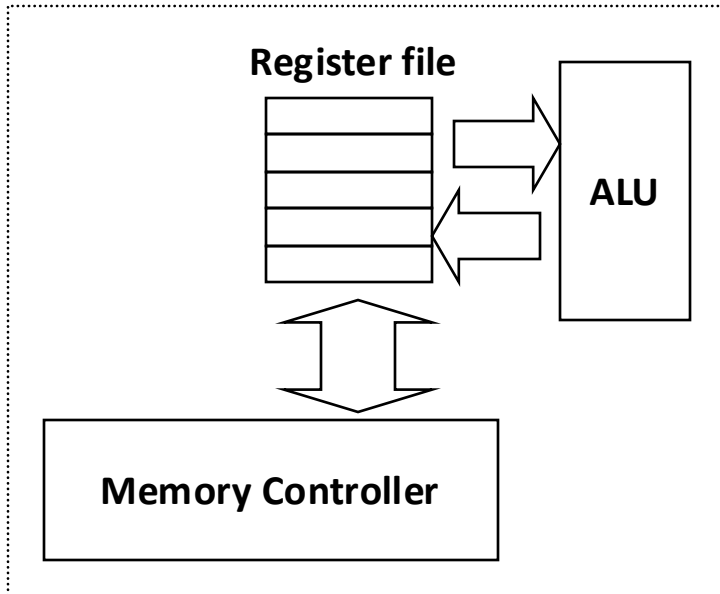
```
movq %rax, (%rbx, %rcx, 2)
```



Write from CPU to memory: “Store”

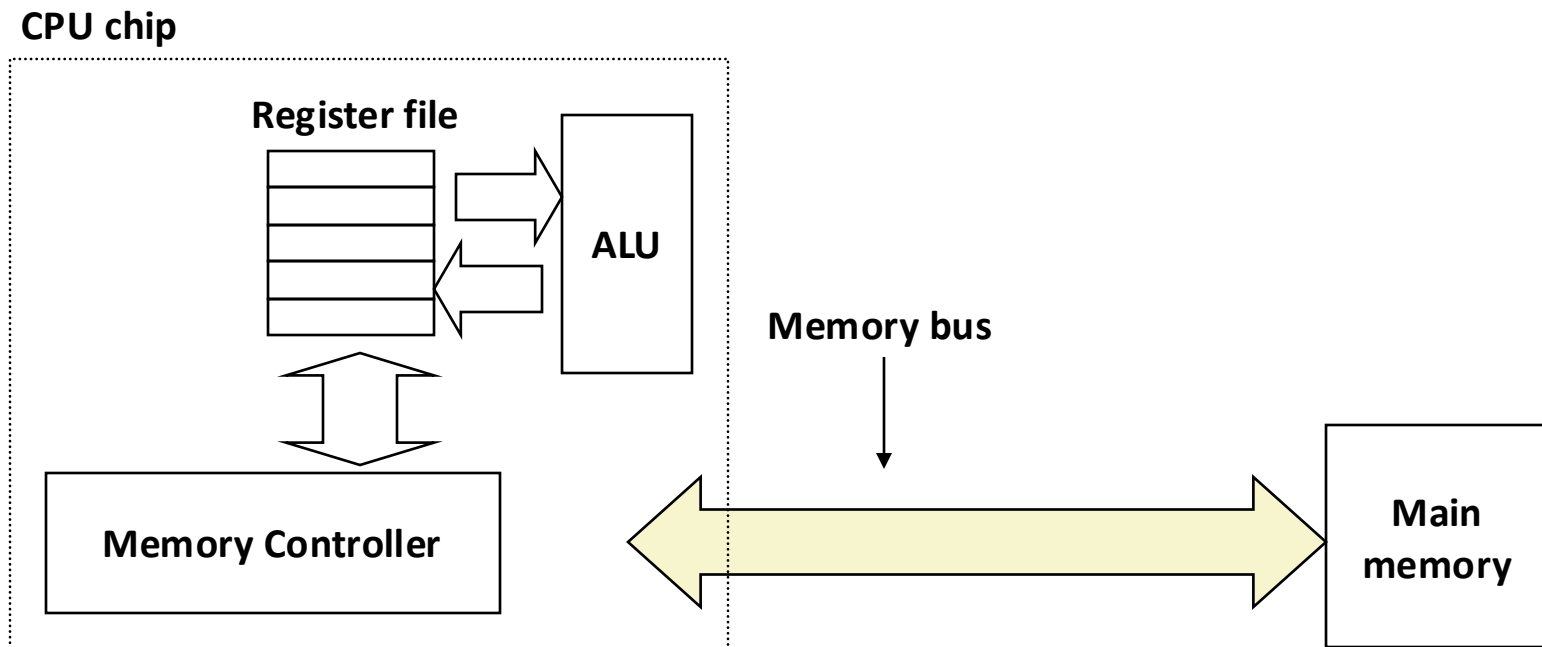
Inside a CPU

CPU chip



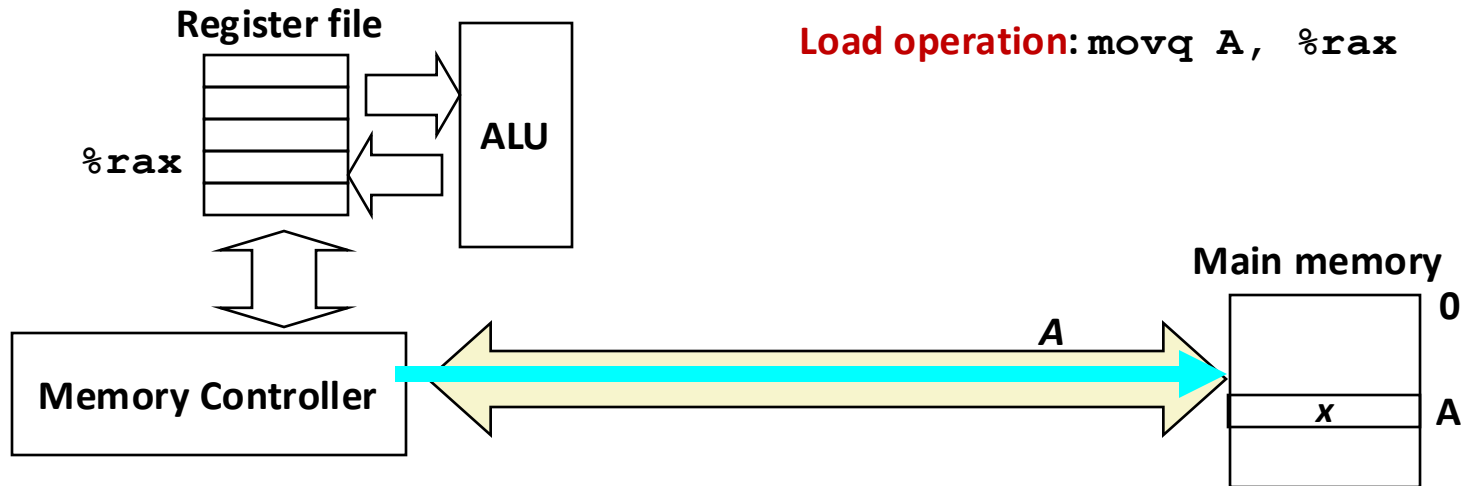
A bus connects the CPU and Memory

- A **bus** is a collection of parallel wires that carry address, data, and control signals.
- Buses are typically shared by multiple devices.



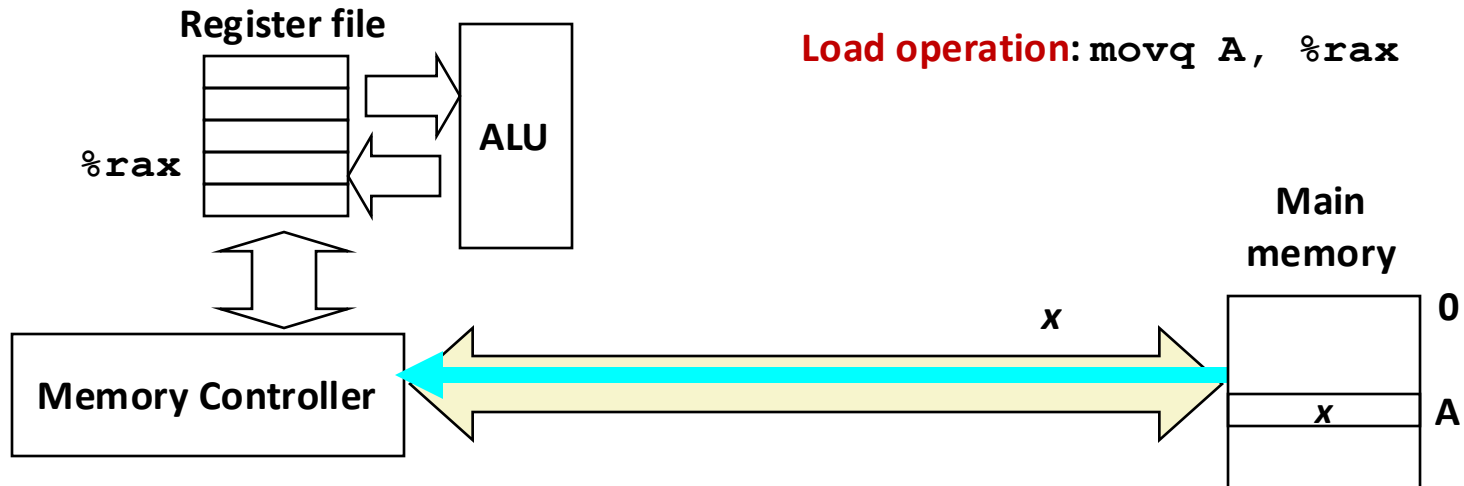
Memory Read Transaction (1)

- CPU places address **A** on the memory bus.



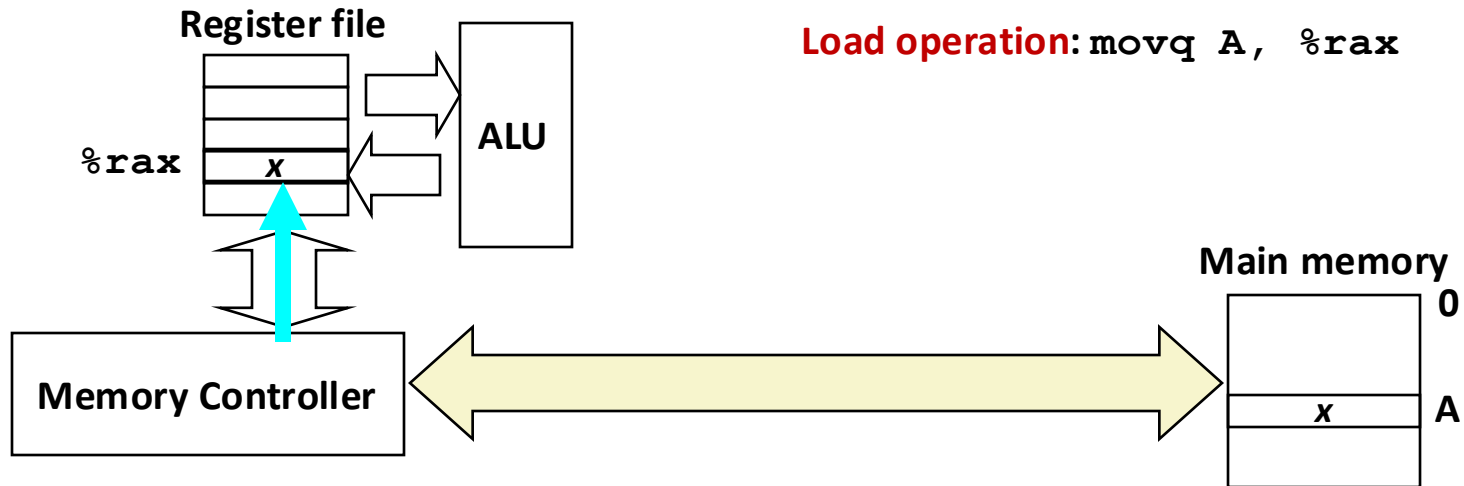
Memory Read Transaction (2)

- Main memory reads A from the memory bus, retrieves word x , and places it on the bus.



