

1 Appendix

```
signature Sequence =
sig
  type 'a t
  type 'a seq = 'a t

  exception Range of string

  val empty : unit -> 'a seq (* span *)
  val tabulate : (int -> 'a) -> int -> 'a seq (* 0(1) *)
  val nth : 'a seq -> int -> 'a (* 0(1) *)
  val length : 'a seq -> int (* 0(1) *)

  val fromList : 'a list -> 'a seq (* 0(n) *)
  val toList : 'a seq -> 'a list (* 0(n) *)

  val map : ('a -> 'b) -> 'a seq -> 'b seq (* 0(1) *)
  val reduce : ('a * 'a -> 'a) -> 'a -> 'a seq -> 'a (* 0(log n) *)
  val reduce1 : ('a * 'a -> 'a) -> 'a seq -> 'a (* 0(log n) *)
  val filter : ('a -> bool) -> 'a seq -> 'a seq (* 0(log n) *)
  val rev : 'a seq -> 'a seq (* 0(1) *)
  val enum : 'a seq -> (int * 'a) seq (* 0(1) *)

  val subseq : 'a seq -> int * int -> 'a seq (* 0(1) *)
  val take : 'a seq -> int -> 'a seq (* 0(1) *)
  val drop : 'a seq -> int -> 'a seq (* 0(1) *)
end
```

```

signature Stream =
sig
  type 'a stream
  datatype 'a front = Empty | Cons of 'a * 'a stream

  val delay : (unit -> 'a front) -> 'a stream
  val expose : 'a stream -> 'a front

  val empty : 'a stream
  val cons : 'a * 'a stream -> 'a stream
  val fromList : 'a list -> 'a stream
  val tabulate : (int -> 'a) -> 'a stream

  val null : 'a stream -> bool
  val hd : 'a stream -> 'a
  val take : 'a stream * int -> 'a list
  val toList : 'a stream -> 'a list

  val tl : 'a stream -> 'a stream
  val drop : 'a stream * int -> 'a stream
  val append : 'a stream * 'a stream -> 'a stream

  val map : ('a -> 'b) -> 'a stream -> 'b stream
  val filter : ('a -> bool) -> 'a stream -> 'a stream
  val zip : 'a stream * 'b stream -> ('a * 'b) stream
end

```