Leveraging Sequence Classification by Taxonomy-based Multitask Learning

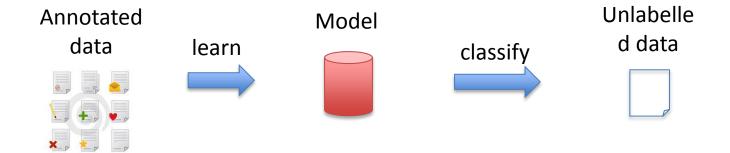
Christian Widmer, Jose Leiva, Yasemin Altun, Gunnar Ratsch

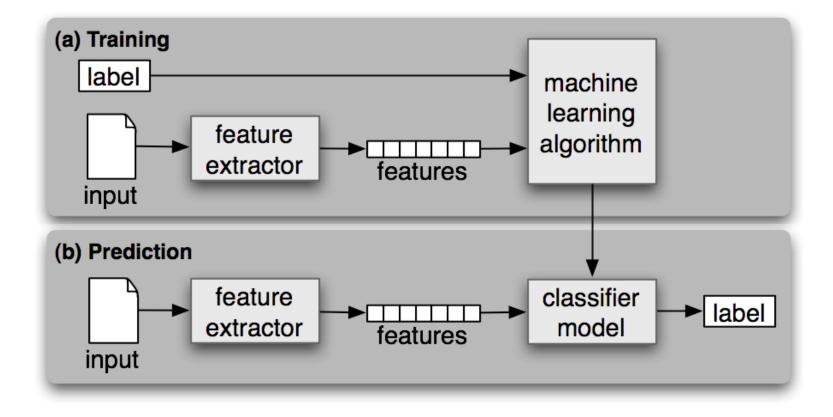
Presented by Meghana Kshirsagar

Outline

- Multitask Learning setting
- Application:
 - prediction of splicing sites across organisms
- 3 approaches to multi-task learning
 - Top-down
 - Pairwise
 - Multitask kernel
- Experiments and Results

Prelude: Classification





Multitask learning setting

Multi-task learning:

- Learning multiple concepts together
 - simultaneously
 - transfer learning between concepts

Why Multi-task learning?

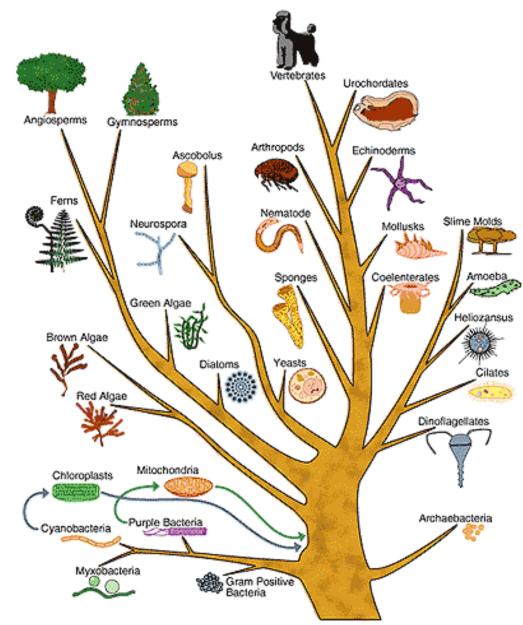
- Model quality limited by insufficient training data
 - exploit similarity between tasks
- In Computational Biology,
 - Organisms share evolutionary history
 - Many biological processes are conserved

Setting

- Consider M tasks: T₁, ..., T_M
- We are given data D_1 , ..., D_M for each task $-D_i = \{ (x_1, y_1), ..., \}$ for each task
- Build M classifiers, using all available information from all tasks
- Use a taxonomy to learn these multiple tasks!