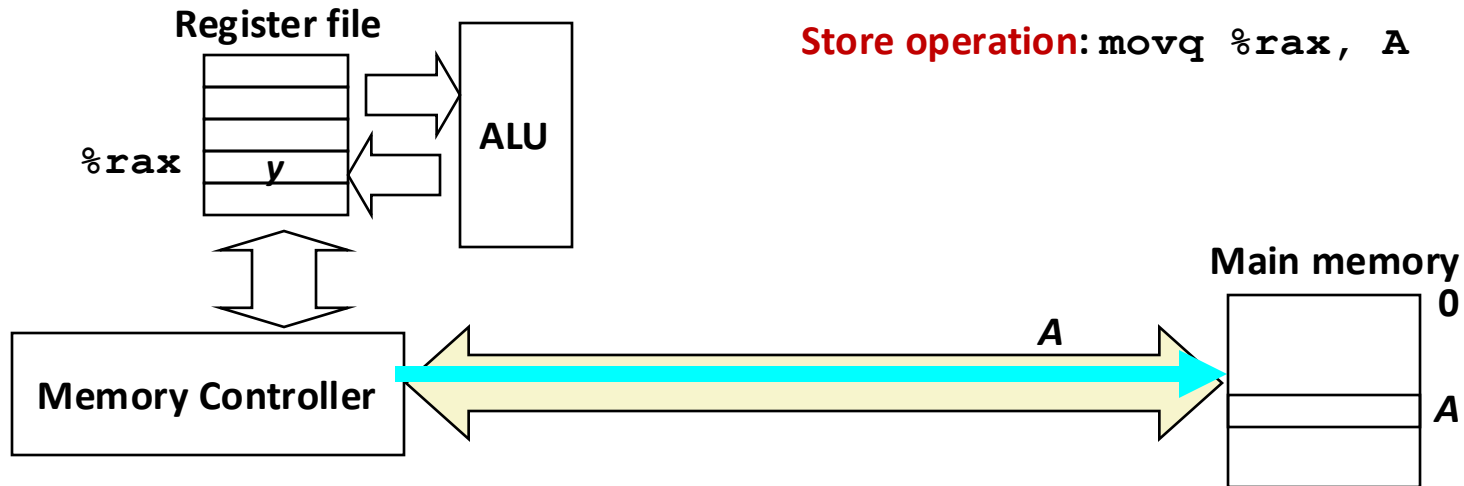
Memory Read Transaction (3)

- CPU reads word x from the bus and copies it into register `%rax`.



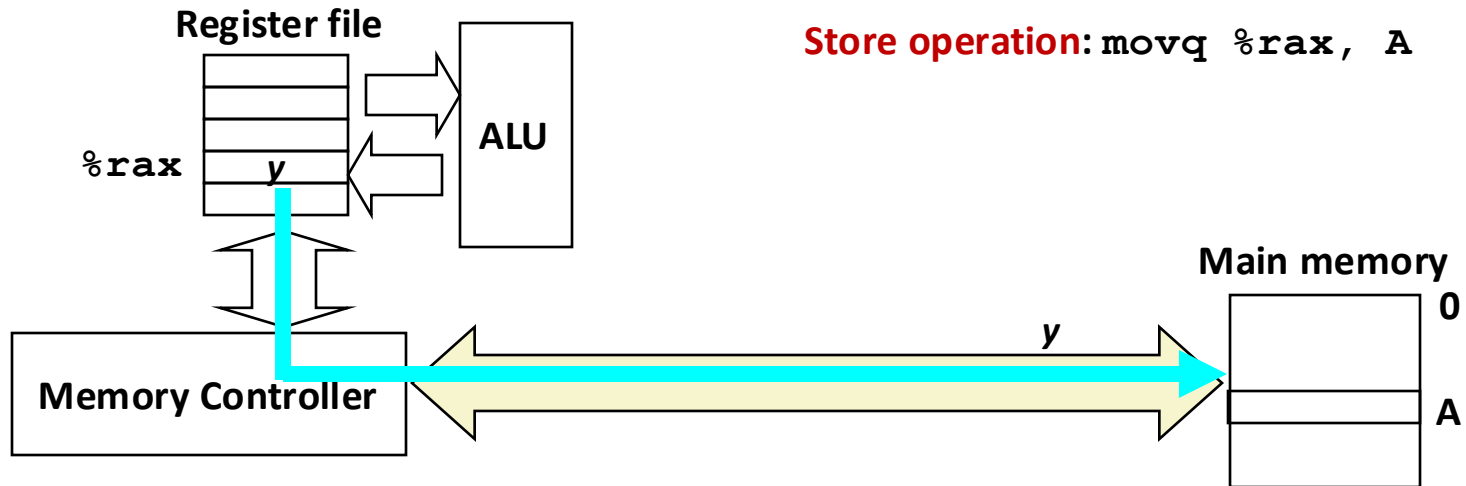
Memory Write Transaction (1)

- CPU places address A on bus. Main memory reads it and waits for the corresponding data word to arrive.



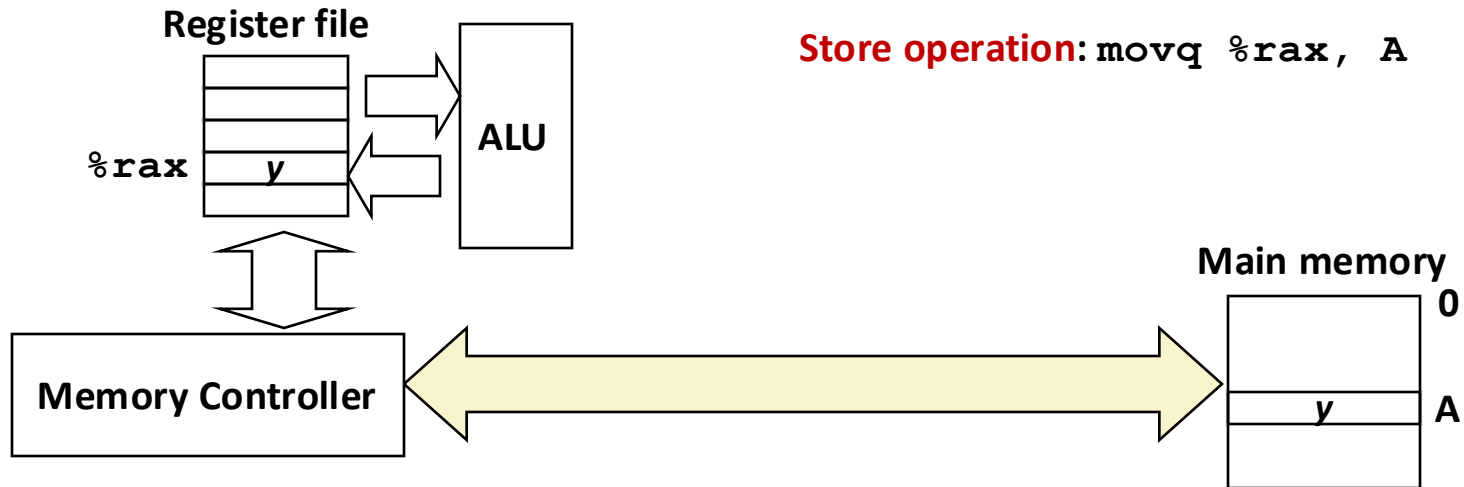
Memory Write Transaction (2)

- CPU places data word y on the bus.



Memory Write Transaction (3)

- Main memory reads data word y from the bus and stores it at address A .



Today

- The memory abstraction
- **RAM : main memory building block**
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Random-Access Memory (RAM)

■ Key features

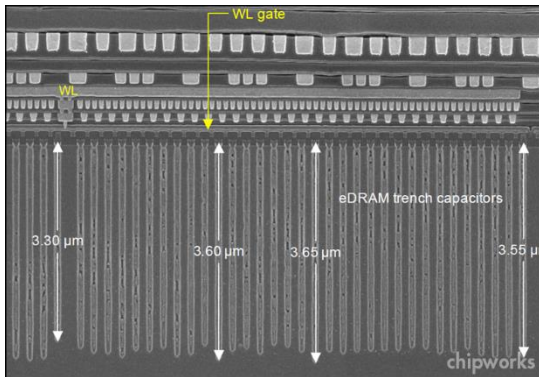
- **RAM** is traditionally packaged as a chip.
 - or embedded as part of processor chip
- Basic storage unit is normally a **cell** (one bit per cell).
- Multiple RAM chips form a memory.

■ RAM comes in two varieties:

- SRAM (Static RAM)
- DRAM (Dynamic RAM)

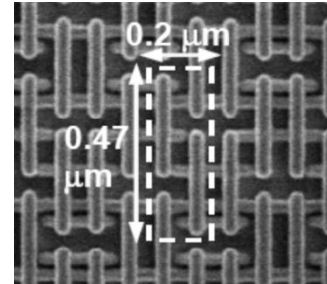
RAM Technologies

■ DRAM



- **1 Transistor + 1 capacitor / bit**
 - Capacitor oriented vertically
- **Must refresh state periodically**

■ SRAM



- **6 transistors / bit**
- **Holds state indefinitely**

SRAM vs DRAM Summary

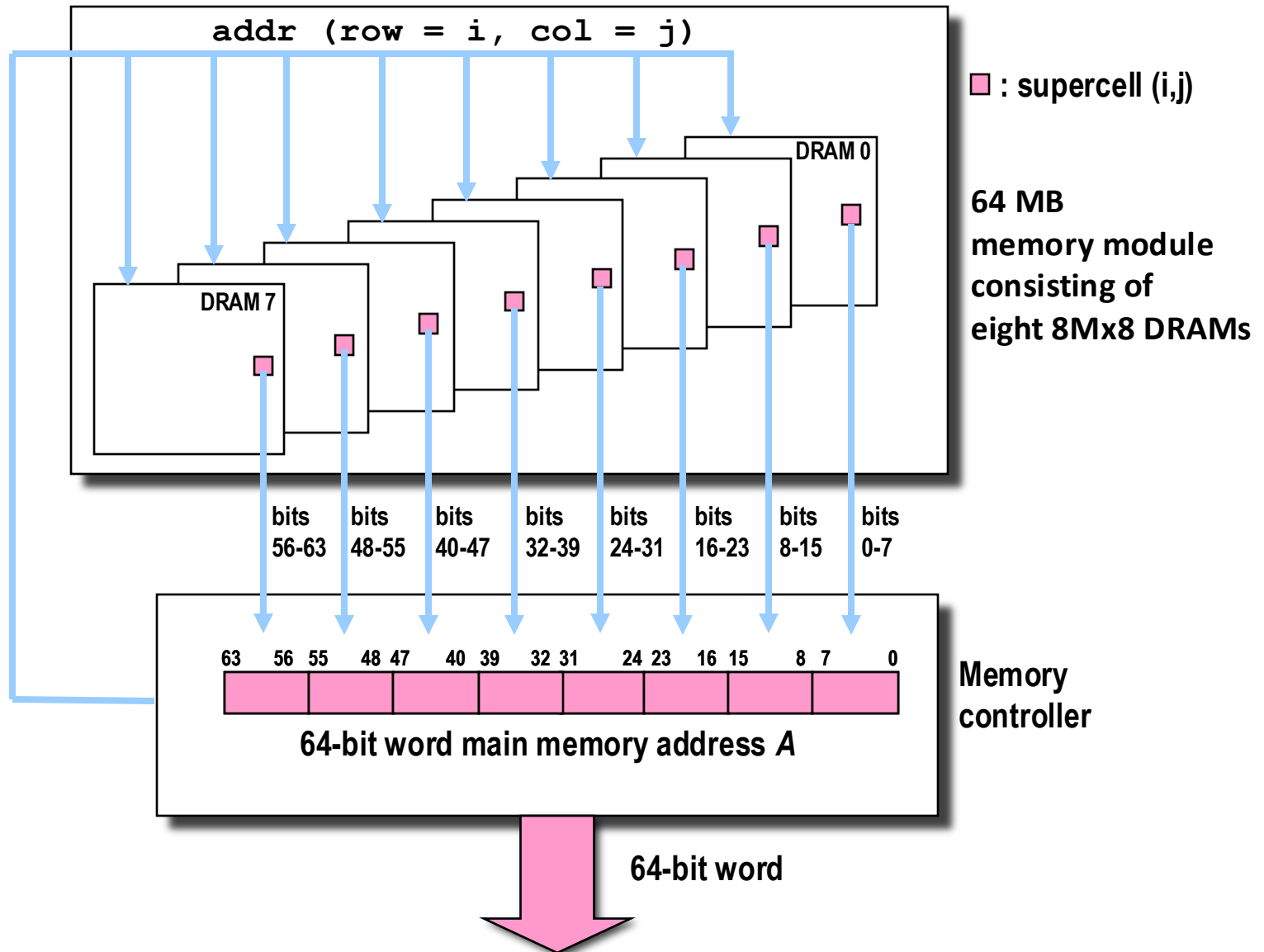
	Trans. per bit	Access time	Needs refresh?	Needs EDC?	Cost	Applications
SRAM	6 or 8	1x	No	Maybe	100x	Cache memories
DRAM	1	10x	Yes	Yes	1x	Main memories, frame buffers

