Notes on efficient online SVM implementation

J. A. Bagnell
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1 Introduction

The linear online support vector machine is probably the fastest implementation of the algorithm available for large data-sets. It also tends to perform very well in practice. It relies directly upon Zinkevich’s [4, 3] projected gradient algorithm. (Improved performance bounds are due to [1] and [2].)

2 Algorithm

In short, the online SVM minimizes a sum of hinge loss and an $l_2$ norm on the weight vector:

$$ \text{loss}(w) = \frac{\lambda}{2} w^T w + \frac{1}{T} \sum_{t=1}^{T} \text{Hinge}(w, x_t, y_t) \quad (1) $$

Computing the gradient of the hinge loss is exactly like that in class. The gradient of the norm on the vector adds a “shrinking” factor at each step. Finally, we can explicitly constrain the solution to lie inside the prior ball using projected gradient descent.

Algorithm 1 Online linear support vector machine.

```
1: procedure OnlineSvm(x, y, λ)
2:     w ← 0
3:     t ← 1
4:     while not done do
5:         αt = 1/(λt) ▷ If Margin Violation
6:         if ytwt x < 1 then ▷ Apply Gradient
7:             w ← (1 − αtλ)w + αtytxt
8:         end if
9:         if wtwd > 1/λ then ▷ Optionally Project to ball of size $\sqrt{λ}$
10:            w = $\frac{w}{\sqrt{w^T w λ}}$
11:         end if
12:     t ← t + 1
13: end while
14: return w ▷ Optionally return the average of all w’s computed during process
15: end procedure
```

In this version of the algorithm, there is only one parameter: the strength of the prior. We’ve directly set the margin to 1, as well as the scale of the learning rate. You should normalize the input data to have unit norm on the input as well.

Additional tricks that also help are to make small batches of, say 100 data points, before doing an update and using the averaged gradient. Be sure your data-points are randomized if you want to ensure good offline performance.
References