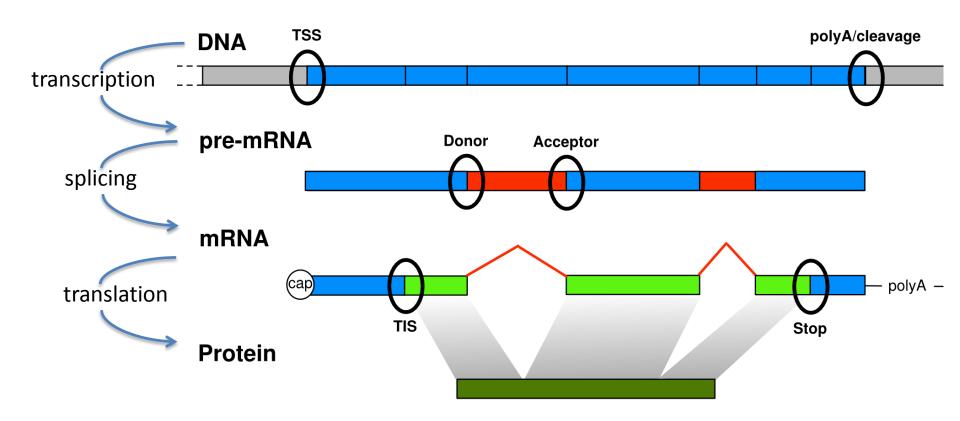
Why use Taxonomy?

- Taxonomy can be used to define relationships between two tasks
- In biology, taxonomy naturally arises from a phylogenic tree
- Closer tasks will benefit more from each other



Application to a biological problem

Prediction of splicing sites

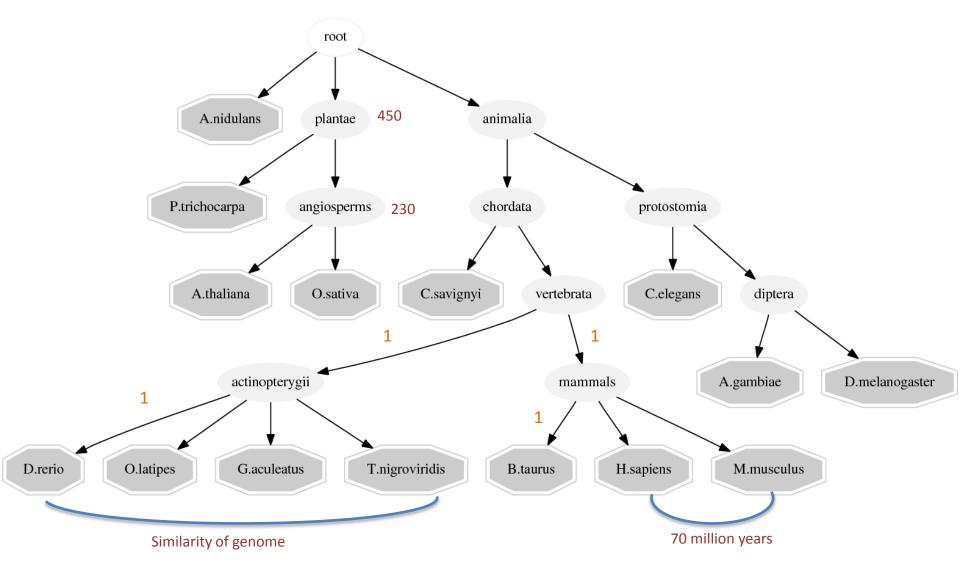


Given: annotated pre-mRNA data in multiple organisms

Find: new splicing sites → find Donor and Acceptor locations

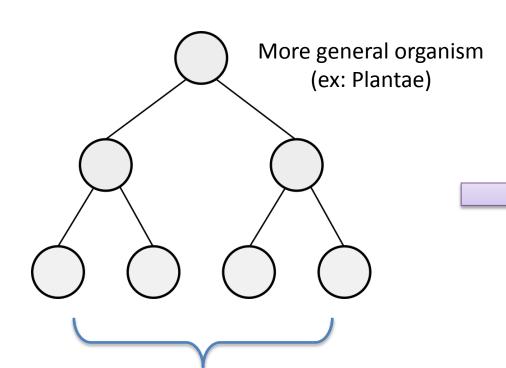
Question: Can we build a better model using data from multiple organisms?