EDC: Error detection and correction

■ Trends

- SRAM scales with semiconductor technology
 - Reaching its limits
- DRAM scaling limited by need for minimum capacitance
 - Aspect ratio limits how deep can make capacitor
 - Also reaching its limits

Data striped across RAM chips in modules

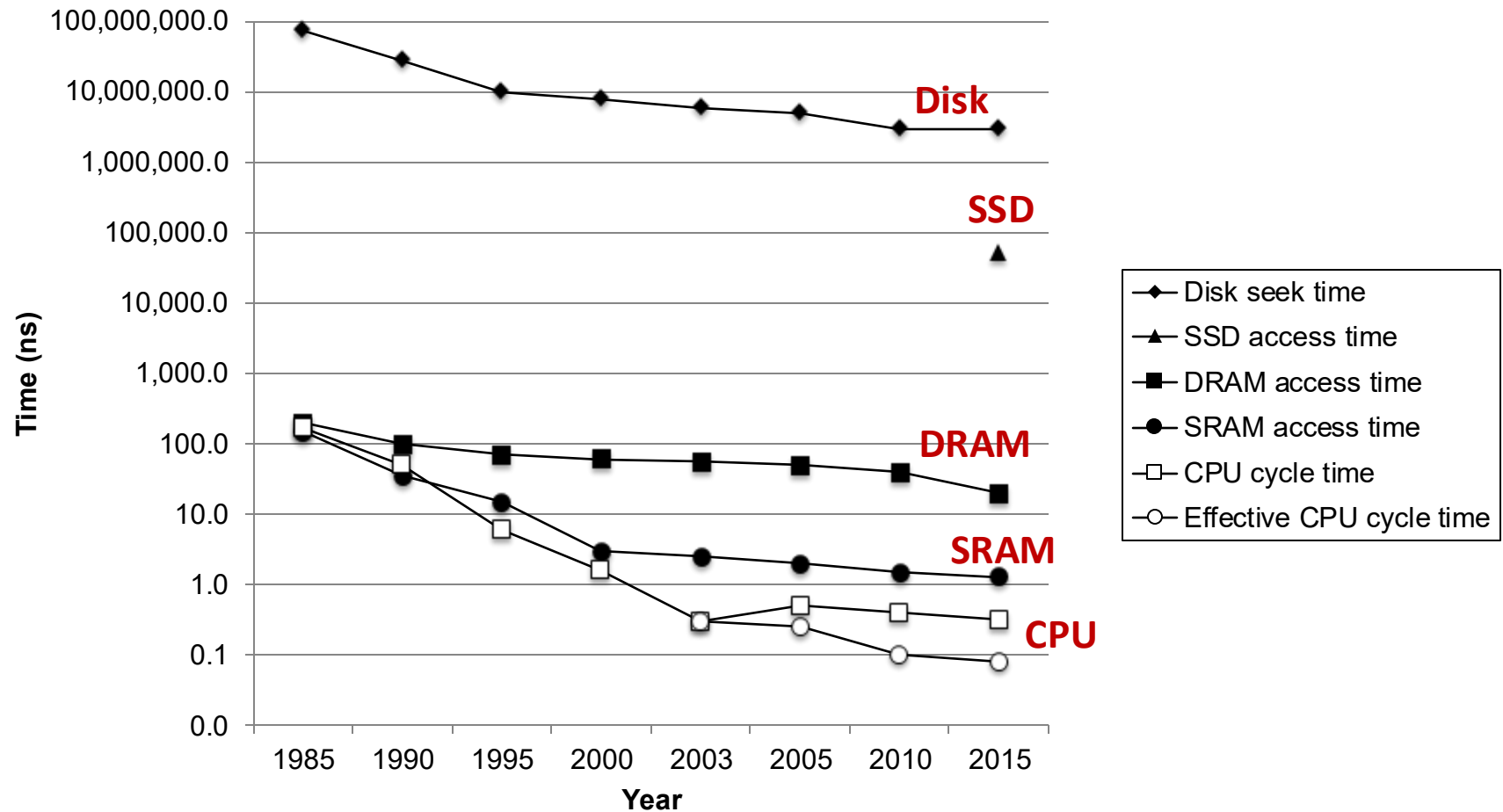


Today

- The memory Abstraction
- DRAM : main memory building block
- **Locality of reference**
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The CPU-Memory Gap Keeps Growing

The gap *widens* between DRAM, disk, and CPU speeds.

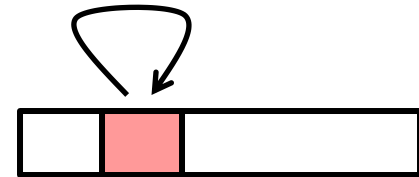


Locality helps us bridge that gap

- **Principle of Locality:** Many programs tend to use data and instructions with addresses near or equal to those they have used recently.

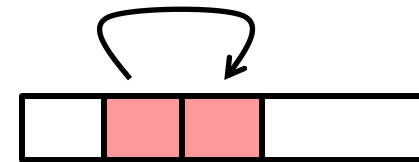
- **Temporal locality:**

- Recently referenced items are likely to be referenced again in the near future



- **Spatial locality:**

- Items with nearby addresses tend to be referenced close together in time



Locality Example

```
sum = 0;  
for (i = 0; i < n; i++)  
    sum += a[i];  
return sum;
```

■ Data references

- Reference array elements in succession (stride-1 reference pattern).
- Reference variable **sum** each iteration.

■ Instruction references

- Reference instructions in sequence.
- Cycle through loop repeatedly.

Spatial or Temporal
Locality?

spatial

temporal

spatial

temporal

Qualitative Estimates of Locality

- **Claim:** Being able to look at code and get a qualitative sense of its locality is a key skill for a professional programmer.
- **Question:** Does this function have good locality with respect to array *a*?

Hint: array layout
is row-major order

Answer: yes

```
int sum_array_rows(int a[M][N])
{
    int i, j, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];

    return sum;
}
```

a		a	a		a		a		a
[0]	...	[0]	[1]	...	[1]	...	[M-1]	...	[M-1]
[0]		[N-1]	[0]		[N-1]		[0]		[N-1]

Locality Example

- **Question:** Does this function have good locality with respect to array *a*?

```
int sum_array_cols(int a[M][N])
{
    int i, j, sum = 0;

    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];
    return sum;
}
```

Answer: no, unless...

M is very small

a		a	a		a		a		a
[0]	...	[0]	[1]	...	[1]	...	[M-1]	...	[M-1]
[0]		[N-1]	[0]		[N-1]		[0]		[N-1]

Locality Example

- **Question:** Can you permute the loops so that the function scans the 3-d array *a* with a stride-1 reference pattern (and thus has good spatial locality)?

```
int sum_array_3d(int a[M][N][N])
{
    int i, j, k, sum = 0;

    for (i = 0; i < N; i++)
        for (j = 0; j < N; j++)
            for (k = 0; k < M; k++)
                sum += a[k][i][j];

    return sum;
}
```

Answer: make *j* the inner loop

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- **The memory hierarchy**

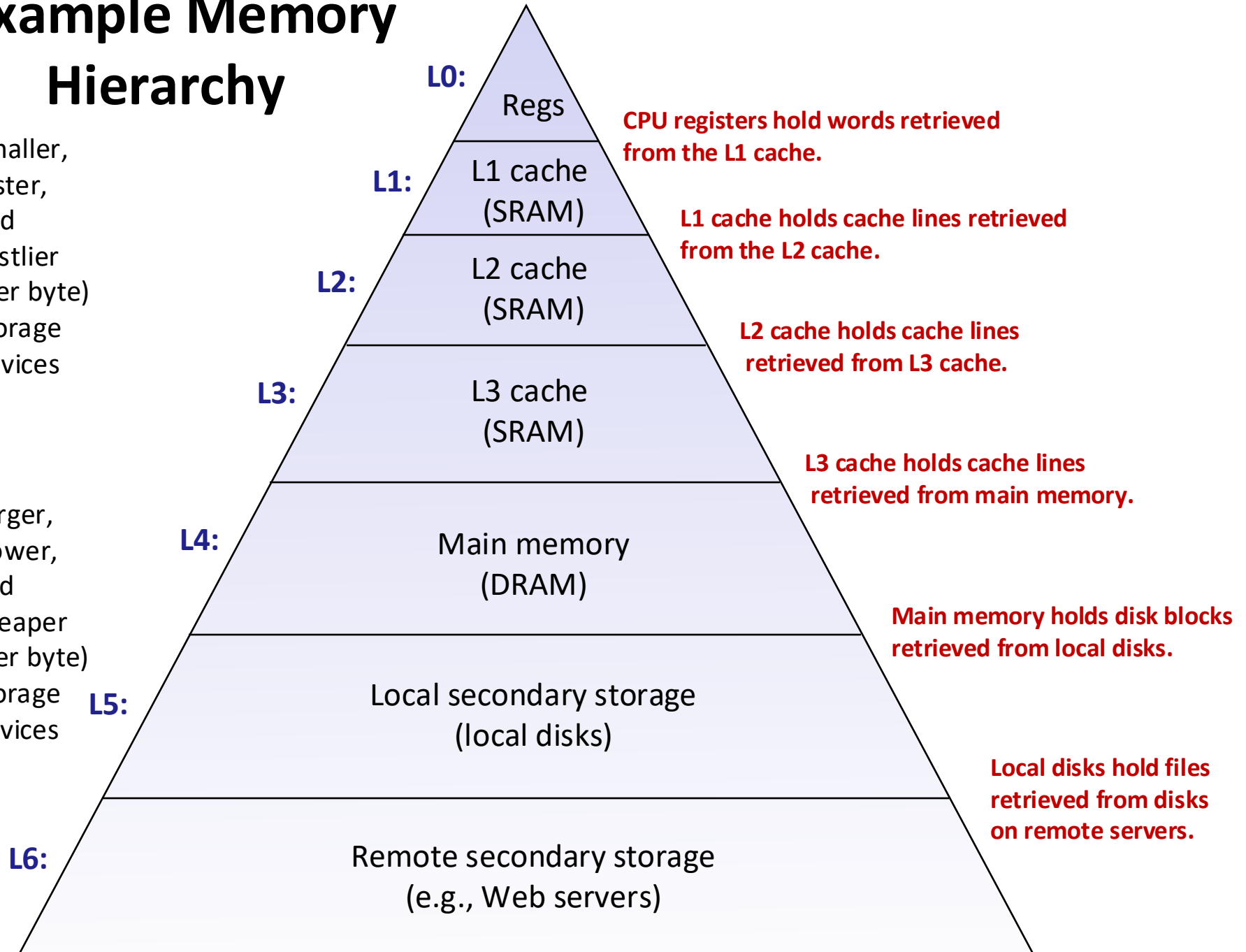
Memory Hierarchies

- **Some fundamental and enduring properties of hardware and software:**
 - Fast storage technologies cost more per byte, have less capacity, and sometimes require more power (heat!).
 - The gap between CPU and main memory speed is widening.
 - Well-written programs tend to exhibit good locality.
- **These properties complement each other well for many types of programs.**
- **They suggest an approach for organizing memory and storage systems known as a **memory hierarchy**.**

Example Memory Hierarchy

↑
Smaller,
faster,
and
costlier
(per byte)
storage
devices

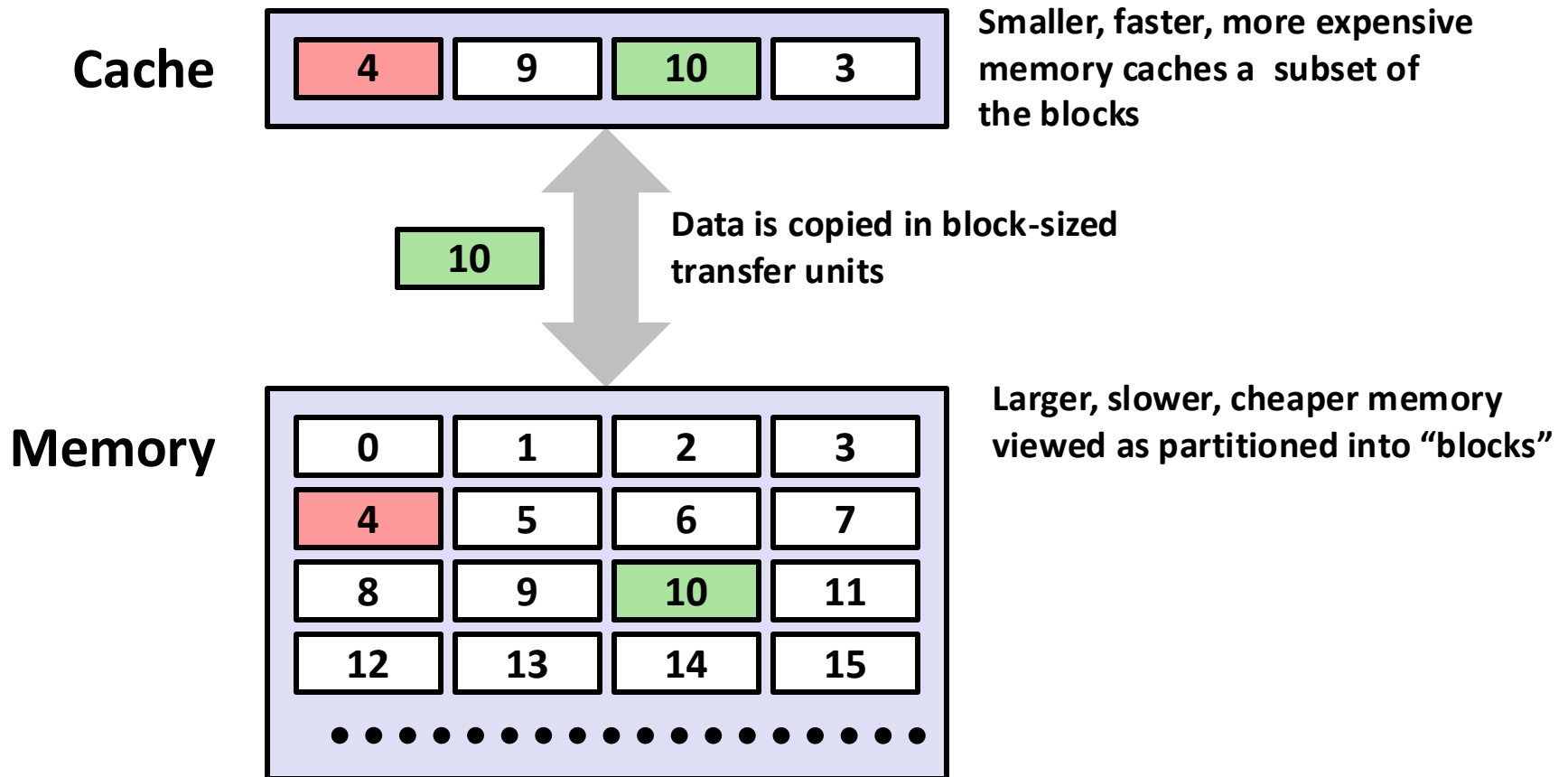
↓
Larger,
slower,
and
cheaper
(per byte)
storage
devices



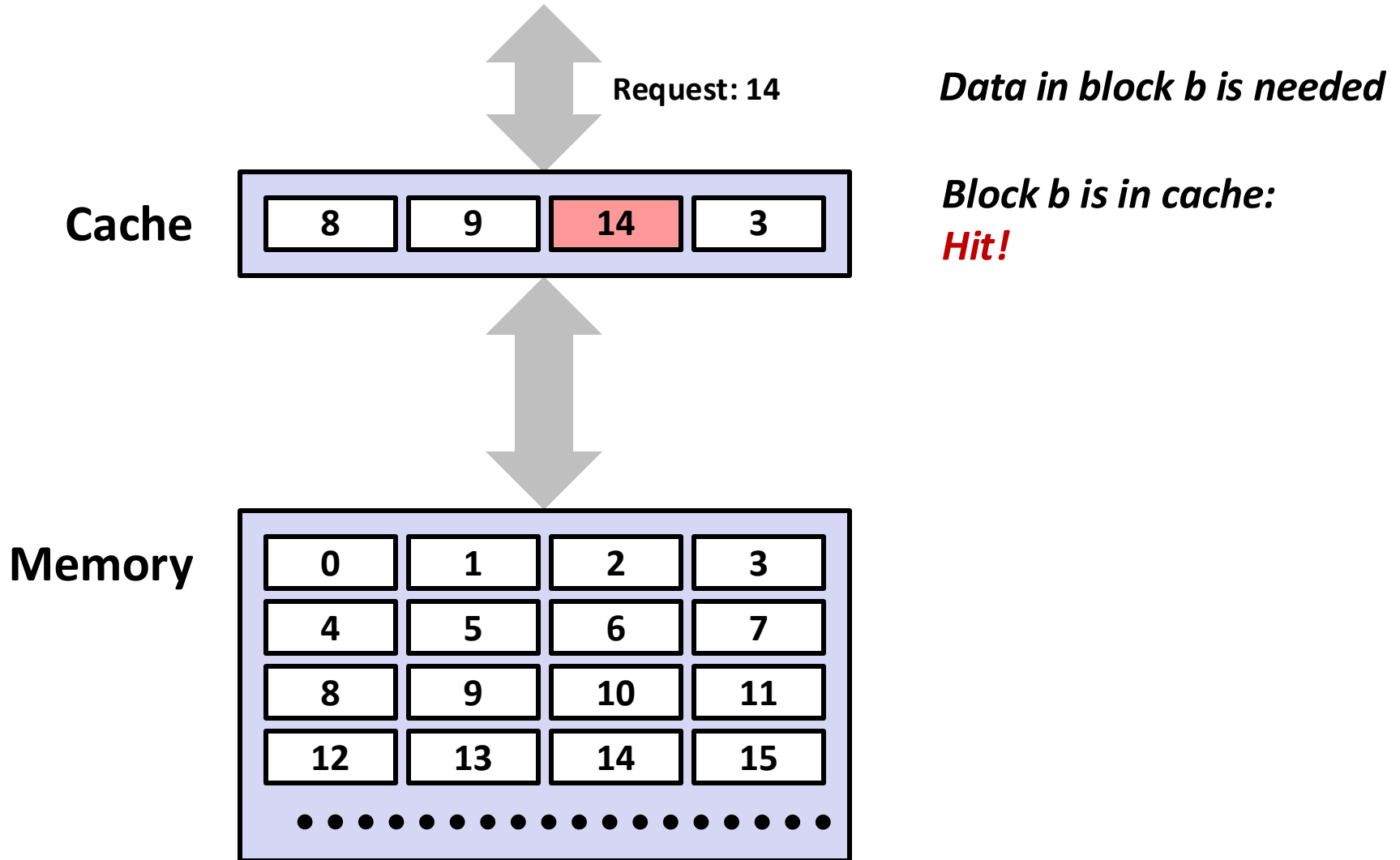
Caches

- **Cache:** A smaller, faster storage device that acts as a staging area for a subset of the data in a larger, slower device.
- **Fundamental idea of a memory hierarchy:**
 - For each k , the faster, smaller device at level k serves as a cache for the larger, slower device at level $k+1$.
- **Why do memory hierarchies work?**
 - Because of locality: programs tend to access the data at level k more often than they access the data at level $k+1$.
 - Thus, the storage at level $k+1$ can be slower, and thus larger and cheaper per bit.
- **Big Idea (Ideal):** The memory hierarchy creates a large pool of storage that costs as much as the cheap storage near the bottom, but that serves data to programs at the rate of the fast storage near the top.

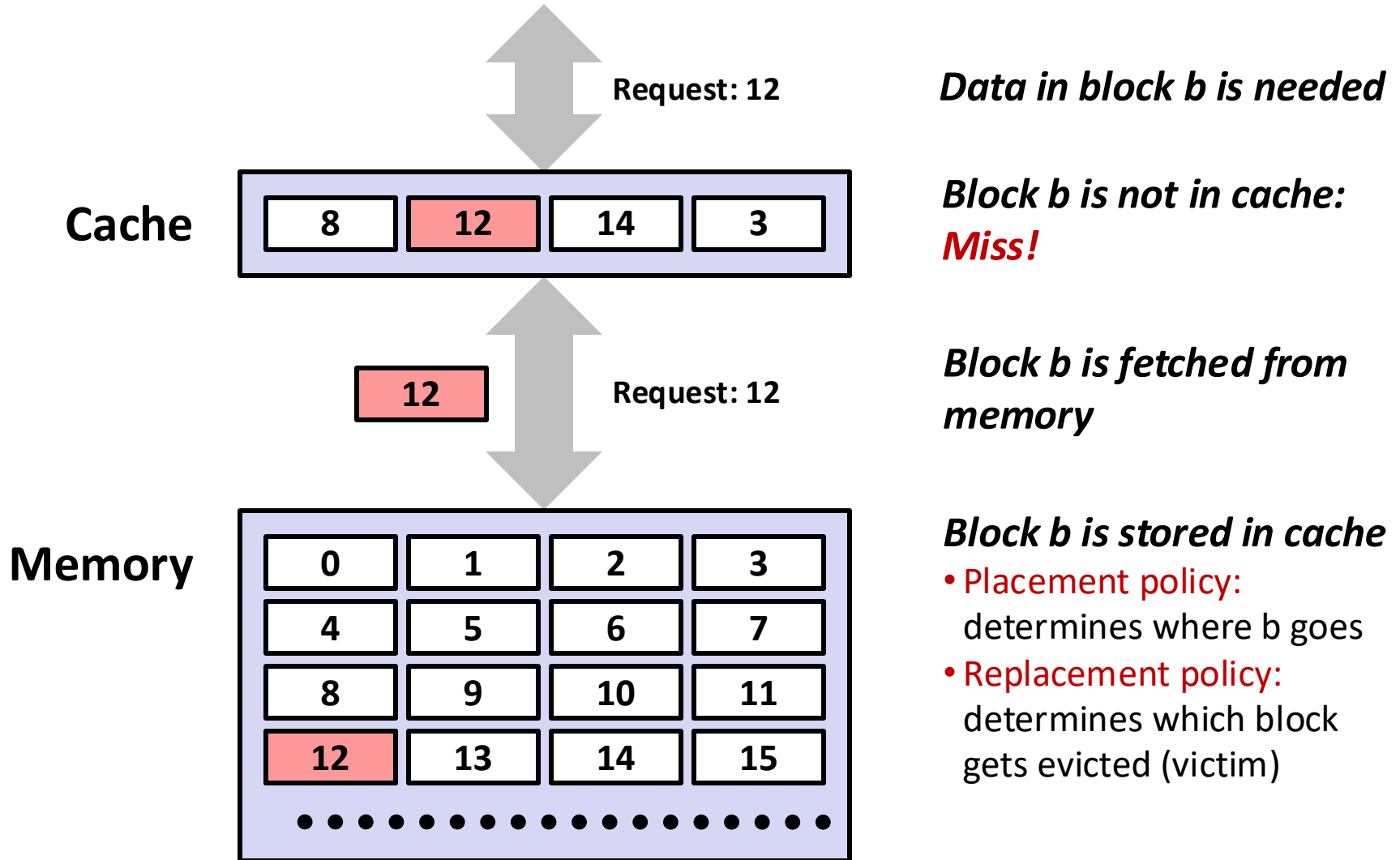
General Cache Concepts



General Cache Concepts: Hit



General Cache Concepts: Miss



General Caching Concepts:

3 Types of Cache Misses

■ Cold (compulsory) miss

- Cold misses occur because the cache starts empty and this is the first reference to the block.