Hierarchy used:



Techniques and algorithms

Exploiting hierarchies - 1



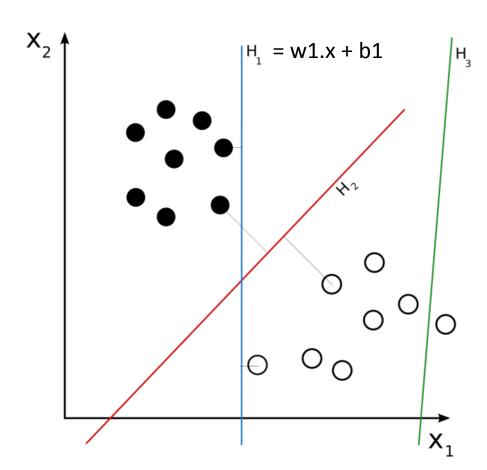
More specific organisms

Top-Down Model

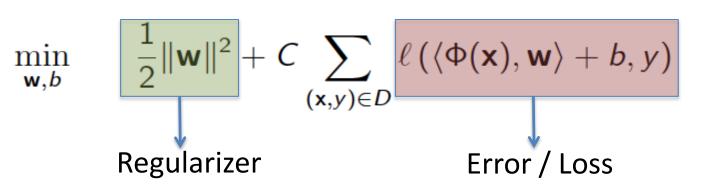
- Build model on root node using data from all leaf nodes of the tree
- 2. Build model on next level, similar to using all data in leaf nodes under that subtree
- 3.

- Can use any machine learning technique to build models at each level!
- How to build "similar" models?

Detour: Support Vector Machine



Mathematical formulation





How to build similar models?

Given : A parent model \overrightarrow{w}_{par}

Want: $W \cong W_{par}$

In other words, want $(w - w_{par})$ to be small

Regular SVM
$$\min_{\mathbf{w},b} \quad \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{(\mathbf{x},y)\in D} \ell\left(\langle \Phi(\mathbf{x}), \mathbf{w} \rangle + b, y\right)$$

$$\sum_{(\mathbf{x},y)\in D} \mathbf{w}$$

$$\min_{\mathbf{w},b} \quad \frac{1}{2} \|\mathbf{w} - \mathbf{w}_{par}\|^2 + C \sum_{(\mathbf{x},y)\in D} \ell\left(\langle \Phi(\mathbf{x}), \mathbf{w} \rangle + b, y\right)$$

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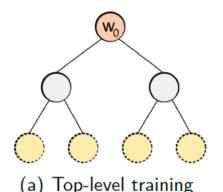
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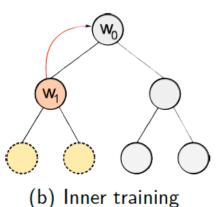
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Hierarchical Top-Down learning



 w_0 is trained using all data from all tasks (all leaf nodes)



- $\qquad \qquad \mathsf{Train} \,\, \mathsf{on} \,\, D_i = \bigcup_{j \preccurlyeq i} D_j$
- ▶ Regularize \mathbf{w}_i against parent predictor \mathbf{w}_{par} : $\|\mathbf{w}_i \mathbf{w}_{par}\|^2$

$$\min_{\mathbf{w},b} \frac{1}{2} \|\mathbf{w} - \mathbf{w}_{par}\|^2 + C \sum_{(\mathbf{x},y) \in D} \ell(\langle \Phi(\mathbf{x}), \mathbf{w} \rangle + b, y)$$

W₁

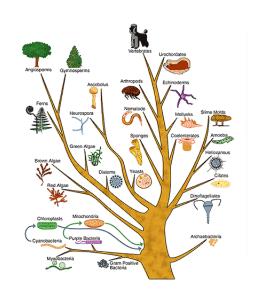
Taxon training

Organism

Leaf node classifiers are used for prediction

 W_{11} is built similar to W_1 and using data from one

Exploiting hierarchies - 2



Task Similarity Matrix

$$\Gamma = \begin{pmatrix} Y_{1,1} & \cdots & Y_{1,M} \\ & \ddots & \\ Y_{M,1} & \cdots & Y_{M,M} \end{pmatrix}$$

,

Pairwise &

Multitask Kernel

Pairwise Approach

- Simultaneous learning of all tasks!
- Train classifiers for all M tasks at the same time

$$\min_{\mathbf{w}_{1},...,\mathbf{w}_{M}} \frac{1}{2} \sum_{t=1}^{M} \sum_{s=1}^{M} \frac{\mathbf{y}_{t,s} \|\mathbf{w}_{t} - \mathbf{w}_{s}\|^{2}}{\uparrow} + \sum_{t=1}^{M} C_{t} \sum_{(\mathbf{x},y) \in D_{t}} \ell\left(\langle \mathbf{x}, \mathbf{w}_{t} \rangle, y\right)}$$