■ Capacity miss

- Occurs when the set of active cache blocks (**working set**) is larger than the cache.

■ Conflict miss

- Most caches limit blocks at level $k+1$ to a small subset (sometimes a singleton) of the block positions at level k .
 - E.g. Block i at level $k+1$ must be placed in block $(i \bmod 4)$ at level k .
- Conflict misses occur when the level k cache is large enough, but multiple data objects all map to the same level k block.
 - E.g. Referencing blocks 0, 8, 0, 8, 0, 8, ... would miss every time.

Examples of Caching in the Mem. Hierarchy

Cache Type	What is Cached?	Where is it Cached?	Latency (cycles)	Managed By
Registers	4-8 byte words	CPU core	0	Compiler
TLB	Address translations	On-Chip TLB	0	Hardware MMU
L1 cache	64-byte blocks	On-Chip L1	4	Hardware
L2 cache	64-byte blocks	On-Chip L2	10	Hardware
Virtual Memory	4-KB pages	Main memory	100	Hardware + OS
Buffer cache	Parts of files	Main memory	100	OS
Disk cache	Disk sectors	Disk controller	100,000	Disk firmware
Network buffer cache	Parts of files	Local disk	10,000,000	NFS client
Browser cache	Web pages	Local disk	10,000,000	Web browser
Web cache	Web pages	Remote server disks	1,000,000,000	Web proxy server

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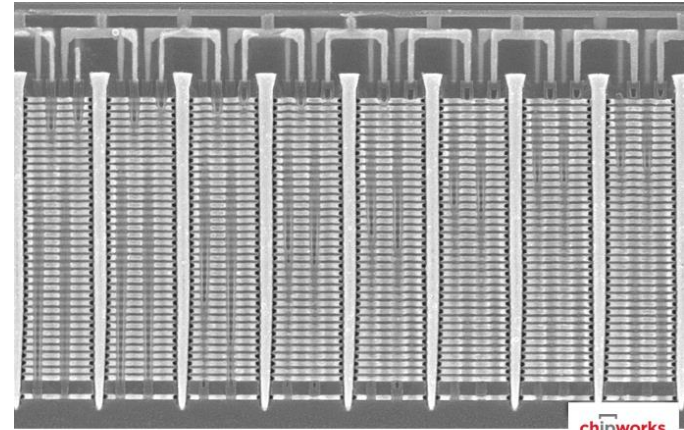
Storage Technologies

- **Magnetic Disks**



- **Store on magnetic medium**
- **Electromechanical access**

- **Nonvolatile (Flash) Memory**



Close-up image of V-NAND flash array

- **Store as persistent charge**
- **Implemented with 3-D structure**
 - 100+ levels of cells
 - 3-4 bits data per cell

What's Inside A Disk Drive?

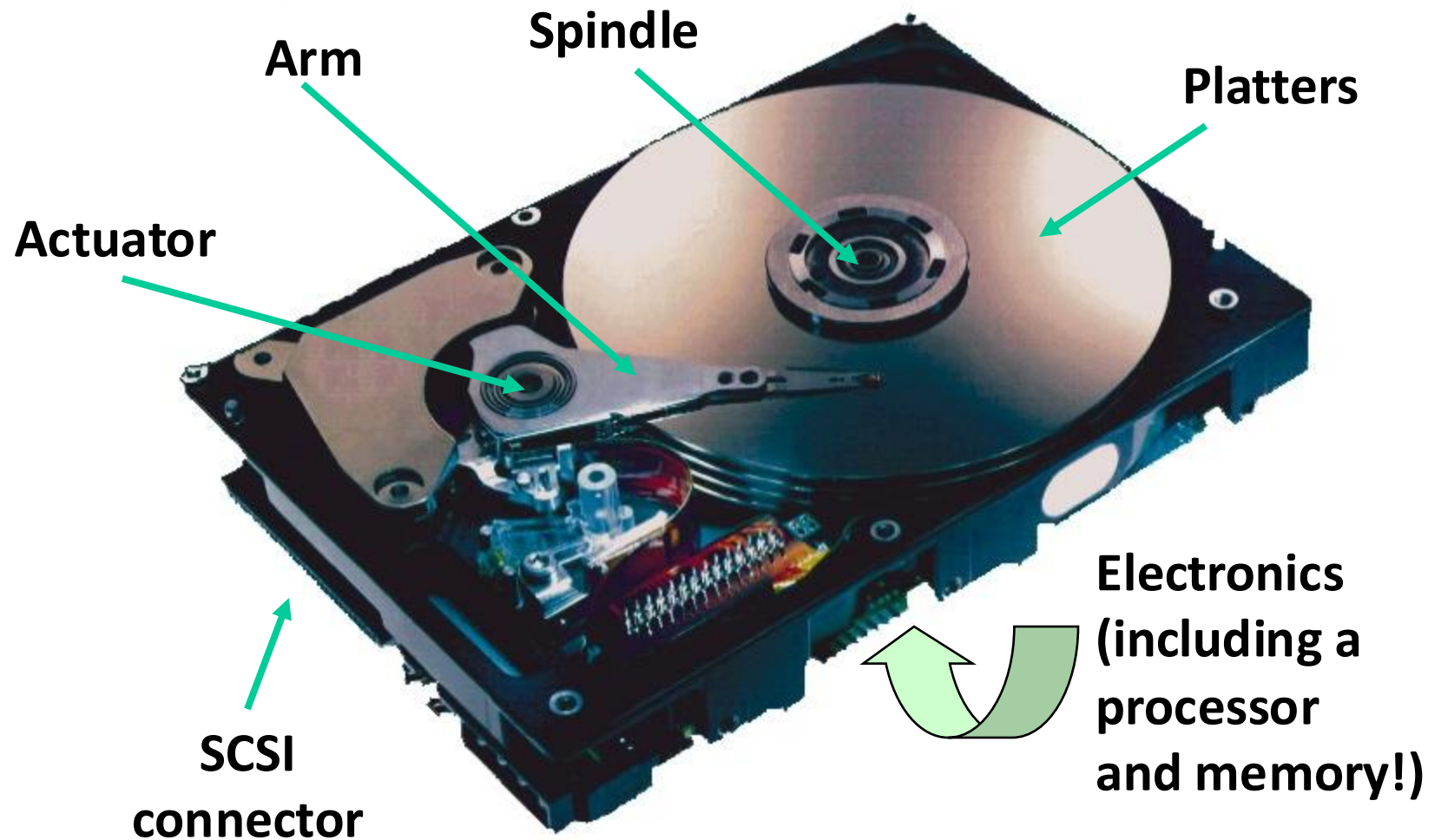
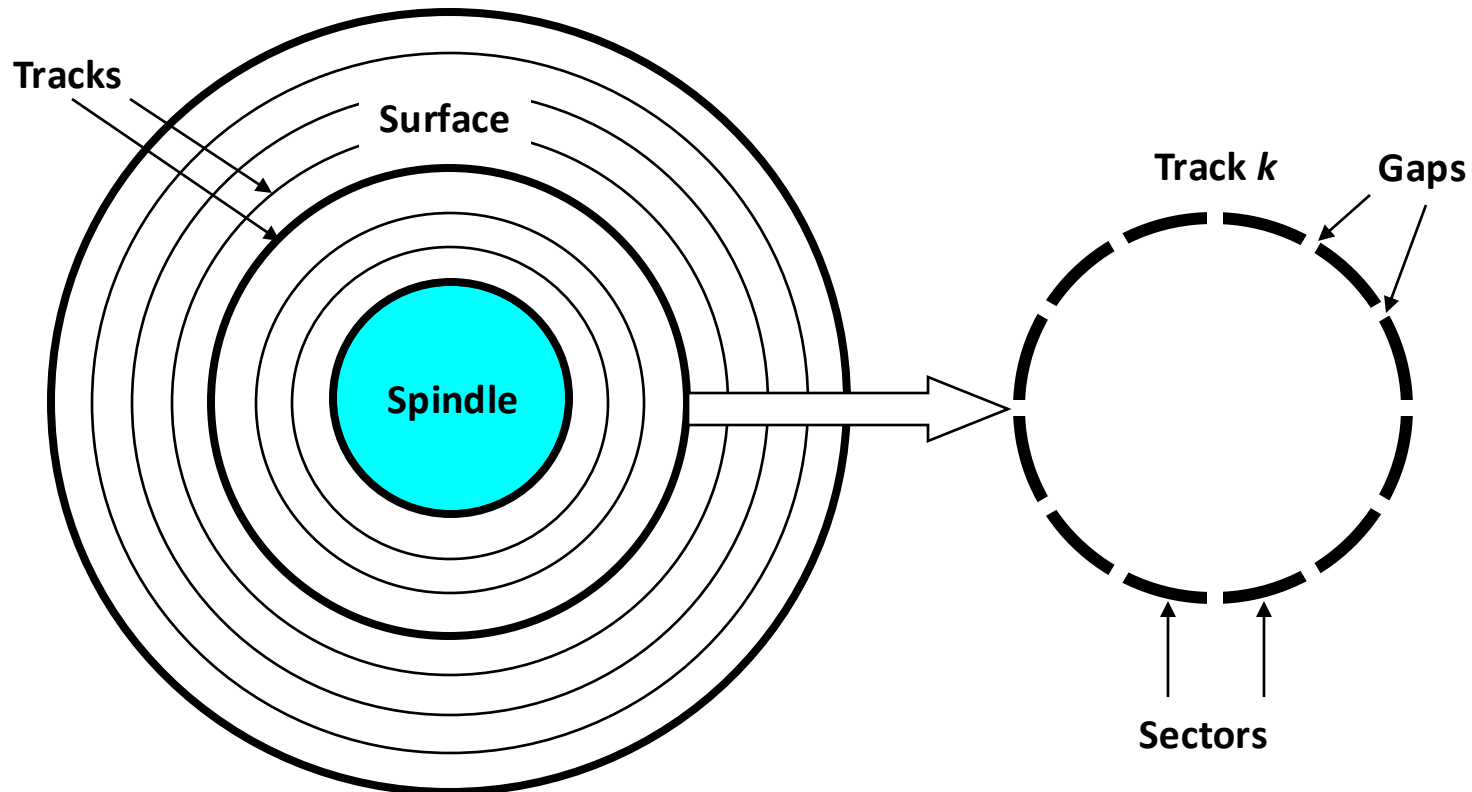


Image courtesy of Seagate Technology

Disk Geometry

- Disks consist of **platters**, each with two **surfaces**.
- Each surface consists of concentric rings called **tracks**.
- Each track consists of **sectors** separated by **gaps**.