 Similarity is enforced by the regularization term and by task similarity matrix values

Experiments and Results

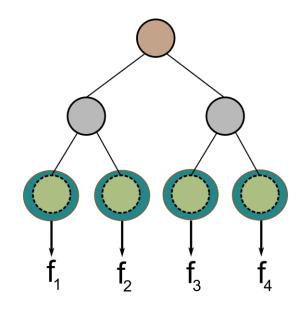
Methods compared

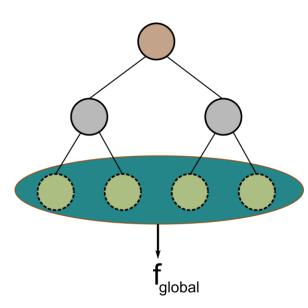
Multitask Learning Methods

- 1. Top-Down
- 2. Pairwise Regularization
- 3. Multitask Kernel

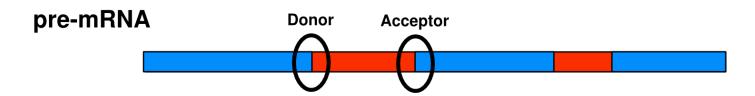
Baselines 2

- Plain
- Common





Splice-site recognition problem



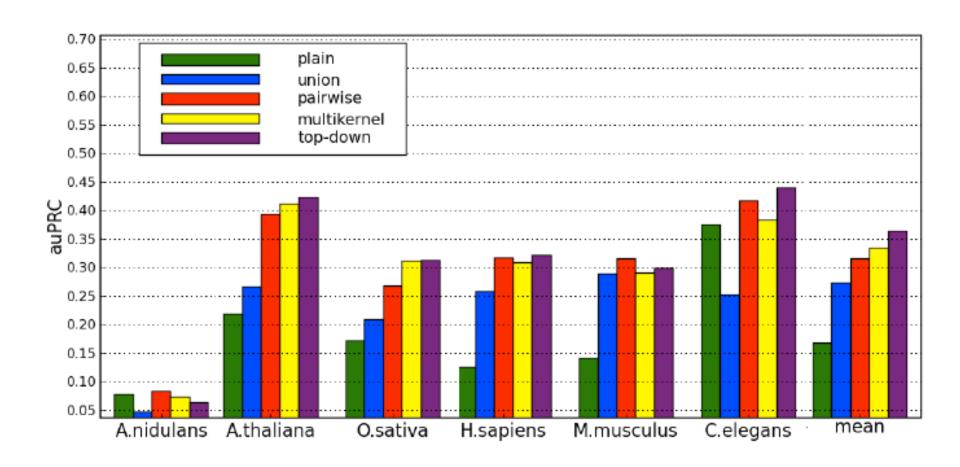
- Use insight:
 - GT or GC exhibited at donor site
 - AG consensus at acceptor site
- Each input sequence is:

```
≈ 150 nucleotides window around dimer

CT...GTCGTA...GAAGCTAGGAGCGC...ACGCGT...GA
```

- Data:
 - 15 organisms
 - Training: 10,000 examples per organism, Test data:
 6,000 examples per organism

Performance : AUC (area under precision recall curve)



Observations

- Gain is more for lower levels in hierarchy
- "A. nidulans": baselines do better!
- "Mouse" doesn't benefit much
 - possible reason: not much similarity in taxonomy
- No performance loss on distantly related organisms

Critique

- Experimental evaluation not very thorough
- Learning in the absence of a hierarchy
 - How to define task similarity measures?
- Assumes that some training (labeled) data is available from all organisms
 - In many scenarios, there is no data available on less studied organisms

Comments? Thoughts?

Multitask Kernel approach

$$\max_{\alpha} -\frac{1}{2} \sum_{i=1}^{n} \sum_{j=1}^{n} \alpha_{i} \alpha_{j} y_{i} y_{j} \hat{k}(\mathbf{x}_{i}, \mathbf{x}_{j}) + \sum_{i=1}^{n} \alpha_{i}$$
s.t. $0 \le \alpha_{i} \le C \ \forall i \in [1, n]$

$$\alpha^{T} \mathbf{y} = 0,$$

where

$$\hat{k}((x_i,s),(x_j,t)) = \underbrace{k_{\mathsf{task}}(s,t)}_{\gamma_{t,s}} \cdot k(x_i,x_j)$$