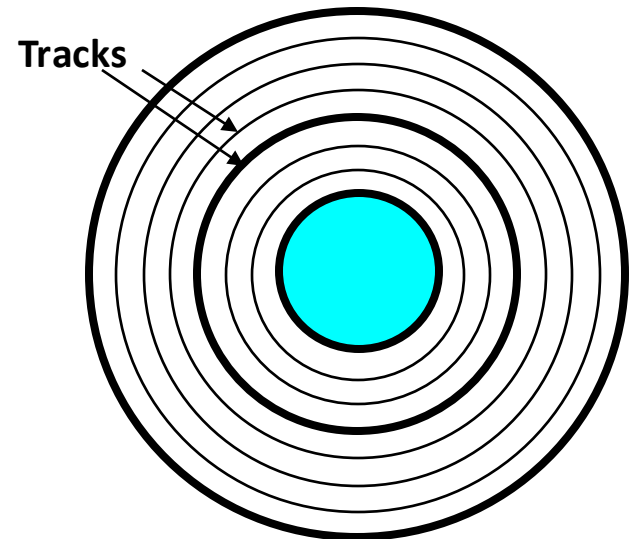
Disk Capacity

- **Capacity**: maximum number of bits that can be stored.

- Vendors express capacity in units of gigabytes (GB) or terabytes (TB), where $1 \text{ GB} = 10^9 \text{ Bytes}$ and $1 \text{ TB} = 10^{12} \text{ Bytes}$

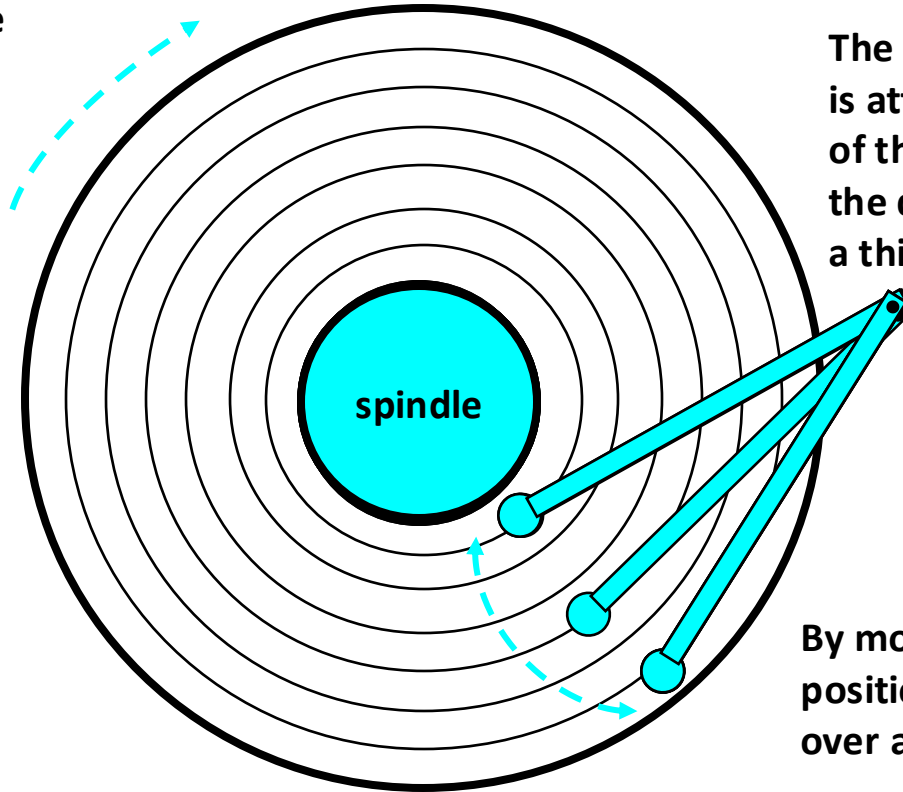
- **Capacity is determined by these technology factors:**

- **Recording density** (bits/in): number of bits that can be squeezed into a 1 inch segment of a track.
- **Track density** (tracks/in): number of tracks that can be squeezed into a 1 inch radial segment.
- **Areal density** (bits/in²): product of recording and track density.



Disk Operation (Single-Platter View)

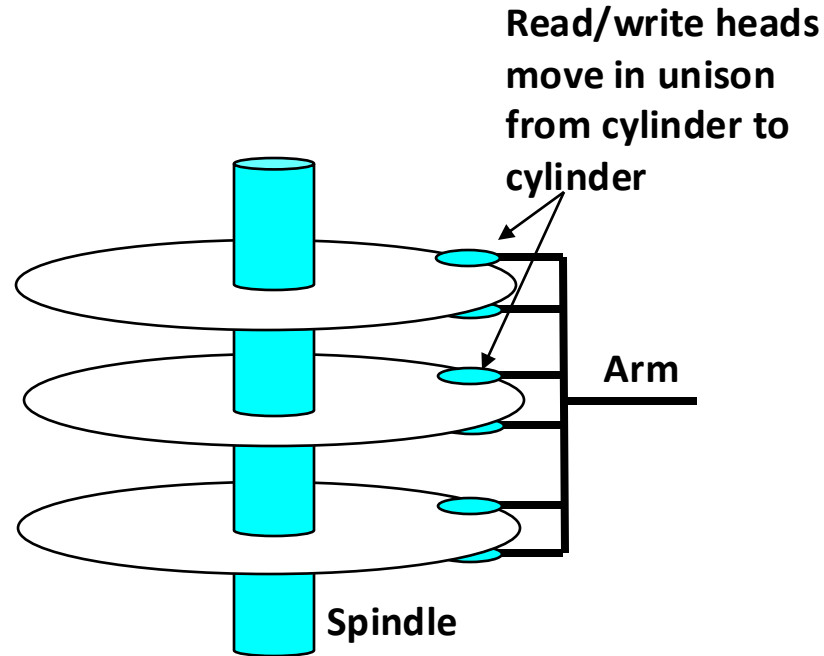
The disk surface spins at a fixed rotational rate



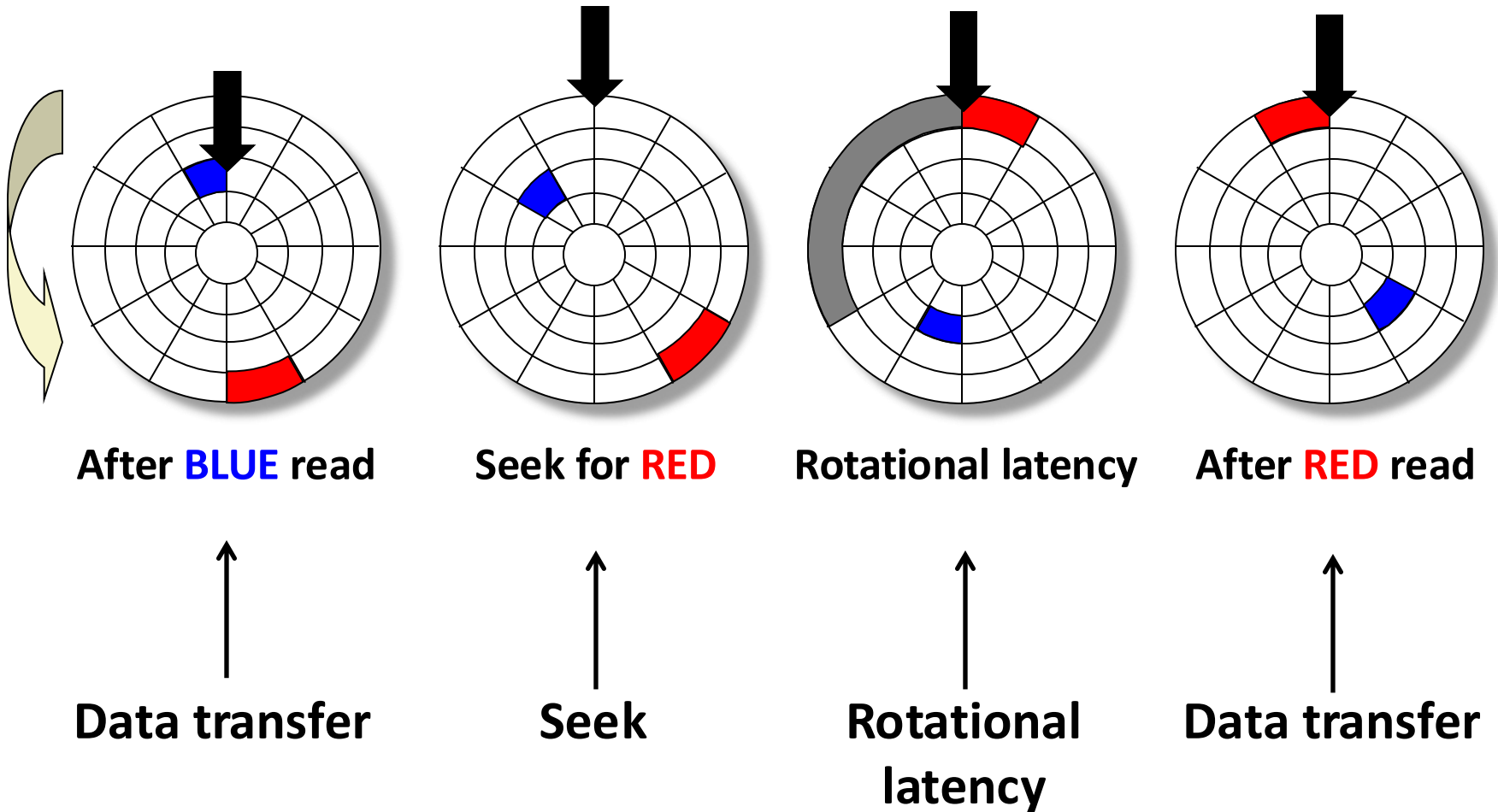
The read/write *head* is attached to the end of the *arm* and flies over the disk surface on a thin cushion of air.

By moving radially, the arm can position the read/write head over any track.

Disk Operation (Multi-Platter View)



Disk Access – Service Time Components



Disk Access Time

■ Average time to access some target sector approximated by:

- $T_{\text{access}} = T_{\text{avg seek}} + T_{\text{avg rotation}} + T_{\text{avg transfer}}$

■ Seek time ($T_{\text{avg seek}}$)

- Time to position heads over cylinder containing target sector.
- Typical $T_{\text{avg seek}}$ is 3—9 ms

■ Rotational latency ($T_{\text{avg rotation}}$)

- Time waiting for first bit of target sector to pass under r/w head.
- $T_{\text{avg rotation}} = 1/2 \times 1/\text{RPMs} \times 60 \text{ sec}/1 \text{ min}$
- Typical rotational rate = 7,200 RPMs

■ Transfer time ($T_{\text{avg transfer}}$)

- Time to read the bits in the target sector.
- $T_{\text{avg transfer}} = 1/\text{RPM} \times 1/(\text{avg \# sectors/track}) \times 60 \text{ secs}/1 \text{ min}$

time for one rotation (in minutes) fraction of a rotation to be read

Disk Access Time Example

■ Given:

- Rotational rate = 7,200 RPM
- Average seek time = 9 ms
- Avg # sectors/track = 400

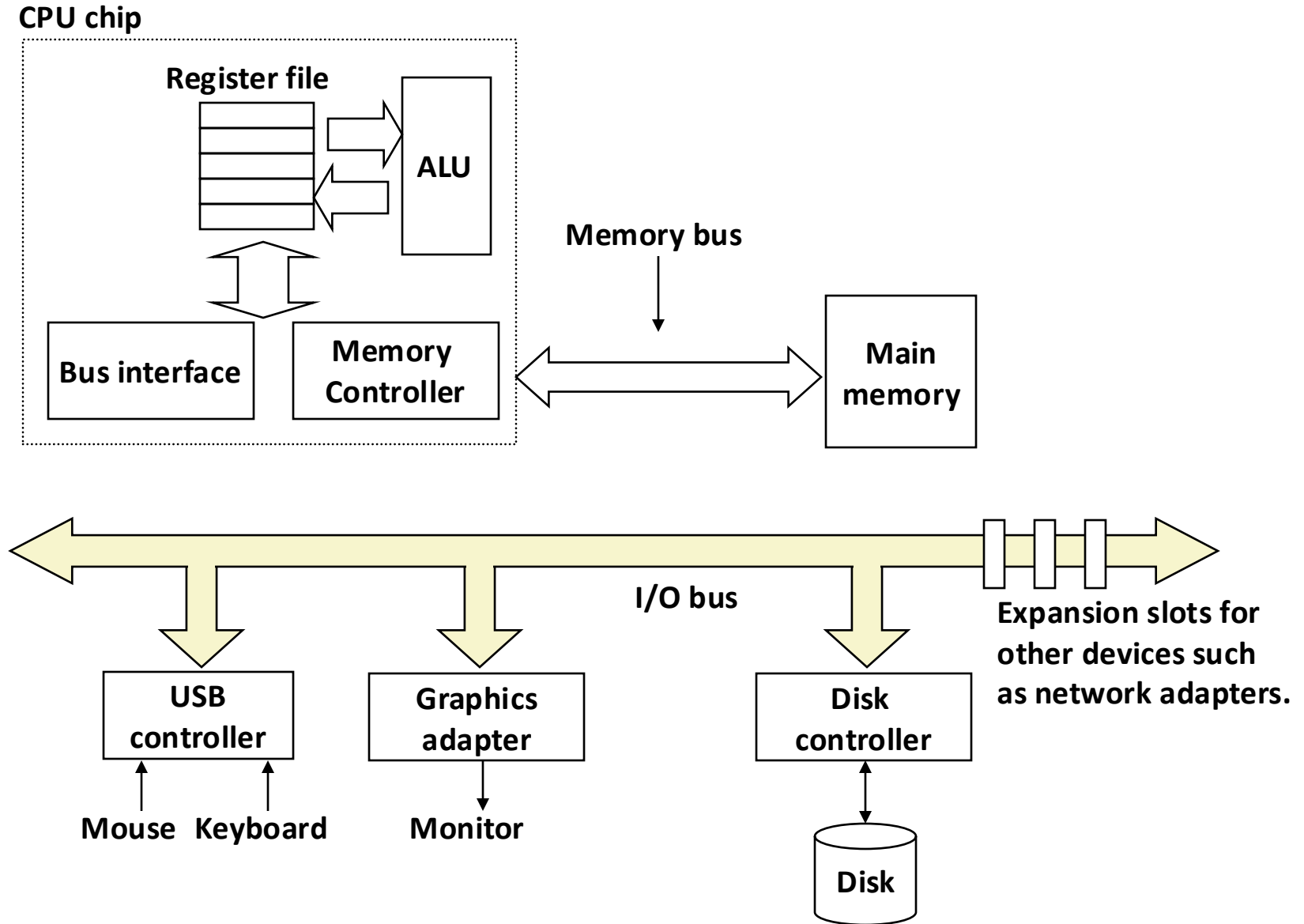
■ Derived:

- $T_{\text{avg rotation}} = 1/2 \times (60 \text{ secs}/7200 \text{ RPM}) \times 1000 \text{ ms/sec} = 4 \text{ ms}$
- $T_{\text{avg transfer}} = 60/7200 \times 1/400 \times 1000 \text{ ms/sec} = 0.02 \text{ ms}$
- $T_{\text{access}} = 9 \text{ ms} + 4 \text{ ms} + 0.02 \text{ ms}$

■ Important points:

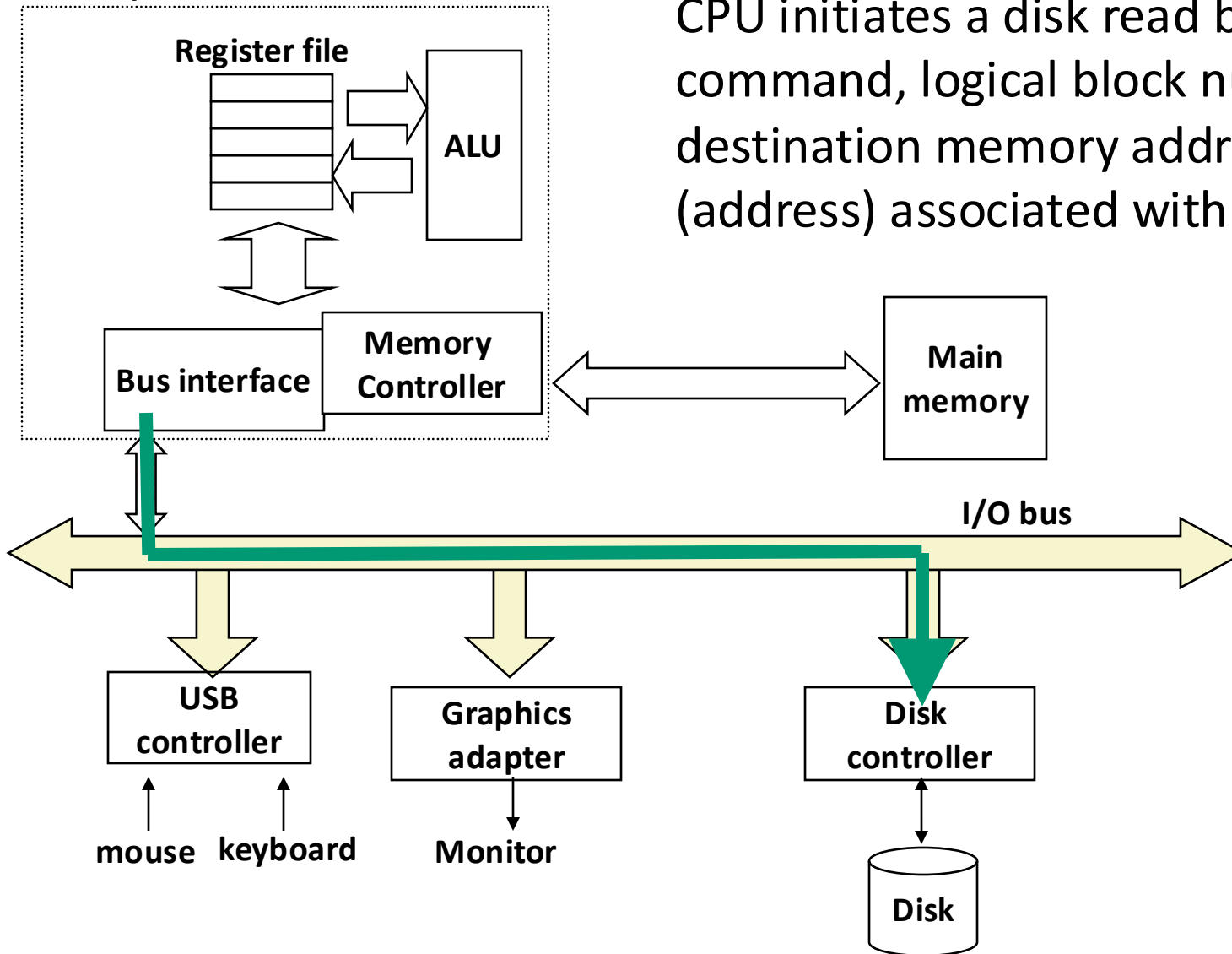
- Access time dominated by seek time and rotational latency.
- First bit in a sector is the most expensive, the rest are free.
- *SRAM access time is about 4 ns/doubleword, DRAM about 60 ns*
 - *Disk is about 40,000 times slower than SRAM,*
 - *2,500 times slower than DRAM.*

I/O Bus



Reading a Disk Sector (1)

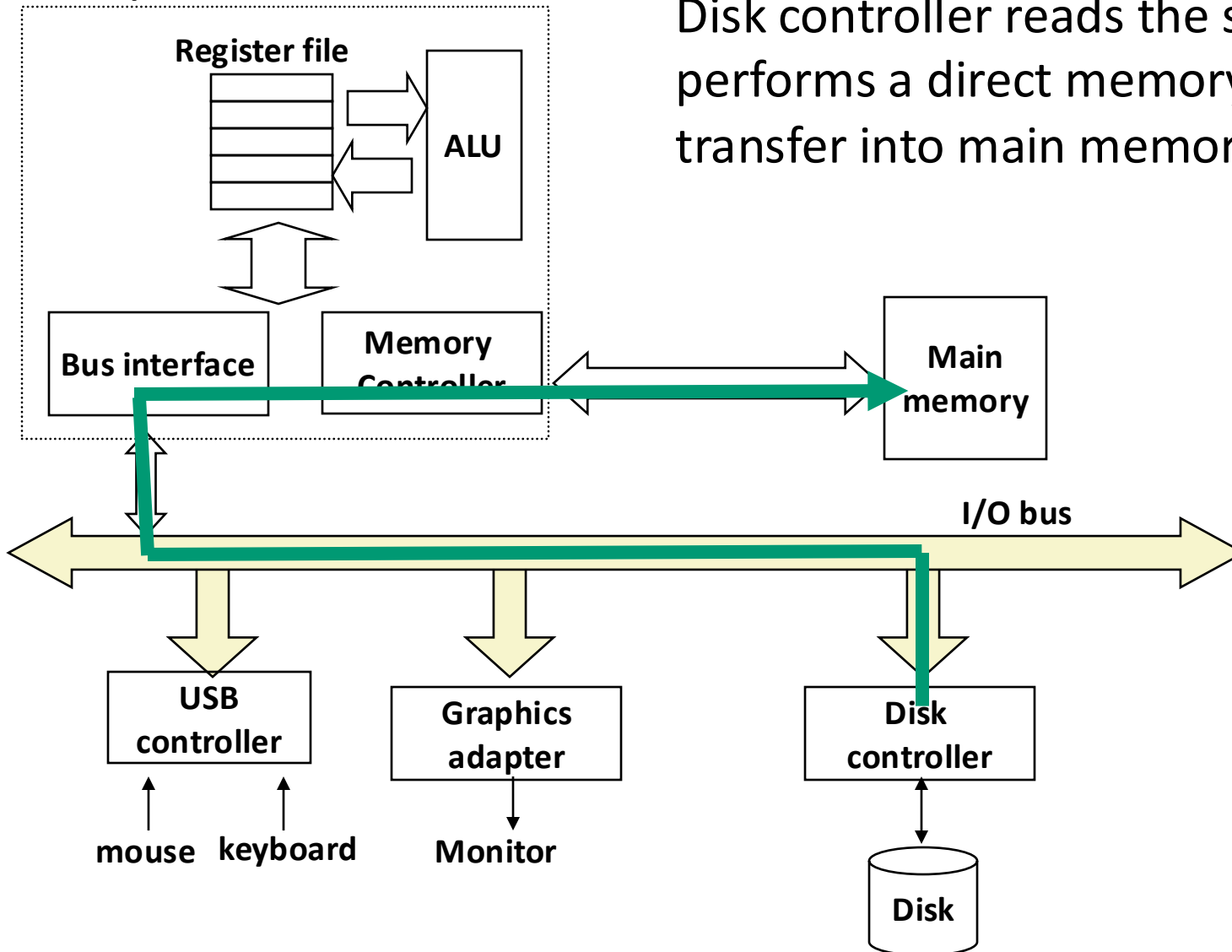
CPU chip



CPU initiates a disk read by writing a command, logical block number, and destination memory address to a **port** (address) associated with disk controller.

Reading a Disk Sector (2)

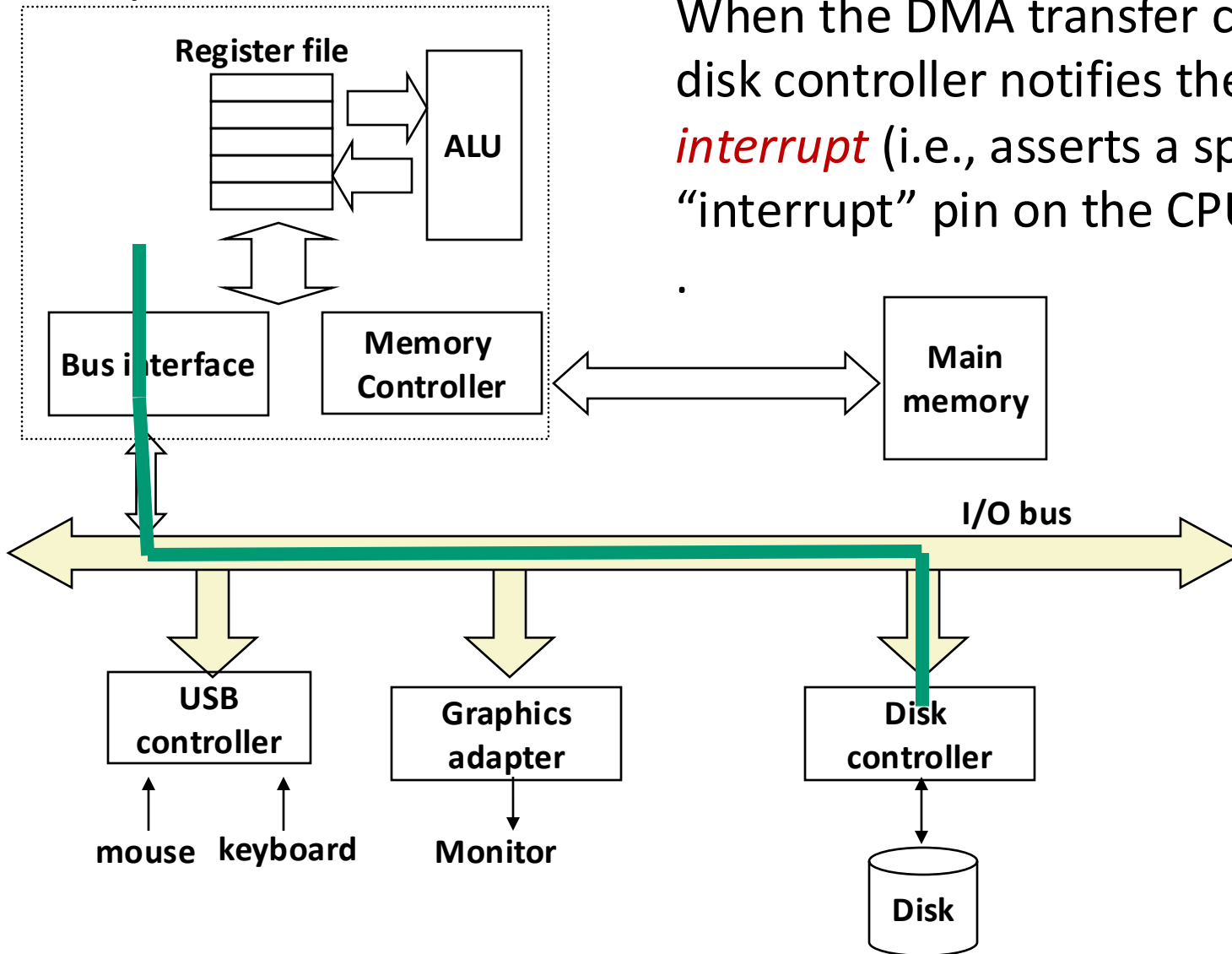
CPU chip



Disk controller reads the sector and performs a direct memory access (**DMA**) transfer into main memory.

Reading a Disk Sector (3)

CPU chip



When the DMA transfer completes, the disk controller notifies the CPU with an *interrupt* (i.e., asserts a special “interrupt” pin on the CPU).

Nonvolatile Memories

■ DRAM and SRAM are volatile memories

- Lose information if powered off.

■ Nonvolatile memories retain value even if powered off

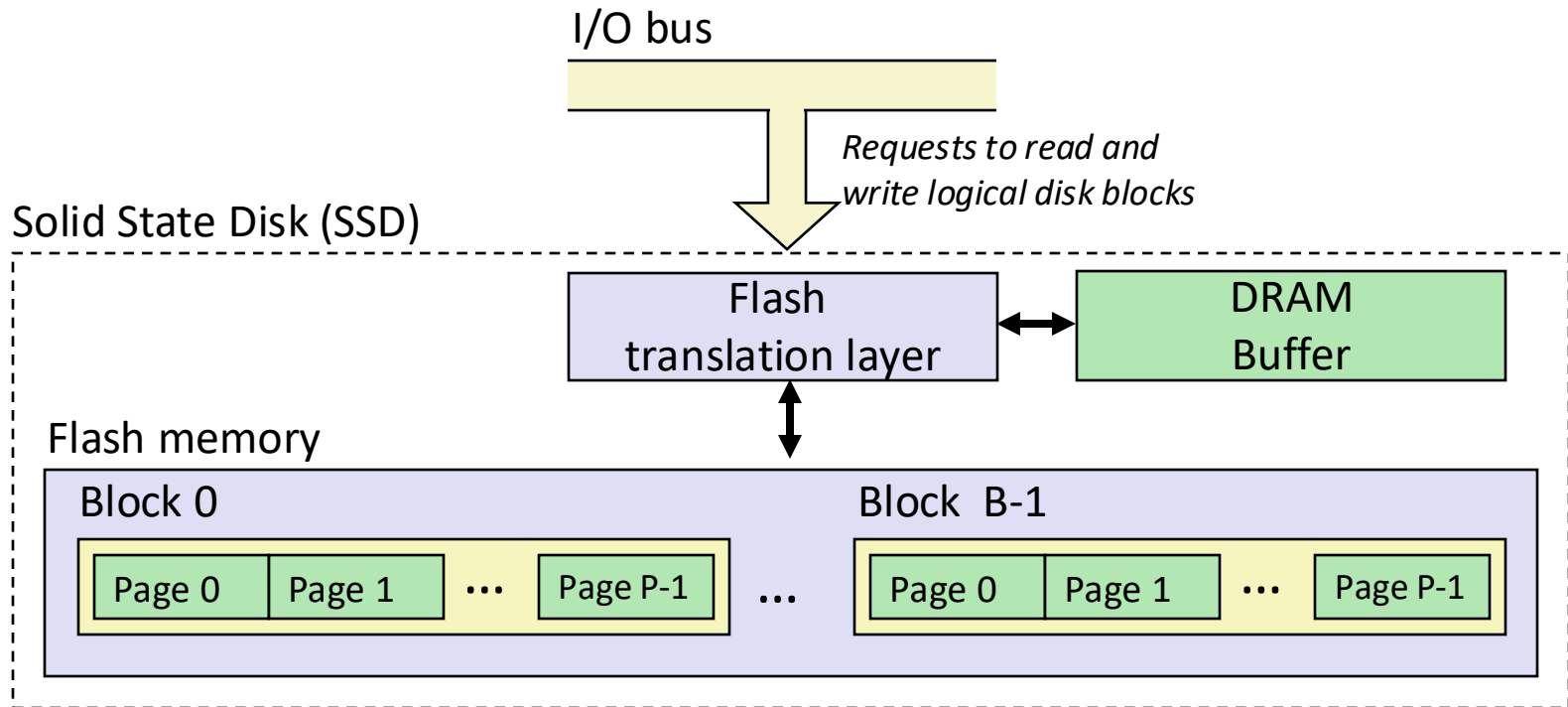
- Read-only memory (**ROM**): programmed during production
- Electrically erasable PROM (**EEPROM**): electronic erase capability
- Flash memory: EEPROMs, with partial (block-level) erase capability
 - Wears out after about 100,000 erasings
- 3D Xpoint? (Intel Optane) & emerging? NVMs
 - New materials



■ Uses for Nonvolatile Memories

- Firmware programs stored in a ROM (BIOS, controllers for disks, network cards, graphics accelerators, security subsystems,...)
- Solid state disks (replacing rotating disks)
- Disk caches

Solid State Disks (SSDs)



- **Pages: 512KB to 4KB, Blocks: 32 to 128 pages**
- **Data read/written in units of pages.**
- **Page can be written only after its block has been erased.**
- **A block wears out after about 10,000 repeated writes.**

SSD Performance Characteristics

■ Benchmark of Samsung 970 EVO Plus

<https://ssd.userbenchmark.com/SpeedTest/711305/Samsung-SSD-970-EVO-Plus-250GB>

Sequential read throughput	2,221 MB/s	Sequential write tput	1,912 MB/s
Random ST throughput	61.7 MB/s	Random write tput	165 MB/s
Random DQ throughput	947 MB/s	Random DQ write	1028 MB/s

■ Sequential access faster than random access

- Common theme in the memory hierarchy
- DQ = deep queue, issuing many concurrent reads (latency hurts!)

■ Random writes are tricky

- Erasing a block takes a long time (~1 ms), but the SSD has a pool of pre-erased blocks
- Modifying a block page requires all other pages to be copied to new block.
- But the SSD has a write cache that it accumulates writes into...

SSD Tradeoffs vs Rotating Disks

■ Advantages

- No moving parts → faster, less power, more rugged

■ Disadvantages

- Have the potential to wear out
 - Mitigated by “wear leveling logic” in flash translation layer
 - E.g. Samsung 940 EVO Plus guarantees 600 writes/byte of writes before they wear out
 - Controller migrates data to minimize wear level
- In 2022, about 4-5 times more expensive per byte
 - Rcost will probably keep dropping

■ Where are rotating disks still used?

- Bulk storage – video, huge datasets / databases, etc.
- Cheap storage – desktops.

Summary

- The speed gap between CPU, memory and mass storage continues to widen.
- Many well-written programs exhibit a property called *locality*.
- Memory hierarchies based on *caching* close the gap by exploiting locality.
- Flash memory progress outpacing all other memory and storage technologies (DRAM, SRAM, magnetic disk)
 - Able to stack cells in three dimensions

Supplemental slides

Storage Trends

SRAM

Metric	1985	1990	1995	2000	2005	2010	2015	2015:1985
\$/MB	2,900	320	256	100	75	60	320	116
access (ns)	150	35	15	3	2	1.5	200	115

DRAM

Metric	1985	1990	1995	2000	2005	2010	2015	2015:1985
\$/MB	880	100	30	1	0.1	0.06	0.02	44,000
access (ns)	200	100	70	60	50	40	20	10
typical size (MB)	0.256	4	16	64	2,000	8,000	16,000	62,500

Disk

Metric	1985	1990	1995	2000	2005	2010	2015	2015:1985
\$/GB	100,000	8,000	300	10	5	0.3	0.03	3,333,333
access (ms)	75	28	10	8	5	3	3	25
typical size (GB)	0.01	0.16	1	20	160	1,500	3,000	300,000

CPU Clock Rates

Inflection point in computer history
when designers hit the “Power Wall”



	1985	1990	1995	2003	2005	2010	2015	2015:1985
CPU	80286	80386	Pentium	P-4	Core 2	Core i7(n)	Core i7(h)	
Clock rate (MHz)	6	20	150	3,300	2,000	2,500	3,000	500
Cycle time (ns)	166	50	6	0.30	0.50	0.4	0.33	500
Cores	1	1	1	1	2	4	4	4
Effective cycle time (ns)	166	50	6	0.30	0.25	0.10	0.08	2,075

(n) Nehalem processor
(h) Haswell processor